

Assignment 1

The objective of this assignment is to experiment with uniform and non-uniform quantization using Matlab

1- Implement a uniform scalar quantizer function with the header

```
q_ind = UniformQuantizer(in_val, n_bits, xmax, m),
```

where `in_val` is a vector with the original samples, `n_bits` is the number of bits available to quantize one sample in the quantizer, `xmax` and `m` define the range of the quantizer from $m\Delta/2 - x_{\max}$ to $m\Delta/2 + x_{\max}$, so that the width of each quantization interval is $\Delta = 2 \times x_{\max}/L$, where L is the number of quantization intervals. `m` defines the mean (or offset) of the quantizer reconstruction levels. Setting `m = 0` defines a “midrise” quantizer, and `m = 1` gives a “midtread” quantizer. The function should return the index of the chosen quantization level in `q_ind`

2- Implement a uniform scalar de-quantizer function with the header

```
deq_val=UniformDequantizer(q_ind, n_bits, xmax, m)
```

where `deq_val` is the corresponding dequantized value for `q_ind`. The rest of the function parameters (i.e., `n_bits`, `xmax`, `m`) are the same as in part 1.

Hint: The uniform scalar quantizer/dequantizer is a highly structured quantizer. They can be implemented essentially by only a scalar division (no multiplications, comparisons or loops are needed), making the computational complexity independent of the bitrate. Make sure your encoder has a computational complexity independent of the bitrate!

- 3- **Test the quantizer/dequantizer functions on a deterministic input** as follows: Generate an input `ramp` signal `x=-6:0.01:6` and pass it through the quantizer-dequantizer assuming that `n_bits= 3` and `xmax = 6`. Plot the input/output signal (on the same graph) for `m=0`. Repeat (on another graph) for `m=1`.

4- Now test your input on a random input signal as follows:

- Generate a sequence of 10,000 independent and identically distributed (i.i.d) continuous uniform random variables between -5 and 5.
- Pass each sample through the two implemented functions, and calculate the quantization error using `xmax = 5` and `m=0`
- Calculate the SNR defined as $E(\text{input}^2)/E(\text{quantization error}^2)$.
- Repeat b-c for `n_bits=2:1:8`,
- On the same plot, sketch the simulation and the theoretical SNR (in dB) on the vertical axis vs `n_bits` on the horizontal axis.

5- Now test the uniform quantizer on a non-uniform random input as follows:

- a. repeat part 4 assuming the input samples are i.i.d. The polarity of each sample is random and it takes the value \pm with probability 0.5. The magnitude of each sample follows an exponential distribution with PDF $f(x) = e^{-x}$.

6- Now quantize the non-uniform signal using a non-uniform μ law quantizer as follows

- a. Repeat part 5 using non-uniform μ quantization. Compare the results for $\mu = 0$ (uniform quantization in part 5), 5, 100, 200 (on the same graph).

Hint: You do not need to alter the uniform quantizer/dequantizer functions, just add a block for expanding the signal before the quantizer and for compressing the signal after the dequantizer