

EQUAZIONI DI EQUILIBRIO

Rotazione intorno a H: aste HG GF GI FE IJ

$$V_j b + H_{ED} b = 4Fb - 1/2 q b^2$$

Traslazione orizzontale: aste GF FE

$$-H_{ED} = -F$$

Rotazione intorno a F: aste FE

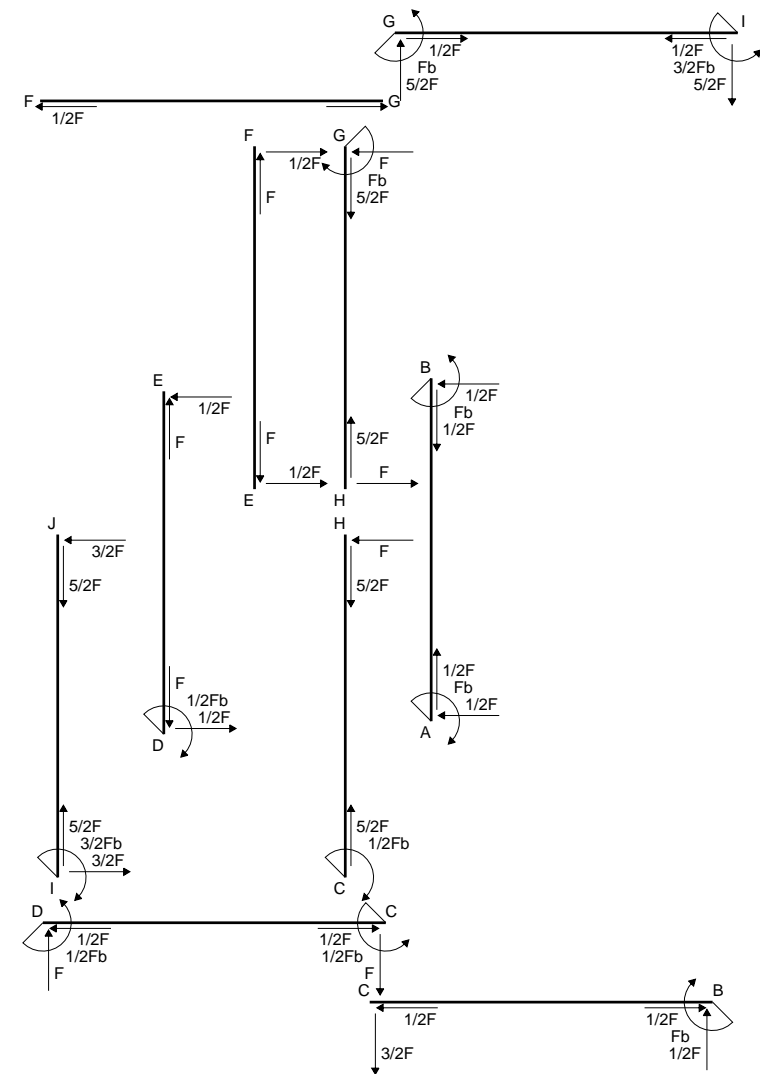
$$V_{ED}b = 1/2qb^2$$

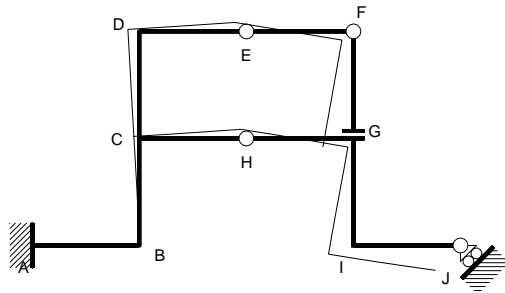
Matrice di equilibrio

$$\begin{bmatrix} \Phi_{HC} \\ u_{GF} \\ \Phi_{FE} \end{bmatrix} \begin{bmatrix} V_{Jb} & H_{EDb} & V_{EDb} \\ 1 & 1 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 4 & -1/2 \\ -1 & 0 \\ 0 & 1/2 \end{bmatrix}$$

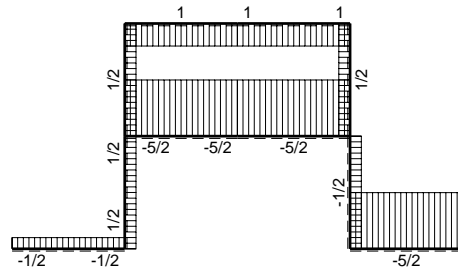
Soluzione del sistema

$$\begin{bmatrix} V_J b \\ H_{ED} b \\ V_{ED} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 3 & -1/2 \\ 1 & 0 \\ 0 & 1/2 \end{bmatrix}$$

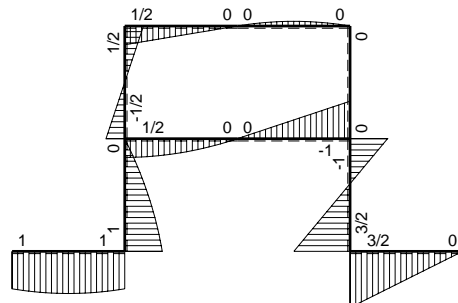
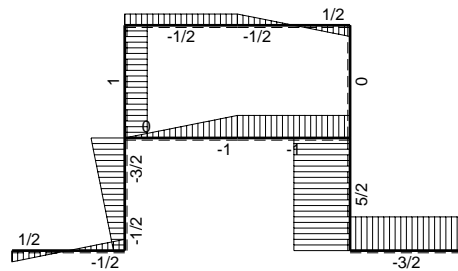


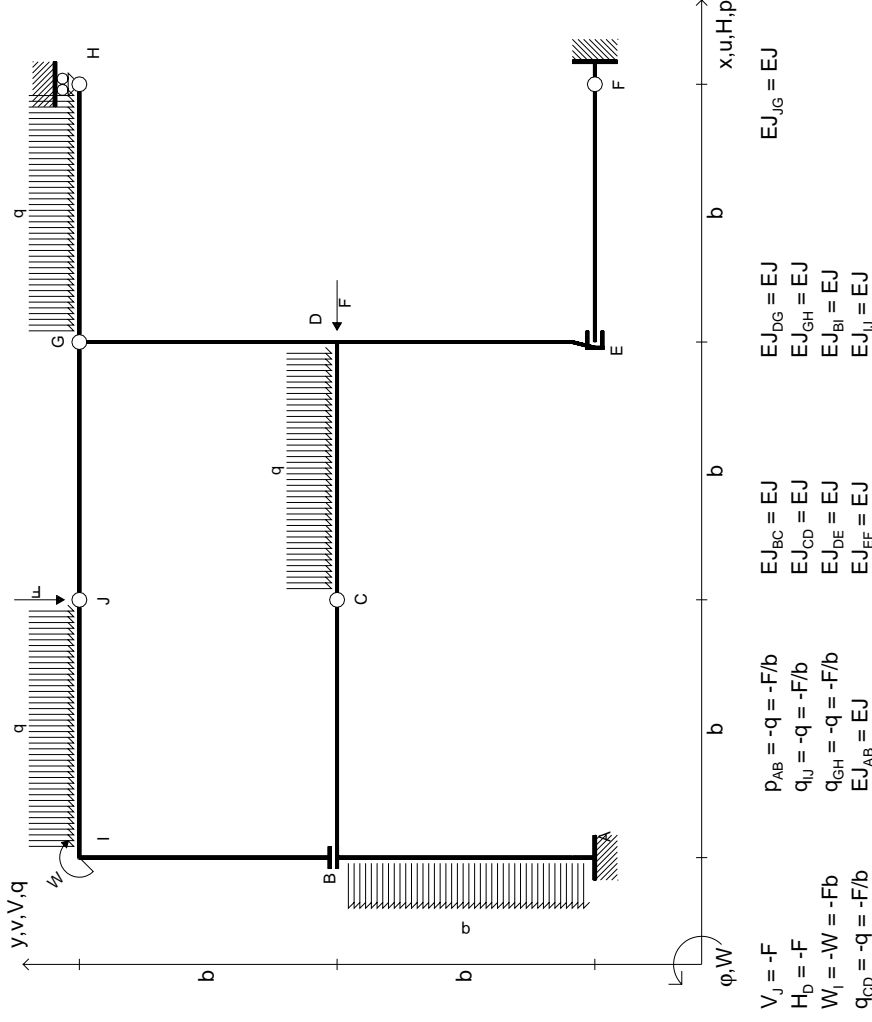


— 20 Fb³/EJ

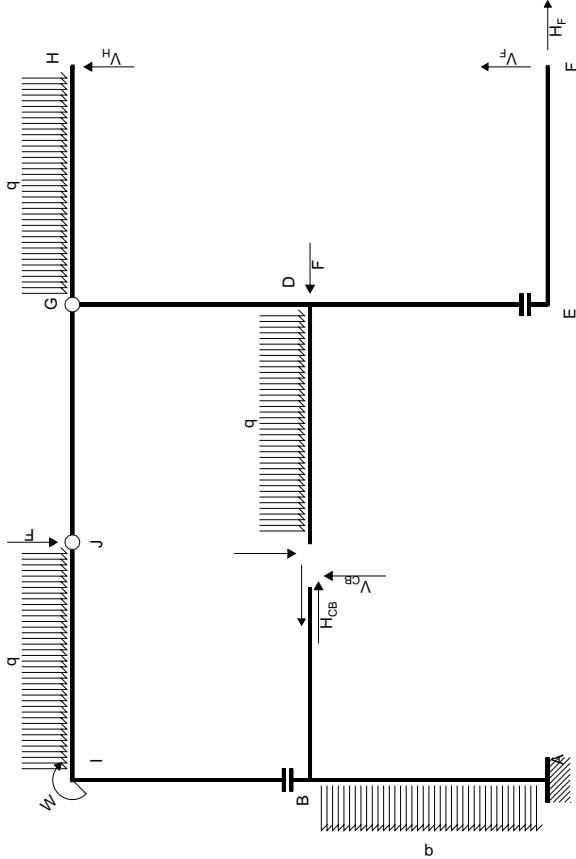


A diagram showing a square box with a plus sign (+) inside. An arrow points to the left from the left side of the box, and another arrow points to the right from the right side of the box. To the right of the right-pointing arrow is the letter 'F'.





Carichi e deformazioni date hanno verso efficace in disegno.
Calcolare reazioni vincolari della struttura e delle aste.
Tracciare i diagrammi quotati delle azioni interne nelle aste.
 $J_{YZ} = x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.
@ Adolfo Zavelani Rossi, Politecnico di Milano, vers.27.03.13



EQUAZIONI DI EQUILIBRIO

Traslazione orizzontale: aste BI IJ JG GD GH DC DE EF

$H_F - H_{CB} = F$

Rotazione intorno a J: aste JG GD GH DC DE EF

$2H_F b + 2V_F b + 2V_{Hb} - H_{CB} b = Fb + 2qb^2$

Rotazione intorno a G: aste GD GH DC DE EF

$2H_F b + V_F b + V_{Hb} - H_{CB} b + V_{CB} b = Fb$

Rotazione intorno a G: aste GD DC DE EF

$2H_F b + V_F b - H_{CB} b + V_{CB} b = Fb - 1/2qb^2$

Traslazione orizzontale: aste EF

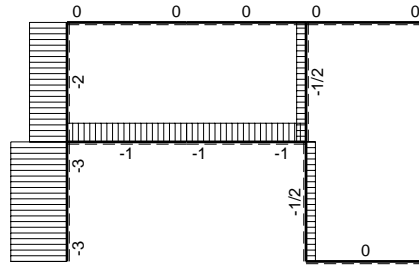
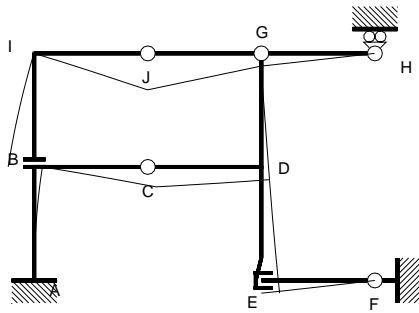
$H_F = 0$

Matrice di equilibrio

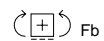
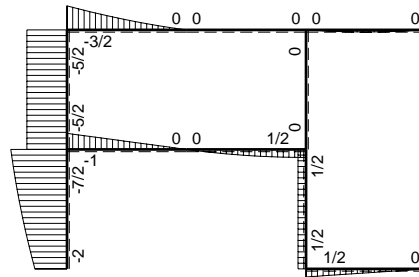
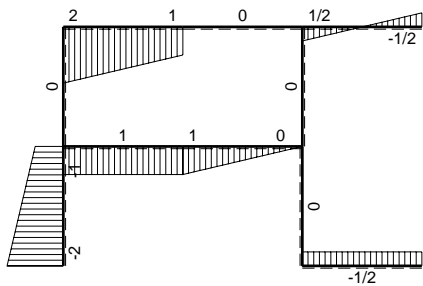
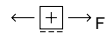
$$\begin{bmatrix} H_F b & V_F b & V_{Hb} & H_{CB} b & V_{CB} b \end{bmatrix} \begin{bmatrix} Fb & W & qb^2 \end{bmatrix}$$
$$\begin{bmatrix} 1 & 0 & 0 & -1 & 0 \\ 2 & 2 & 2 & -1 & 0 \\ 2 & 1 & 1 & -1 & 1 \\ 2 & 1 & 0 & -1 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 0 & 2 \\ 1 & 0 & 0 \\ 1 & 0 & -1/2 \\ 0 & 0 & 0 \end{bmatrix}$$

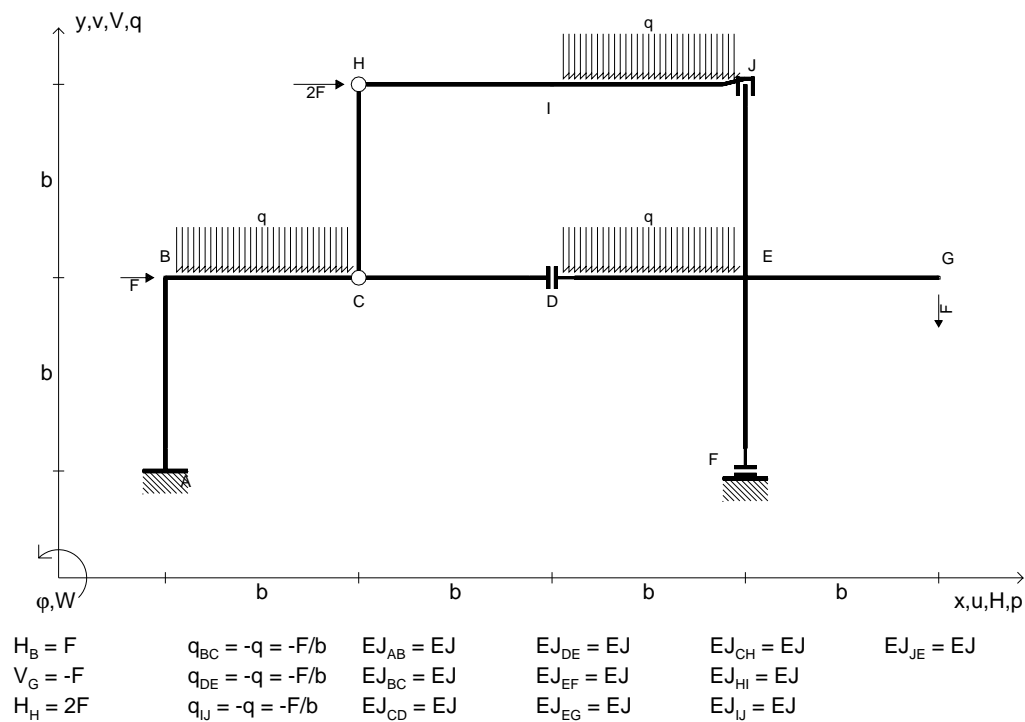
Soluzione del sistema

$$\begin{bmatrix} H_F b \\ V_F b \\ H_{CB} b \\ V_{Hb} \\ V_{CB} b \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1/2 \\ -1 & 0 & 0 \\ 0 & 0 & 1/2 \\ 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} Fb & W & qb^2 \end{bmatrix}$$



12 Fb³/EJ





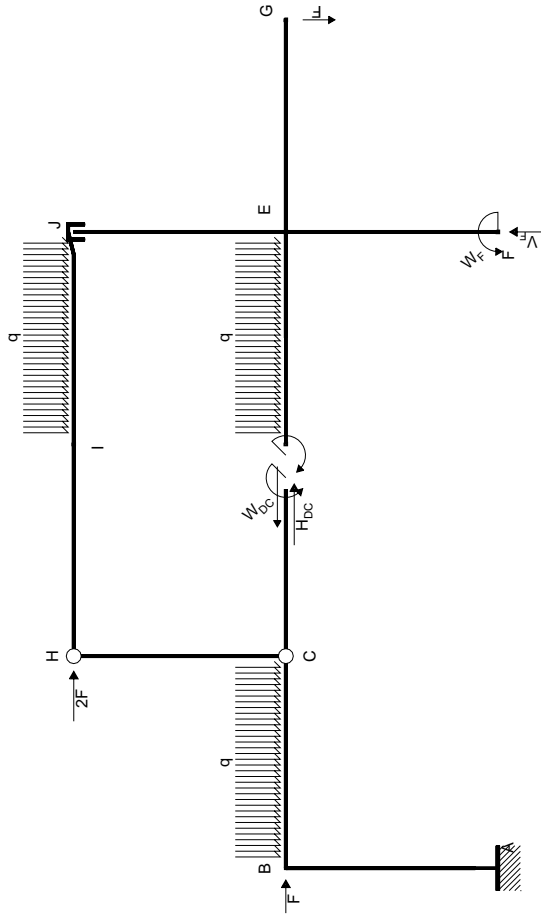
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Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: aste CD CH HI IJ JE ED EF EG

$2V_F b + W_F = 5Fb + 3qb^2$

Rotazione intorno a C: aste CH HI IJ JE ED EF EG

$2V_F b + W_F - W_{DC} = 5Fb + 3qb^2$

Rotazione intorno a H: aste HI IJ JE ED EF EG

$2V_F b + W_F - H_{DC} b - W_{DC} = 3Fb + 3qb^2$

Traslazione verticale: aste JE ED EF EG

$V_F = F + qb$

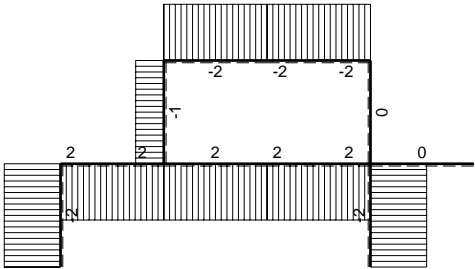
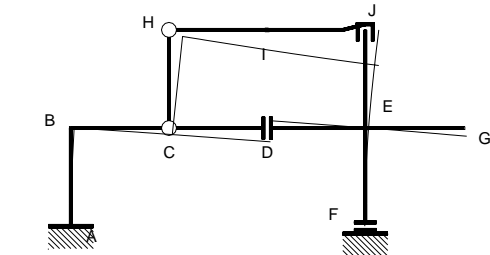
Matrice di equilibrio

$$\begin{bmatrix} V_F b & W_F & H_{DC} b & W_{DC} \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix} = \begin{bmatrix} 5 & 3 \\ 5 & 3 \\ 3 & 3 \\ 1 & 1 \end{bmatrix}$$

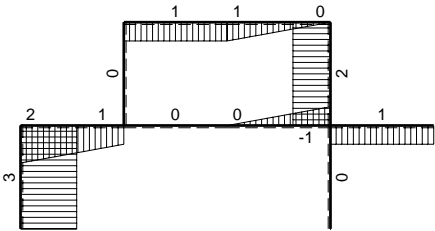
Soluzione del sistema

$$\begin{bmatrix} V_F b \\ W_{DC} \\ H_{DC} b \\ W_F \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 0 & 0 \\ 2 & 0 \\ 3 & 1 \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$

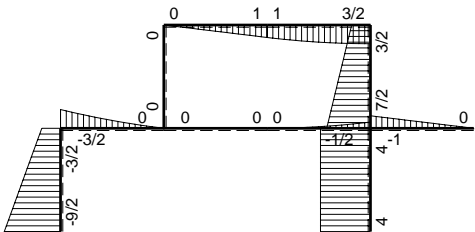
$\frac{1}{40} \frac{Fb^3}{EJ}$



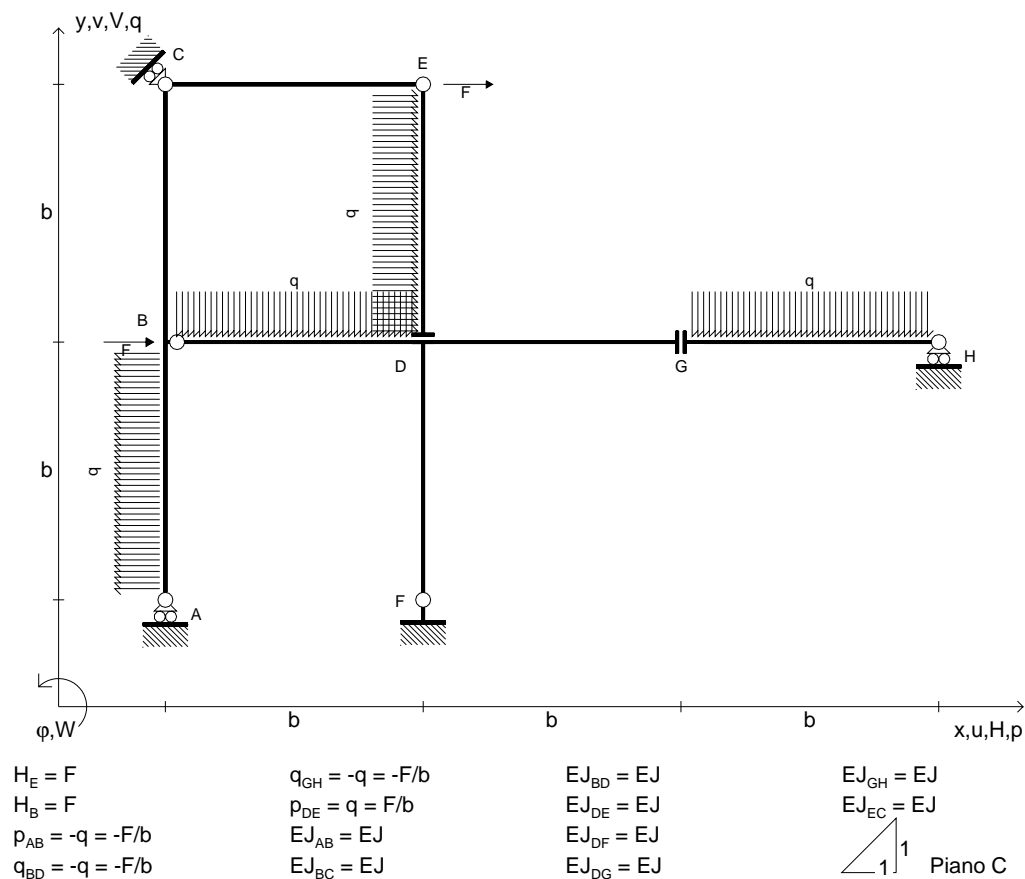
$\leftarrow \boxed{+} \rightarrow F$



$\uparrow \boxed{+} \downarrow F$



$\curvearrowright \boxed{+} \curvearrowleft Fb$



Carichi e deformazioni date hanno verso efficace in disegno.

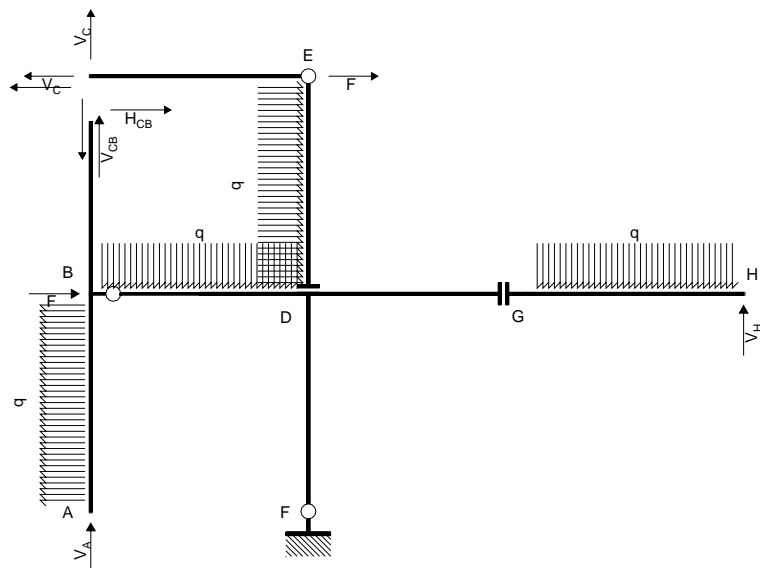
Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

Piano di scorrimento del vincolo con inclinazione assegnata.

@ Adolfo Zavelani Rossi, Politecnico di Milano, vers.27.03.13



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a F

$$-V_A b + V_C b + 2V_H b = 3Fb + 2qb^2$$

Rotazione intorno a B: aste BA BC

$$-H_{CB} b = 1/2 qb^2$$

Traslazione orizzontale: aste DE EC

$$-V_C - H_{CB} = -F - qb$$

Traslazione verticale: aste GH

$$V_H = qb$$

Rotazione intorno a E: aste EC

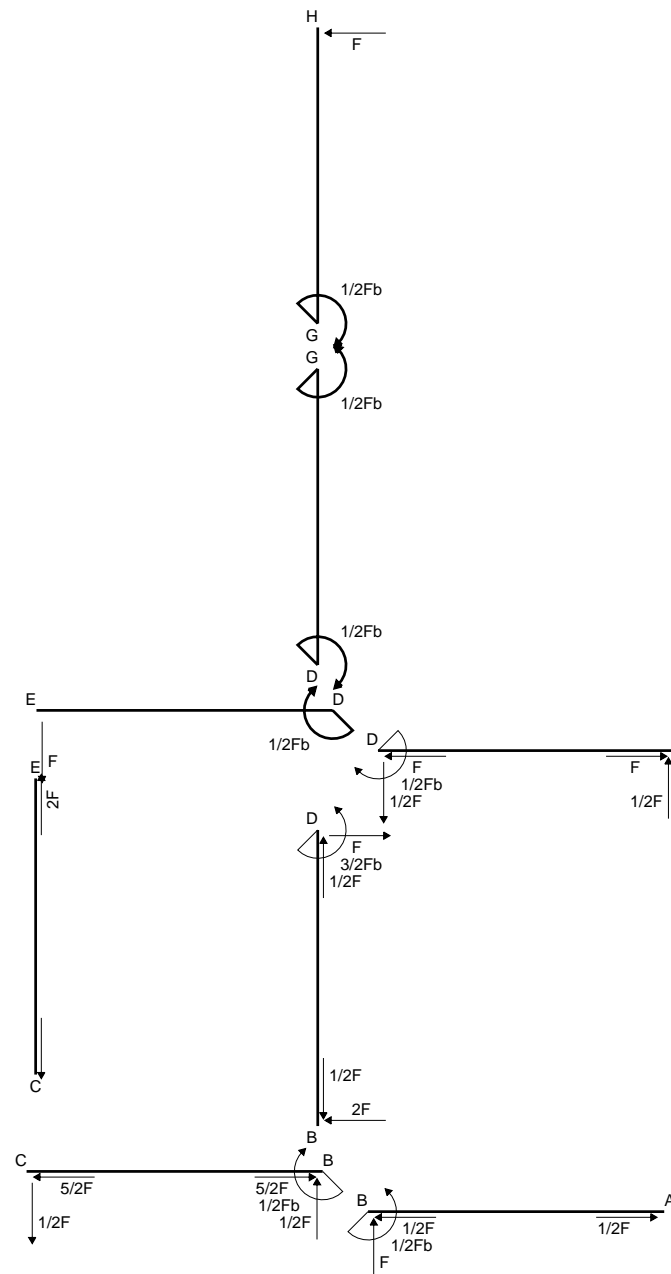
$$-V_C b + V_{CB} b = 0$$

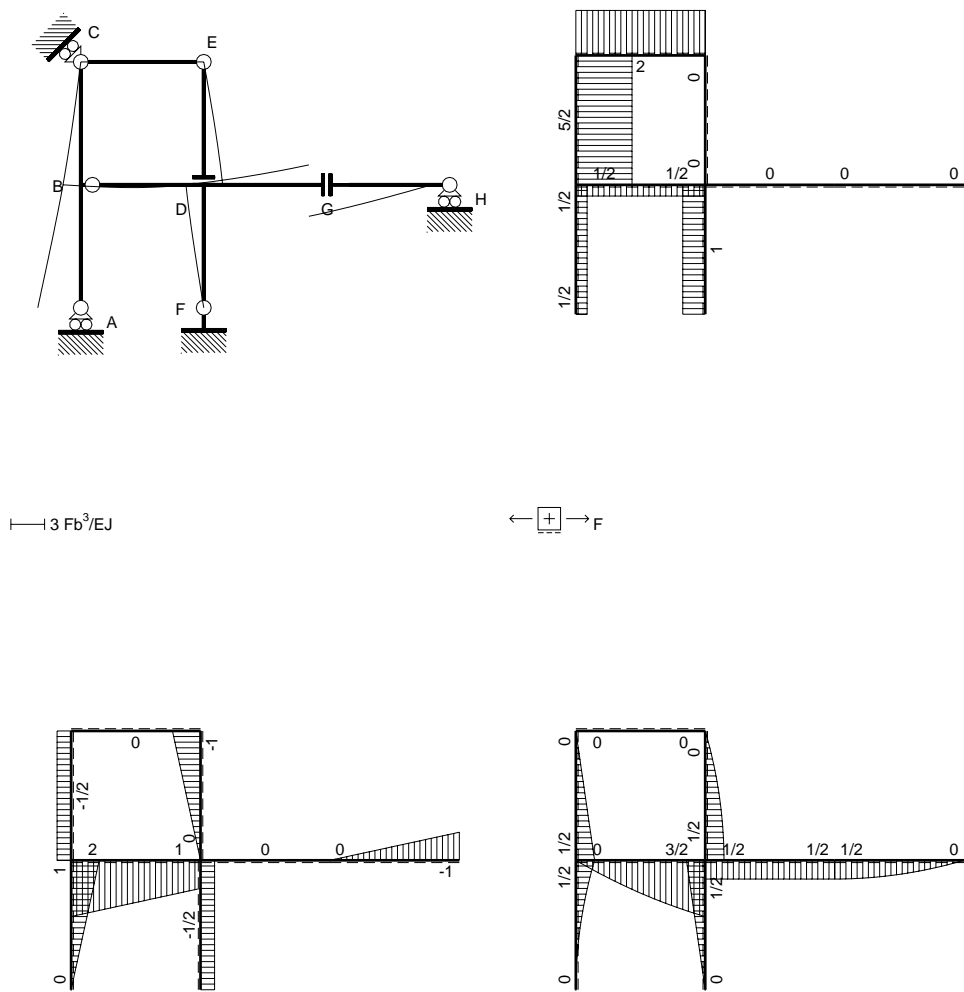
Matrice di equilibrio

$$\begin{bmatrix} \varphi_F \\ \varphi_{BD} \\ u_{DE} \\ v_{GD} \\ \varphi_{EC} \end{bmatrix} \begin{bmatrix} V_A b & V_C b & V_H b & H_{CB} b & V_{CB} b \\ -1 & 1 & 2 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & -1 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & -1 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 3 & 2 \\ 0 & 1/2 \\ -1 & -1 \\ 0 & 1 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

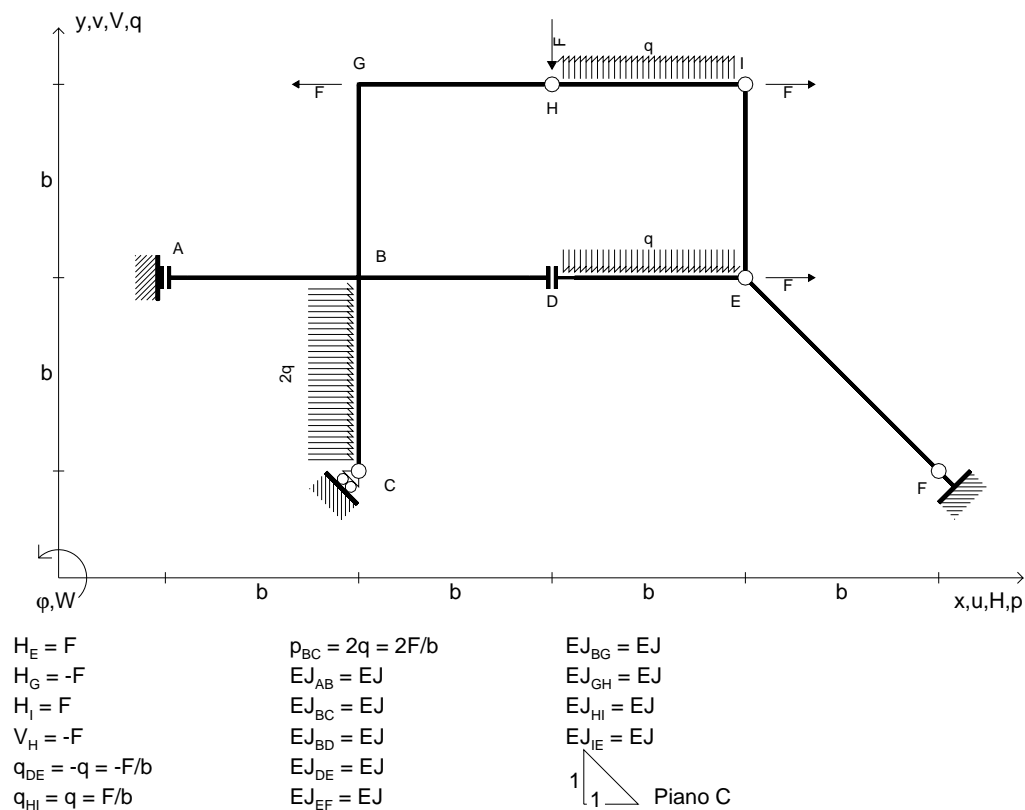
$$\begin{bmatrix} V_A b \\ H_{CB} b \\ V_C b \\ V_H b \\ V_{CB} b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -2 & 3/2 \\ 0 & -1/2 \\ 1 & 3/2 \\ 0 & 1 \\ 1 & 3/2 \end{bmatrix}$$





$\uparrow \downarrow F$

$\uparrow \downarrow F_b$



Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

J_{YZ} - x_{YZ} - θ_{YZ} riferimento locale asta YZ con origine in Y.

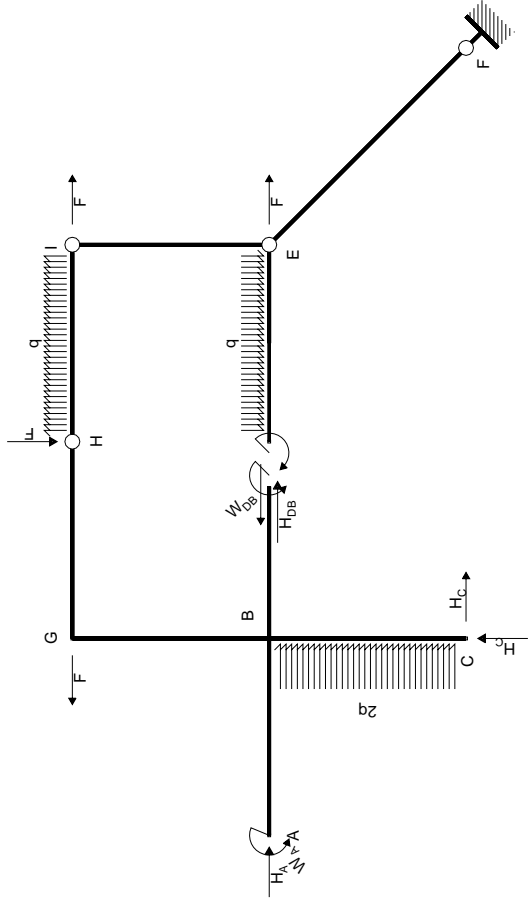
Piano di scorrimento del vincolo con inclinazione assegnata.

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13.01.16

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13.01.16



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a F

$-H_A b + W_A - 3H_C b = -Fb + qb^2$

Rotazione intorno a E: aste ED

$-W_{DB} = -1/2qb^2$

Rotazione intorno a E: aste EI IH HG GB BA BC BD

$W_A - H_C b + W_{DB} = -Fb - 1/2qb^2$

Rotazione intorno a I: aste IH HG GB BA BC BD

$H_A b + W_A + H_{DB} b + W_{DB} = -Fb - 5/2qb^2$

Rotazione intorno a H: aste HG GB BA BC BD

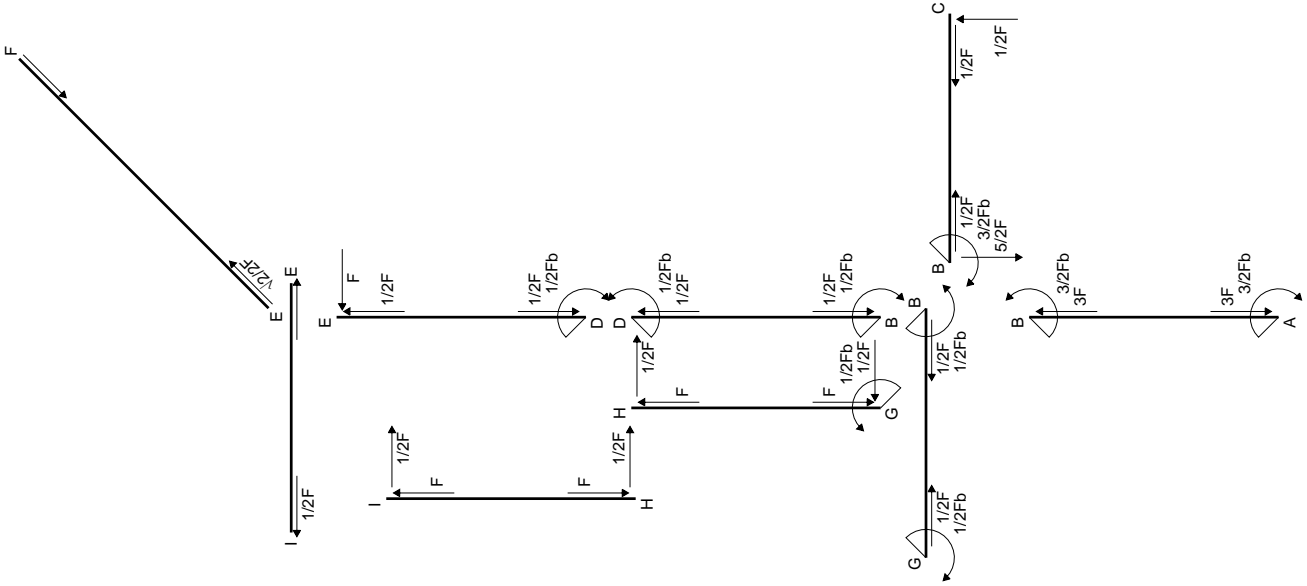
$H_A b + W_A + H_C b + H_{DB} b + W_{DB} = -3qb^2$

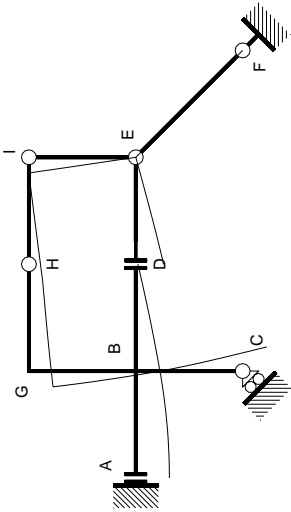
Matrice di equilibrio

$$\begin{bmatrix} H_A b & W_A & H_C b & H_{DB} b & W_{DB} \\ \varphi_F & -1 & 1 & -3 & 0 & 0 \\ \varphi_{ED} & 0 & 0 & 0 & -1 & 0 \\ \varphi_{EI} & 0 & 1 & -1 & 0 & 1 \\ \varphi_{IH} & 1 & 1 & 0 & 1 & 1 \\ \varphi_{HG} & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix} = \begin{bmatrix} -1 & 1 \\ 0 & -1/2 \\ -1 & -1/2 \\ -1 & -5/2 \\ 0 & -3 \end{bmatrix}$$

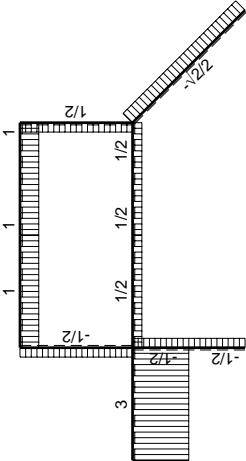
Soluzione del sistema

$$\begin{bmatrix} H_A b \\ W_{DB} \\ H_C b \\ H_{DB} b \\ W_A \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix} = \begin{bmatrix} -2 & -1 \\ 0 & 1/2 \\ 1 & -1/2 \\ 1 & -1/2 \\ 0 & -3/2 \end{bmatrix}$$

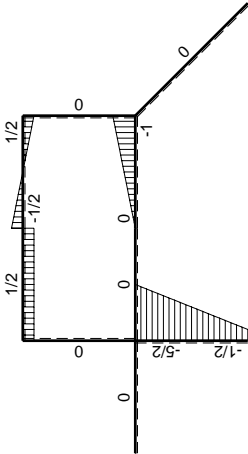




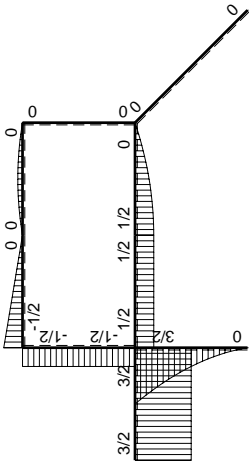
$\frac{1}{6} F b^3 / E J$



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