

Ongoing Lectures Collection

CS241

Linear Control Systems

Ahmed Waleed

February 13, 2020

GitHub Repository
Lectures Collection

Preface

Using \LaTeX , at least a hope that this work continues exists. I don't have much else to say, so I will just insert some blind text. Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

Ahmed Waleed

Contents

Preface	ii
Contents	iii
1 First Lecture	1
1.1 Introduction	1
1.2 Control Systems	1
Open-loop control system	1
Closed-loop control system	1
1.3 Mathematical Model	2
1.4 Block Diagram Reduction	2
Overall transfer function	2
APPENDIX	3
A Table of Laplace Transforms	4

List of Tables

1.1 Canonical form of feedback control system	2
A.1 Laplace transform theorems	4
A.2 Laplace general transforms	4

First Lecture

1

1.1 Introduction

Analysis of linear continuous system analysis of a system means simply checking the goodness of its measure of performance. Analysis could be done in two different ways:

- In the lab: by putting test input to the system and checking if the output satisfies the measure of performance.
- Using analytical techniques: which is our concern in this course.

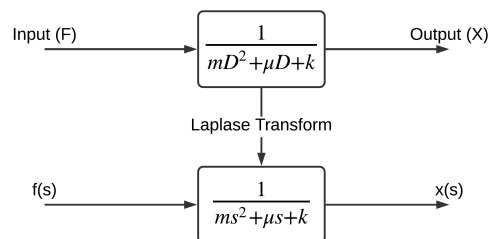
The first step is to make a mathematical model to the system.

$$\Sigma F_x = m\ddot{x}$$

$$F - \mu\dot{x} + kx = m\ddot{x}$$

$$\therefore F = m\ddot{x} + \mu\dot{x} + kx$$

Then defining the measure of performance and studying how we can check these measure of performance.



Transfer function ratio between Laplace transform of the output and Laplace transform of the input, assuming zero initial conditions.

1.2 Control Systems

A control system is an interconnection of components forming a system configuration that will provide a desired system response.

Open-loop control system (without feedback):

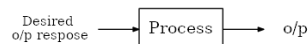


Figure 1.3: Its output does not track the input, and it is more affected by noise.

Closed-loop feedback control system (with feedback):

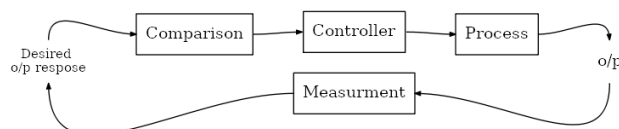


Figure 1.4: Closed loop control can improve accuracy, also the actuating signal is a function of the output.

1.1 Introduction	1
1.2 Control Systems	1
Open-loop control system . .	1
Closed-loop control system . .	1
1.3 Mathematical Model	2
1.4 Block Diagram Reduction . .	2
Overall transfer function . . .	2

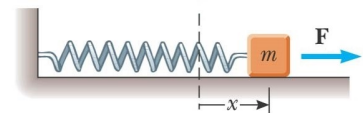


Figure 1.1: A block attached to a spring. ©

Figure 1.2: Since D is an operator (can't have a value), the transfer function is obtained by the Laplace transform of the first relation.

Switch cases to match Laplace

1.3 Mathematical Model

Any linear continuous system can be represented either by a linear algebraic equation or an ordinary differential equation such as:

$$(mD^2 + \mu D + k)x(t) = y(t)$$

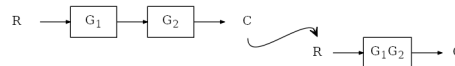
Solving the differential equation using Laplace transform assuming zero initial conditions made it possible to get the transfer function.

Add copyrights to lec.

1.4 Block Diagram Reduction

A Block Diagram is a shorthand pictorial representation of the cause-and-effect relationship of a system. Control systems require the arithmetic manipulation in order to obtain the overall transfer function and this is the start point for the analysis of the system.

Cascade connection :



Parallel connection :



Summation point :

a small circle, with plus or minus sign associated with the inputs, and the output is the algebraic sum of the inputs.

Take-off point :

a takeoff (or pickoff) point is used in order to have the same signal input to more than one block.

Table 1.1: Terminology

R	:	reference input / desired output response.
E	:	actuating / error signal.
G	:	control element and controlled system.
C	:	controlled variable / actual output.
H	:	feedback / backward transfer element.
B	:	primary feedback.
s	:	summation point.
t	:	takeoff point.

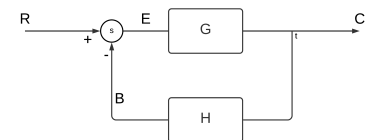


Figure 1.5: Canonical feedback loop.

negative feedback

Overall transfer function (feedback loop elimination):

Applying reduction techniques mentioned above, we can obtain the overall transfer function of Figure 1.5

$$\begin{aligned} @s : \quad E &= R - B && \text{(summation point)} \\ \therefore B &= CH && \text{(block)} \\ \therefore E &= R - CH \\ \therefore C &= GE && \text{(block)} \\ \therefore C &= G(R - CH) \\ C + CGH &= GR \\ C(1 + GH) &= GR \end{aligned}$$

$$\frac{C}{R} = \frac{G}{1 + GH}$$

End ?

Give more space between each pair

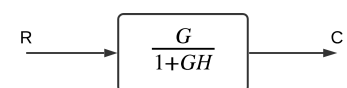


Figure 1.6: Feedback loop equivalent

Missed super position in multi i/p and postponed the mathematical models

APPENDIX

Table of Laplace Transforms

Thanks . . .

[illegible]

$f(t)$	$\mathcal{L}[f(t)] = \int_0^\infty f(t) e^{-st} dt = F(s)$
$f(at)$	$\frac{1}{a} F\left(\frac{s}{a}\right)$
$\dot{f}(t)$	$sF(s) - F(0)$
$\int_0^t f(x)dx$	$\frac{1}{s} F(s)$
$tf(t)$	$-\dot{F}(s)$
$\frac{1}{t} f(t)$	$\int_s^\infty F(x)dx$
$e^{at} f(t)$	$F(s - a)$
$f(t - a)\mathcal{U}(t - a)$	$e^{-as} F(s)$
$\int_0^t f(x)g(t - x)dx$	$F(s) G(s)$

Provide a link to the file