



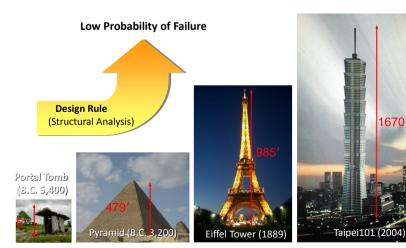
## Intro: Structural Reliability

#### Center of Excellence for Product Reliability and Optimization Based on Prof. Ramana Grandhi's Lecture



## The Magic of Design





1670'



## Life, Full of Uncertainties



**Space Shuttle Catastrophes, USA, 1986 and 2003:** Unforeseen variations of system conditions cause accidents of two shuttles (Challenger and Columbia)





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# Life, Full of Uncertainties (Cntd.) RIGHT STATE

**Collapse of the Tacoma Narrow Bridge, USA, 1940:** Turbulent winds cause torsional vibrations







## Life, Full of Uncertainties (Cntd.) RIGHT STATE

Risk of Aging Aircraft, Aloha Airlines Flight 243 (19-year-old aircraft), Hawaii, 1988: Undetected fatigue causes critical damage



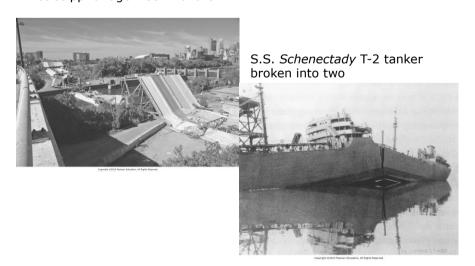


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# Life, Full of Uncertainties (Cntd.) RIGHT STATE

#### Mississippi bridge I-35W failure





## The life of a bulb, the arrival time of the next bus at a stop: these are examples of random variables that are encountered in everyday life.







## Representative Risk of Death WRIGHT STATE UNIVERSITY



Activity/Cause	Number of Deaths Per Year Per 10 <sup>6</sup> Persons
Air travel	9
Rail travel	4
Water transport	9
Motor vehicles	300
Poison	20
Lightning	0.5
Fires	40
Machinery	10
Structural failures	0.2



#### Sources of Uncertainties



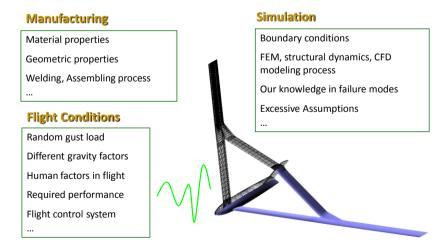
- Uncertainty in the design process can arise from many sources:
  - Inaccurate parameters
  - Unmodeled physics
  - Numerical errors
  - Uncertain operating conditions
  - Disagreement among model responses
- It is crucial to be able to quantify this uncertainty to obtain accurate estimates of system performance and reliability

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## **Design Under Uncertainties**

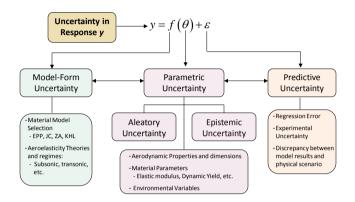






## **Uncertainty Breakdown**





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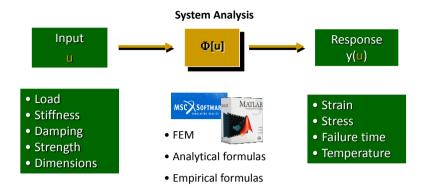


## Overview of Uncertainty Quantification



#### **Deterministic Analysis**





The simulation of a single design point is extremely unrealistic when we attempt to identify the complete information of systems under varying loads and material properties.

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#### Deterministic Analysis with Safety Factor



#### Safety Factor (Factor of Safety)

provides a design margin over the theoretical design capacity to allow for uncertainty in the design process

$$F = \frac{R}{S}$$

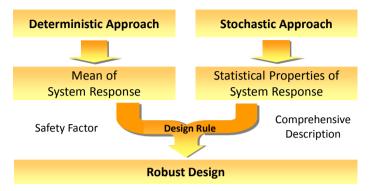
where R is the resistance and S is the capacity or loading of the system

The selection of the appropriate safety factor in design of components is essentially a compromise between the associated additional cost and weight and the benefit of increased safety or reliability



## If it Works, Make It Better





#### Both the resistance R and load S of the safety factor are random variables

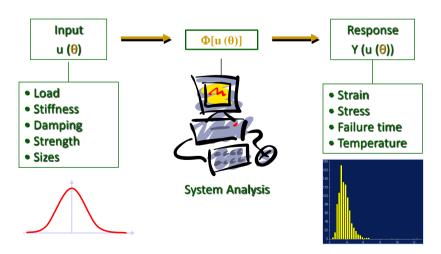
→ When the scatter in the variables is considered, the safety factor could potentially be less than unity

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## Stochastic Analysis







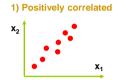
## **Stochastic Analysis**



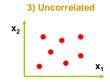
Stochastic analysis is a mathematical process involving a randomly determined sequence of observations, each of which is considered as a sample of one element from a probability distribution

#### **Components of Stochastic Analysis:**

- Random Variable: Measurable values in probability space associated with events of experiments
- Probabilistic Distribution: Indicates a relative probability of observing each random variable
- Covariance (not independent):







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#### When is Stochastic Analysis Useful?



#### When we have unconventional designs:

- There is little relevant data with unconventional designs
- Difficult to estimate risks of new technology or design concepts
  - Appropriate understanding and treatment of uncertainty in the design process is essential for safe and efficient decisions









## When is Stochastic Analysis Useful? WRIGHT STATE



#### When there are large variation of design variables and system properties:

- Real world is highly variable
  - Significant variability in fatigue crack growth properties is possible for different batches of 2024-T3 Aluminum (NASA Report, 1988)
- Modelers often try to present results of "best-case / worst-case" scenario or averaged properties
  - Lack the mathematical soundness of applying statistical principles to account for model input parameter variability

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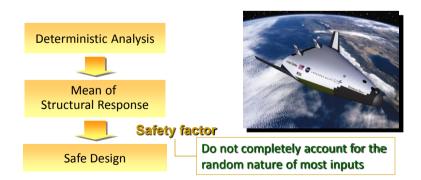


#### When is Stochastic Analysis Useful?



#### When fair safety is not good enough:

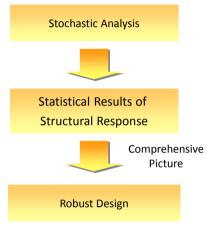
For people in spaceships, "survival" should be taken very seriously

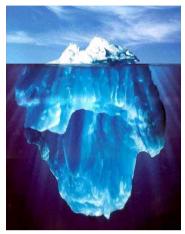




# When is Stochastic Analysis Useful?







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# Advantages of Stochastic Analysis



#### Why to quantify uncertainty?

- Uncertainty is inevitable or sometimes foreseeable (bounded)
- Appropriate understanding of uncertainty is essential for safe and efficient design
- There is little relevant data with unconventional designs

#### **Advantages**

- More comprehensive picture for safe designs
- Better ability to detect when a structural system is staying outside the normal limits of uncertainty
- Analysts are able to quantify their confidence in performance estimates
- Risk informed designs / decisions



### Representation of Uncertainty



#### What is the probability of that a selected person has a birthday on July 4th?

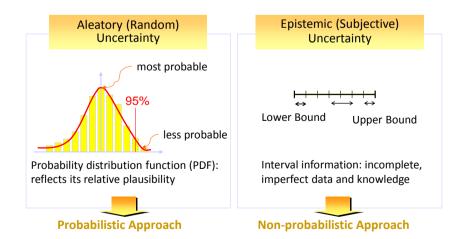


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# Representation of Parametric Uncertainty

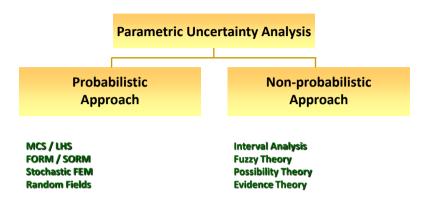






# Parametric Uncertainty Analysis Categories





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# UQ Using Probability Theory GIGHT STATE UNIVERSITY

