

# ADVANCED TOPICS ON ALGORITHMS

## Search & Sorting

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# Course Outline

1 Search Algorithms

2 Sorting Algorithms



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2 Sorting Algorithms



# Linear Search Algorithm and Analysis

## Definition

**Linear search** is a **sequential** algorithm that checks each element in a data structure until the target element is found or all elements have been examined.

```
1: Algorithm LINEARSEARCH( $A, x$ )  
2: // Input: Array  $A[1..n]$ , search value  $x$   
3: // Output: Index of  $x$  in  $A$ , or -1 if not found  
4: for  $i = 1$  to  $\text{length}(A)$  do  
5:   if  $A[i] = x$  then  
6:     return  $i$   
7:   end if  
8: end for  
9: return -1 // Element not found
```



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# Sequential Access Principles

## Characteristics:

- **Order Independence:** Works on unsorted data
- **Memory Efficiency:** Constant space complexity  $O(1)$
- **Simple Implementation:** Easy to understand and code
- **No Preprocessing:** Can search immediately

### Advantages

- Works on any data structure
- No sorting requirement
- Simple to implement
- Guaranteed to find element (if exists)

### Disadvantages

- Slow for large datasets
- Cannot skip elements
- Time increases linearly with size
- No early termination optimization



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# Study Case: Searching in Phone Directory

## Problem

Find a person's phone number in a phone directory containing 1000 entries.

## Example

### Linear Search Approach:

```
Algorithm FINDPHONENUMBER(directory, name)  
for  $i = 1$  to  $\text{length}(\text{directory})$  do  
    if  $\text{directory}[i].\text{name} = \text{name}$  then  
        return  $\text{directory}[i].\text{phone}$   
    end if  
end for  
return "Not Found"
```



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# Binary Search Algorithm and Requirements

## Definition

**Binary search** is a **divide-and-conquer** algorithm that finds an element in a sorted array by repeatedly dividing the search **interval in half**.

Prerequisites:

- 1 **Sorted Data:** Array must be sorted in ascending or descending order
- 2 **Random Access:** Ability to access any element directly (arrays, not linked lists)
- 3 **Comparison Operation:** Elements must be comparable



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# Binary Search Algorithm

```
1: Algorithm BINARYSEARCH( $A, x, low, high$ )
2: while  $low \leq high$  do
3:    $mid \leftarrow \lfloor \frac{low+high}{2} \rfloor$ 
4:   if  $A[mid] = x$  then
5:     return  $mid$ 
6:   else if  $A[mid] < x$  then
7:      $low \leftarrow mid + 1$ 
8:   else
9:      $high \leftarrow mid - 1$ 
10:  end if
11: end while
12: return  $-1$ 
```



# Study Case: Library Book Location System

## Problem

Locate a book in a library catalog system with 100,000 books organized by ISBN.



# Study Case: Library Book Location System

## Example

**Algorithm** `FINDBOOK(catalog, target_isbn)`

*low*  $\leftarrow 1$

*high*  $\leftarrow \text{length}(\text{catalog})$

**while** *low*  $\leq$  *high* **do**

*mid*  $\leftarrow \lfloor \frac{\text{low} + \text{high}}{2} \rfloor$

**if** *catalog*[*mid*].*isbn* = *target\_isbn* **then**

**return** *catalog*[*mid*] // Return book information

**else if** *catalog*[*mid*].*isbn* < *target\_isbn* **then**

*low*  $\leftarrow \text{mid} + 1$

**else**

*high*  $\leftarrow \text{mid} - 1$

**end if**

**end while**

**return** "Book not found"

# Interpolation Search Introduction

## Definition

**Interpolation search** improves upon binary search by making educated **guesses** about where the target element might be located, based on the values at the endpoints.

## Key Concept

Instead of always choosing the middle element, interpolation search estimates the position using:

$$pos = low + \frac{(x - A[low])}{(A[high] - A[low])} \times (high - low)$$





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# Interpolation Search Algorithm

```

1: Algorithm INTERPOLATIONSEARCH( $A, x, low, high$ )
2: while  $low \leq high$  and  $x \geq A[low]$  and  $x \leq A[high]$  do
3:    $pos \leftarrow low + \frac{(x - A[low])}{(A[high] - A[low])} \times (high - low)$ 
4:   if  $A[pos] = x$  then
5:     return  $pos$ 
6:   else if  $A[pos] < x$  then
7:      $low \leftarrow pos + 1$ 
8:   else
9:      $high \leftarrow pos - 1$ 
10:  end if
11: end while
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```



# Search Algorithm Selection Criteria

## Decision Framework

- **Data Size:** How many elements to search?
- **Data Organization:** Is the data sorted?
- **Search Frequency:** One-time or repeated searches?
- **Data Distribution:** Uniformly distributed values?
- **Memory Constraints:** Available space for preprocessing?

## Algorithm Comparison:

Algorithm	Prerequisites	Best Use Case
Linear Search	None	Small, unsorted data
Binary Search	Sorted array	Large, sorted data
Interpolation	Sorted, uniform	Large, uniform data



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# Study Case: Guess the Number (Large Space)

## Problem

Guess a secret number between 1 and 1,000,000 with minimum guesses.



# Outline

- 1 Search Algorithms
- 2 Sorting Algorithms



# Bubble Sort Algorithm and Mechanism

## Definition

**Bubble sort** is a simple sorting algorithm that **repeatedly** steps through the list, compares adjacent elements, and swaps them if they are in the wrong order.

```
1: Algorithm BUBBLESORT( $A$ )  
2:  $n \leftarrow \text{length}(A)$   
3: for  $i = 1$  to  $n - 1$  do  
4:   for  $j = 1$  to  $n - i$  do  
5:     if  $A[j] > A[j + 1]$  then  
6:       SWAP( $A[j], A[j + 1]$ )  
7:     end if  
8:   end for  
9: end for
```

*Large elements "bubble up" to their correct position, just like air bubbles rising to the surface of water.*



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# Adjacent Element Comparison Approach

## Core Mechanism

**Bubble sort** works by making **multiple passes** through the array, comparing each pair of **adjacent elements** and swapping them if they're out of order.

## Example

**Step-by-step example:** Sort [64, 34, 25, 12, 22, 11, 90]

### Pass 1:

- Compare 64, 34 → Swap → [34, 64, 25, 12, 22, 11, 90]
- Compare 64, 25 → Swap → [34, 25, 64, 12, 22, 11, 90]
- Compare 64, 12 → Swap → [34, 25, 12, 64, 22, 11, 90]
- Compare 64, 22 → Swap → [34, 25, 12, 22, 64, 11, 90]
- Compare 64, 11 → Swap → [34, 25, 12, 22, 11, 64, 90]
- Compare 64, 90 → No swap → [34, 25, 12, 22, 11, 64, 90]

After Pass 1: Largest element (90) is in correct position!

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**Step-by-step example:** Sort [64, 34, 25, 12, 22, 11, 90]

**Pass 1:**

- Compare 64, 34 → Swap → [34, 64, 25, 12, 22, 11, 90]
- Compare 64, 25 → Swap → [34, 25, 64, 12, 22, 11, 90]
- Compare 64, 12 → Swap → [34, 25, 12, 64, 22, 11, 90]
- Compare 64, 22 → Swap → [34, 25, 12, 22, 64, 11, 90]
- Compare 64, 11 → Swap → [34, 25, 12, 22, 11, 64, 90]
- Compare 64, 90 → No swap → [34, 25, 12, 22, 11, 64, 90]

After Pass 1: Largest element (90) is in correct position!

# Study Case: Sorting Playing Cards

## Real-World Application

You have a hand of playing cards and want to sort them by value. How would you naturally do this?



# Selection Sort Algorithm and Approach

## Definition

**Selection sort** sorts by repeatedly finding the **minimum element** from the unsorted portion and placing it at the beginning.

Key Characteristics:

- **Invariant:** After  $i$  iterations, first  $i$  elements are sorted
- **Selections:** Makes exactly  $n - 1$  swaps
- **Comparisons:** Always  $\frac{n(n-1)}{2}$  comparisons



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**Selection sort** sorts by repeatedly finding the **minimum element** from the unsorted portion and placing it at the beginning.

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- **Comparisons:** Always  $\frac{n(n-1)}{2}$  comparisons



# Selection Sort Algorithm

```
1: Algorithm SELECTIONSORT( $A$ )
2:  $n \leftarrow \text{length}(A)$ 
3: for  $i = 1$  to  $n - 1$  do
4:    $\text{min\_index} \leftarrow i$ 
5:   for  $j = i + 1$  to  $n$  do
6:     if  $A[j] < A[\text{min\_index}]$  then
7:        $\text{min\_index} \leftarrow j$ 
8:     end if
9:   end for
10:  SWAP( $A[i], A[\text{min\_index}]$ )
11: end for
```



# Minimum/Maximum Selection Strategy

## Core Strategy

Selection sort maintains two regions:

- **Sorted region:** Elements already in final position
- **Unsorted region:** Elements yet to be processed

## Example

Sorting [64, 25, 12, 22, 11]:

Pass	Array State	Action
Initial	[64, 25, 12, 22, 11]	Find min in [64,25,12,22,11]
1	[11, 25, 12, 22, 64]	Min=11, swap with 64
2	[11, 12, 25, 22, 64]	Min=12, swap with 25
3	[11, 12, 22, 25, 64]	Min=22, swap with 25
4	[11, 12, 22, 25, 64]	Min=25, no swap needed





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Selection sort maintains two regions:

- **Sorted region:** Elements already in final position
- **Unsorted region:** Elements yet to be processed

## Example

Sorting [64, 25, 12, 22, 11]:

Pass	Array State	Action
Initial	[64, 25, 12, 22, 11]	Find min in [64,25,12,22,11]
1	[11, 25, 12, 22, 64]	Min=11, swap with 64
2	[11, 12, 25, 22, 64]	Min=12, swap with 25
3	[11, 12, 22, 25, 64]	Min=22, swap with 25
4	[11, 12, 22, 25, 64]	Min=25, no swap needed



# Study Case: Student Grades Enrollment Schedule

## Problem

A professor needs to organize student grades for enrollment priority. Students with higher GPAs get priority registration.

## Example

### Student Records:

Student Name	GPA
Alice	3.8
Bob	2.5
Charlie	3.9
Diana	2.1
Eve	3.7



# Study Case: Student Grades Enrollment Schedule [Solution]

```

1: Algorithm ORGANIZEBYGPA(students)
2: for  $i = 1$  to  $\text{length}(\text{students}) - 1$  do
3:    $\text{max\_gpa\_index} \leftarrow i$ 
4:   for  $j = i + 1$  to  $\text{length}(\text{students})$  do
5:     if  $\text{students}[j].\text{gpa} > \text{students}[\text{max\_gpa\_index}].\text{gpa}$  then
6:        $\text{max\_gpa\_index} \leftarrow j$ 
7:     end if
8:   end for
9:   SWAP( $\text{students}[i]$ ,  $\text{students}[\text{max\_gpa\_index}]$ )
10: end for

```

Result: Priority Order

Charlie (3.9)  $\rightarrow$  Alice (3.8)  $\rightarrow$  Eve (3.7)  $\rightarrow$  Bob (2.5)  $\rightarrow$  Diana (2.1)



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# Insertion Sort Algorithm and Methodology

## Definition

**Insertion sort** builds the final sorted array one element at a time by repeatedly taking an element from the unsorted portion and **inserting** it into its correct position in the sorted portion.

```
1: Algorithm INSERTIONSORT( $A$ )
2: for  $i = 2$  to  $\text{length}(A)$  do
3:    $\text{key} \leftarrow A[i]$ 
4:    $j \leftarrow i - 1$ 
5:   while  $j \geq 1$  and  $A[j] > \text{key}$  do
6:      $A[j + 1] \leftarrow A[j]$ 
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7:      $j \leftarrow j - 1$ 
8:   end while
9:    $A[j + 1] \leftarrow key$ 
10: end for
```



# Incremental Sorting Approach I

Insertion sort works like organizing playing cards in your hand:

- 1 Start with first card (trivially sorted)
- 2 Pick next card from unsorted pile
- 3 Find correct position in sorted portion
- 4 Shift other cards as needed
- 5 Insert card in correct position
- 6 Repeat until all cards are sorted



# Incremental Sorting Approach I

## Example

Sorting [5, 2, 4, 6, 1, 3]:

Step	Array State	Action
Initial	[5, 2, 4, 6, 1, 3]	Start with first element
1	[2, 5, 4, 6, 1, 3]	Insert 2 before 5
2	[2, 4, 5, 6, 1, 3]	Insert 4 between 2 and 5
3	[2, 4, 5, 6, 1, 3]	6 already in position
4	[1, 2, 4, 5, 6, 3]	Insert 1 at beginning
5	[1, 2, 3, 4, 5, 6]	Insert 3 between 2 and 4





# Study Case: Alphabetical Name Sorting

## Problem

Sort a class roster alphabetically for easy lookup during attendance.

## Example

**Class Roster:** [David, Alice, Charlie, Bob, Eve]

**Insertion Sort Process:**

Step	Roster State
Initial	[David, Alice, Charlie, Bob, Eve]
1	[Alice, David, Charlie, Bob, Eve]
2	[Alice, Charlie, David, Bob, Eve]
3	[Alice, Bob, Charlie, David, Eve]
4	[Alice, Bob, Charlie, David, Eve]



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# Study Case: UD Students Code Sorting (Sort Battle)

## Programming Challenge!

Universidad Distrital students are identified by codes like "20192578001". Sort student codes efficiently for registration processing.

## Challenge Rules

- Input: 1000 student codes in random order
- Goal: Sort in ascending order
- Competition: Which algorithm performs best?
- Test different algorithms with same dataset

## Example

**Sample Student Codes:** [20192578001, 20202589123, 20171098765]

**Sorted Result:** [20171098765, 20192578001, 20202589123]



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**Sorted Result:** [20171098765, 20192578001, 20202589123]



# Quick Sort Algorithm (Divide & Conquer Application) I

## Definition

**Quick sort** is a divide-and-conquer algorithm that sorts by selecting a **pivot** element and partitioning the array around it, then recursively sorting the subarrays.

- 1: **Algorithm** QUICKSORT( $A, low, high$ )
- 2: **if**  $low < high$  **then**
- 3:    $pivot\_index \leftarrow \text{PARTITION}(A, low, high)$
- 4:   QUICKSORT( $A, low, pivot\_index - 1$ )
- 5:   QUICKSORT( $A, pivot\_index + 1, high$ )
- 6: **end if**



# Quick Sort Algorithm (Divide & Conquer Application) II

```
1: Algorithm PARTITION( $A, low, high$ )
2:  $pivot \leftarrow A[high]$  // Choose last element as pivot
3:  $i \leftarrow low - 1$  // Index of smaller element
4: for  $j = low$  to  $high - 1$  do
5:   if  $A[j] \leq pivot$  then
6:      $i \leftarrow i + 1$ 
7:     SWAP( $A[i], A[j]$ )
8:   end if
9: end for
10: SWAP( $A[i + 1], A[high]$ )
11: return  $i + 1$ 
```



# Partition Strategy and Pivot Selection

## Partitioning Process

The partition operation rearranges the array so that:

- Elements smaller than pivot are on the left
- Elements greater than pivot are on the right
- Pivot is in its final sorted position

Pivot Selection Strategies:

- 1 **First Element:** Simple but poor for sorted data
- 2 **Last Element:** Common choice, same issue
- 3 **Random Element:** Good average performance
- 4 **Median-of-Three:** Choose median of first, middle, last
- 5 **True Median:** Best but expensive to compute



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# Study Case: UD Students Code Sorting (The Final Challenge)

## Ultimate Sorting Challenge!

Now we face the final boss: Sort 100,000 UD student codes using Quick Sort. Can it handle the massive dataset?

### Challenge Specifications

- **Dataset Size:** 100,000 student codes
- **Format:** 11-digit codes (e.g., 20192578001)
- **Goal:** Sort in under 1 second
- **Memory Limit:** In-place sorting preferred



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# Merge Sort Algorithm (Divide & Conquer Application) I

## Definition

**Merge sort** is a stable, divide-and-conquer algorithm that divides the array into **halves**, recursively **sorts** them, and then **merges the sorted** halves.

```
1: Algorithm MERGESORT( $A, left, right$ )  
2: if  $left < right$  then  
3:    $mid \leftarrow \lfloor \frac{left+right}{2} \rfloor$   
4:   MERGESORT( $A, left, mid$ )  
5:   MERGESORT( $A, mid + 1, right$ )  
6:   MERGE( $A, left, mid, right$ )  
7: end if
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- 6:   MERGE( $A, left, mid, right$ )
- 7: **end if**



# Merge Sort Algorithm (Divide & Conquer Application) II

- 1: **Algorithm** MERGE( $A, left, mid, right$ )
- 2: Create temporary arrays  $L[left..mid]$  and  $R[mid + 1..right]$
- 3: Copy data to temporary arrays
- 4:  $i \leftarrow 0, j \leftarrow 0, k \leftarrow left$
- 5: **while**  $i < len(L)$  **and**  $j < len(R)$  **do**
- 6:   **if**  $L[i] \leq R[j]$  **then**
- 7:      $A[k] \leftarrow L[i]; i \leftarrow i + 1$
- 8:   **else**
- 9:      $A[k] \leftarrow R[j]; j \leftarrow j + 1$
- 10:   **end if**
- 11:    $k \leftarrow k + 1$
- 12: **end while**
- 13: Copy remaining elements of  $L$  and  $R$  to  $A$



# Merge Strategy and Stability

## Merge Strategy

The merge operation combines two sorted subarrays into one sorted array:

- 1 Compare the first elements of both subarrays
- 2 Select the smaller element and add to result
- 3 Move pointer in that subarray
- 4 Repeat until one subarray is exhausted
- 5 Copy remaining elements from other subarray

## Stability Property

Merge sort is **stable** because when elements are equal, we always take from the left array first, preserving the original relative order.



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# Study Case: Real-time Sorting

## Problem

A live streaming platform needs to sort viewer comments by timestamp in real-time while new comments continuously arrive.

## Example

**Scenario:** Comments arrive every millisecond during a popular stream

### Requirements:

- Sort existing comments while new ones arrive
- Maintain chronological order (stability important)
- Handle high volume (100,000+ comments/minute)
- Provide sorted output for display





# When to Use Which Sorting Algorithm

## Decision Matrix

Algorithm	Time Complexity	Stable	Best Use Case
Bubble Sort	$O(n^2)$	Yes	Educational/tiny datasets
Selection Sort	$O(n^2)$	No	Minimizing swaps
Insertion Sort	$O(n^2)$	Yes	Nearly sorted data
Quick Sort	$O(n \log n)$	No	General purpose
Merge Sort	$O(n \log n)$	Yes	Stability required

Choose Based on Requirements:

- **Stability needed:** Merge sort or Insertion sort
- **Memory limited:** Quick sort or Insertion sort
- **Partially sorted:** Insertion sort
- **Random data:** Quick sort
- **Guaranteed performance:** Merge sort



# Performance Trade-offs Analysis

## Comprehensive Performance Comparison

Let's analyze the trade-offs between different sorting algorithms across multiple dimensions.

## Key Insights

- **Simplicity vs. Efficiency:**  $O(n^2)$  algorithms are simpler but slower
- **Memory vs. Speed:** Faster algorithms often use more memory
- **Stability Cost:** Stable algorithms may be slightly slower
- **Adaptive Algorithms:** Some perform better on partially sorted data



# Summary: Advanced Sorting & Searching I

## Search Algorithms Summary

- **Linear Search:** Simple, works on any data,  $O(n)$  time
- **Binary Search:** Efficient for sorted data,  $O(\log n)$  time
- **Interpolation Search:** Best for uniform data,  $O(\log \log n)$  average

## Sorting Algorithms Summary

- **Simple Sorts ( $O(n^2)$ ):** Bubble, Selection, Insertion - good for small data
- **Advanced Sorts ( $O(n \log n)$ ):** Quick Sort (fast), Merge Sort (stable)
- **Algorithm Choice:** Depends on data size, memory, stability requirements



# Summary: Advanced Sorting & Searching I

## Search Algorithms Summary

- **Linear Search:** Simple, works on any data,  $O(n)$  time
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# Summary: Advanced Sorting & Searching II

## Key Takeaways

- **Understand your data:** Size, order, distribution affect algorithm choice
- **Know your constraints:** Memory, time, stability requirements matter
- **Practice implementation:** Understanding helps with optimization
- **Benchmark performance:** Theory vs. practice can differ



# Outline

- 1 Search Algorithms
- 2 Sorting Algorithms



# Thanks!

## Questions?



Repo: <https://github.com/EngAndres/ud-public/tree/main/courses/computer-sciences-i>

