

$$\begin{array}{lll}
 V_I = -F & q_{AB} = -q = -F/b & EJ_{FG} = EJ \\
 H_F = F & EJ_{AB} = EJ & EJ_{CH} = EJ \\
 V_J = -F & EJ_{BC} = EJ & EJ_{HG} = EJ \\
 p_{BC} = q = F/b & EJ_{CD} = EJ & EJ_{GI} = EJ \\
 q_{CH} = -q = -F/b & EJ_{DE} = EJ & EJ_{IJ} = EJ \\
 q_{EF} = q = F/b & EJ_{EF} = EJ &
 \end{array}$$

1] 1 Piano J

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

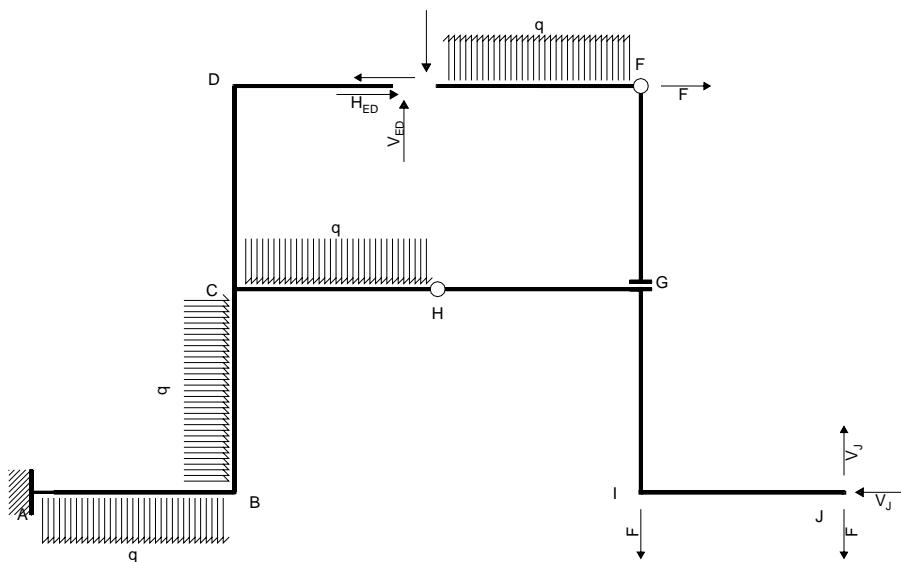
Piano di scorrimento del vincolo con inclinazione assegnata.

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EQUAZIONI DI EQUILIBRIO

Rotazione intorno a H: aste HG GF GI FE IJ

$$V_J b + H_{ED} b = 4Fb - 1/2qb^2$$

Traslazione orizzontale: aste GF FE

$$-\mathbf{H}_{ED} = -\mathbf{F}$$

Rotazione intorno a F: aste FE

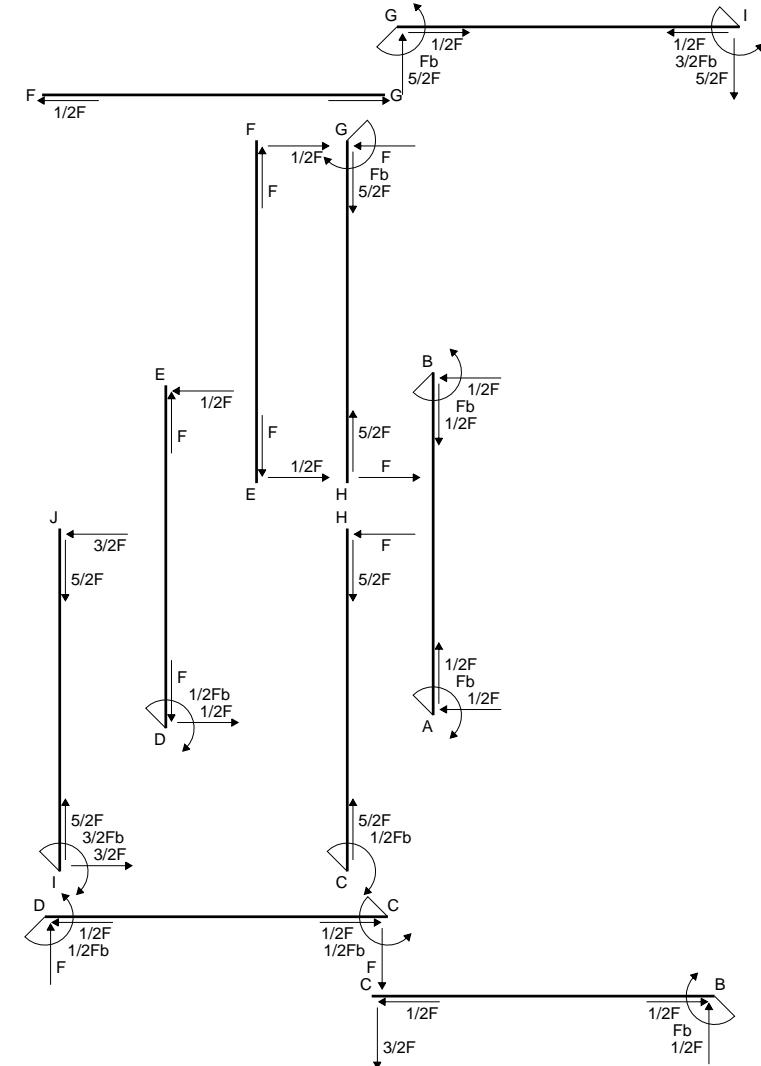
$$V_{ED}b = 1/2qb^2$$

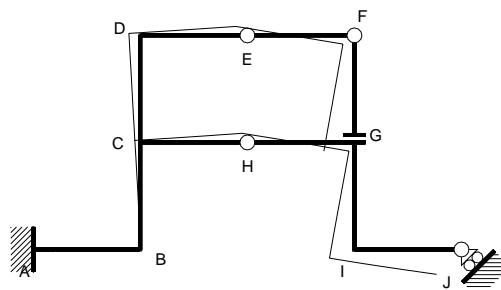
Matrice di equilibrio

$$\begin{matrix} \Phi_{HC} \\ u_{GF} \\ \Phi_{FE} \end{matrix} \begin{bmatrix} V_J b & H_{ED} b & V_{ED} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -1/2 & 0 \\ 0 & 1/2 \end{bmatrix}$$

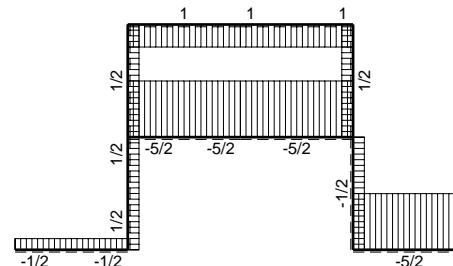
Soluzione del sistema

$$\begin{bmatrix} V_J b \\ H_{ED} b \\ V_{ED} b \end{bmatrix} = \begin{bmatrix} F_b & qb^2 \\ 3 & -1/2 \\ 1 & 0 \\ 0 & 1/2 \end{bmatrix}$$

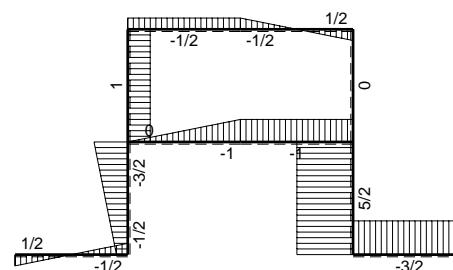




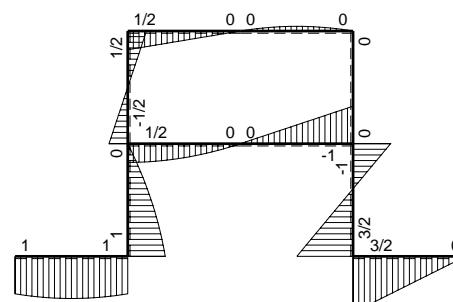
$\square \rightarrow 20 F_b^3/EJ$



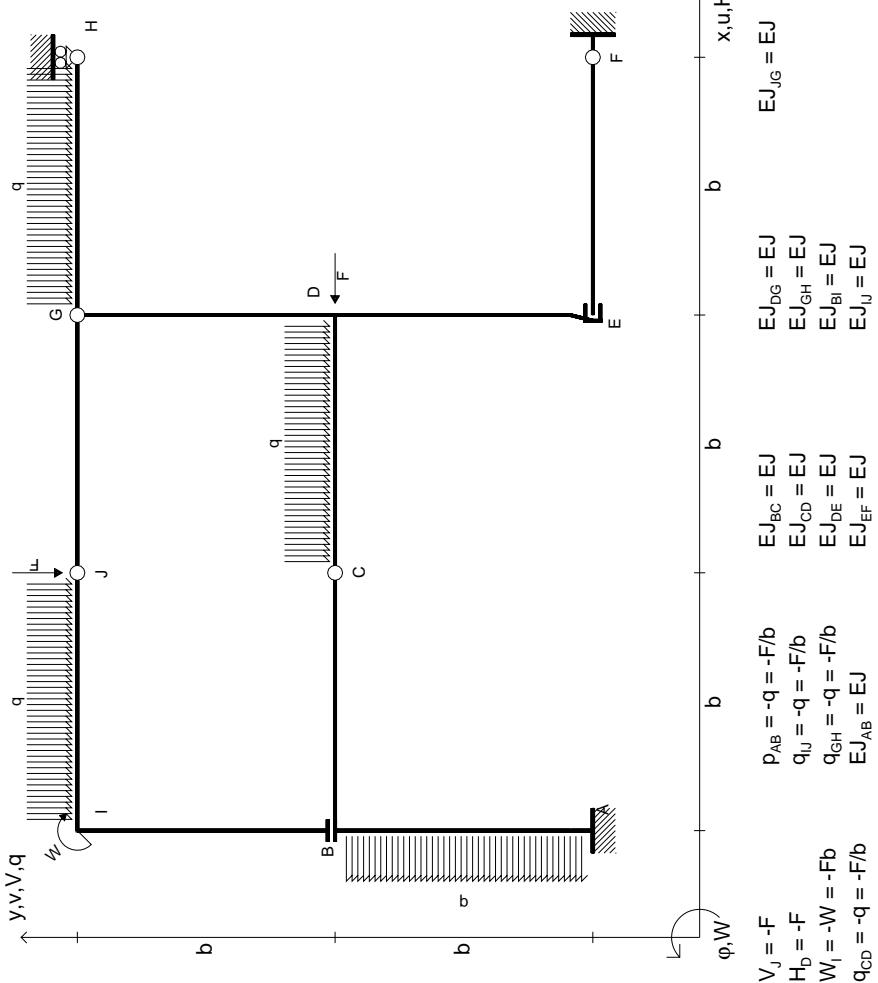
$\leftarrow \square \rightarrow F$



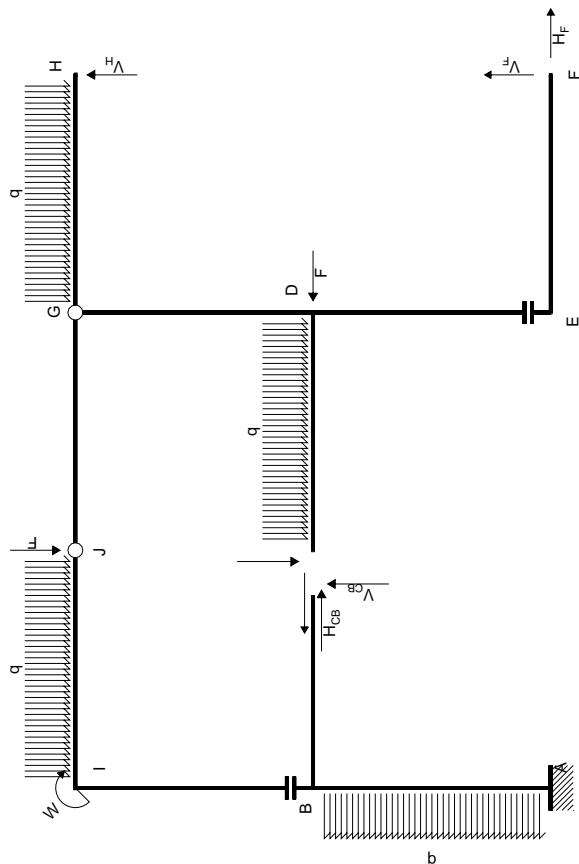
$\uparrow \square \downarrow F$



$\zeta \square \zeta F_b$



Carichi e deformazioni date hanno verso efficace in disegno.
 Calcolare reazioni vincolari della struttura e delle aste.
 Tracciare i diagrammi quotati delle azioni interne nelle aste.
 $J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y .
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EQUAZIONI DI EQUILIBRIO

Traslazione orizzontale: aste BI JU JG GD GH DC DE EF

$$H_F - H_{CB} = F$$

Rotazione intorno a J: aste JG GD GH DC DE EF

$$2H_F + 2V_F b + 2V_H b - H_{CB} b = Fb + 2qb^2$$

Rotazione intorno a G: aste GD GH DC DE EF

$$2H_F + V_F b + V_H b - H_{CB} b + V_{CB} b = Fb$$

Rotazione intorno a G: aste GD DC DE EF

$$2H_F + V_F b - H_{CB} b + V_{CB} b = Fb - 1/2qb^2$$

Traslazione orizzontale: aste EF

$$H_F = 0$$

$$\text{Matrice di equilibrio}$$

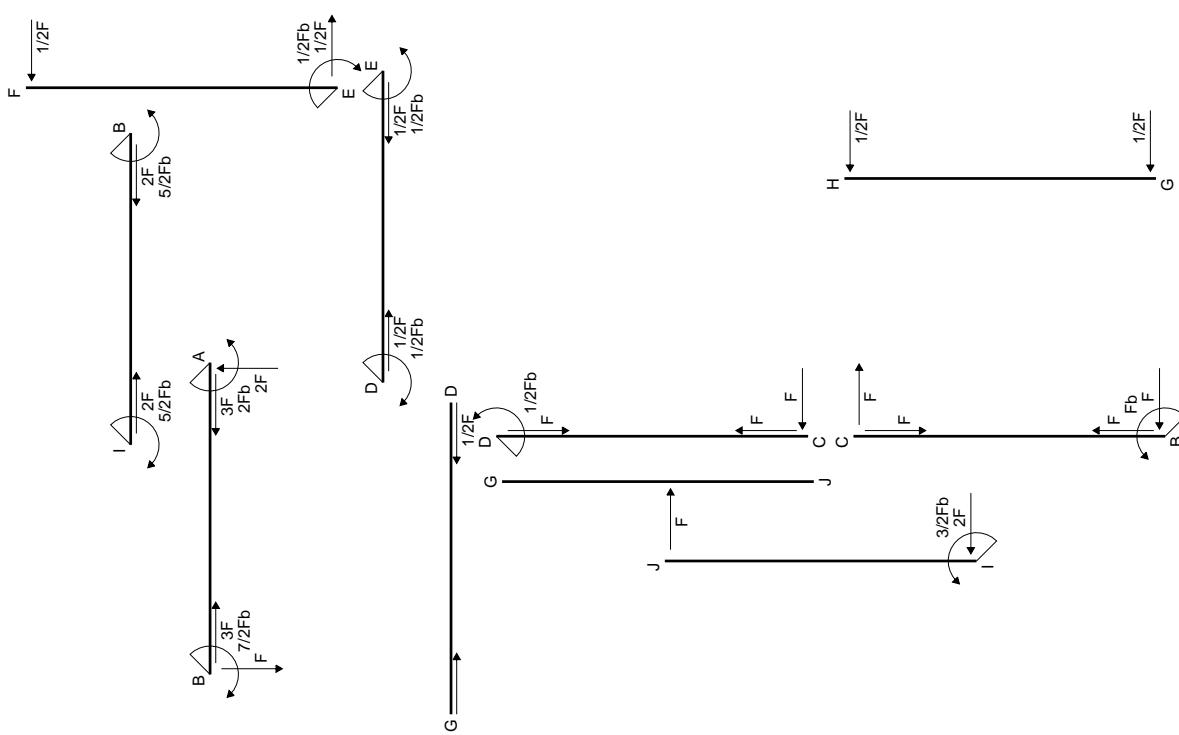
$$\begin{bmatrix} H_F b & V_F b & V_H b & H_{CB} b & V_{CB} b \end{bmatrix} \begin{bmatrix} Fb & W & qb^2 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & -1 & 0 \\ 2 & 2 & 2 & -1 & 0 \\ 2 & 1 & 1 & -1 & 1 \\ 2 & 1 & 0 & -1 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 0 & 2 \\ 1 & 0 & 0 \\ 1 & 0 & -1/2 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\text{Soluzione del sistema}$$

$$\begin{bmatrix} H_F b \\ V_F b \\ H_{CB} b \\ V_H b \\ V_{CB} b \end{bmatrix} = \begin{bmatrix} Fb \\ W \\ qb^2 \\ 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1/2 \\ -1 & 0 & 0 \\ 0 & 0 & 1/2 \\ 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} Fb \\ W \\ qb^2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$



EQUAZIONI DI EQUILIBRIO

Traslazione orizzontale: aste BI JU JG GD GH DC DE EF

$$H_F - H_{CB} = F$$

Rotazione intorno a J: aste JG GD GH DC DE EF

$$2H_F + 2V_F b + 2V_H b - H_{CB} b = Fb + 2qb^2$$

Rotazione intorno a G: aste GD GH DC DE EF

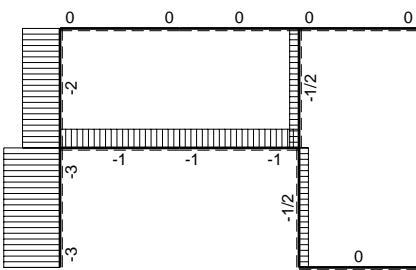
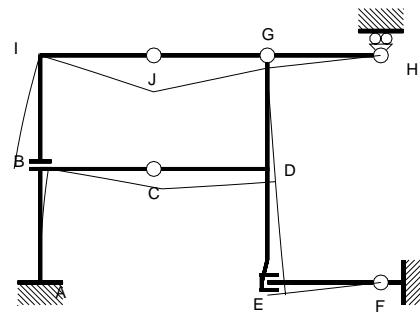
$$2H_F + V_F b + V_H b - H_{CB} b + V_{CB} b = Fb$$

Rotazione intorno a G: aste GD DC DE EF

$$2H_F + V_F b - H_{CB} b + V_{CB} b = Fb - 1/2qb^2$$

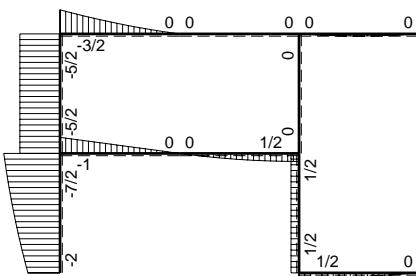
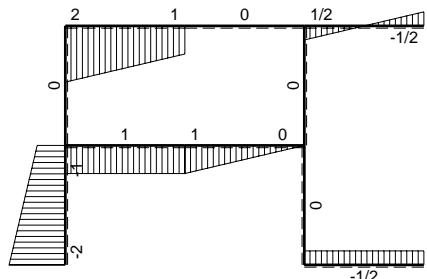
Traslazione orizzontale: aste EF

$$H_F = 0$$



$\square \rightarrow 12 F b^3 / E J$

$\leftarrow \square \rightarrow F$



$\uparrow \square \downarrow F$

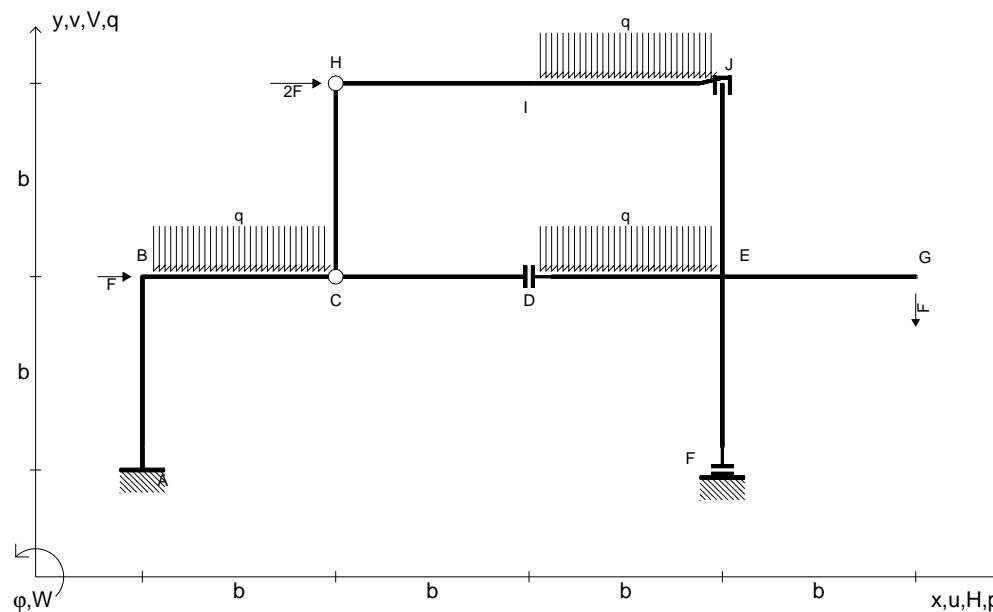
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$\curvearrowleft \square \curvearrowright F_b$

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13.01.16



$$\begin{array}{lllll}
 H_B = F & q_{BC} = -q = -F/b & EJ_{AB} = EJ & EJ_{DE} = EJ & EJ_{CH} = EJ \\
 V_G = -F & q_{DE} = -q = -F/b & EJ_{BC} = EJ & EJ_{EF} = EJ & EJ_{HI} = EJ \\
 H_H = 2F & q_{IJ} = -q = -F/b & EJ_{CD} = EJ & EJ_{EG} = EJ & EJ_{IJ} = EJ
 \end{array}$$

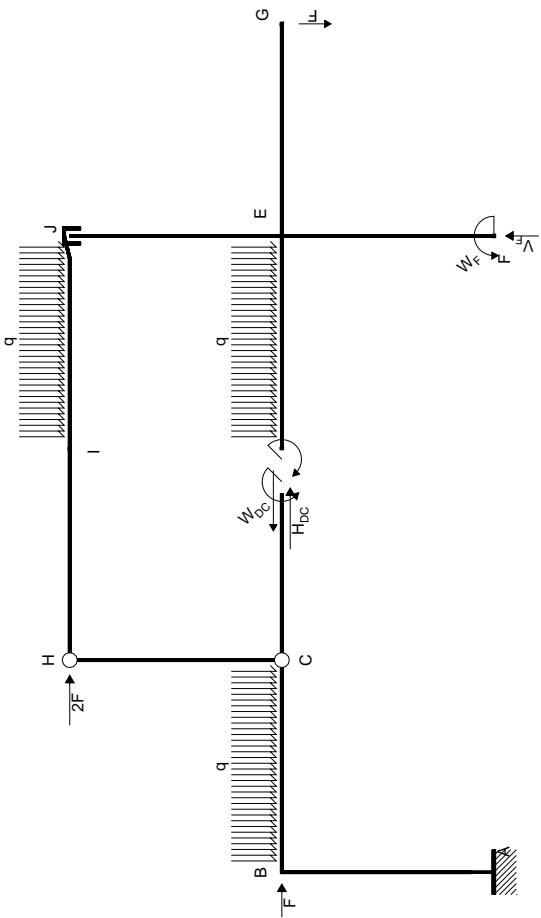
Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

$J_{yz} = X_{yz} = \theta_{yz}$ riferimento locale asta YZ con origine in Y.

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EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: aste CD CH HI Y JE ED EF EG

$$2V_r b + W_r = 5Fb + 3qb^2$$

Rotazione intorno a C: $\Sigma_{VFS} : VWF = \Sigma_{L2} : \Sigma_{L3}$ **aste CH HII** | E ED EE EG

Risoluzione in modo a C: \hat{a}

Detailed description of the detector is given in Section 2.

Rotazione intorno a H: a

$$2V_F b + W_F - H_{DC} b - W_{DC} = 3Fb + 3qb^2$$

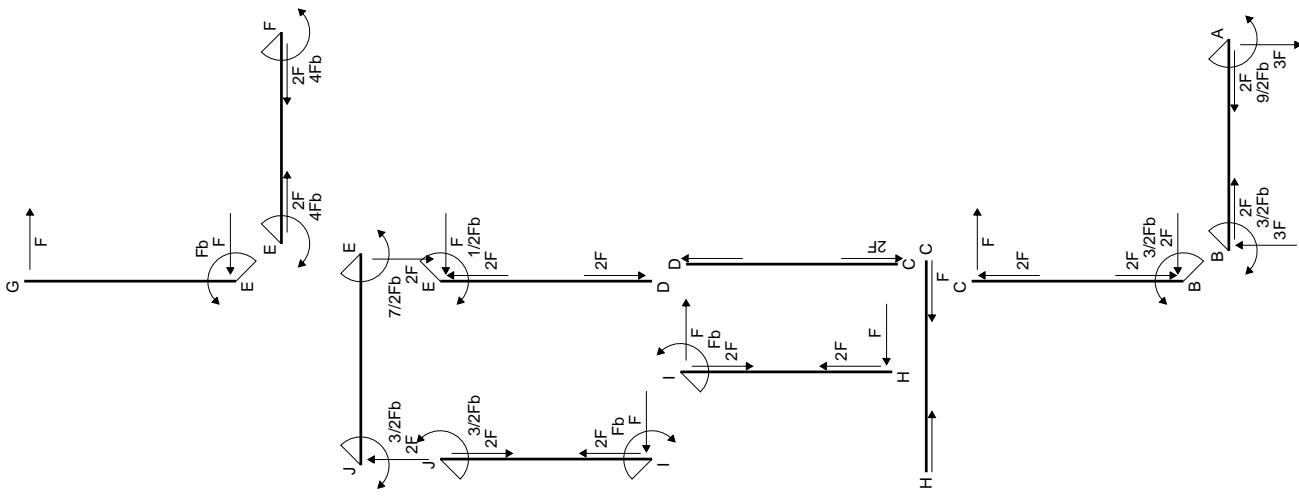
Traslazione verticale: as

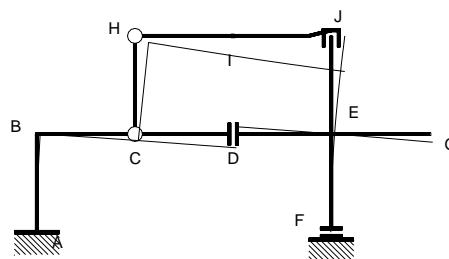
MATERIALS

$$\begin{matrix} \text{Matrice di equilibrio} \\ \left[\begin{matrix} V_F b & W_F & H_{DC} b & W_{DC} \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & -1 \\ 2 & 1 & -1 & -1 \\ 1 & 0 & 0 & 0 \end{matrix} \right] \end{matrix} = \begin{matrix} \left[\begin{matrix} Fb & qb^2 \\ 5 & 3 \\ 5 & 3 \\ 3 & 3 \\ 1 & 1 \end{matrix} \right] \end{matrix}$$

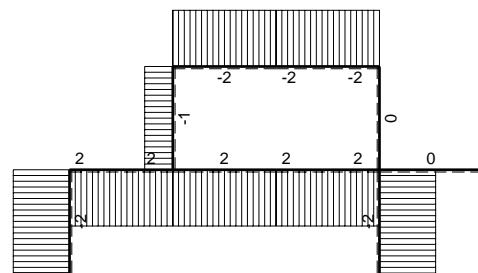
Soluzione del sistema

$$\begin{bmatrix} F_b & qb^2 \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 0 & 0 \\ 0 & 0 \\ 2 & 0 \\ 3 & 1 \end{bmatrix}$$

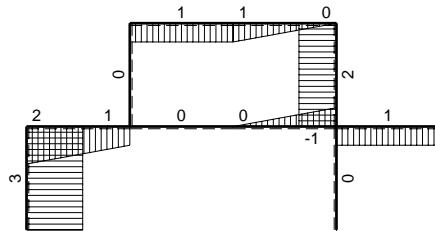




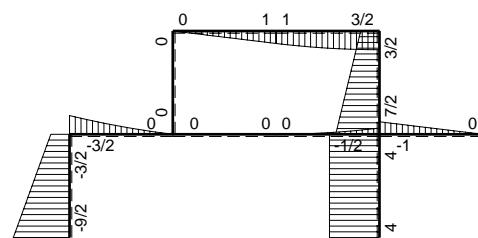
$\downarrow 40 F b^3 / E J$



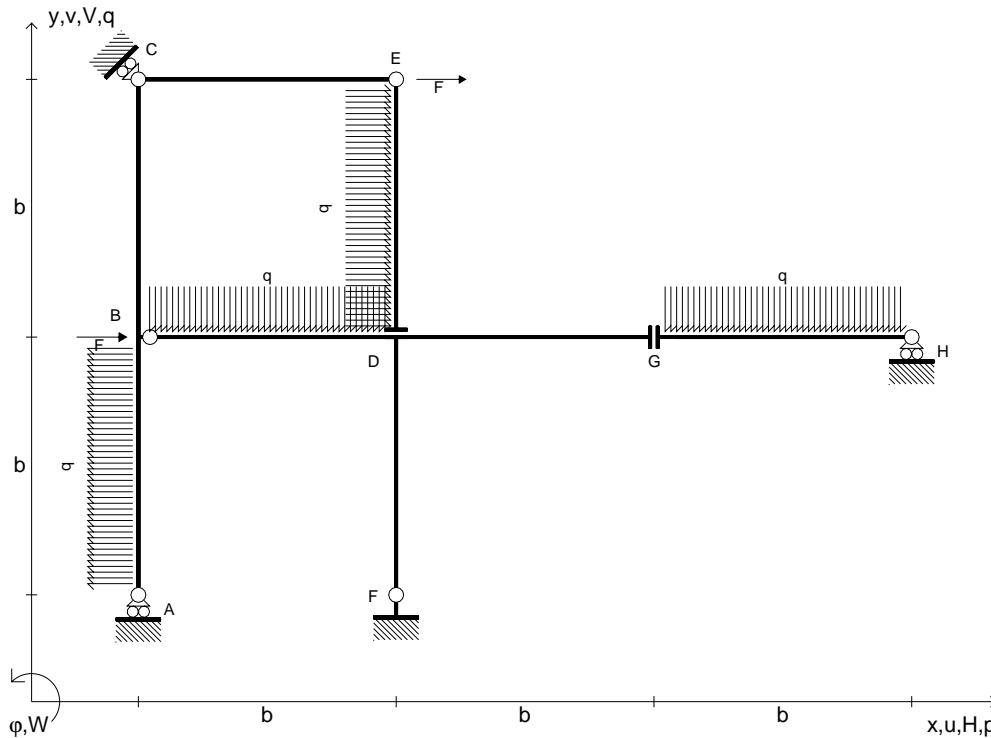
$\leftarrow \boxed{+} \rightarrow F$



$\uparrow \boxed{+} \downarrow F$



$\zeta \boxed{+} \zeta F_b$



$$\begin{aligned} H_E &= F \\ H_B &= F \\ p_{AB} &= -q = -F/b \\ q_{BD} &= -q = -F/b \end{aligned}$$

$$\begin{aligned} q_{GH} &= -q = -F/b \\ p_{DE} &= q = F/b \\ EJ_{AB} &= EJ \\ EJ_{BC} &= EJ \end{aligned}$$

$$\begin{aligned}EJ_{BD} &= EJ \\EJ_{DE} &= EJ \\EJ_{DF} &= EJ \\EJ_{DG} &= EJ\end{aligned}$$

$$\begin{aligned}EJ_{GH} &= EJ \\EJ_{EC} &= EJ\end{aligned}$$

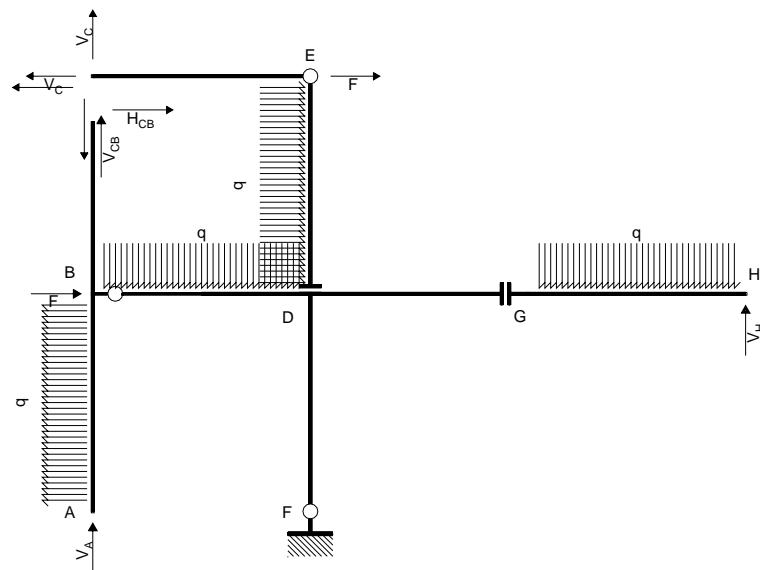
Carichi e deformazioni date hanno verso efficace in disegno.

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Piano di scorrimento del vincolo con inclinazione assegnata.



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a F

$$-V_A b + V_C b + 2V_H b = 3Fb + 2qb^2$$

Rotazione intorno a B: aste BA BC

$$-H_{CB}b = 1/2qb^2$$

Traslazione orizzontale: aste DE EC

$$-V_C - H_{CB} = -F - qb$$

Traslazione verticale: aste GH

$$V_H = qb$$

Rotazione intorno a E: aste EC

$$-V_C b + V_{CB} b = 0$$

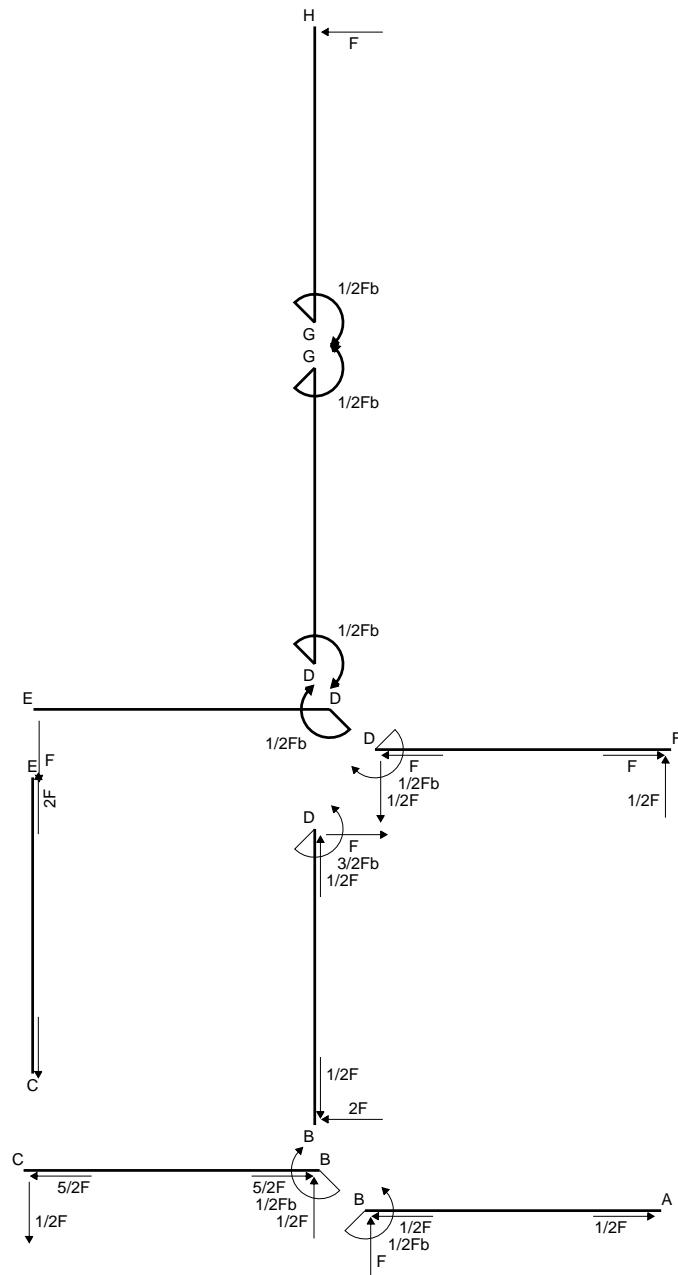
Matrice di equilibrio

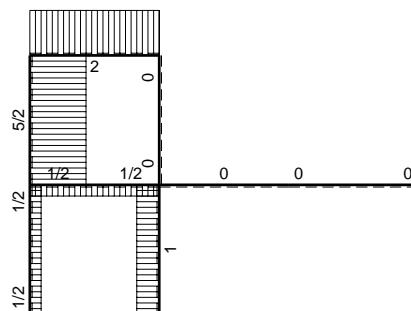
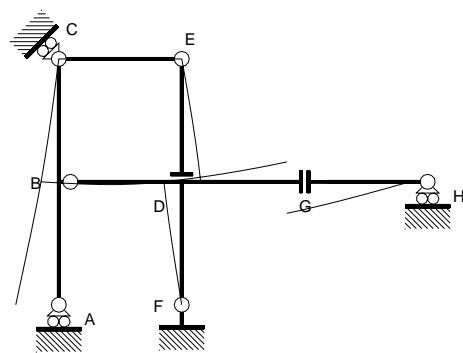
$$\begin{bmatrix} V_A b & V_C b & V_H b & H_{CB} b & V_{CB} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$

$$\begin{bmatrix} \Phi_F \\ \Phi_{BD} \\ U_{DE} \\ V_{GD} \\ \Phi_{EC} \end{bmatrix} = \begin{bmatrix} -1 & 1 & 2 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & -1 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & -1 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 3 & 2 \\ 0 & 1/2 \\ -1 & -1 \\ 0 & 1 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

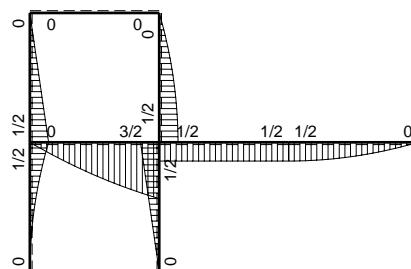
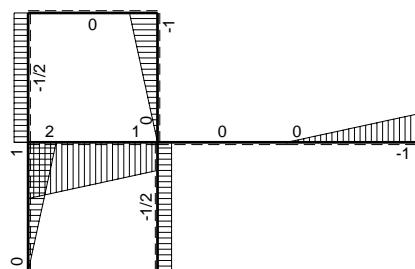
$$\begin{bmatrix} V_A b \\ H_{CB} b \\ V_C b \\ V_H b \\ V_{CB} b \end{bmatrix} = \begin{bmatrix} -2 & 3/2 \\ 0 & -1/2 \\ 1 & 3/2 \\ 0 & 1 \\ 1 & 3/2 \end{bmatrix}$$





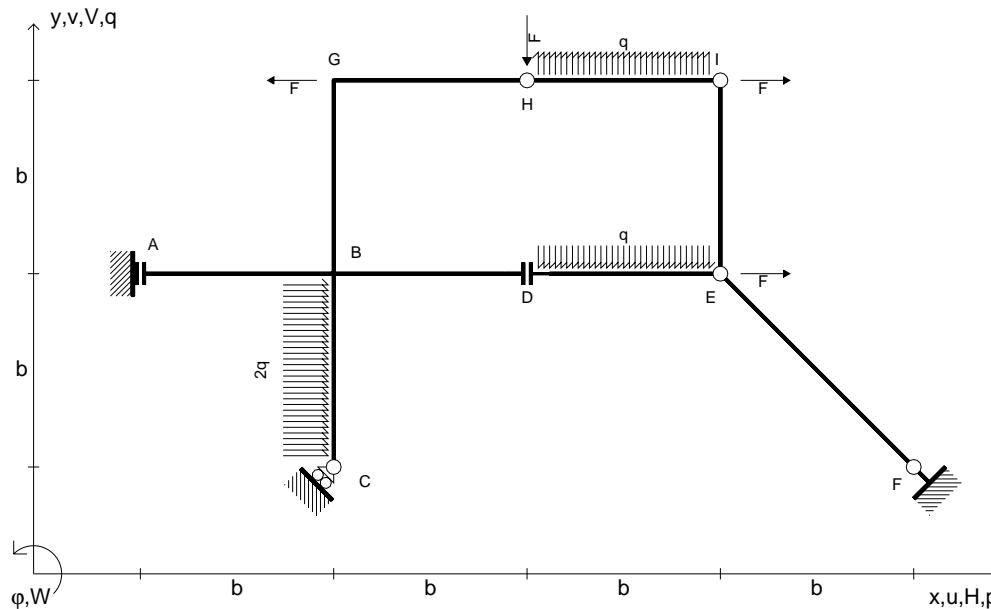
$\square - 3 Fb^3/EJ$

$\leftarrow \square + \rightarrow F$



$\uparrow \square \downarrow F$

$\square + \square \circ Fb$



$$H_E = F$$

$$H_G = -F$$

$$H_I = F$$

$$V_H = -F$$

$$q_{DE} = -q = -F/b$$

$$q_{HI} = q = F/b$$

$$p_{BC} = 2q = 2F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{BD} = EJ$$

$$EJ_{DE} = EJ$$

$$EJ_{EF} = EJ$$

$$EJ_{BG} = EJ$$

$$EJ_{GH} = EJ$$

$$EJ_{HI} = EJ$$

$$EJ_{IE} = EJ$$

Piano C

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

J_{YZ} - x_{YZ} - θ_{YZ} riferimento locale asta YZ con origine in Y.

Piano di scorrimento del vincolo con inclinazione assegnata.

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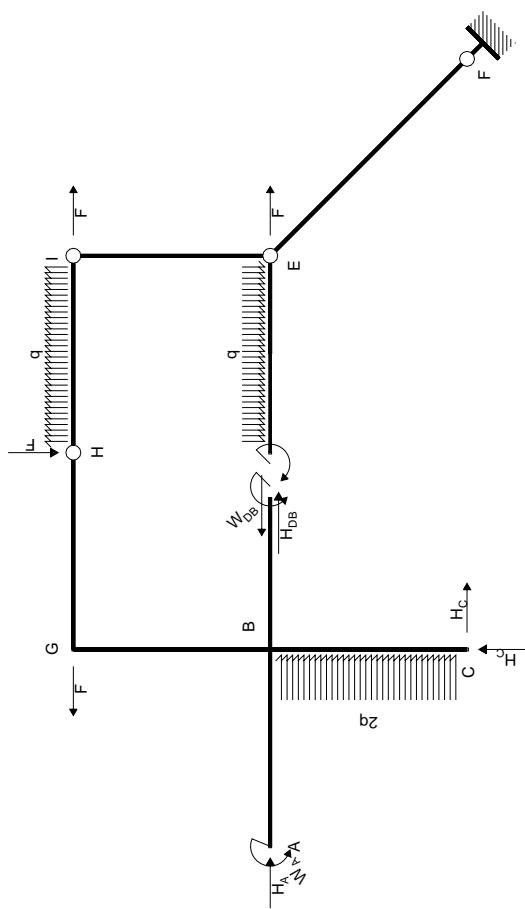
13.01.16

EQUILIBRIO Nome:

REAZIONI Nome:

Struttura Isostatica.001

Struttura Isostatica.001



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a F
 $-H_A b + W_A - 3H_C b = -Fb + qb^2$

Rotazione intorno a E: asta ED
 $-W_{DB} = -1/2qb^2$

Rotazione intorno a E: asta EI IH HG GB BA BC BD
 $W_A - H_C b + W_{DB} = -Fb - 1/2qb^2$

Rotazione intorno a I: asta IH HG GB BA BC BD
 $H_A b + W_A + H_{DB} b + W_{DB} = -Fb - 5/2qb^2$

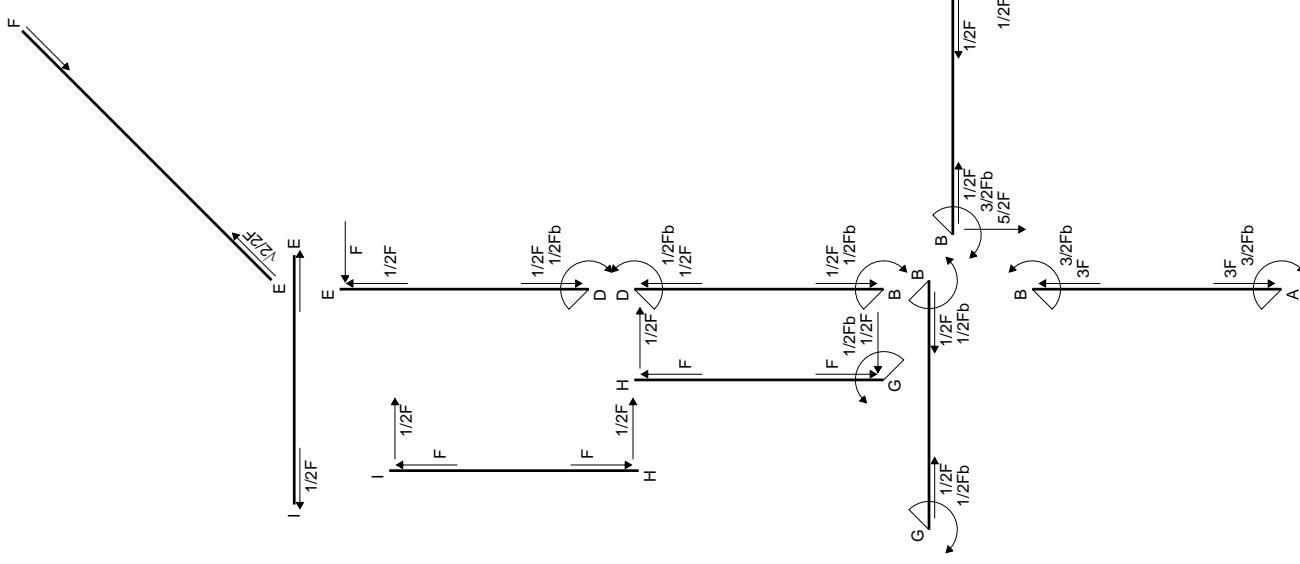
Rotazione intorno a H: asta HG GB BA BC BD
 $H_A b + W_A + H_C b + W_{DB} = -3qb^2$

Matrice di equilibrio

$$\begin{bmatrix} H_A b & W_A & H_C b & H_{DB} b & W_{DB} \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix} = \begin{bmatrix} -1 & 1 \\ 0 & 0 & 0 & 0 & -1 \\ 0 & 1 & -1 & 0 & 1 \\ 1 & 1 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} -1/2 \\ 0 \\ 1 \\ -1/2 \\ -5/2 \\ 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_A b \\ W_{DB} \\ H_C b \\ H_{DB} b \\ W_A \end{bmatrix} = \begin{bmatrix} Fb \\ qb^2 \\ -2 \\ 0 \\ 1/2 \\ 1 \\ -1/2 \\ 1 \\ -1/2 \\ 0 \\ -3/2 \end{bmatrix}$$

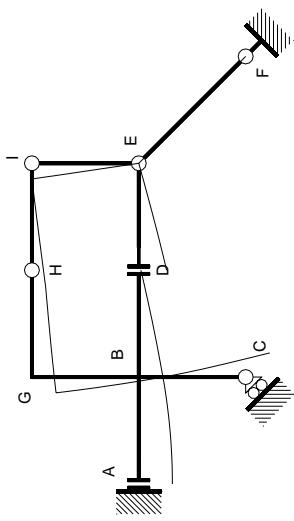


DEFORMATA E AZIONI INTERNE Nome:

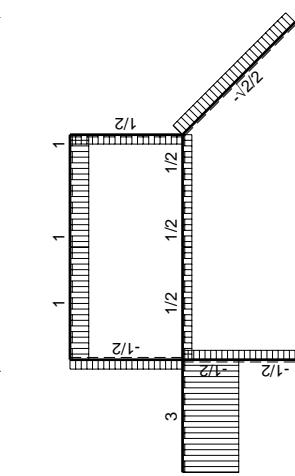
Struttura Isostatica.001

PROCEDIMENTO E RISULTATI Nome:

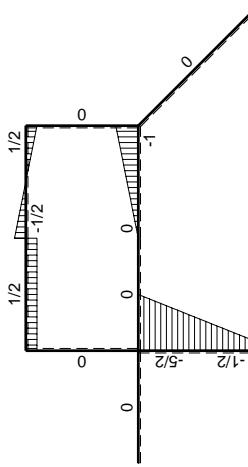
Struttura Isostatica.001



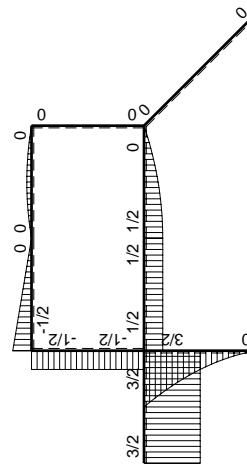
→ -6 Fb^3/EJ



← $\left[\begin{array}{c} + \\ - \end{array} \right] \rightarrow F$



↑ $\left[\begin{array}{c} + \\ - \end{array} \right] F$



$\zeta \left[\begin{array}{c} + \\ - \end{array} \right] F_b$