

$$H_C = F$$

$$q_{BD} = -q = -F/b$$

$$p_{FG} = -q = -F/b$$

$$q_{GH} = -q = -F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{BD} = EJ$$

$$EJ_{DE} = EJ$$

$$EJ_{DF} = EJ$$

$$EJ_{FG} = EJ$$

$$EJ_{GH} = EJ$$

$$EJ_{GI} = EJ$$

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

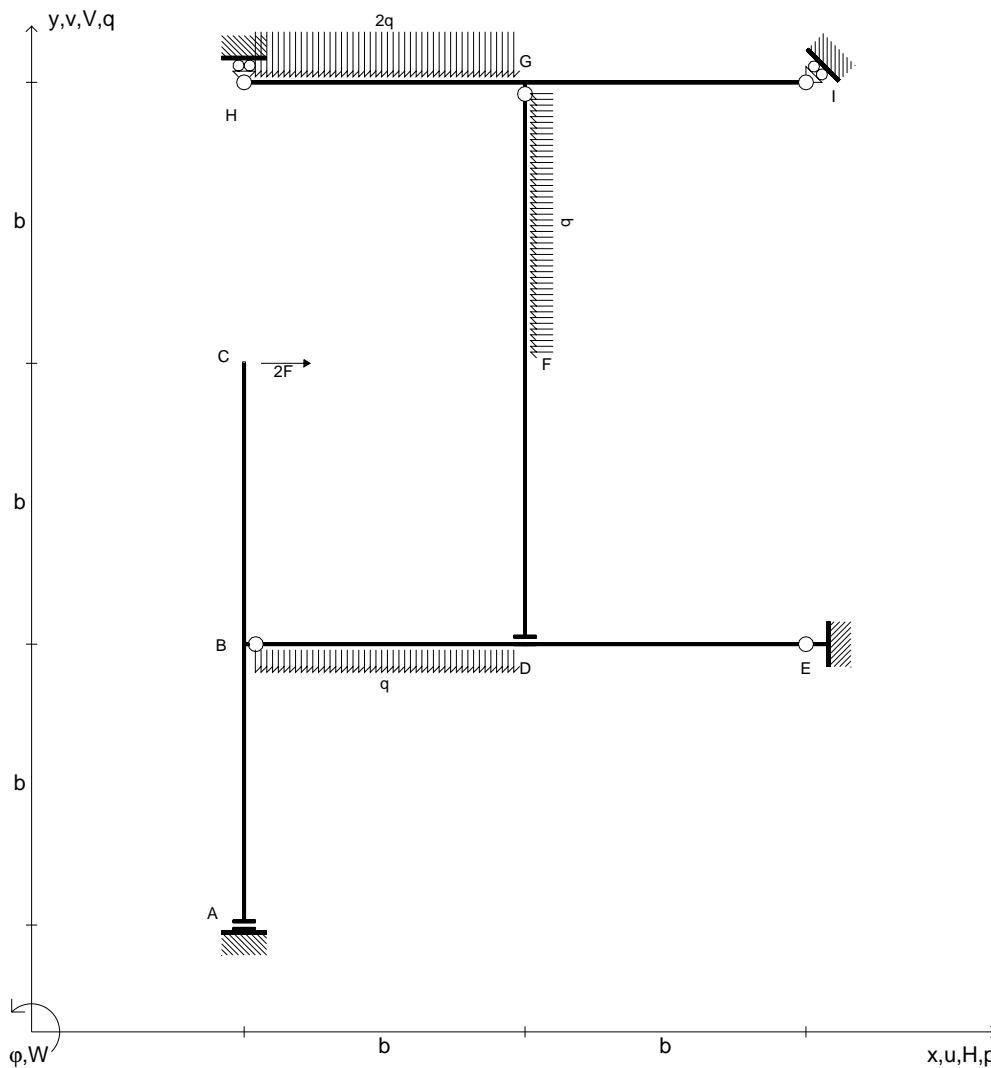
Tracciare i diagrammi quotati delle azioni interne nelle aste.

$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

Piano di scorrimento del vincolo con inclinazione assegnata.

@ Adolfo Zavelani Rossi, Politecnico di Milano, vers.27.03.13





$$H_C = 2F$$

$$q_{BD} = -q = -F/b$$

$$p_{FG} = -q = -F/b$$

$$q_{GH} = -2q = -2F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{BD} = EJ$$

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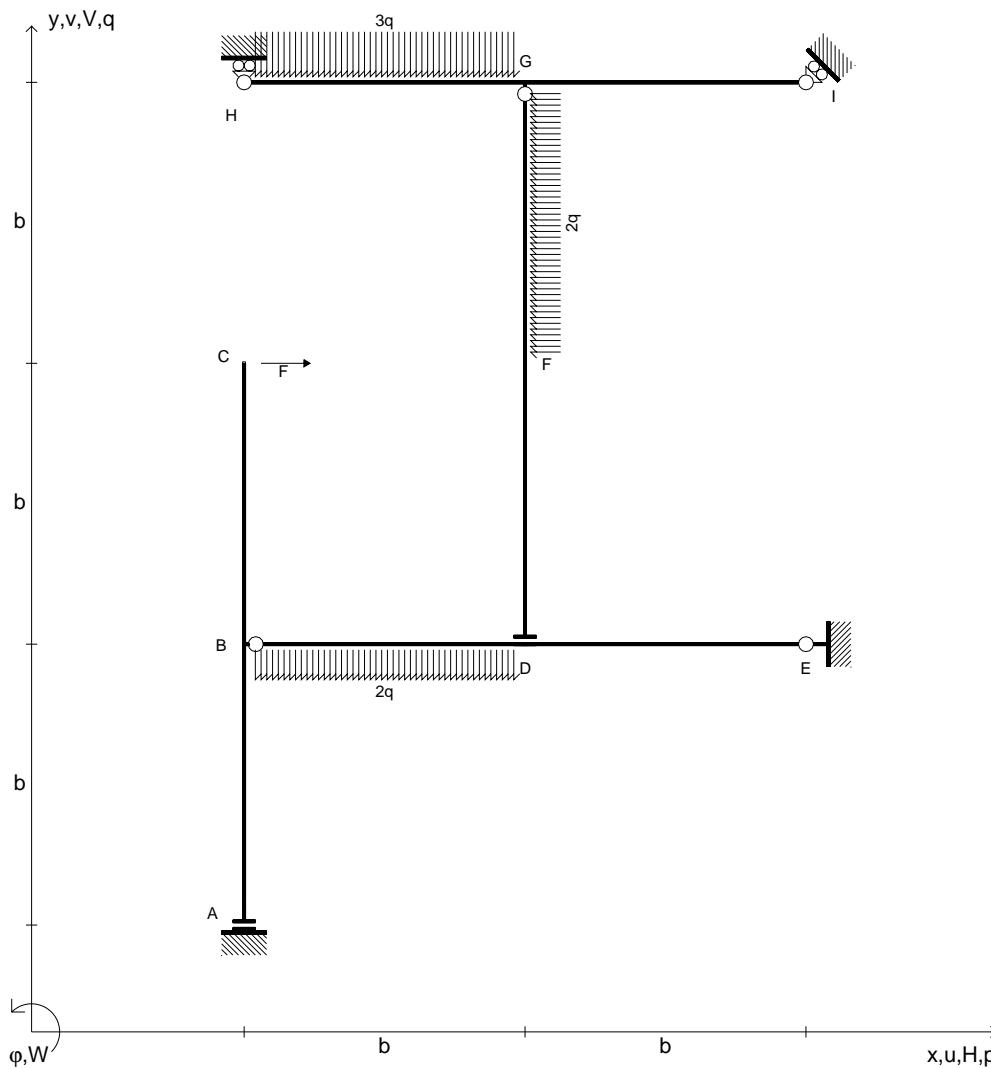
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Piano di scorrimento del vincolo con inclinazione assegnata.



$$H_C = F$$

$$q_{BD} = -2q = -2F/b$$

$$p_{FG} = -2q = -2F/b$$

$$q_{GH} = -3q = -3F/b$$

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$$EJ_{BC} = EJ$$

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$$EJ_{DE} = EJ$$

$$EJ_{DF} = EJ$$

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Carichi e deformazioni date hanno verso efficace in disegno.

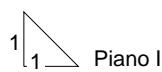
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$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

Piano di scorrimento del vincolo con inclinazione assegnata.

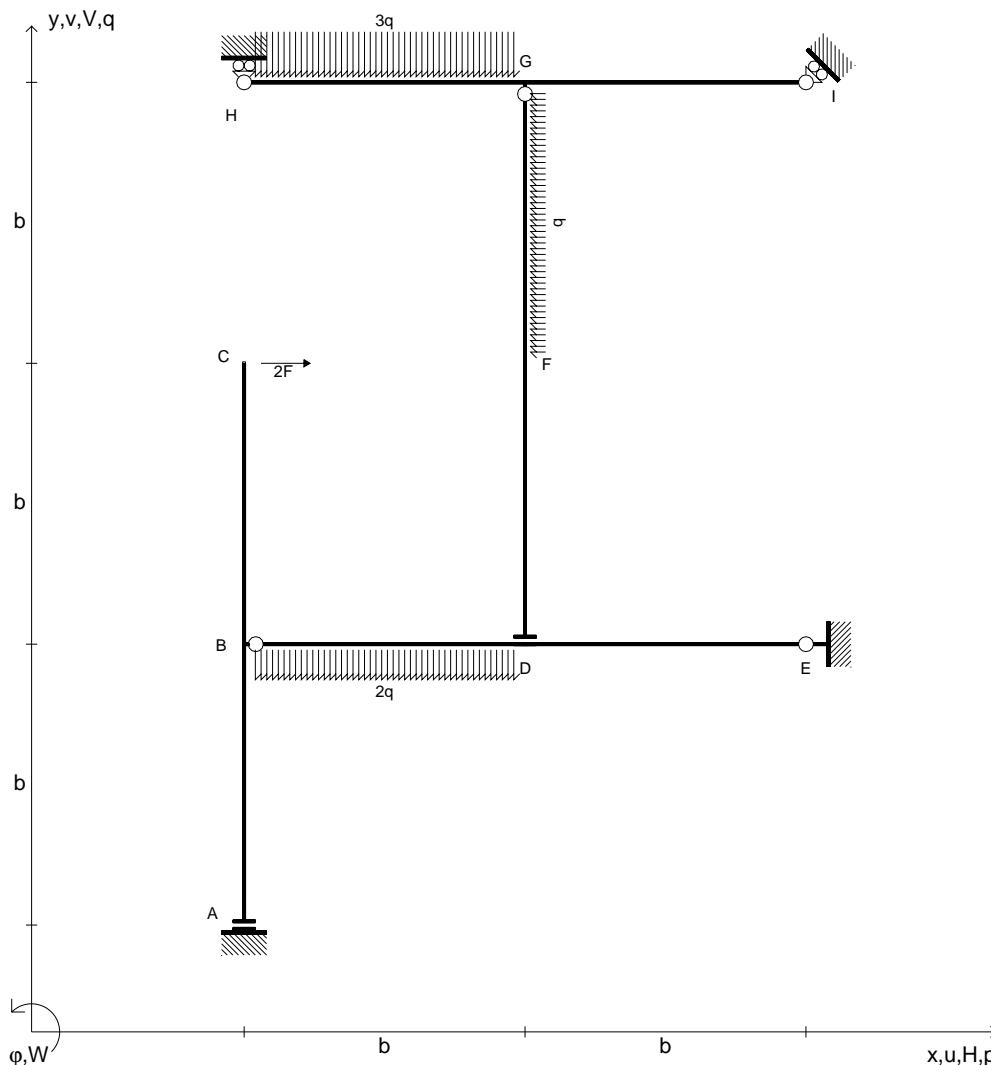
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13.11.13

@ Adolfo Zavelani Rossi, Politecnico di Milano, vers.27.03.13

13.11.13



$$H_C = 2F$$

$$q_{BD} = -2q = -2F/b$$

$$p_{FG} = -q = -F/b$$

$$q_{GH} = -3q = -3F/b$$

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$$EJ_{BC} = EJ$$

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$$EJ_{DF} = EJ$$

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Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

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$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

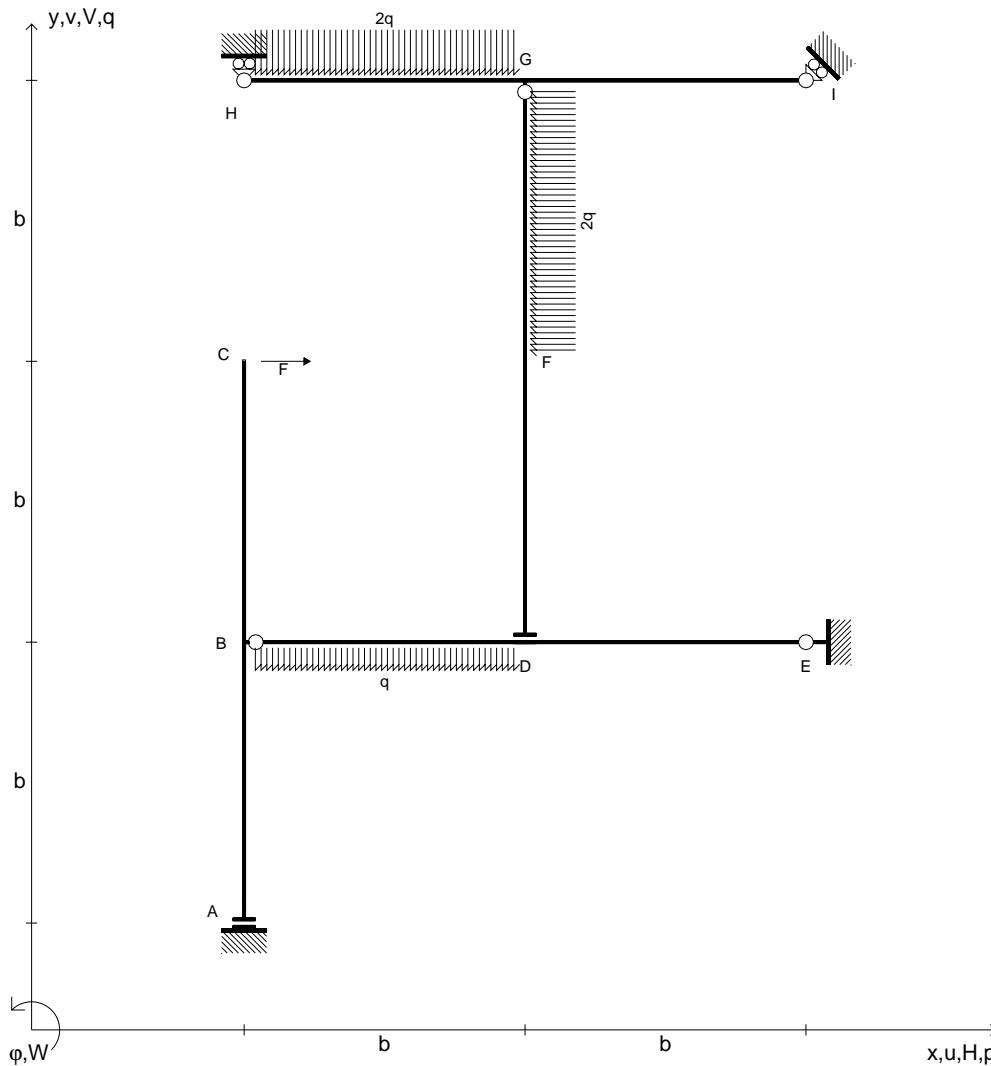
Piano di scorrimento del vincolo con inclinazione assegnata.

@ Adolfo Zavelani Rossi, Politecnico di Milano, vers.27.03.13

13.11.13

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$$H_C = F$$

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$$EJ_{DE} = EJ$$

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$$EJ_{GH} = EJ$$

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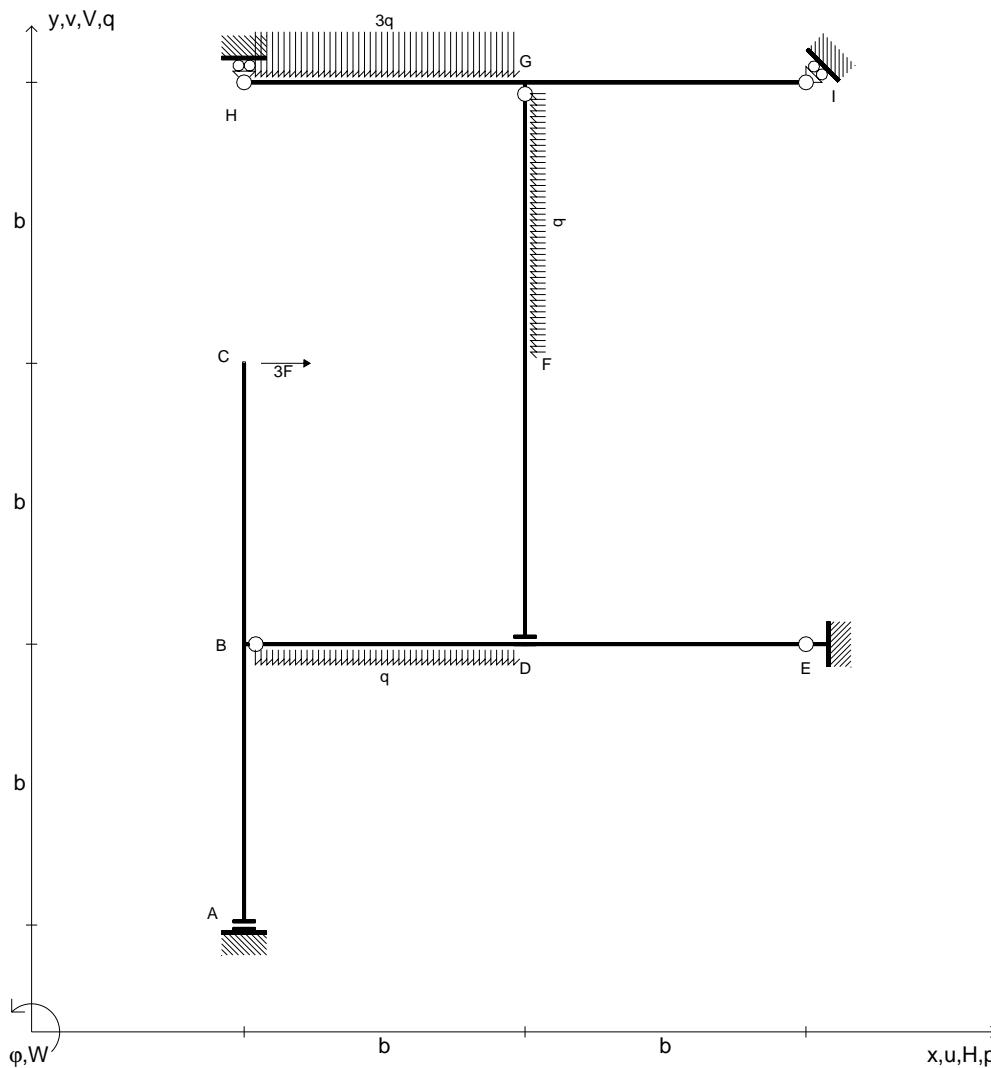
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Tracciare i diagrammi quotati delle azioni interne nelle aste.

$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

Piano di scorrimento del vincolo con inclinazione assegnata.



$$H_C = 3F$$

$$q_{BD} = -q = -F/b$$

$$p_{FG} = -q = -F/b$$

$$q_{GH} = -3q = -3F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{BD} = EJ$$

$$EJ_{DE} = EJ$$

$$EJ_{DF} = EJ$$

$$EJ_{FG} = EJ$$

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Carichi e deformazioni date hanno verso efficace in disegno.

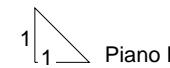
Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

Piano di scorrimento del vincolo con inclinazione assegnata.

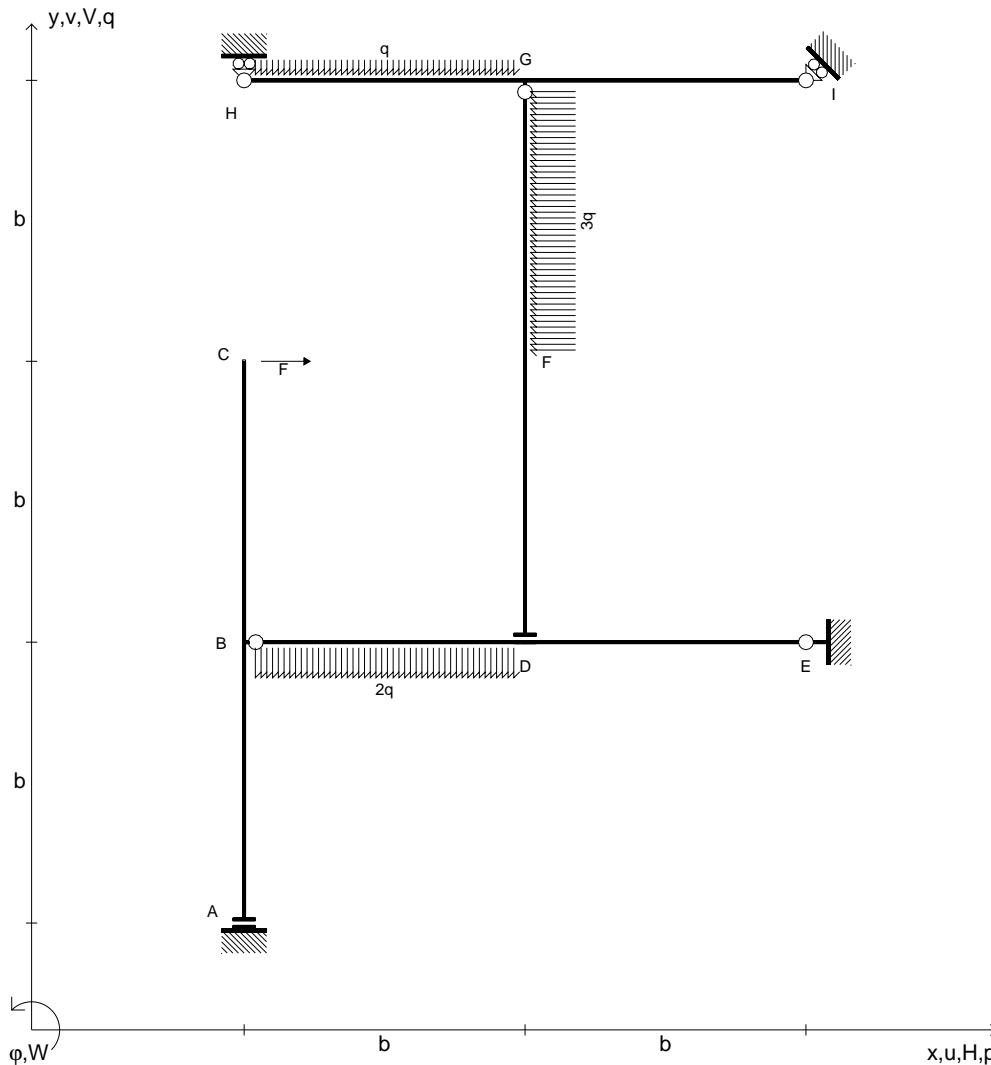
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13.11.13

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$$q_{BD} = -2q = -2F/b$$

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Piano I

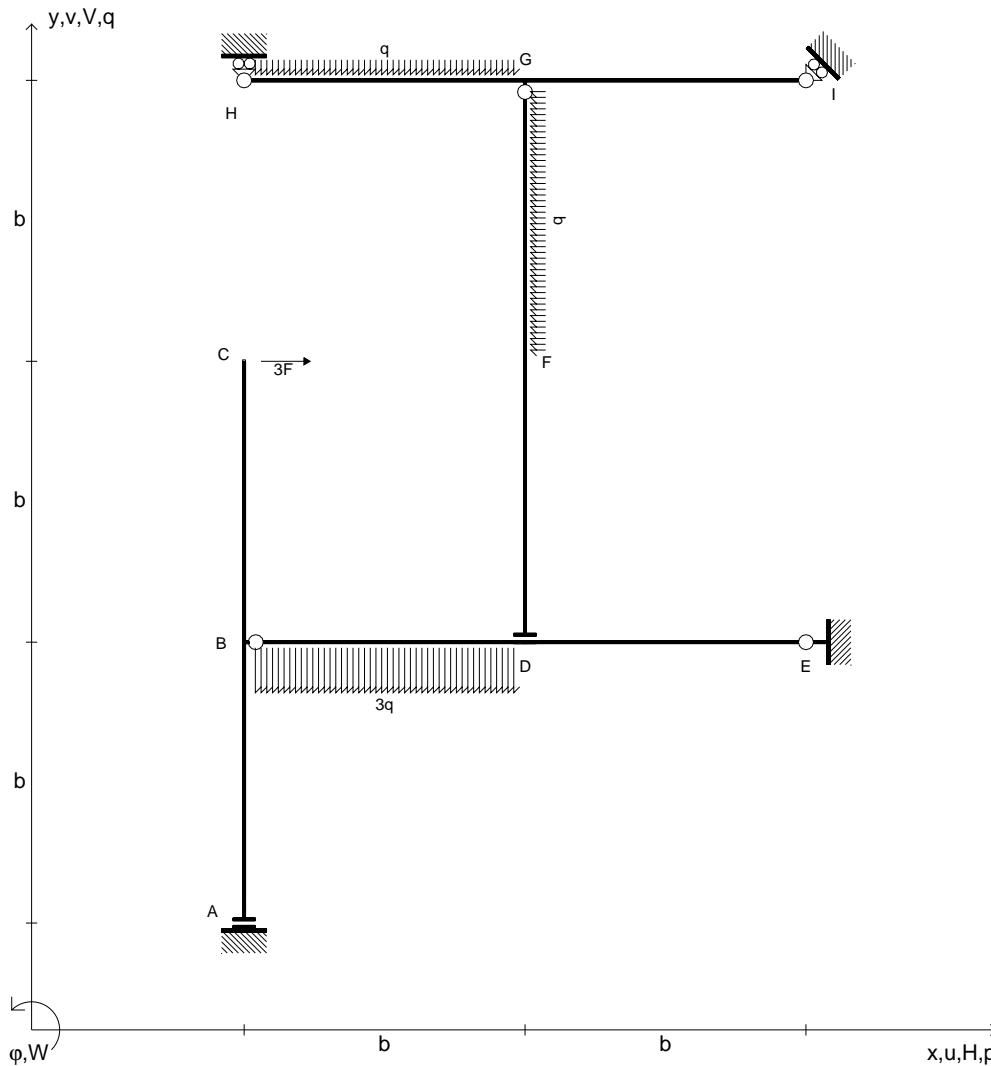
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$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

Piano di scorrimento del vincolo con inclinazione assegnata.



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$$q_{BD} = -3q = -3F/b$$

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Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

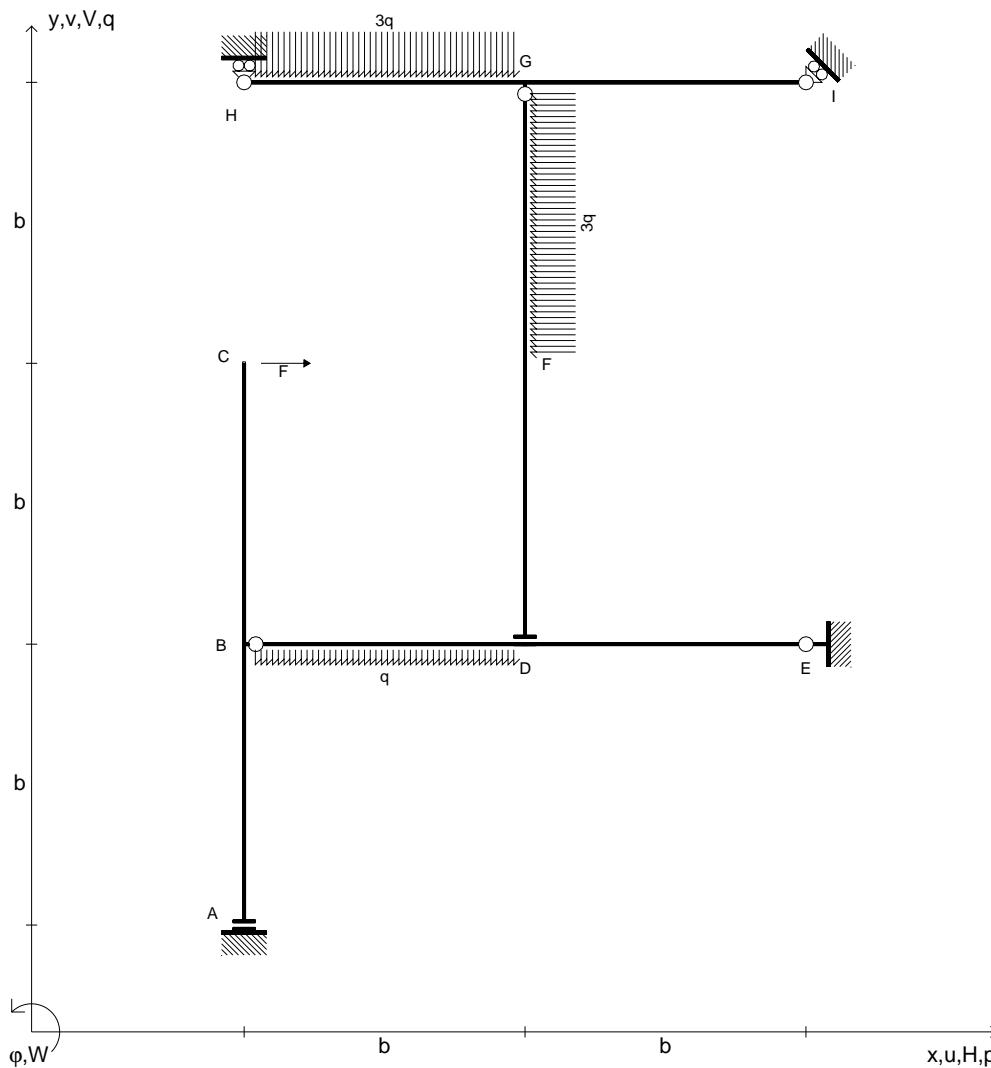
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Piano di scorrimento del vincolo con inclinazione assegnata.

@ Adolfo Zavelani Rossi, Politecnico di Milano, vers.27.03.13





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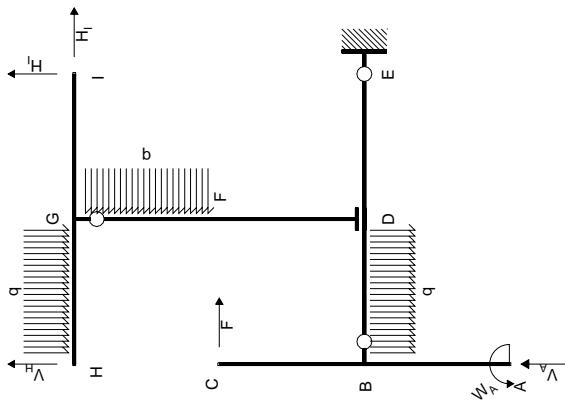
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$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

Piano di scorrimento del vincolo con inclinazione assegnata.



EQUAZIONI DI EQUILIBRIO Rotazione globale intorno a E

$$-2V_A b + W_A -2V_H b -2H|b = Fb -9/2qb^2$$

Rotazione intorno a B: aste BA BC

$$W_A = Fb$$

Traslazione orizzontale: aste DF FG GH GI

$$H_i = qb$$

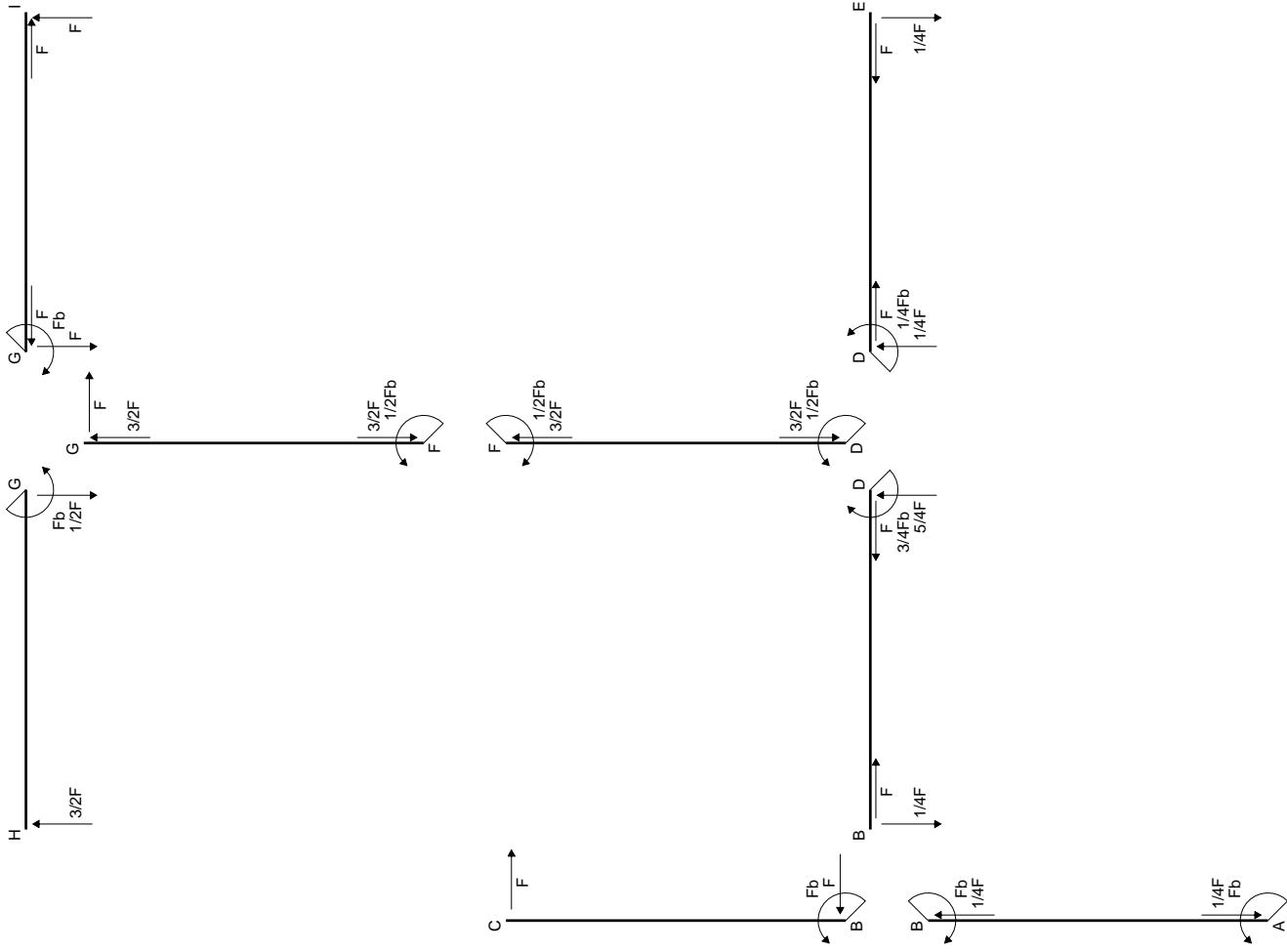
$$-\nabla b + H = -1/2qb^2$$

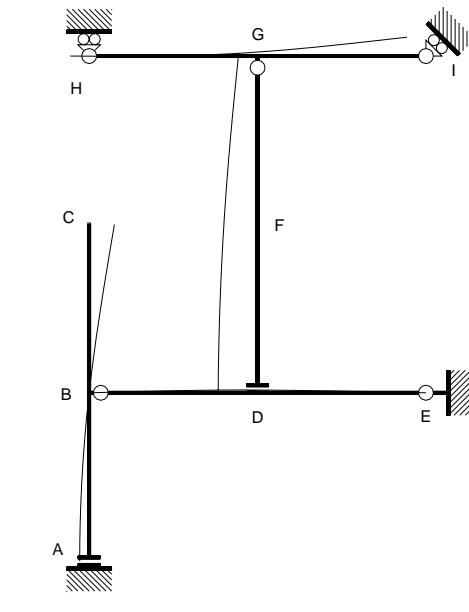
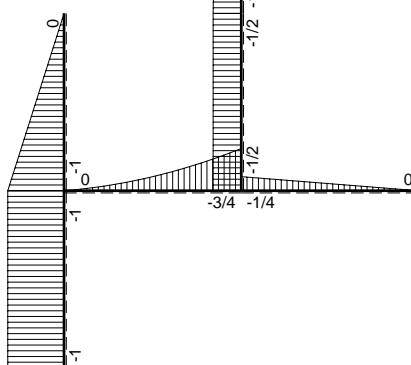
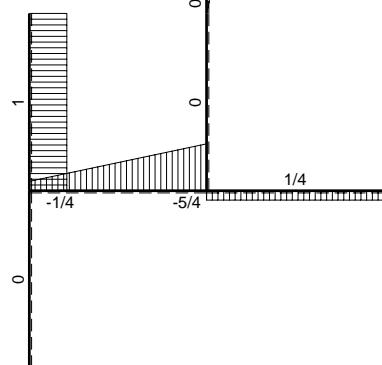
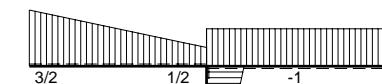
卷之三

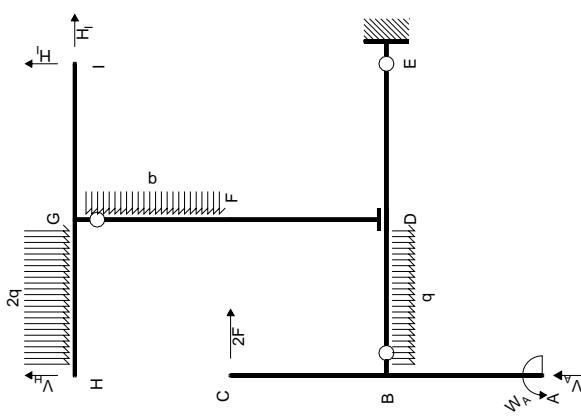
Matrice di equilibrio

$$\begin{bmatrix} \Phi_E & \Phi_{BD} & U_{DF} & \Phi_{GF} \\ -2 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ V_A^B & V_B^B & V_D^B & V_D^B \\ \end{bmatrix} = \begin{bmatrix} q_B \\ 1 \\ -9/2 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ -1/2 \\ \end{bmatrix}$$

$$\begin{array}{l} \text{Soluzione del sistema} \\ \left[\begin{array}{cc} F_b & qb^2 \\ 0 & -1/4 \end{array} \right] = \left[\begin{array}{cc} 1 & 0 \\ 0 & 1 \\ 0 & 3/2 \end{array} \right] \\ \left[\begin{array}{c} V_A b \\ W_A \\ H b \\ V_H b \end{array} \right] \end{array}$$




 $\int -4 F b^3 / E J$
 $\leftarrow \begin{array}{|c|} \hline + \\ \hline \end{array} \rightarrow F$

 $\uparrow \begin{array}{|c|} \hline + \\ \hline \end{array} \downarrow F$
 $\curvearrowleft \begin{array}{|c|} \hline + \\ \hline \end{array} \curvearrowright F_b$



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a E

$$-2V_A b + W_A - 2V_H b - 2H_l b = 2Fb - 6qb^2$$

Rotazione intorno a B: asta BA BC

$$W_A = 2Fb$$

Traslazione orizzontale: asta DF FG GH GI

$$H_l = qb$$

Rotazione intorno a G: asta GH GI

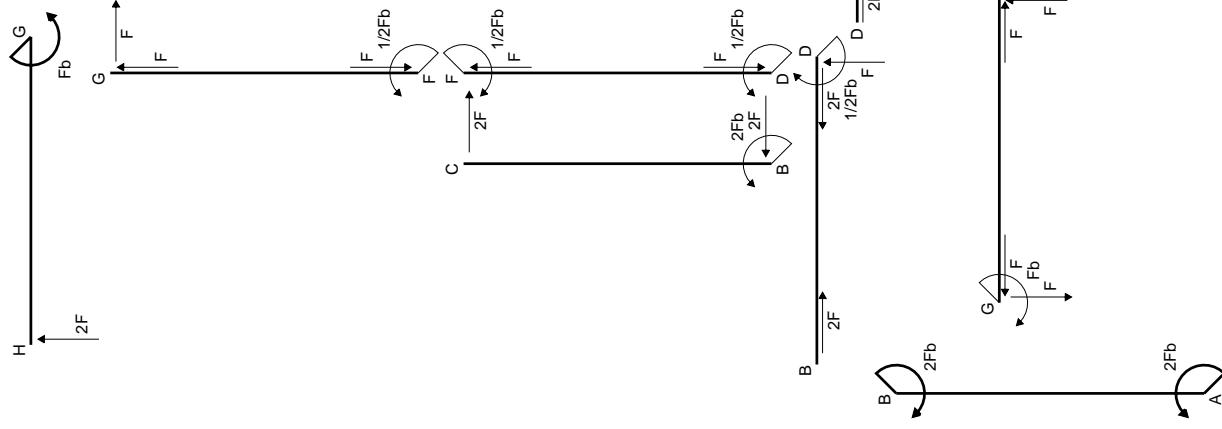
$$-V_H b + H_l b = -qb^2$$

Matrice di equilibrio

$$\begin{bmatrix} V_A b & W_A & V_H b & H_l b \\ \Phi_E & -2 & 1 & -2 \\ \Phi_{BD} & 0 & 1 & 0 \\ U_{DF} & 0 & 0 & 1 \\ \Phi_{GF} & 0 & 0 & -1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -6 \\ 2 & 0 \\ 0 & 1 \\ 0 & -1 \end{bmatrix}$$

$$\text{Soluzione del sistema}$$

$$\begin{bmatrix} V_A b \\ W_A \\ V_H b \\ H_l b \\ V_H b \end{bmatrix} = \begin{bmatrix} Fb \\ 0 \\ 2 \\ 0 \\ 0 \end{bmatrix}$$



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a E

$$-2V_A b + W_A - 2V_H b - 2H_l b = 2Fb - 6qb^2$$

Rotazione intorno a B: asta BA BC

$$W_A = 2Fb$$

Traslazione orizzontale: asta DF FG GH GI

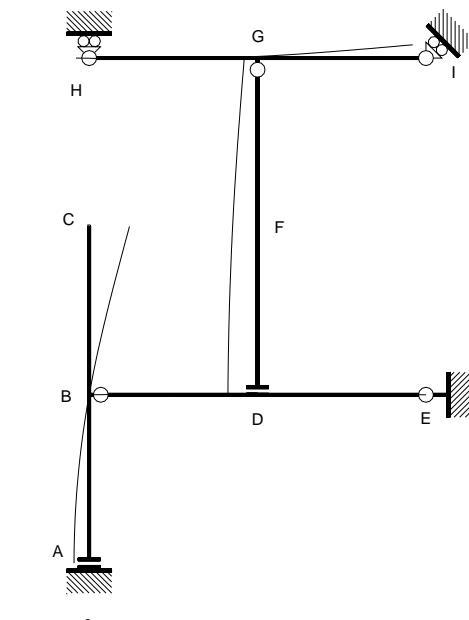
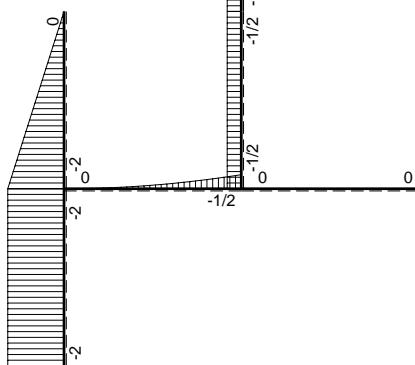
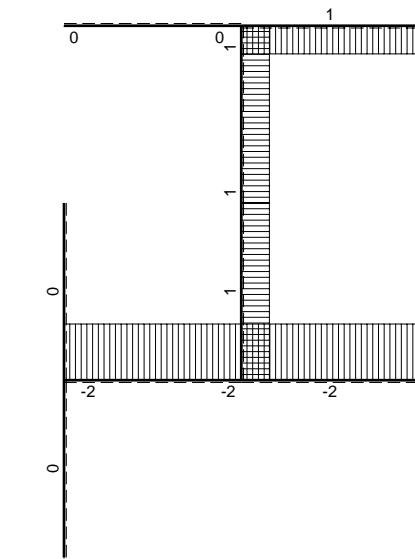
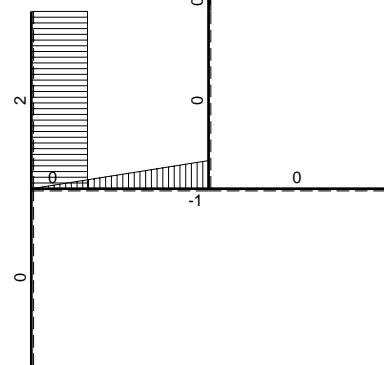
$$H_l = qb$$

Rotazione intorno a G: asta GH GI

$$-V_H b + H_l b = -qb^2$$

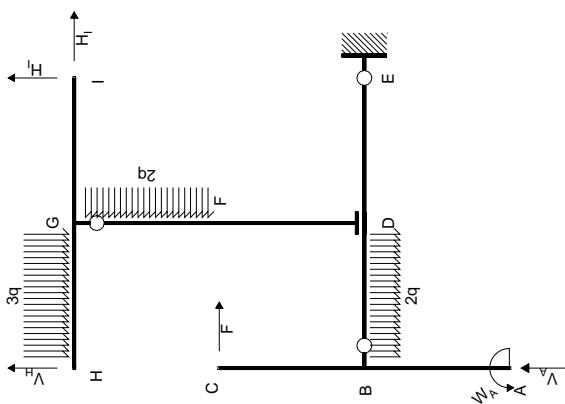
Matrice di equilibrio

$$\begin{bmatrix} V_A b & W_A & V_H b & H_l b \\ \Phi_E & -2 & 1 & -2 \\ \Phi_{BD} & 0 & 1 & 0 \\ U_{DF} & 0 & 0 & 1 \\ \Phi_{GF} & 0 & 0 & -1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -6 \\ 2 & 0 \\ 0 & 1 \\ 0 & -1 \end{bmatrix}$$

 $\square \rightarrow 5 Fb^3/EJ$ $\leftarrow \square \rightarrow F$  $\uparrow \square \downarrow F$ $\square \rightarrow Fb$

EQUILIBRIO Nome:

Struttura Isostatica.003 REAZIONI Nome:



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a E
 $-2V_A + W_A - 2V_H b - 2H_b = F_b - 21/2qb^2$

Rotazione intorno a B: asta BA BC
 $W_A = Fb$

Traslazione orizzontale: asta DF FG GH GI
 $H_l = 2qb$

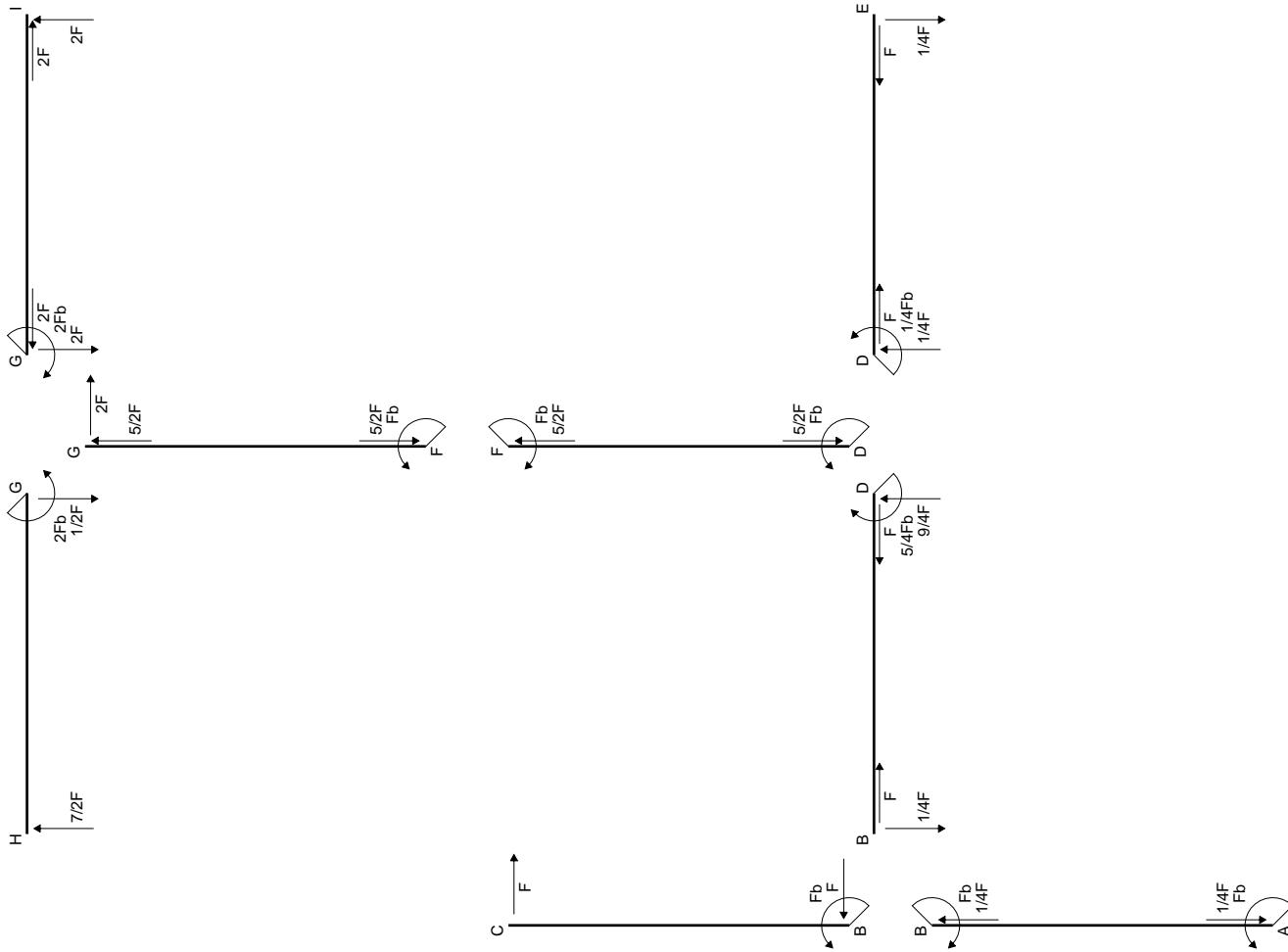
Rotazione intorno a G: asta GH GI
 $-V_H b + H_b = -3/2qb^2$

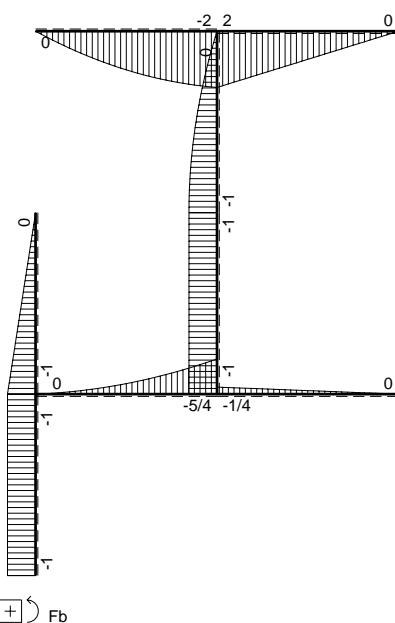
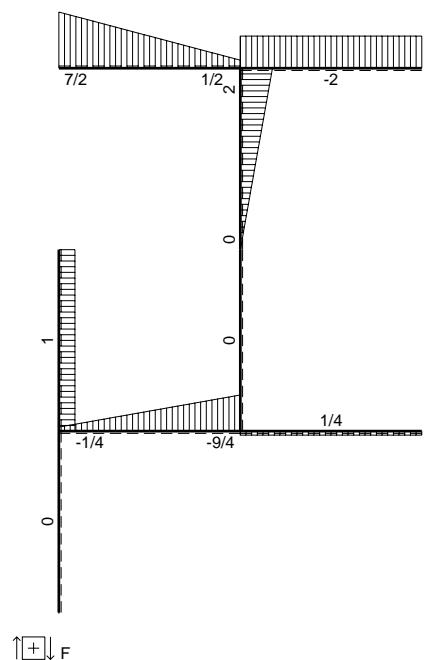
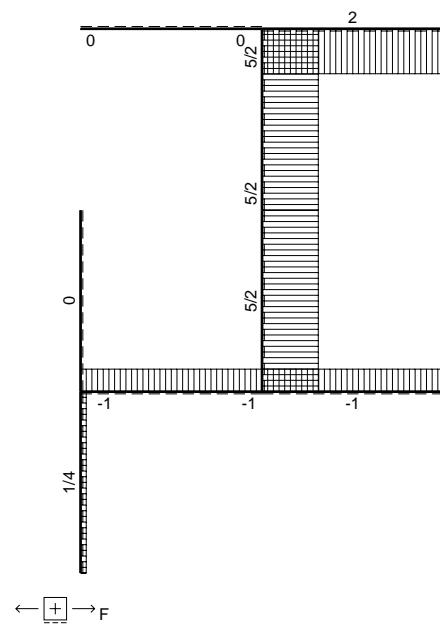
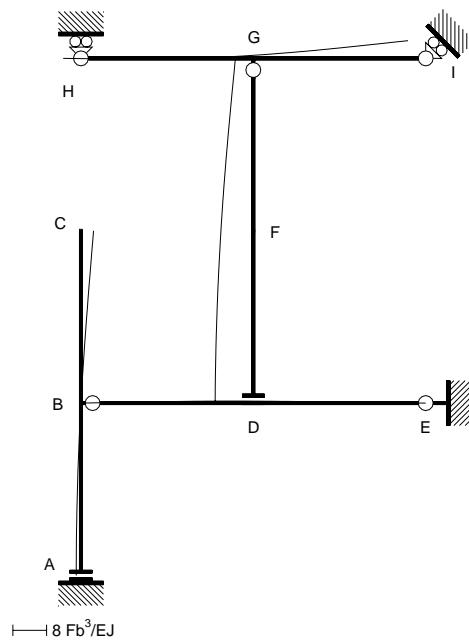
$$\text{Matrice di equilibrio}$$

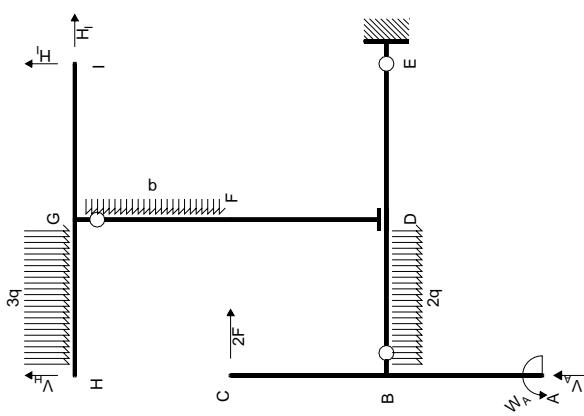
$$\begin{bmatrix} V_A & W_A & V_H b & H_b \\ \Phi_E & -2 & 1 & -2 \\ \Phi_{BD} & 0 & 1 & 0 \\ U_{DF} & 0 & 0 & 1 \\ \Phi_{GF} & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} F_b & qb^2 \\ 1 & -21/2 \\ 1 & 0 \\ 0 & 2 \\ 0 & -3/2 \end{bmatrix}$$

$$\text{Soluzione del sistema}$$

$$\begin{bmatrix} V_A \\ W_A \\ V_H b \\ H_b \\ V_H b \end{bmatrix} = \begin{bmatrix} F_b \\ qb^2 \\ 0 \\ -1/4 \\ 1 \\ 0 \\ 0 \\ 2 \\ 0 \\ 7/2 \end{bmatrix}$$







EQUAZIONI DI EQUILIBRIO

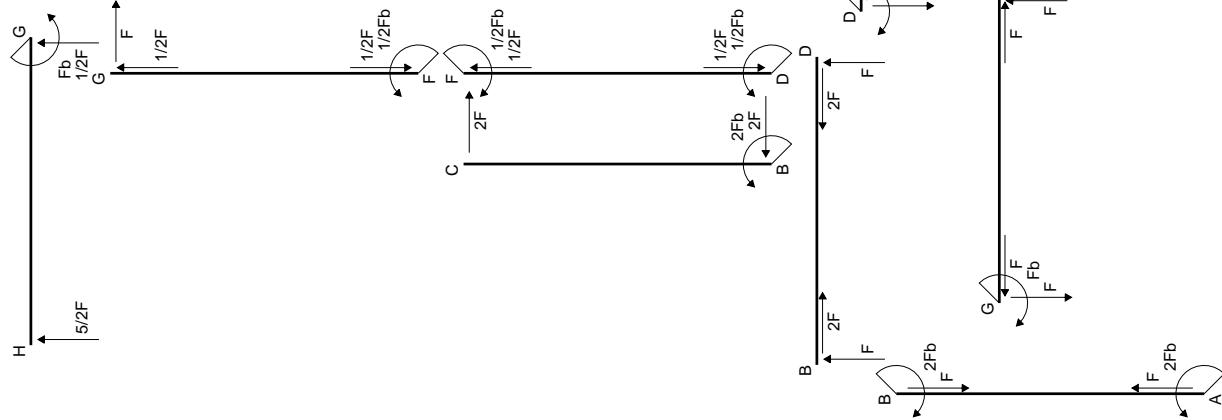
Rotazione globale intorno a E
 $-2V_A b + W_A - 2V_H b - 2H_l b = 2Fb - 9qb^2$ Rotazione intorno a B: asta BA BC
 $W_A = 2Fb$ Traslazione orizzontale: asta DF FG GH GI
 $H_l = qb$ Rotazione intorno a G: asta GH GI
 $-V_H b + H_l b = -3/2qb^2$

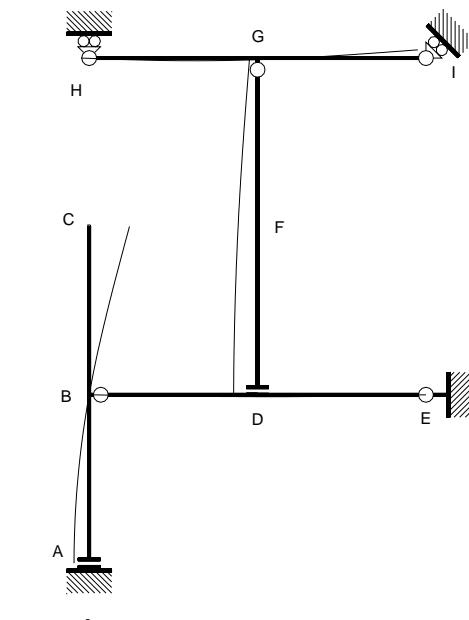
Matrice di equilibrio

$$\begin{bmatrix} V_A b & W_A & V_H b & H_l b \\ \Phi_E & -2 & 1 & -2 \\ \Phi_{BD} & 0 & 1 & 0 \\ U_{DF} & 0 & 0 & 1 \\ \Phi_{GF} & 0 & 0 & -1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -9 \\ 2 & 0 \\ 0 & 1 \\ 0 & -3/2 \end{bmatrix}$$

Soluzione del sistema

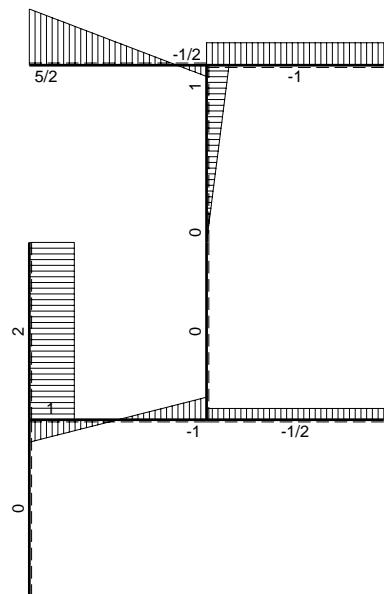
$$\begin{bmatrix} V_A b \\ W_A \\ H_l b \\ V_H b \end{bmatrix} = \begin{bmatrix} Fb \\ 0 \\ 2 \\ 0 \\ 0 \\ 1 \\ 0 \\ 5/2 \end{bmatrix}$$





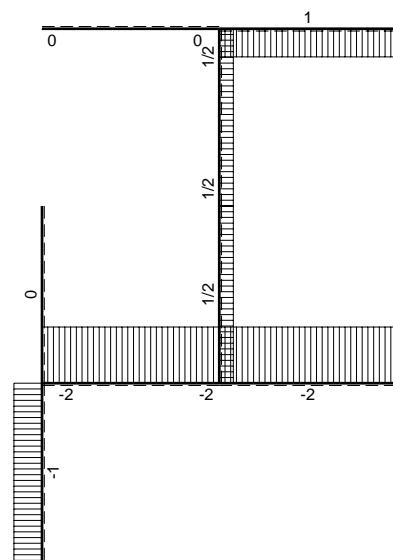
$\square \rightarrow 5 Fb^3/EJ$

$\leftarrow \square \rightarrow F$

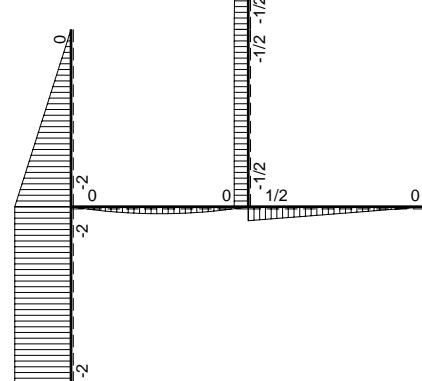


$\uparrow \square \downarrow F$

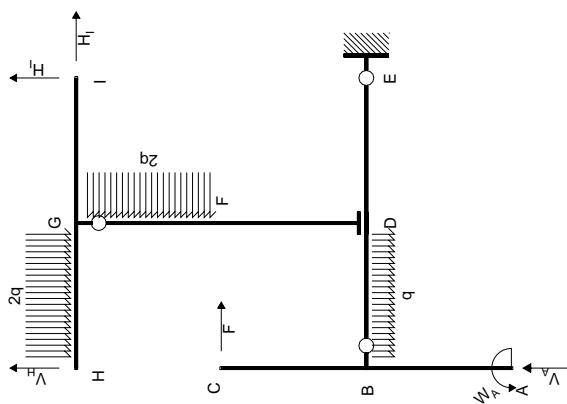
$\square \rightarrow Fb$



$\leftarrow \square \rightarrow F$



$\square \rightarrow Fb$



EQUAZIONI DI EQUILIBRIO Rotazione globale intorno a F

R0uzi0ne gologale m0010 a E
-2V^Ab +W^A-2V^bb -2H^b=Fb -15/2qb²

Rotazione intorno a B: aste BA BC

Traslazione orizzontale: $z_{\text{DE}} = z_{\text{EG}}$

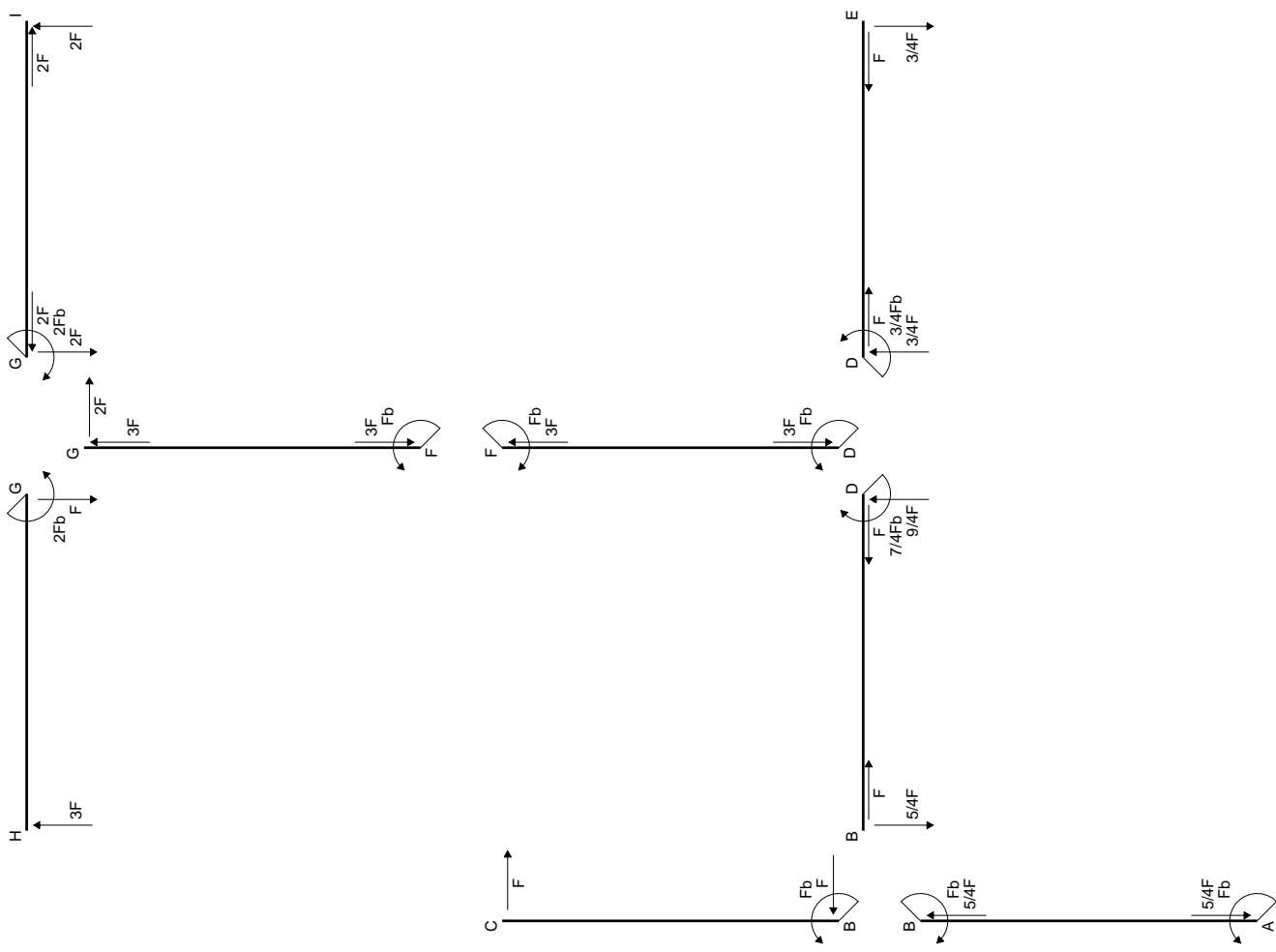
$H_1 = 2qb$

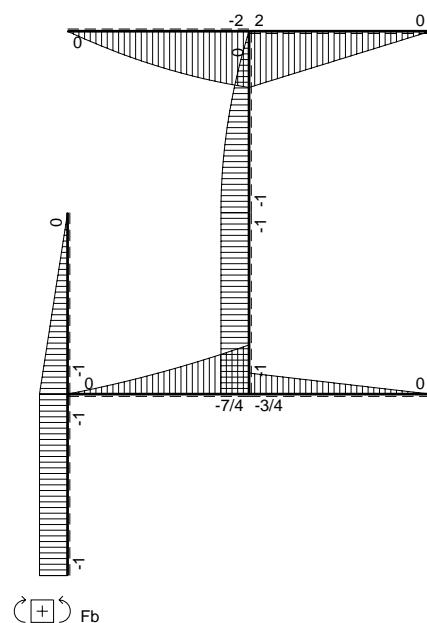
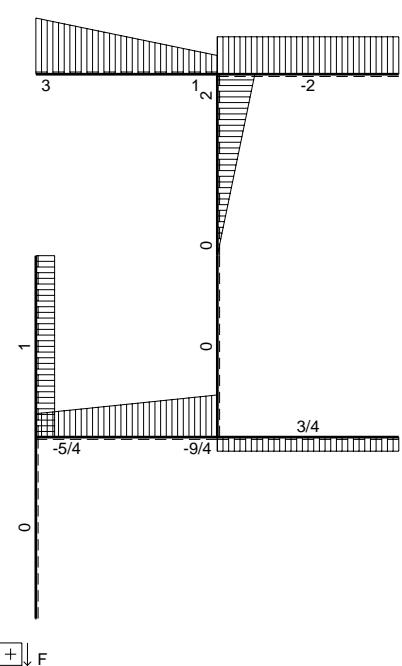
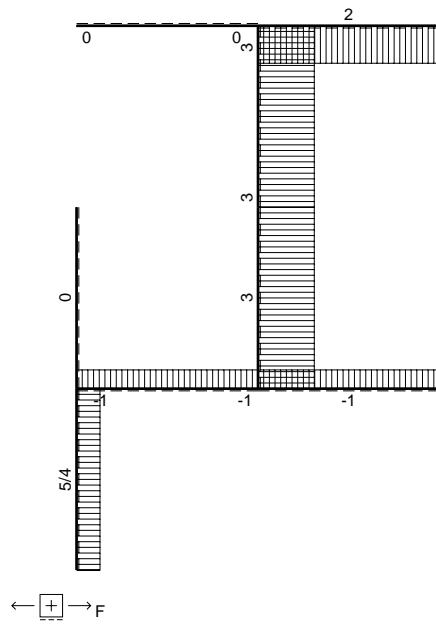
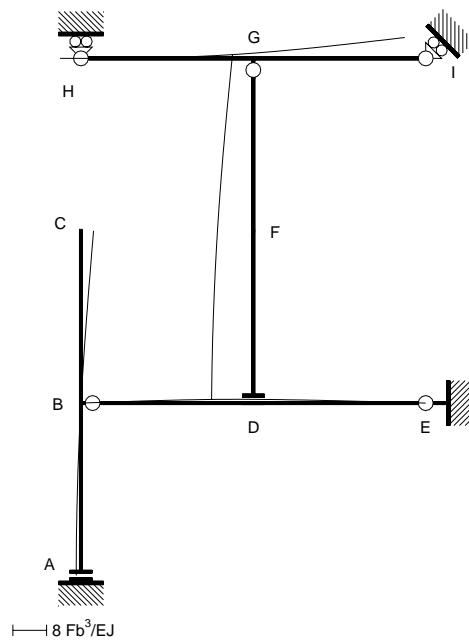
Rotazione intorno a G: aste GH GI

Matrice di equilibrio

$$\begin{bmatrix} \Phi_E & \Phi_{BD} & U_{DF} & \Phi_{GF} \\ V_A & V_B & H_B \\ -2 & 1 & -2 & -2 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} F_B & q_B^z \\ 1 & -15/2 \\ 1 & 0 \\ 0 & 2 \\ 0 & 1 \\ 0 & -1 \end{bmatrix}$$

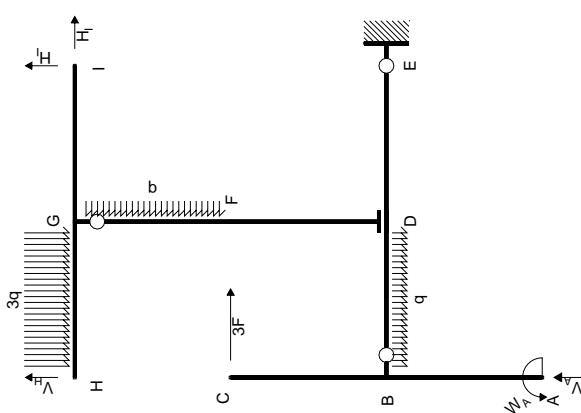
$$\text{Soluzione del sistema} \quad \begin{bmatrix} F_b \\ qb^2 \\ 0 \\ -5/4 \end{bmatrix} = \begin{bmatrix} V_A b \\ W_A \\ H_1 b \\ V_H b \end{bmatrix}$$





EQUILIBRIO Nome:

Struttura Isostatica.006 REAZIONI Nome:



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a E

$$-2V_A b + W_A - 2V_H b - 2H_b = 3F_D - 15/2qb^2$$

Rotazione intorno a B: asta BA BC

$$W_A = 3F_D$$

Traslazione orizzontale: asta DF FG GH GI

$$H_1 = qb$$

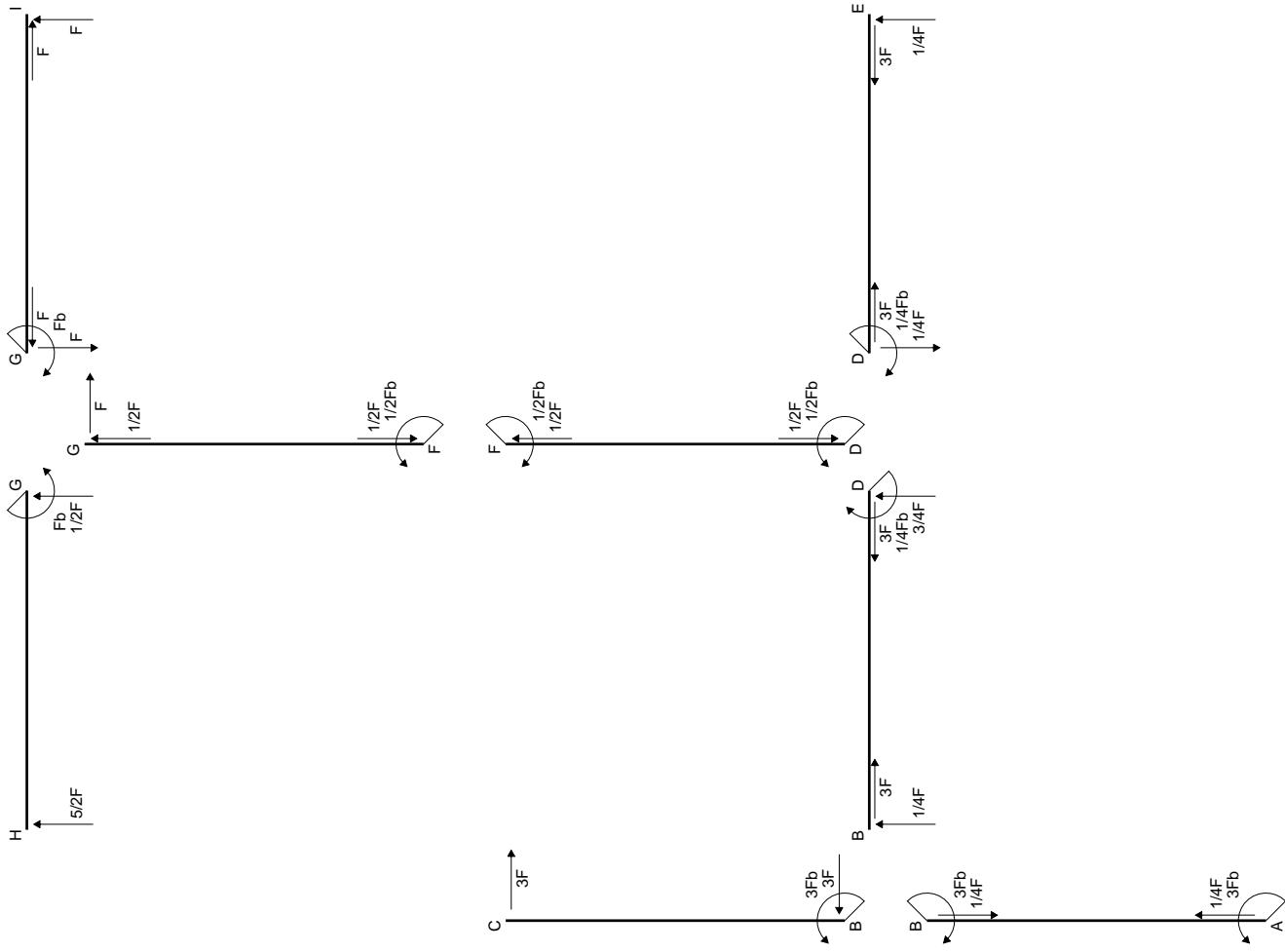
Rotazione intorno a G: asta GH GI

$$-V_H b + H_1 b = -3/2qb^2$$

Matrice di equilibrio

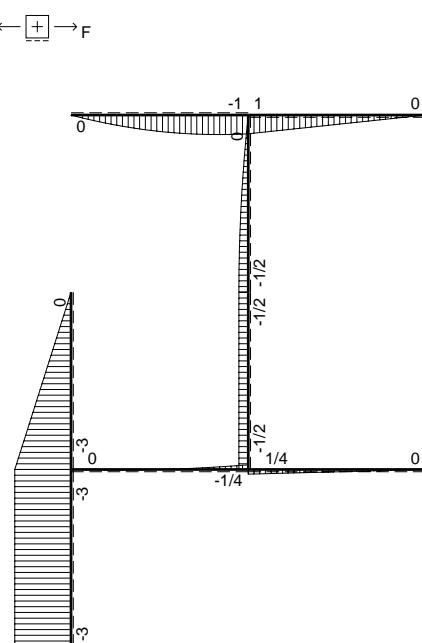
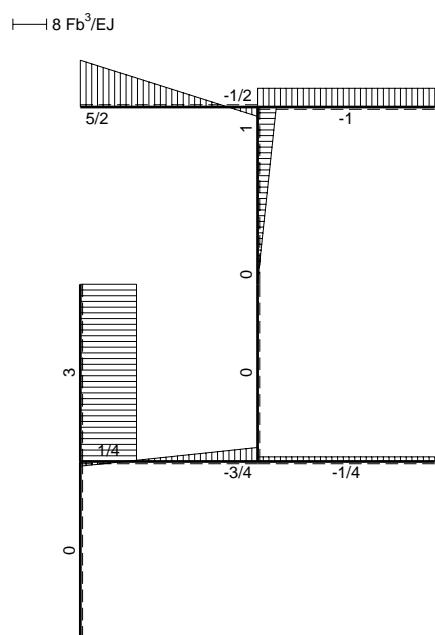
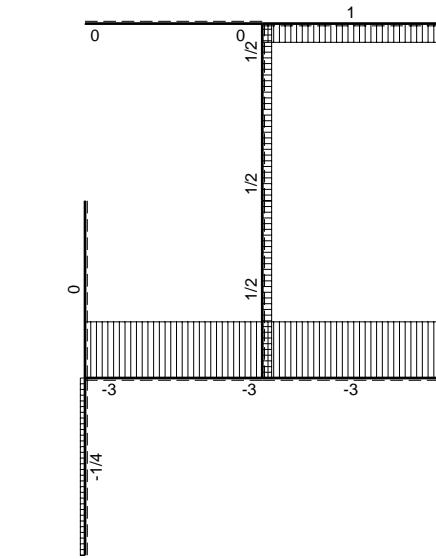
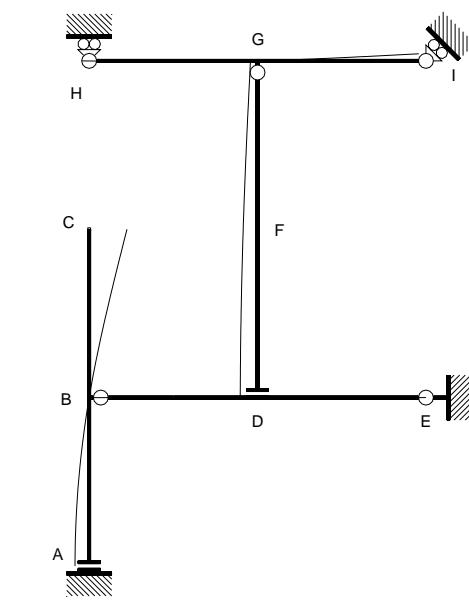
$$\begin{bmatrix} V_A b & W_A & V_H b & H_1 b \\ \Phi_E & -2 & 1 & -2 \\ \Phi_{BD} & 0 & 1 & 0 \\ U_{DF} & 0 & 0 & 1 \\ \Phi_{GF} & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} F_D & qb^2 \\ 3 & -15/2 \\ 3 & 0 \\ 0 & 1 \\ 0 & -3/2 \end{bmatrix}$$

$$\begin{bmatrix} V_A b \\ W_A \\ V_H b \\ H_1 b \\ V_H b \end{bmatrix} = \begin{bmatrix} F_D \\ qb^2 \\ 0 & 1/4 \\ 3 & 0 \\ 0 & 1 \\ 0 & 5/2 \end{bmatrix}$$

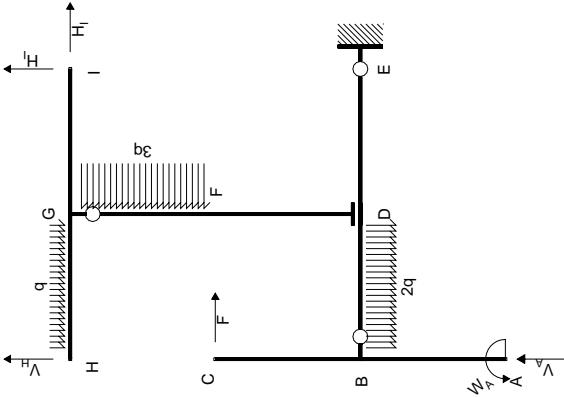


Struttura Isostatica.006 REAZIONI Nome:

Struttura Isostatica.006



$\uparrow \square \downarrow F$



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a E

- $ZV_AU + VV_A - ZV_HU - ZV_H \equiv F_U - ZV_H$

$$W_A = Fb$$

Traslazione orizzontale: aste DF FG GH GI

Rotazione intorno a G: $H_i = 3qb$ aste GH GI

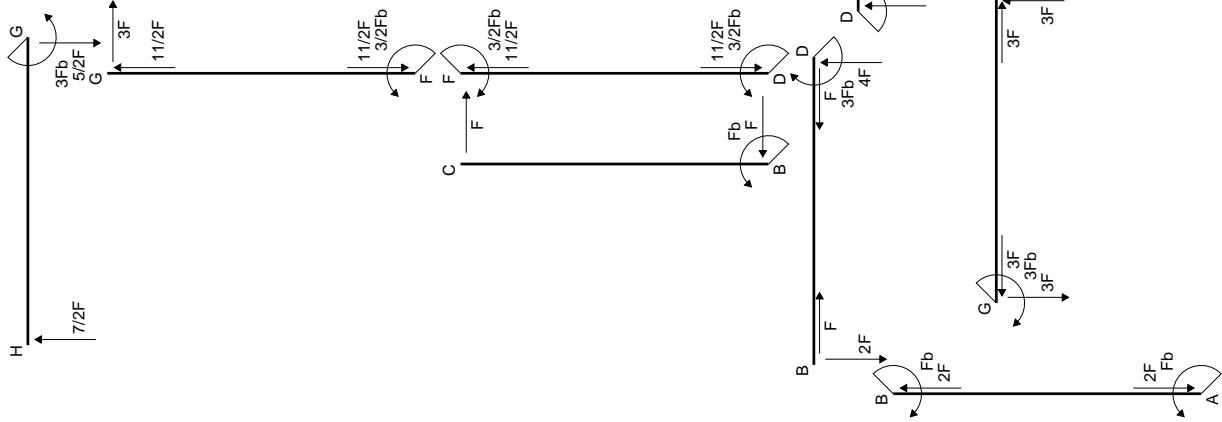
$$-V_H b + H_1 b = -1/2 q b^2$$

Motivación y conciencia

Matrice di equilibrio

$$\begin{bmatrix} \Phi_E \\ \Phi_{BD} \\ \Phi_{DF} \\ \Phi_{GF} \end{bmatrix} = \begin{bmatrix} -2 & 1 & -2 & -2 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & -1 \end{bmatrix} \begin{bmatrix} V_A \\ V_B \\ V_D \\ V_F \end{bmatrix}$$

$$\begin{array}{l} \text{Soluzione del sistema} \\ \left[\begin{matrix} Fb & qb^2 \\ 0 & -2 \\ 1 & 0 \\ 0 & 3 \\ 0 & 7/2 \end{matrix} \right] = \\ \left[\begin{matrix} V_A b \\ W_A \\ H b \\ V_H b \end{matrix} \right] \end{array}$$



104

1

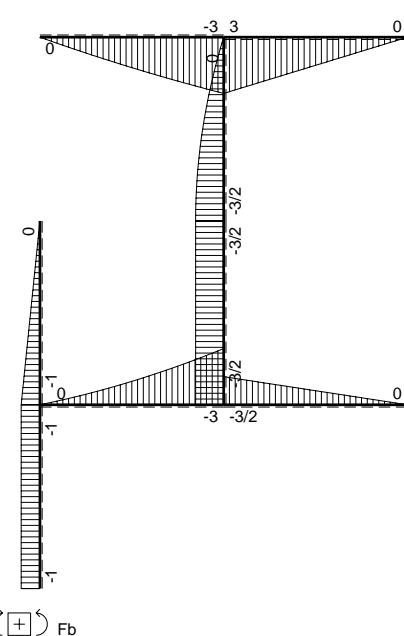
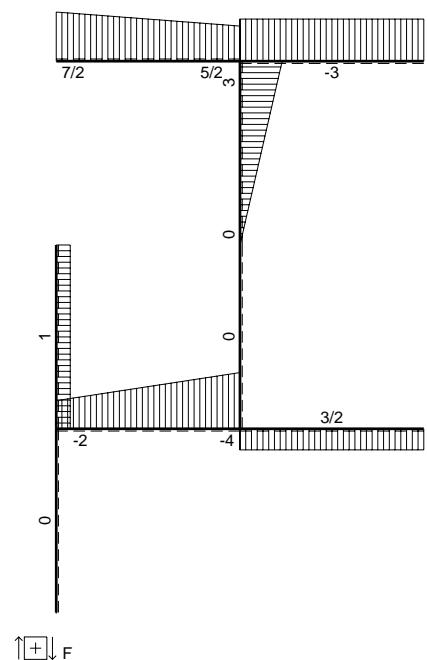
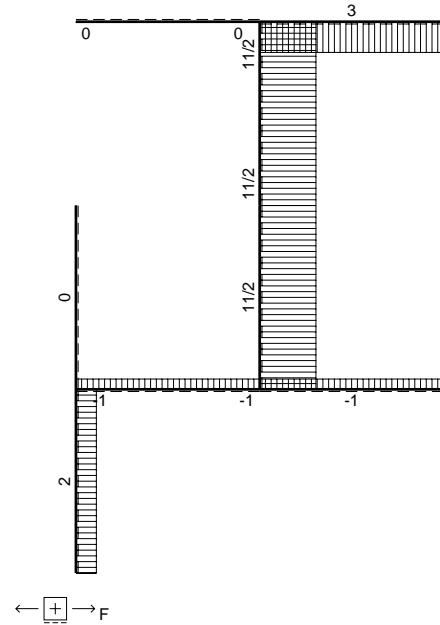
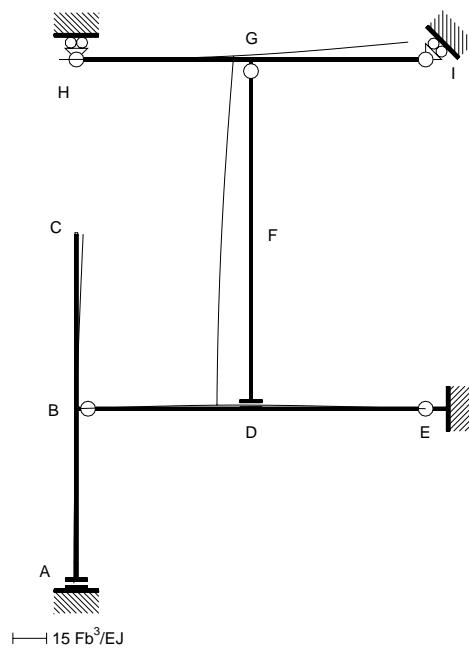
11/2F
3/2Fb

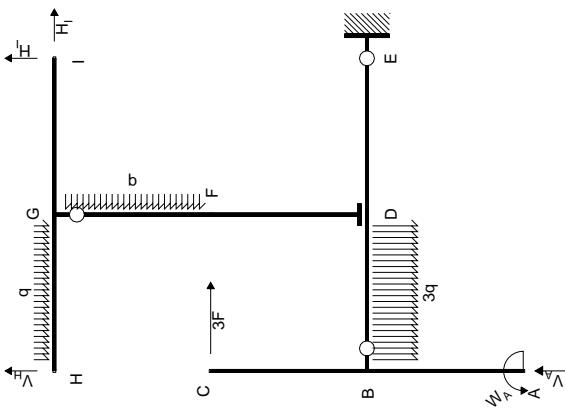
10

4F

3F

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EQUAZIONI DI EQUILIBRIO
Rotazione globale intorno a F

$$-2V_A b + W_A - 2V_H b - 2H_b = 3Fb - 15/2qb^2$$

Rotazione intorno a B: aste BA BC

$$W_A = 3Fb$$

Traslazione orizzontale: aste DF FG GH GI

$$H_i = qb$$

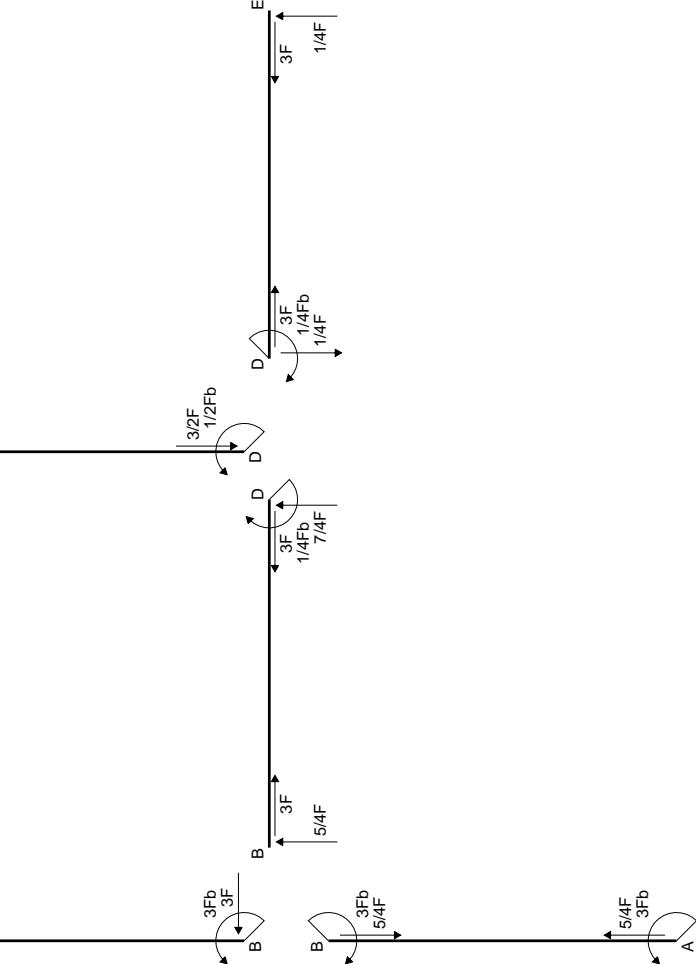
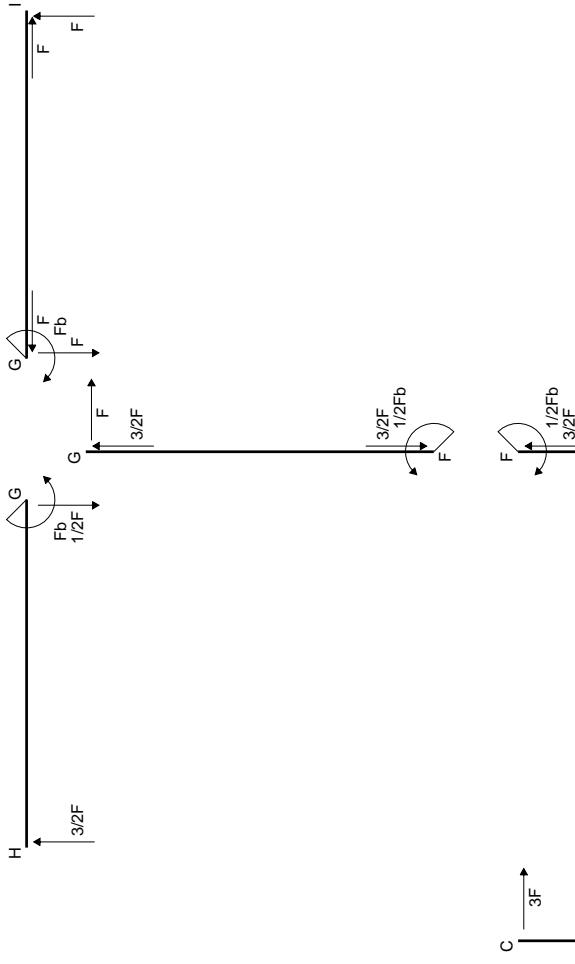
Rotazione intorno a G: $\ddot{\theta} = -V_H b + H_b = -1/2qb^2$

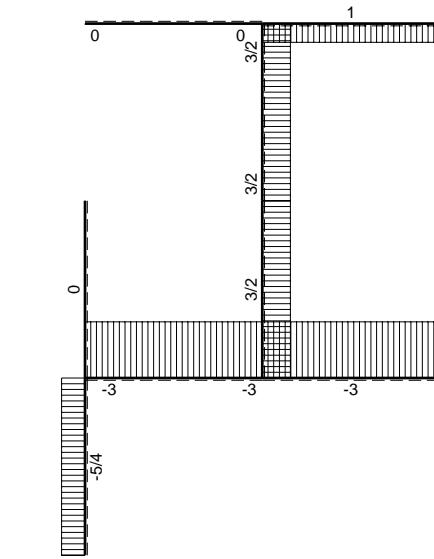
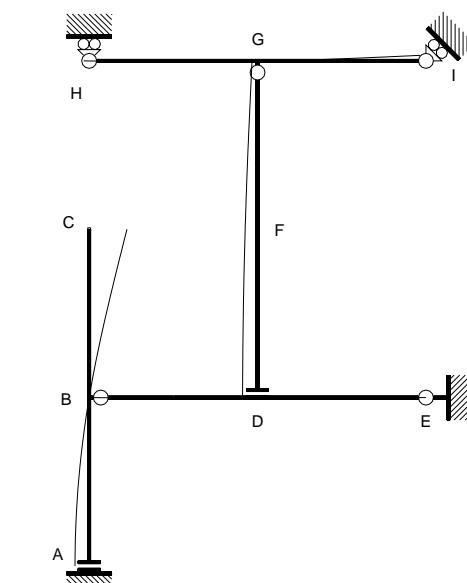
$$\text{Matrice di equilibrio} \quad \begin{bmatrix} V_A & W_A & H_B \\ -2 & 1 & -2 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} F_B \\ 3 \\ 3 \\ 0 \\ 1 \end{bmatrix} \quad \begin{bmatrix} qB^2 \\ -15/2 \\ 3 \\ 0 \\ 1/2 \end{bmatrix}$$

Matrice di equilibrio

$$\begin{bmatrix} V_A b \\ W_A \\ H b \\ V_b \end{bmatrix} = \begin{bmatrix} 0 & 5/4 \\ 3 & 0 \\ 0 & 1 \\ 0 & 3/2 \end{bmatrix} \begin{bmatrix} 2 \\ 5/4 \\ 5/4 \\ F \end{bmatrix}$$

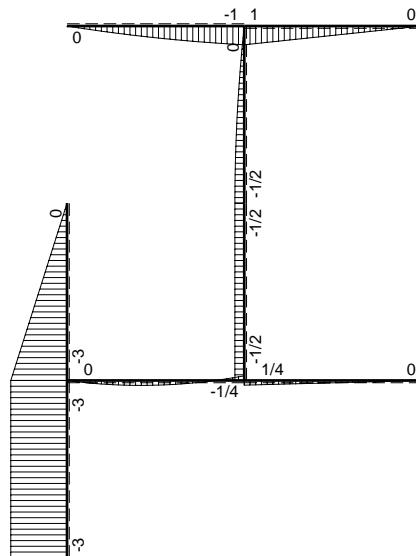
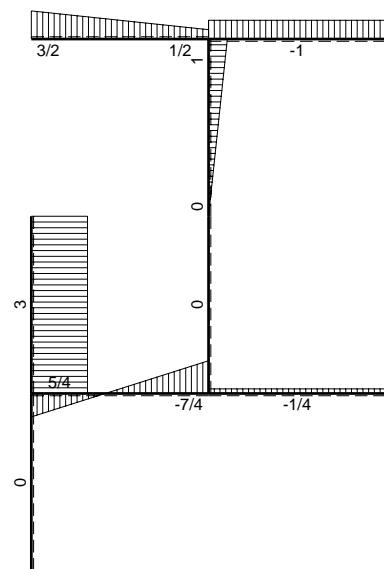
Soluzione del sistema





$\square \rightarrow 8 Fb^3/EJ$

$\leftarrow \square \rightarrow F$

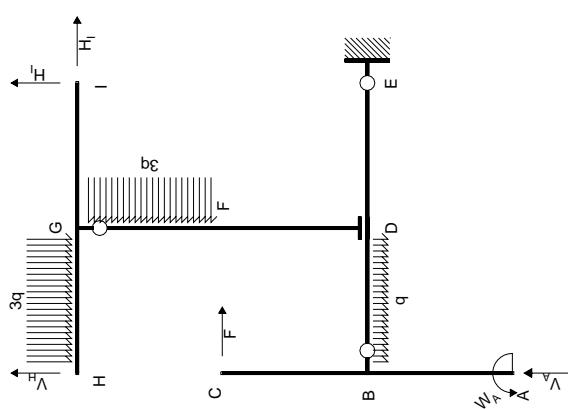


$\square \rightarrow F$

$\square \rightarrow Fb$

EQUILIBRIO Nome:

Struttura Isostatica.009



EQUAZIONI DI EQUILIBRIO

Rotazione globale intorno a E

$$-2V_A + W_A - 2V_H b - 2H_b = F_b - 21/2qb^2$$

Rotazione intorno a B: asta BA BC

$$W_A = Fb$$

Traslazione orizzontale: asta DF FG GH GI

$$H_l = 3qb$$

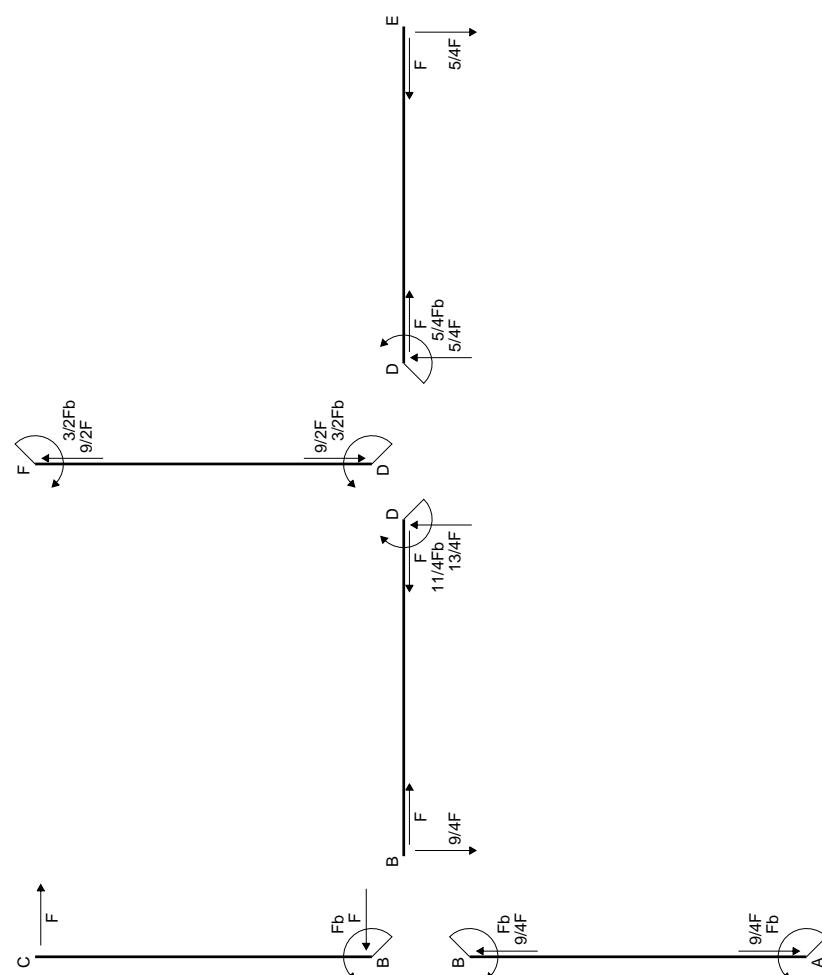
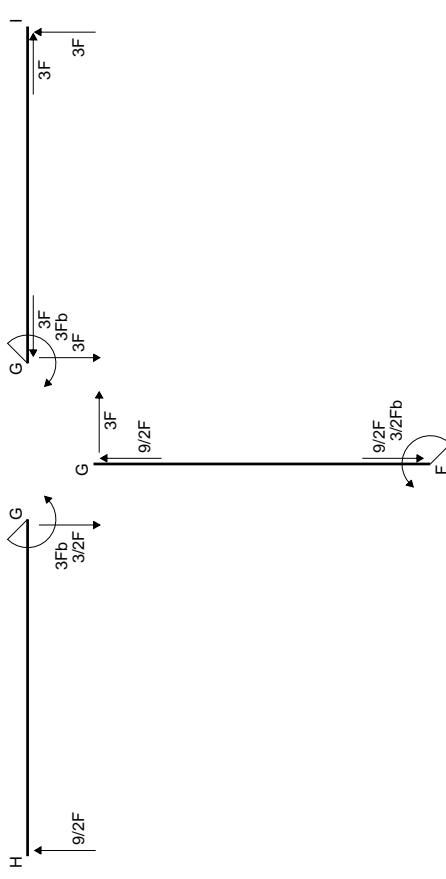
Rotazione intorno a G: asta GH GI

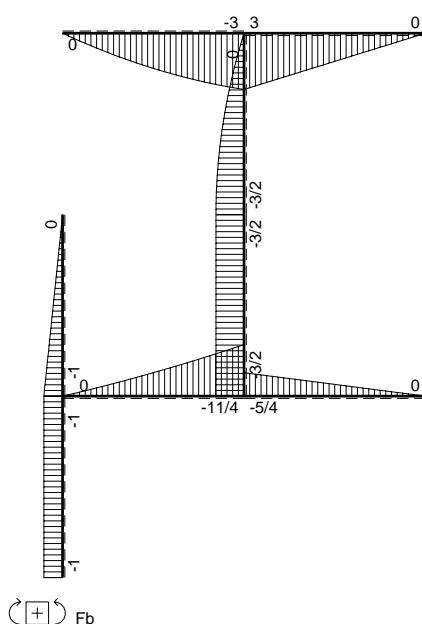
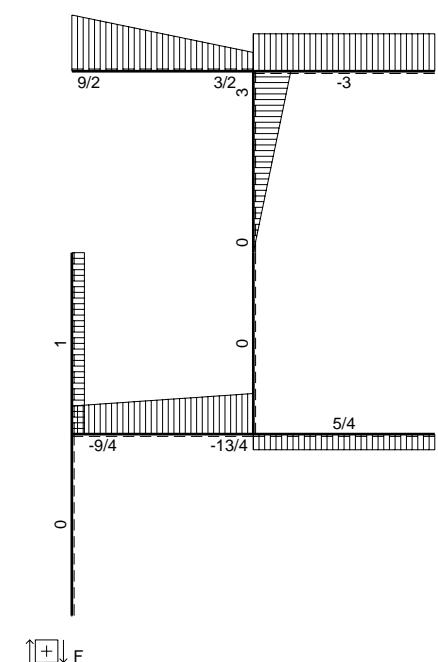
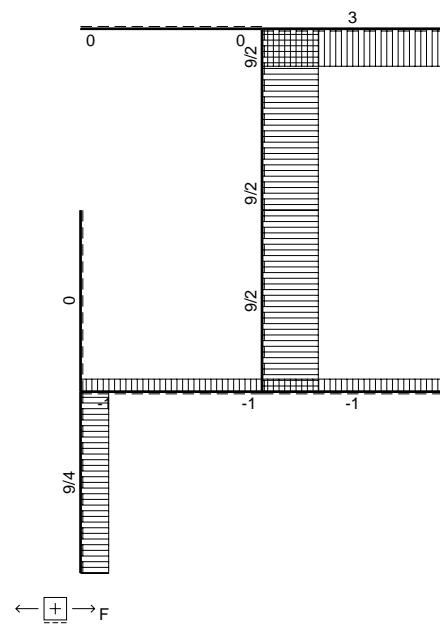
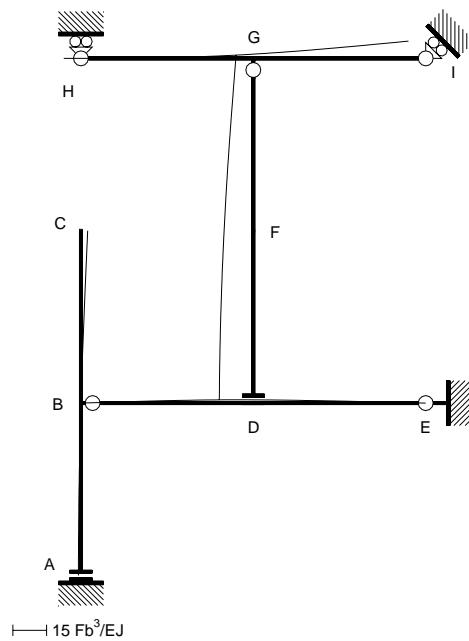
$$-V_H b + H_l b = -3/2qb^2$$

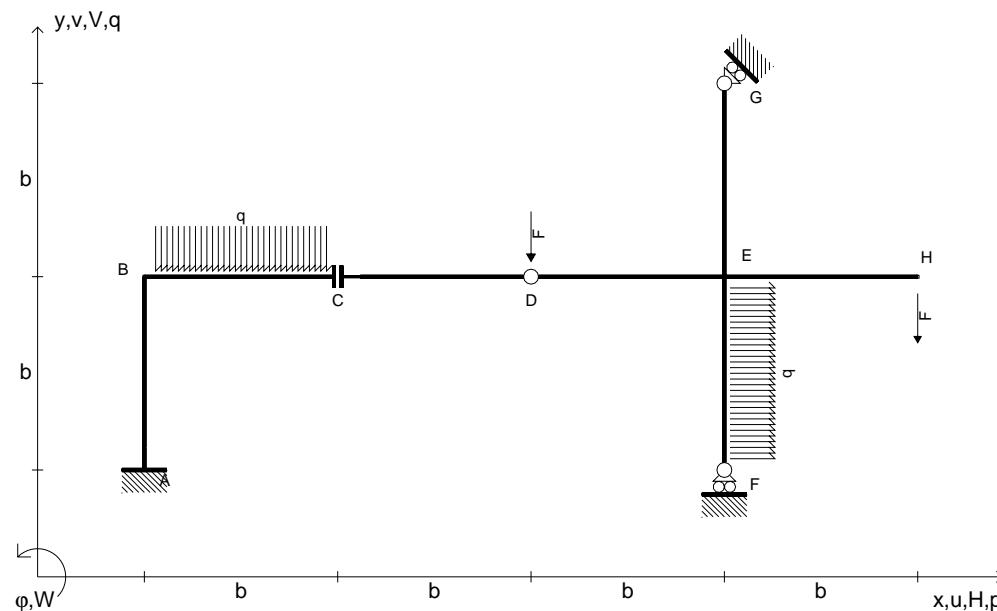
Matrice di equilibrio

$$\begin{bmatrix} V_A b & W_A & V_H b & H_l b \\ \Phi_E & -2 & 1 & -2 \\ \Phi_{BD} & 0 & 1 & 0 \\ U_{DF} & 0 & 0 & 1 \\ \Phi_{GF} & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} F_b & qb^2 \\ 1 & -21/2 \\ 1 & 0 \\ 0 & 3 \\ 0 & -3/2 \end{bmatrix}$$

$$\text{Soluzione del sistema} \quad \begin{bmatrix} V_A b \\ W_A \\ V_H b \\ H_l b \\ V_G b \end{bmatrix} = \begin{bmatrix} F_b \\ 0 \\ 1 \\ 0 \\ 0 \end{bmatrix} \quad \begin{bmatrix} qb^2 \\ -9/4 \\ 1 \\ 3 \\ 9/2 \end{bmatrix}$$







$$V_H = -F$$

$$V_D = -F$$

$$q_{BC} = -q = -F/b$$

$$p_{EF} = q = F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{CD} = EJ$$

$$EJ_{DE} = EJ$$

$$EJ_{EF} = EJ$$

$$EJ_{EG} = EJ$$

$$EJ_{EH} = EJ$$



Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

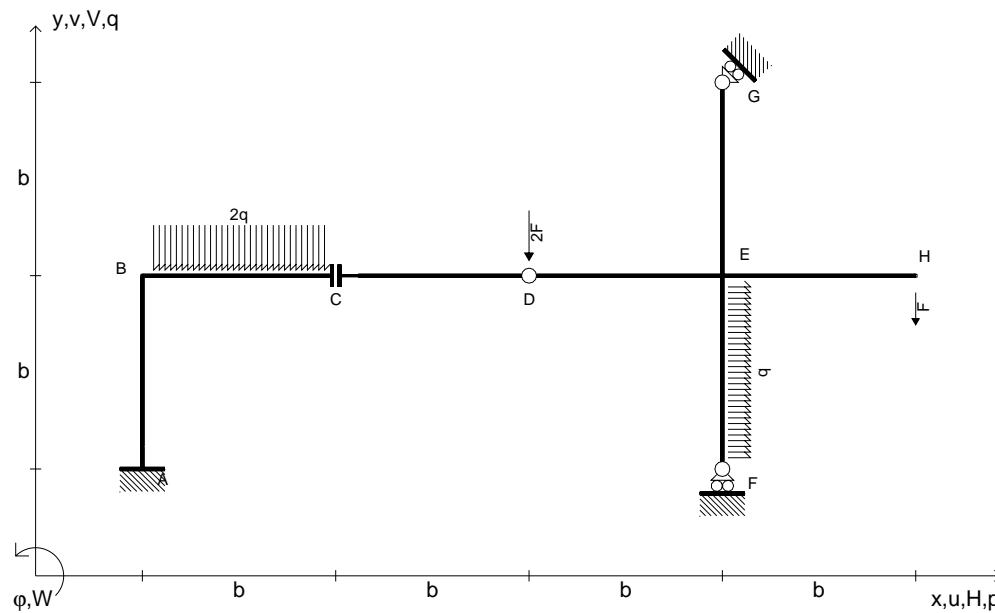
Piano di scorrimento del vincolo con inclinazione assegnata.

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$$\begin{aligned} V_H &= -F \\ V_D &= -2F \\ q_{BC} &= -2q = -2F/b \\ p_{EF} &= q = F/b \end{aligned}$$

$$\begin{aligned} EJ_{AB} &= EJ \\ EJ_{BC} &= EJ \\ EJ_{CD} &= EJ \\ EJ_{DE} &= EJ \end{aligned}$$

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1 | 1 Piano G

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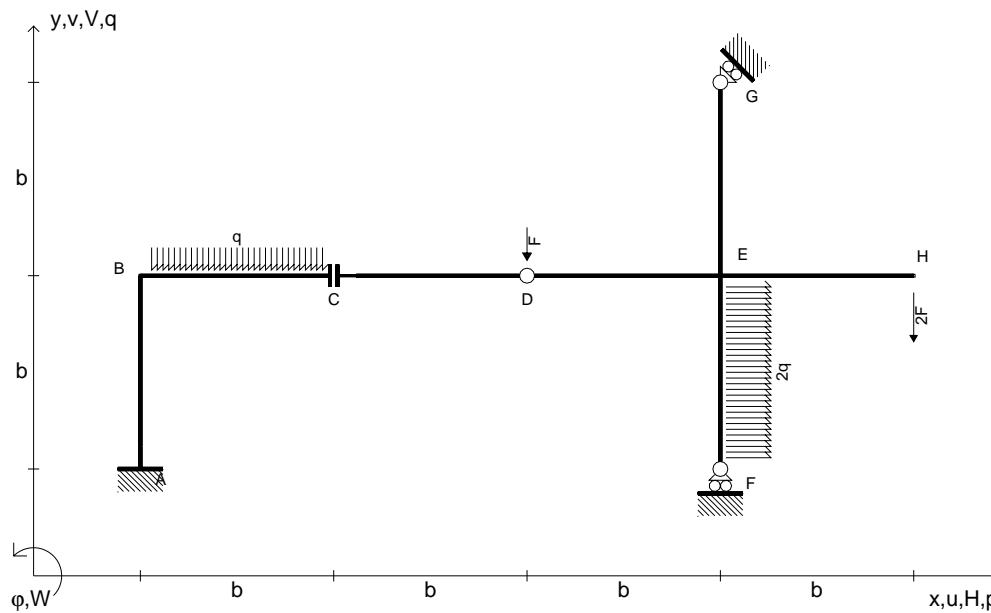
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$$\begin{aligned}V_H &= -2F \\V_D &= -F \\q_{BC} &= -q = -F/b \\p_{EF} &= 2q = 2F/b\end{aligned}$$

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1 | 1
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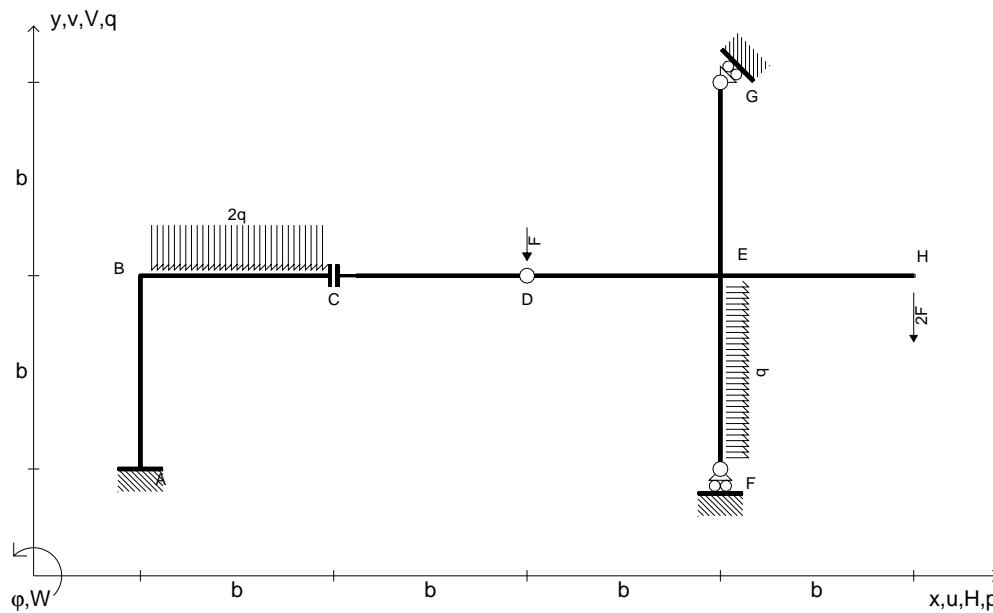
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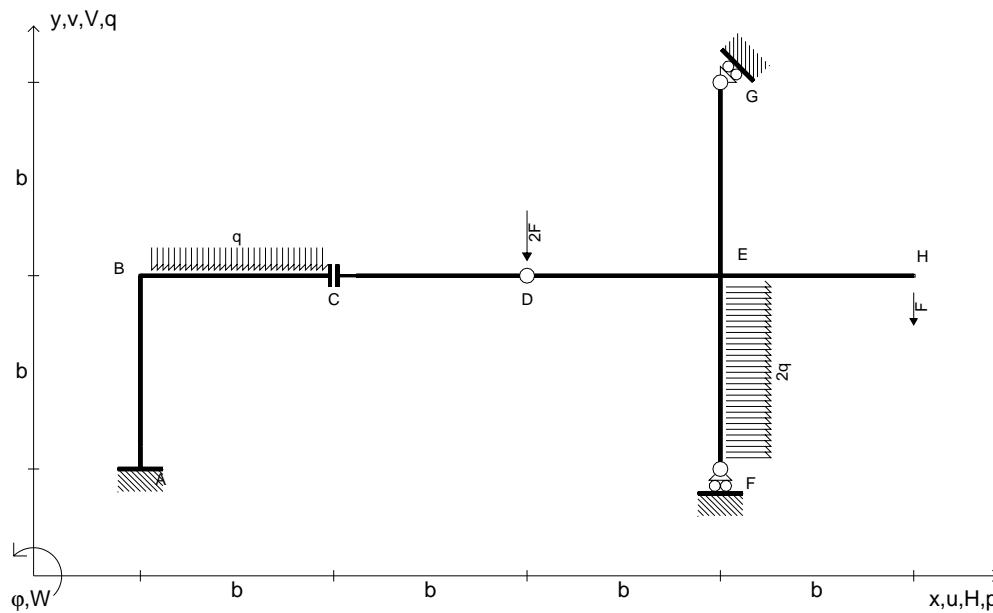
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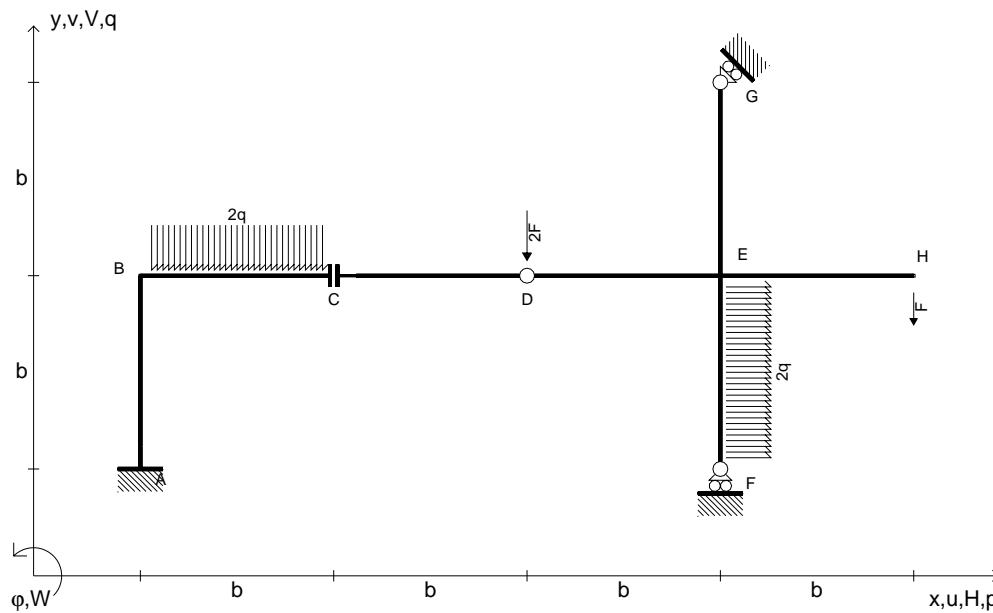
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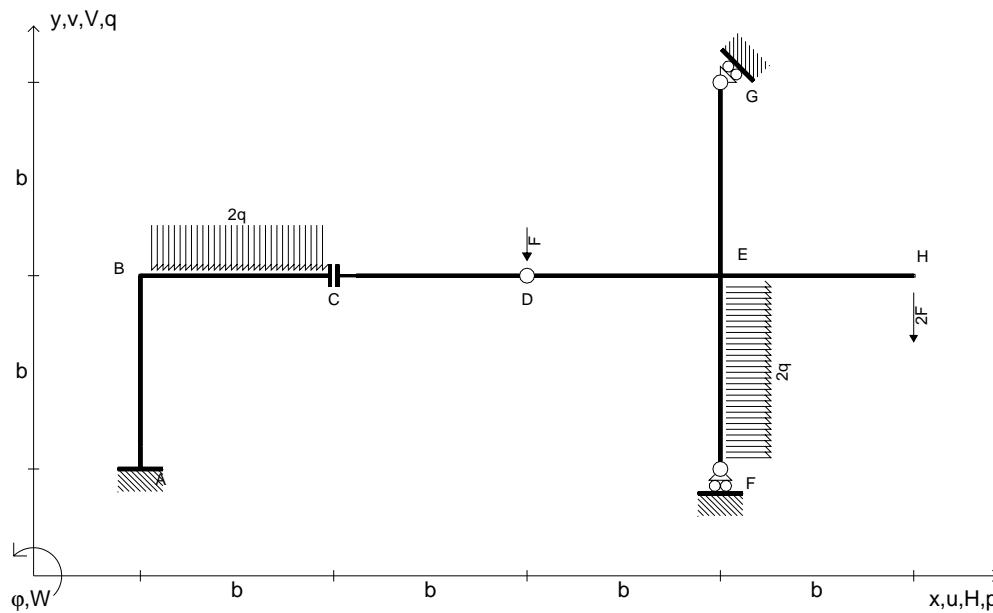
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$$\begin{aligned}V_H &= -2F \\V_D &= -F \\q_{BC} &= -2q = -2F/b \\p_{EF} &= 2q = 2F/b\end{aligned}$$

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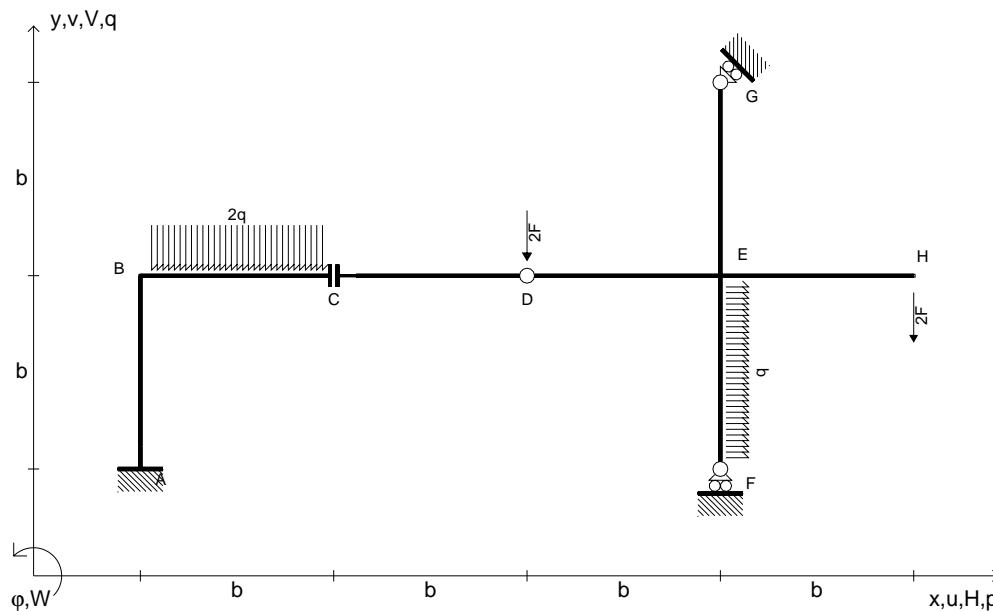
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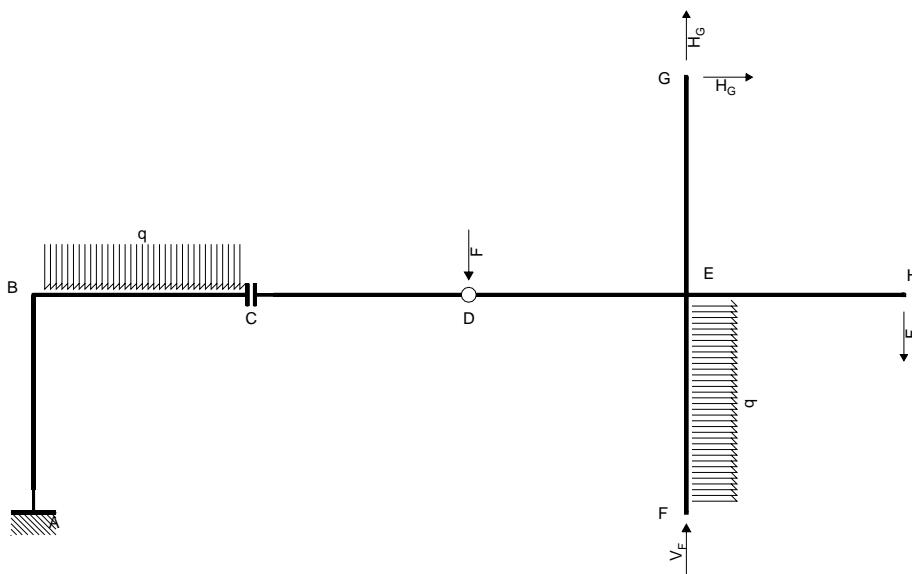
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EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG EH

$$V_F + H_G = 2F$$

Rotazione intorno a D: aste DE EF EG EH

$$V_F b = 2Fb - 1/2qb^2$$

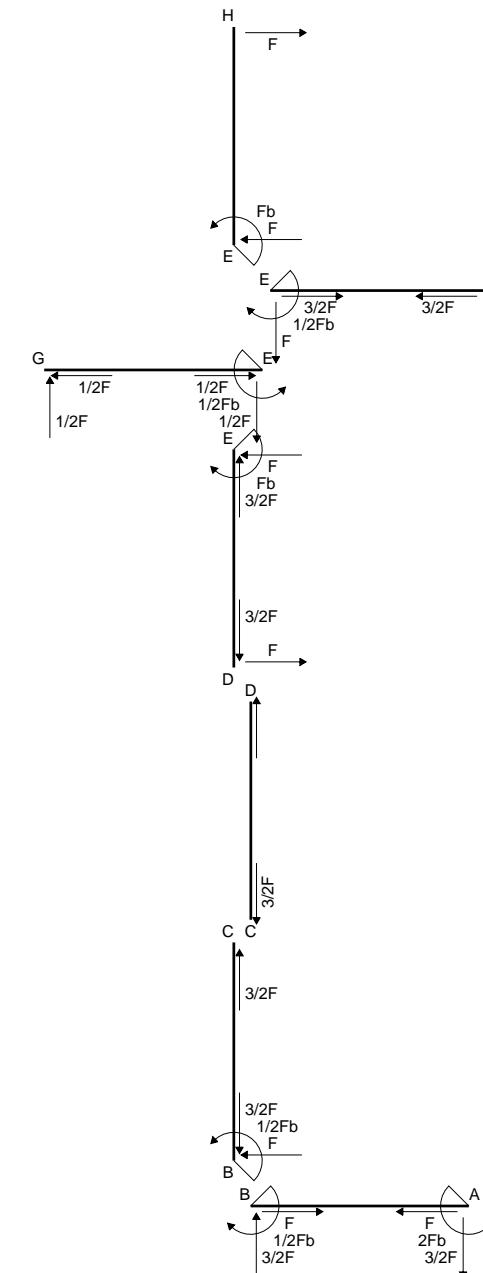
Matrice di equilibrio

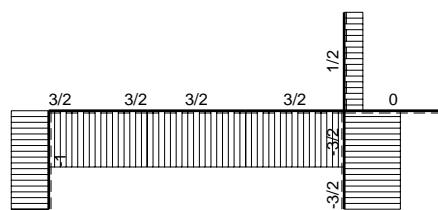
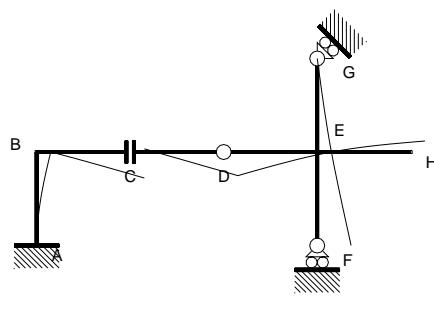
$$\begin{bmatrix} V_F b & H_G b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$

$$\begin{bmatrix} V_{CB} \\ \Phi_{DC} \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 2 & 0 \\ 2 & -1/2 \end{bmatrix}$$

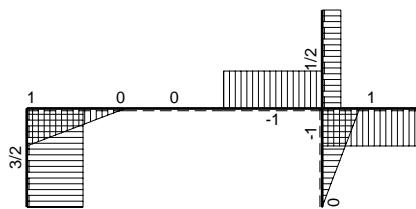
Soluzione del sistema

$$\begin{bmatrix} V_F b \\ H_G b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -1/2 \\ 0 & 1/2 \end{bmatrix}$$

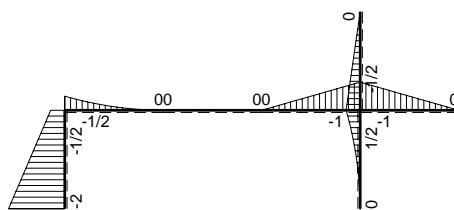




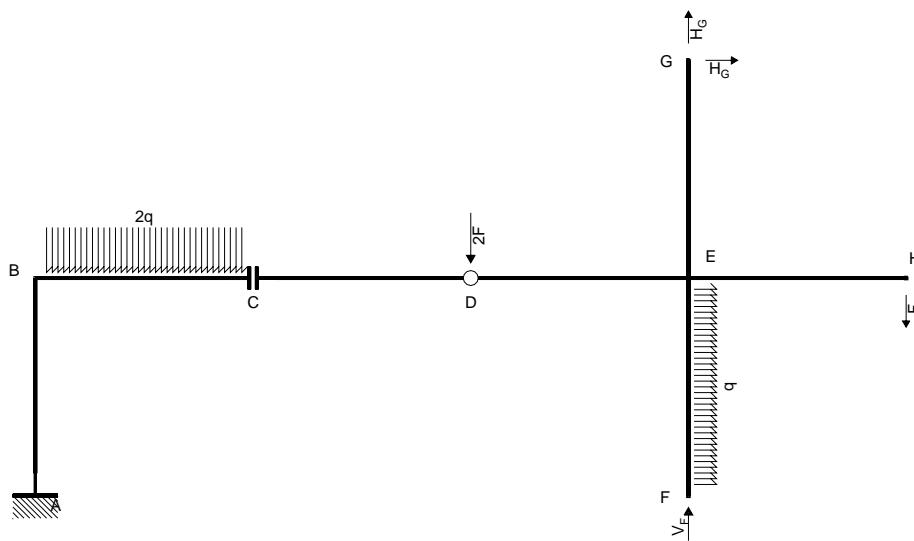
$\leftarrow \boxed{+} \rightarrow F$



$\uparrow \boxed{+} \downarrow F$



$\zeta \boxed{+} \zeta F_b$



EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG EH

$$V_F + H_G = 3F$$

Rotazione intorno a D: aste DE EF EG EH

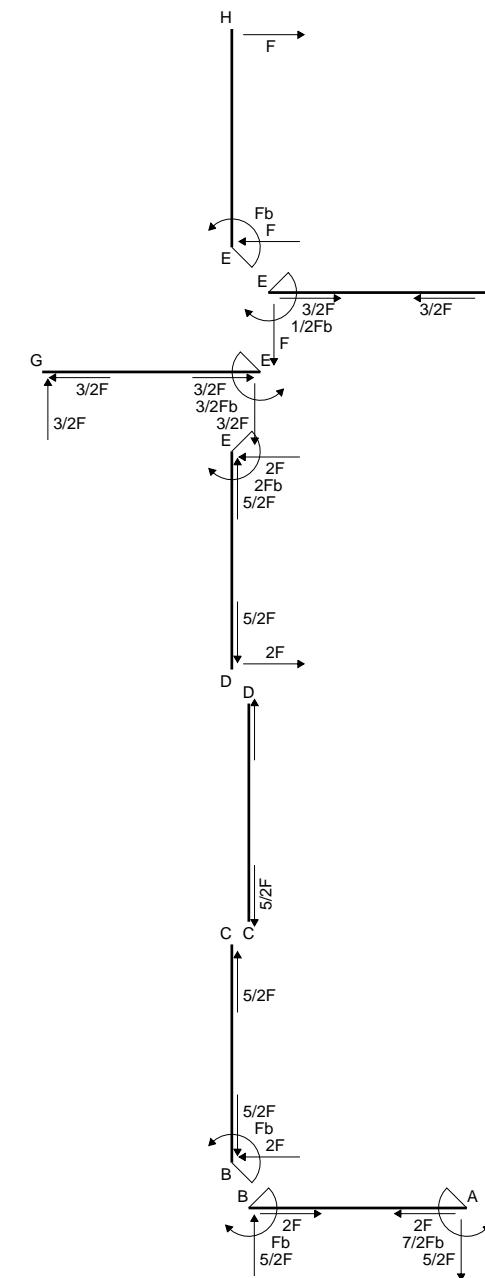
$$V_F b = 2Fb - 1/2qb^2$$

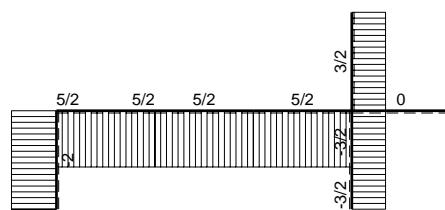
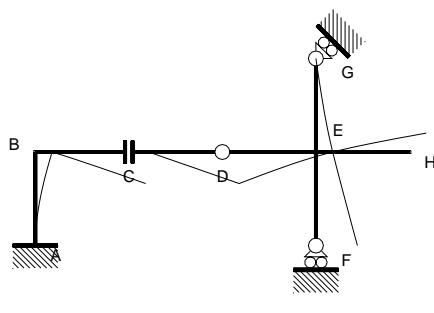
Matrice di equilibrio

$$\begin{bmatrix} V_{FB} & H_{GB} \\ 1 & 1 \\ \Phi_{DC} & 1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 3 & 0 \\ 2 & -1/2 \end{bmatrix}$$

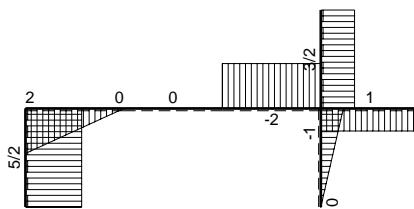
Soluzione del sistema

$$\begin{bmatrix} V_F b \\ H_G b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -1/2 \\ 1 & 1/2 \end{bmatrix}$$

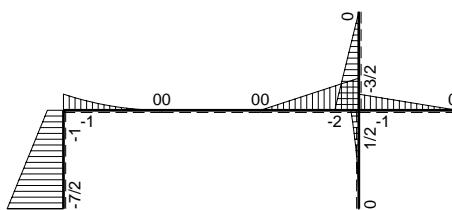




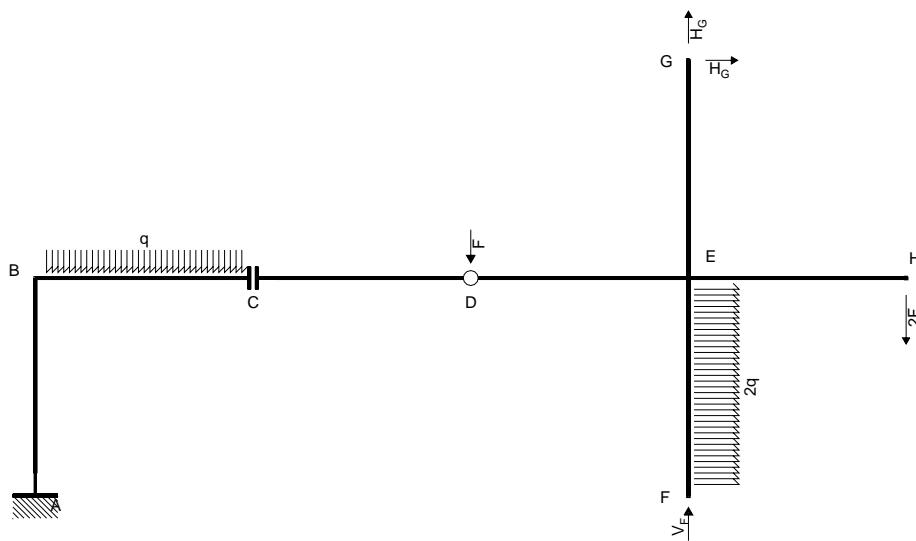
$\leftarrow \square \rightarrow F$



$\uparrow \square \downarrow F$



$\zeta \square \zeta Fb$



EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG EH

$$V_F + H_G = 3F$$

Rotazione intorno a D: aste DE EF EG EH

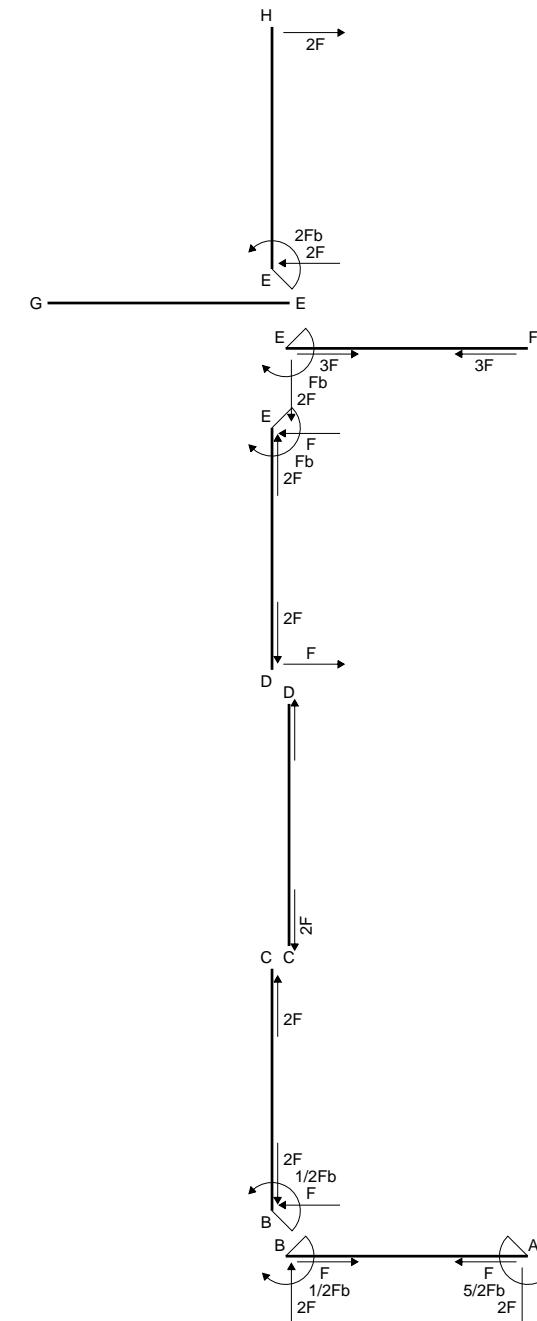
$$V_F b = 4Fb - qb^2$$

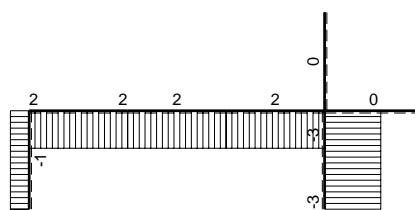
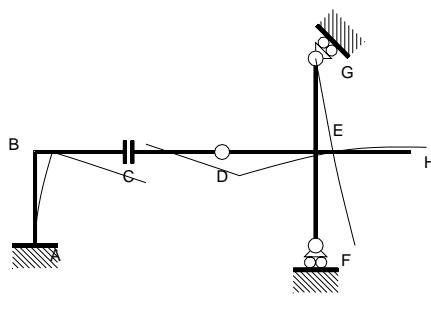
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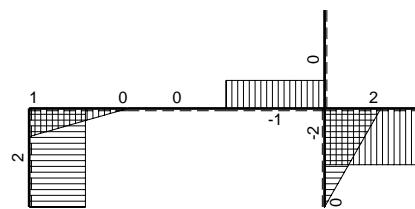
Soluzione del sistema

$$\begin{bmatrix} V_F b \\ H_G b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 4 & -1 \\ -1 & 1 \end{bmatrix}$$

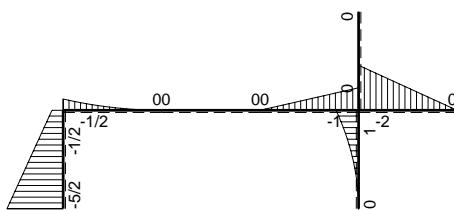




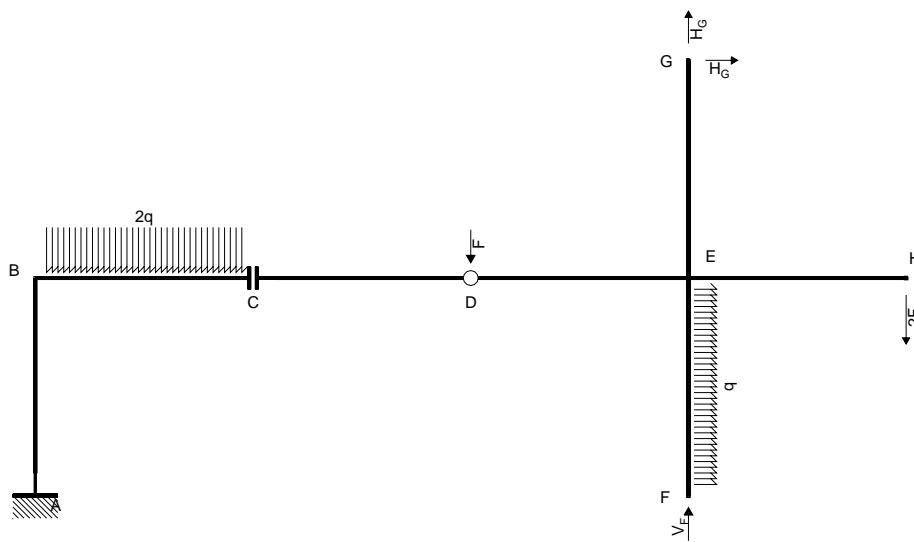
$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$



$\zeta [+] \zeta F_b$



EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG EH

$$V_F + H_G = 3F$$

Rotazione intorno a D: aste DE EF EG EH

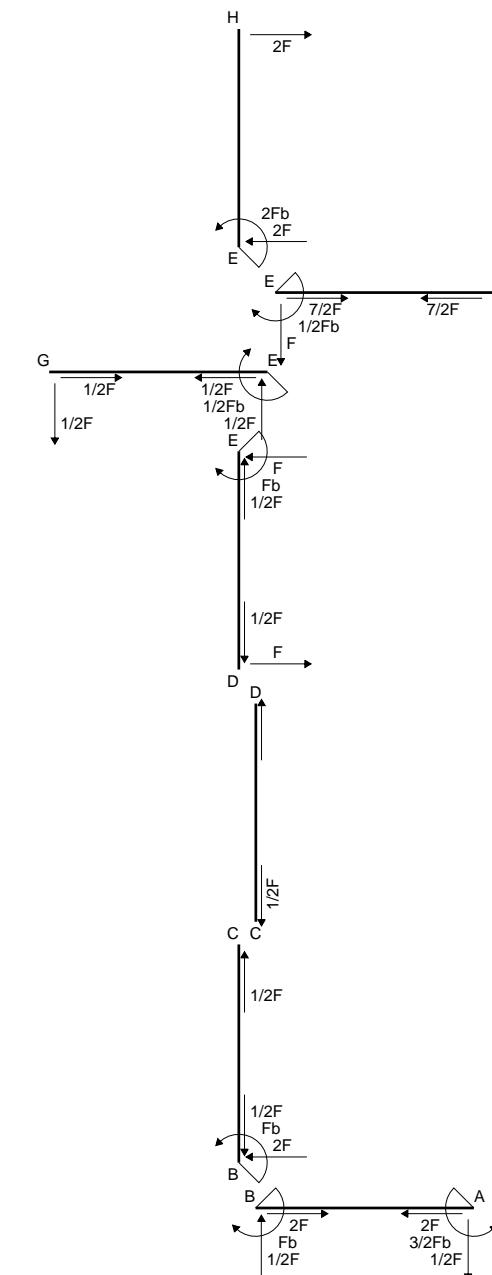
$$V_F b = 4Fb - 1/2qb^2$$

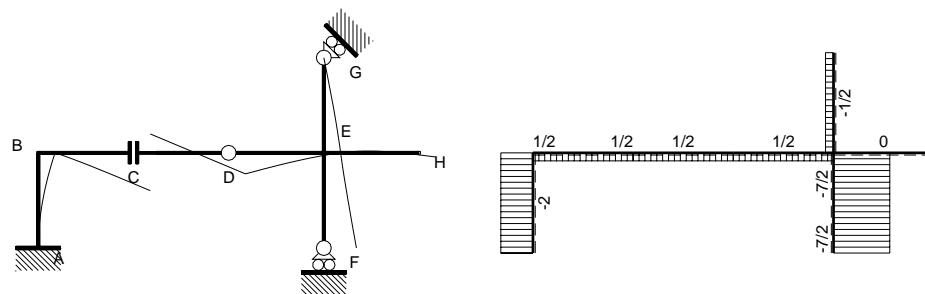
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$$\begin{bmatrix} V_F b & H_G b \\ V_{CB} & 1 & 1 \\ \Phi_{DC} & 1 & 0 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 3 & 0 \\ 4 & -1/2 \end{bmatrix}$$

Soluzione del sistema

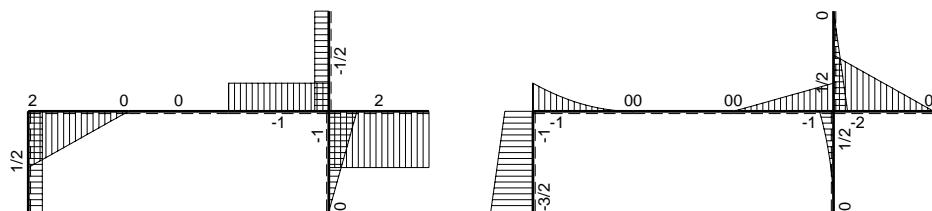
$$\begin{bmatrix} V_F b \\ H_G b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 4 & -1/2 \\ -1 & 1/2 \end{bmatrix}$$



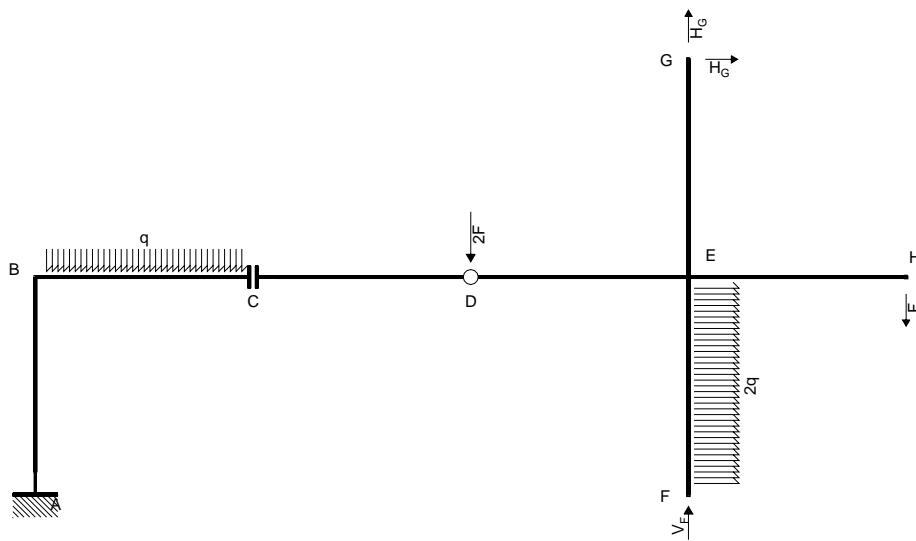


$\square \rightarrow 3 Fb^3/EJ$

$\leftarrow \square \rightarrow F$



$\square \rightarrow F$



EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG EH

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Rotazione intorno a D: aste DE EF EG EH

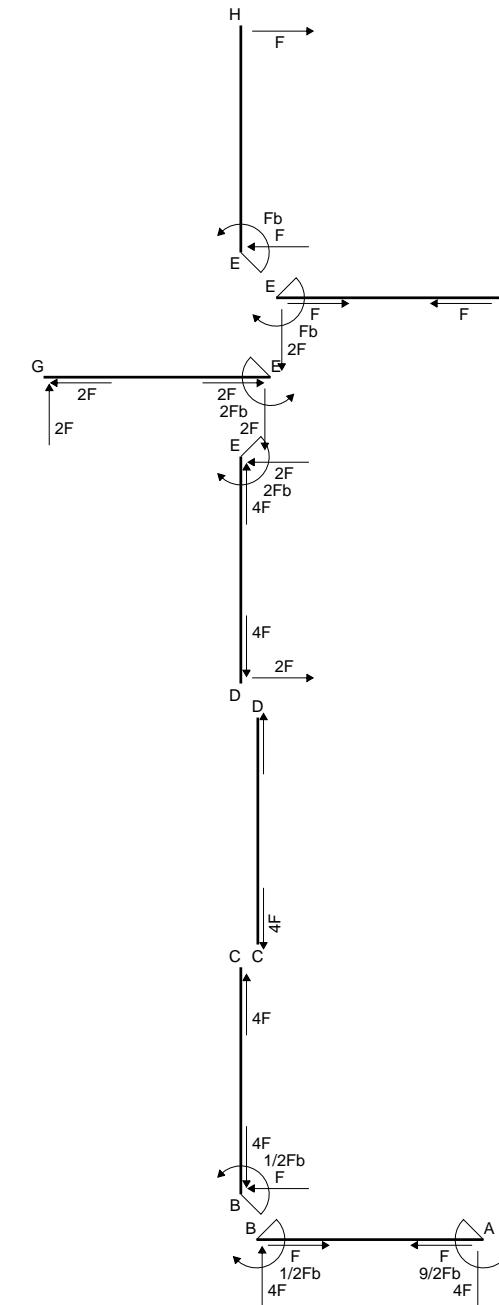
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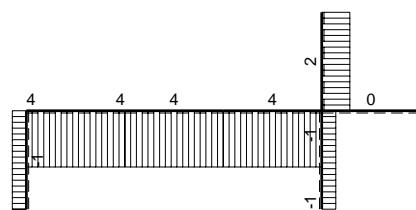
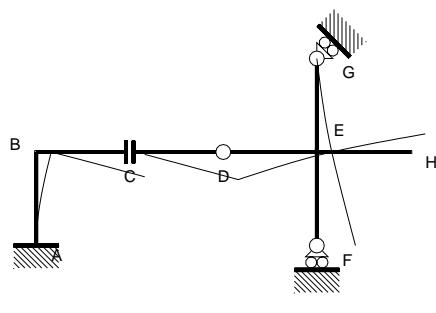
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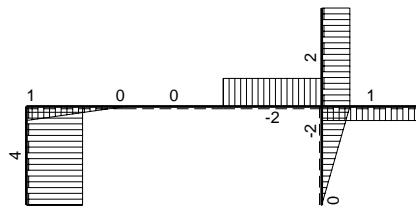
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$$\begin{bmatrix} V_F b \\ H_G b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -1 \\ 1 & 1 \end{bmatrix}$$

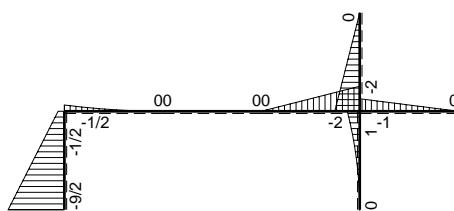




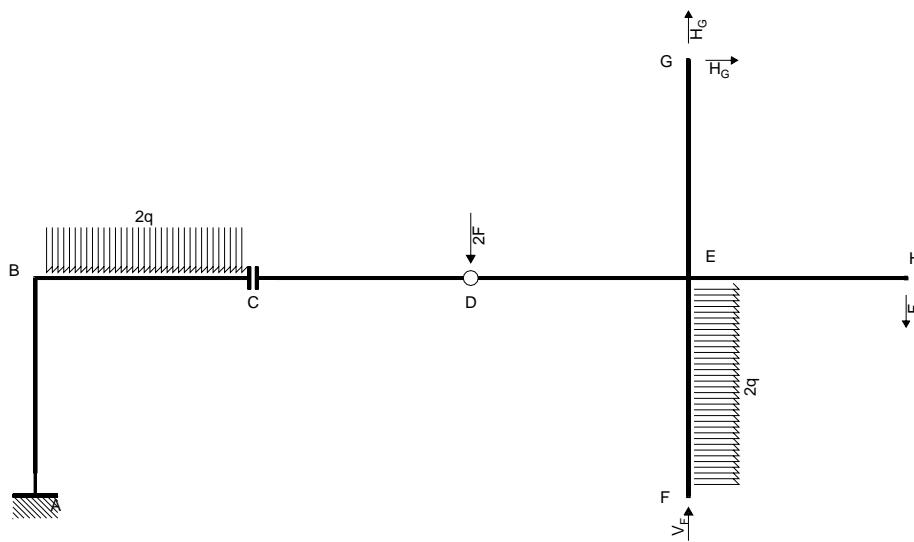
$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$



$\zeta [+] \zeta Fb$



EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG EH

$$V_F + H_G = 3F$$

Rotazione intorno a D: aste DE EF EG EH

$$V_F b = 2Fb - qb^2$$

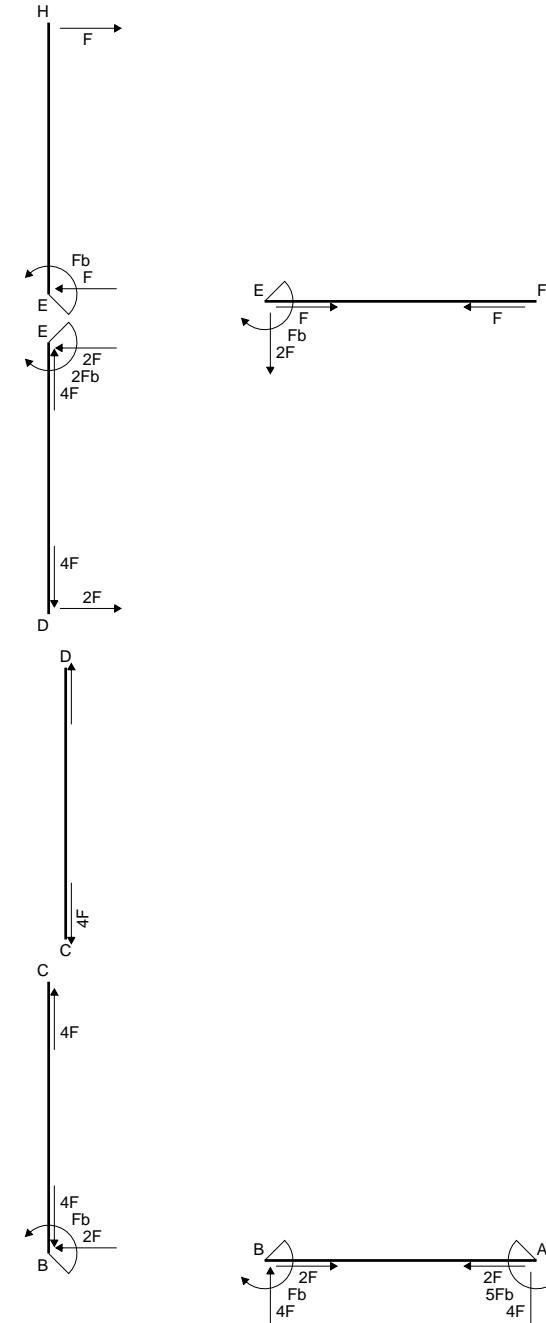
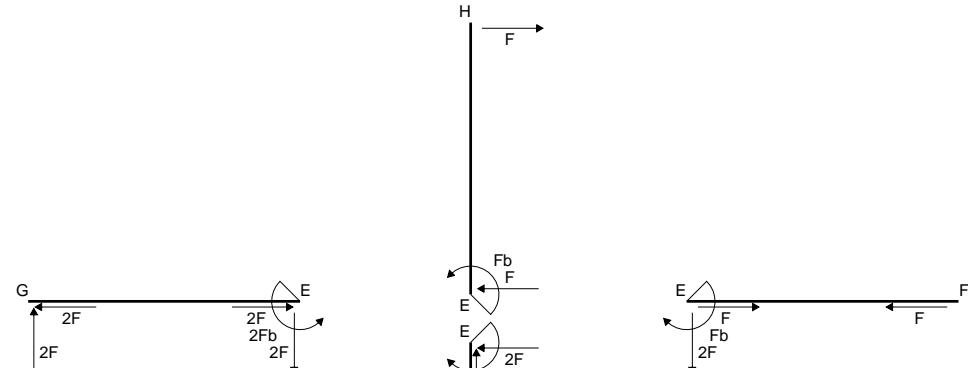
Matrice di equilibrio

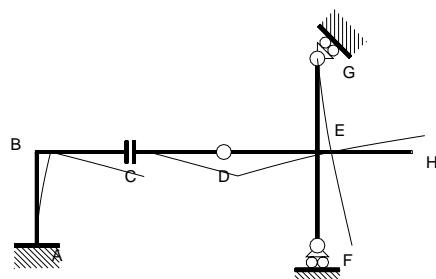
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$$\begin{bmatrix} V_{CB} & 1 & 1 \\ \Phi_{DC} & 1 & 0 \end{bmatrix} = \begin{bmatrix} 3 & 0 \\ 2 & -1 \end{bmatrix}$$

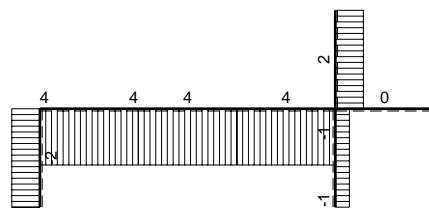
Soluzione del sistema

$$\begin{bmatrix} V_F b \\ H_G b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -1 \\ 1 & 1 \end{bmatrix}$$

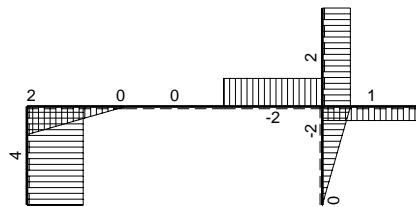




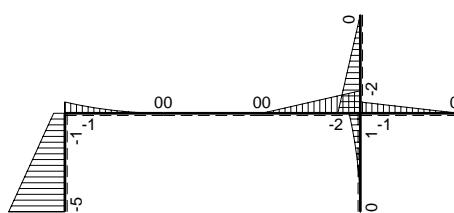
10 Fb³/EJ



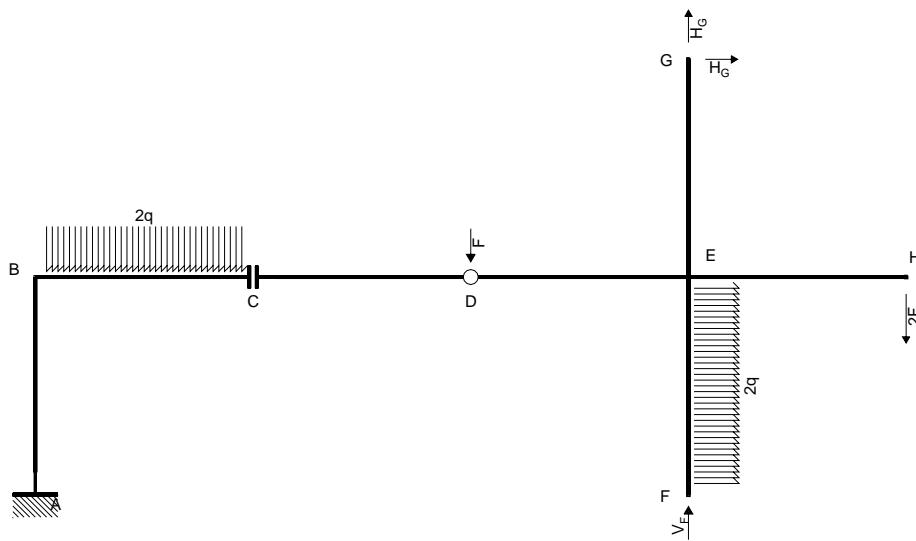
$$\longleftrightarrow \boxed{+} \longrightarrow F$$



A diagram showing a rectangular block with a plus sign (+) inside, indicating the center of mass. The block is positioned between two vertical arrows pointing upwards and downwards, labeled F.



$$\text{F}_b$$



EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG EH

$$V_F + H_G = 3F$$

Rotazione intorno a D: aste DE EF EG EH

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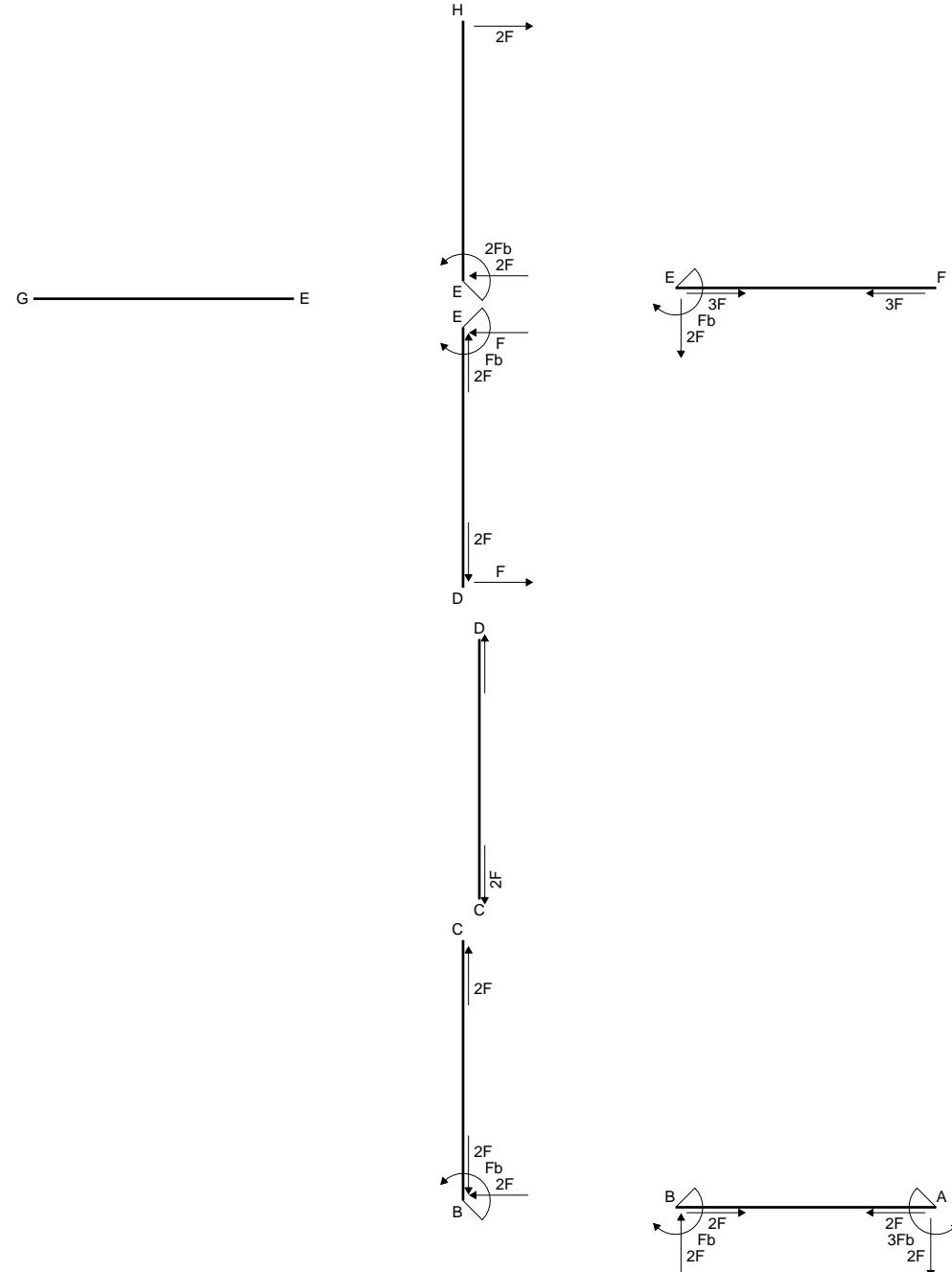
Matrice di equilibrio

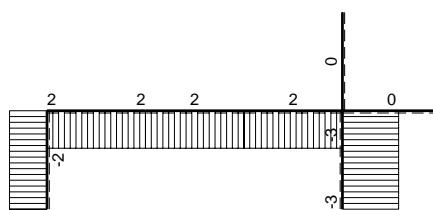
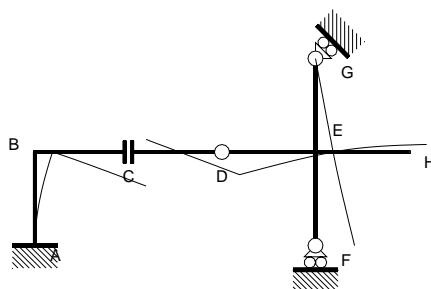
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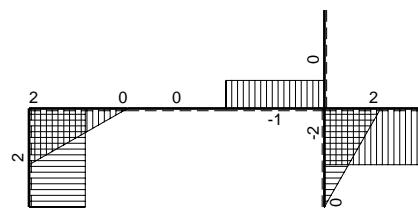
Soluzione del sistema

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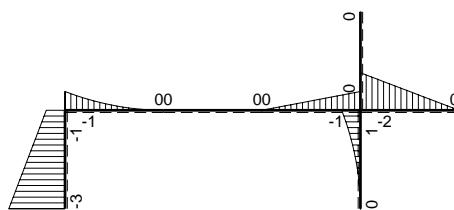




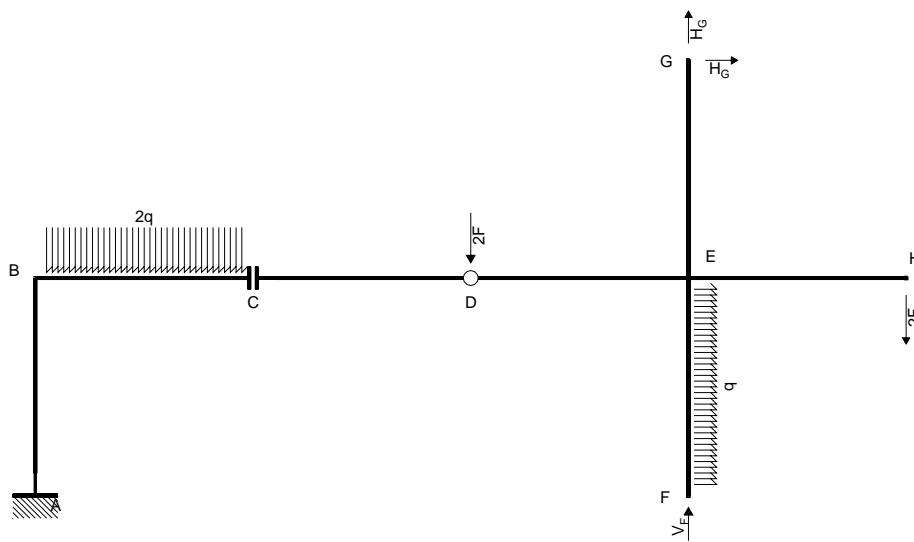
$\leftarrow \boxed{+} \rightarrow F$



$\uparrow \boxed{+} \downarrow F$



$\zeta \boxed{+} \zeta F_b$



EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG EH

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Rotazione intorno a D: aste DE EF EG EH

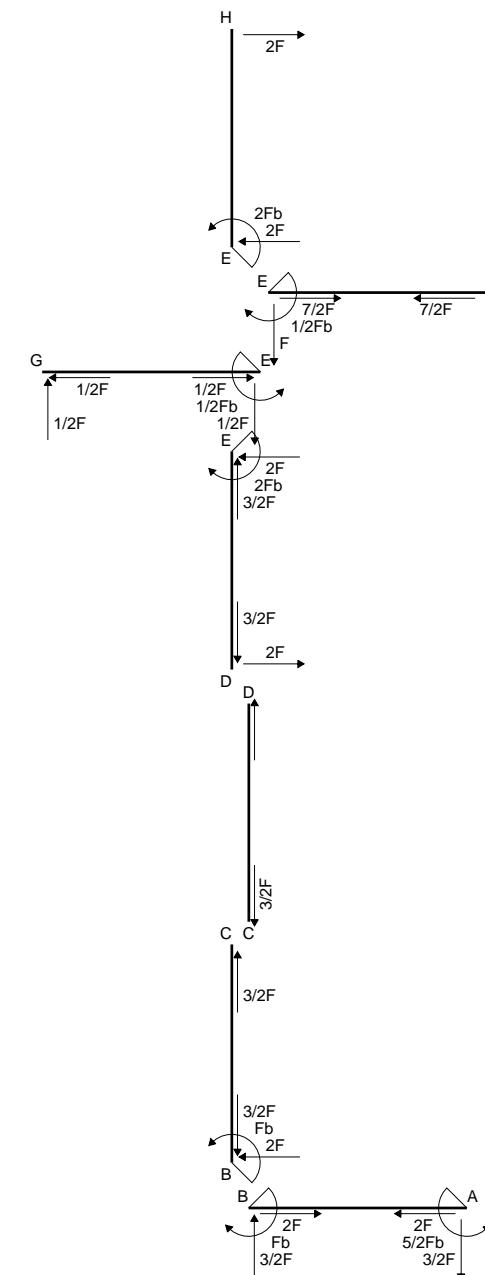
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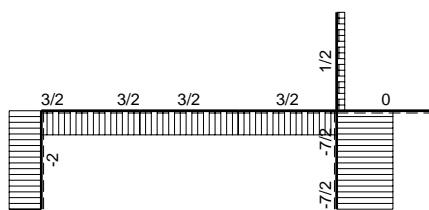
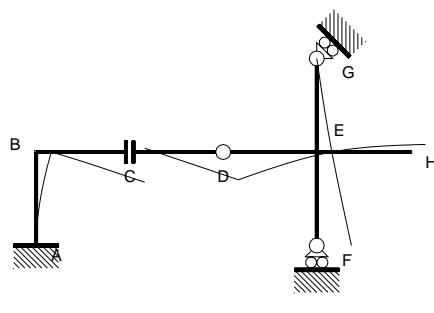
Matrice di equilibrio

$$\begin{bmatrix} V_F b & H_G b \\ V_{CB} & H_{DC} \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 1 & 1 \\ 4 & 0 \\ 4 & -1/2 \end{bmatrix}$$

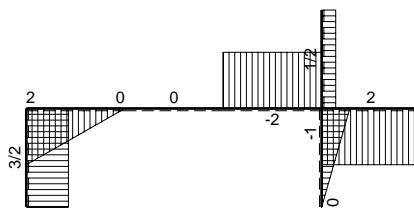
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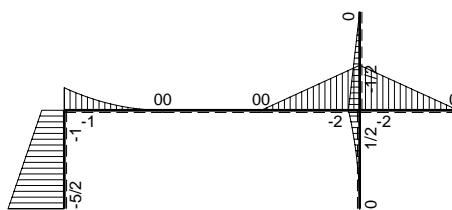




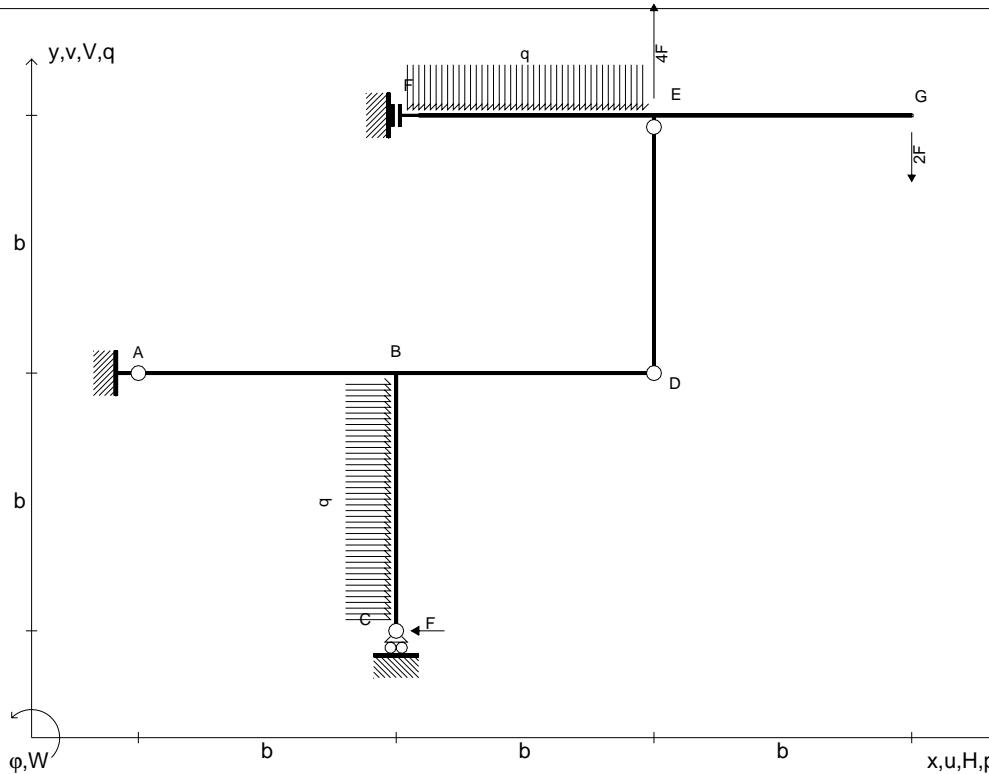
$\leftarrow \boxed{+} \rightarrow F$



$\uparrow \boxed{+} \downarrow F$



$\zeta \boxed{+} \zeta F_b$



$$H_C = -F$$

$$V_E = 4F$$

$$V_G = -2F$$

$$p_{BC} = q = F/b$$

$$q_{EF} = -q = -F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{BD} = EJ$$

$$EJ_{DE} = EJ$$

$$EJ_{EF} = EJ$$

$$EJ_{EG} = EJ$$

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

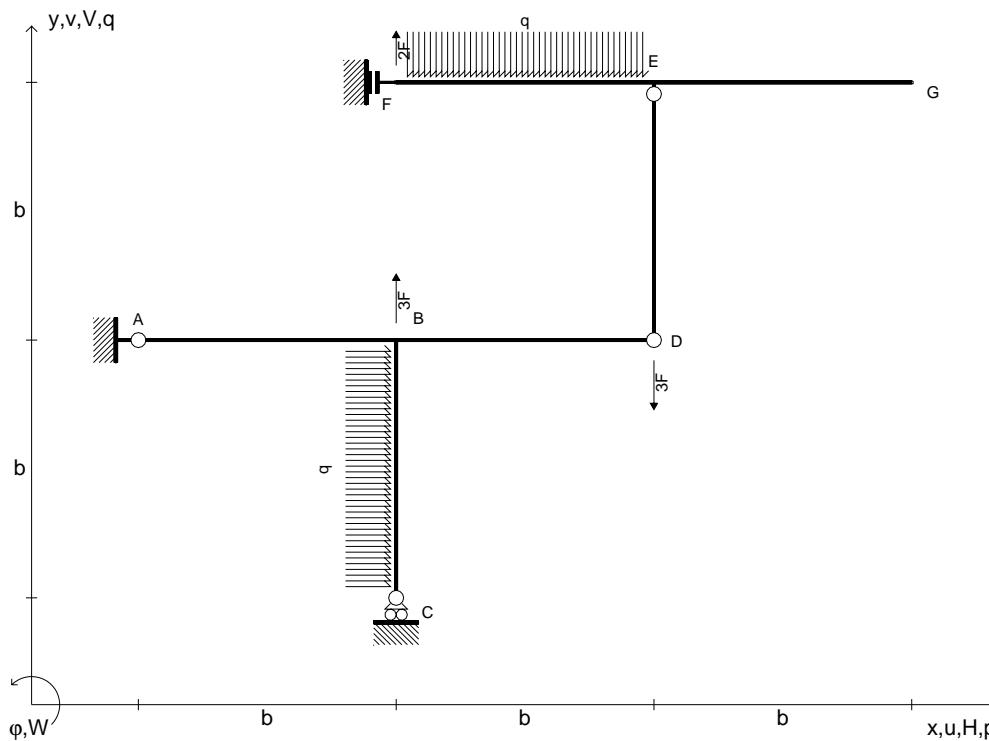
J_{YZ} - x_{YZ} - θ_{YZ} riferimento locale asta YZ con origine in Y.

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03.02.11

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$$V_B = 3F$$

$$V_D = -3F$$

$$V_F = 2F$$

$$V_D = -3F$$

$$q_{EF} = -q = -F/b$$

$$p_{BC} = q = F/b$$

$$EJ_{BC} = EJ$$

$$EJ_{AB} = EJ$$

$$EJ_{BD} = EJ$$

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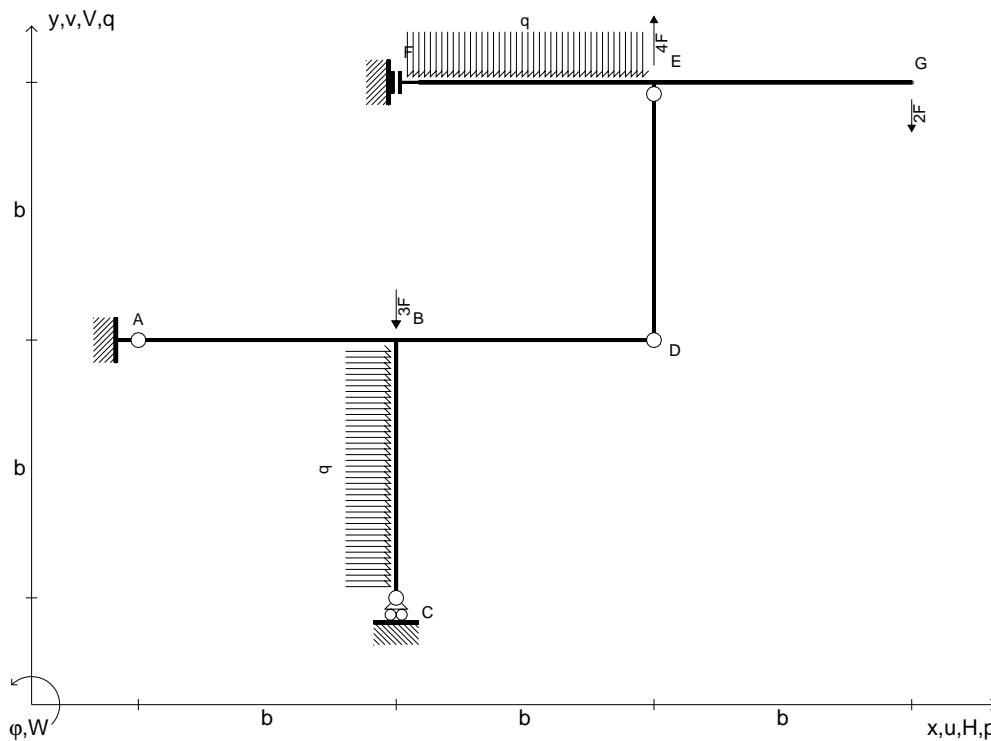
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$$V_E = 4F$$

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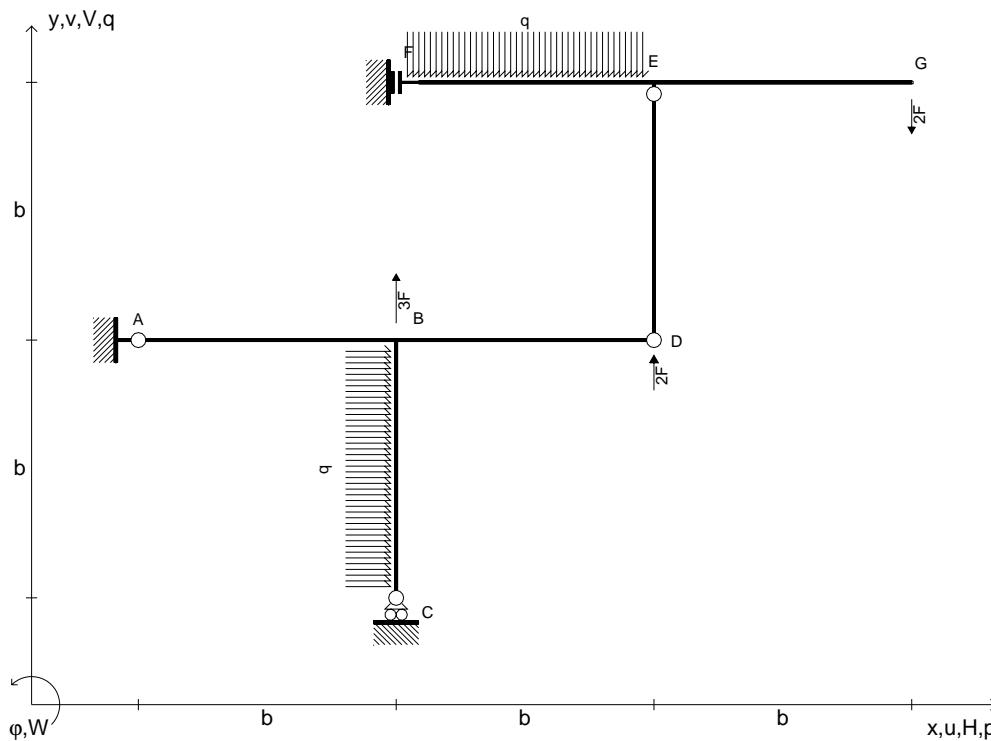
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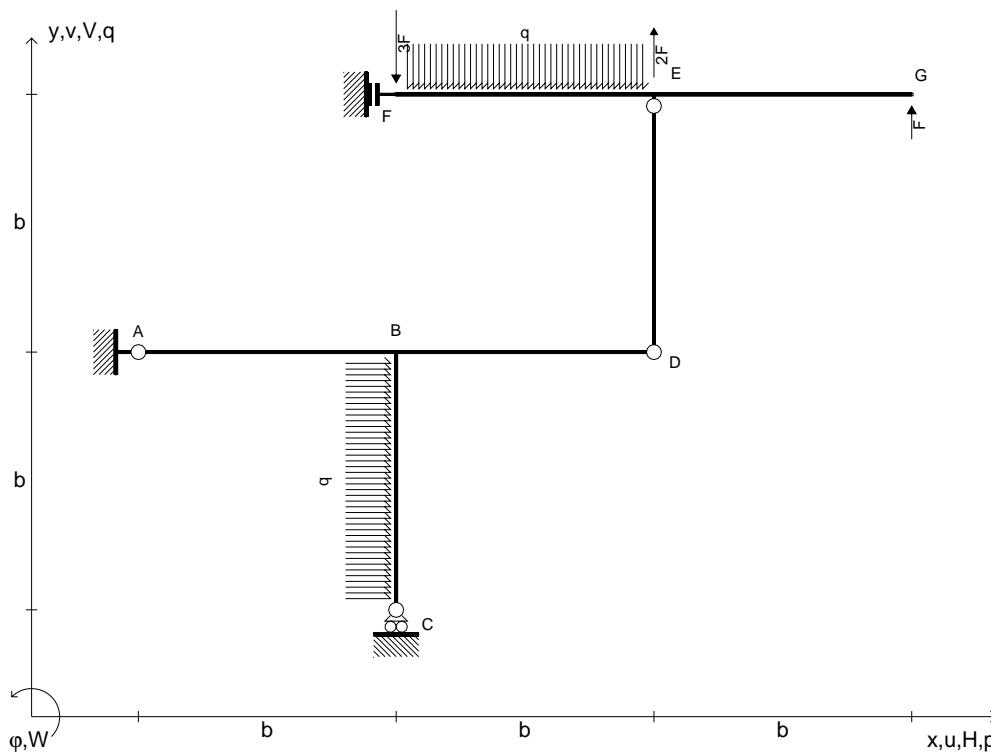
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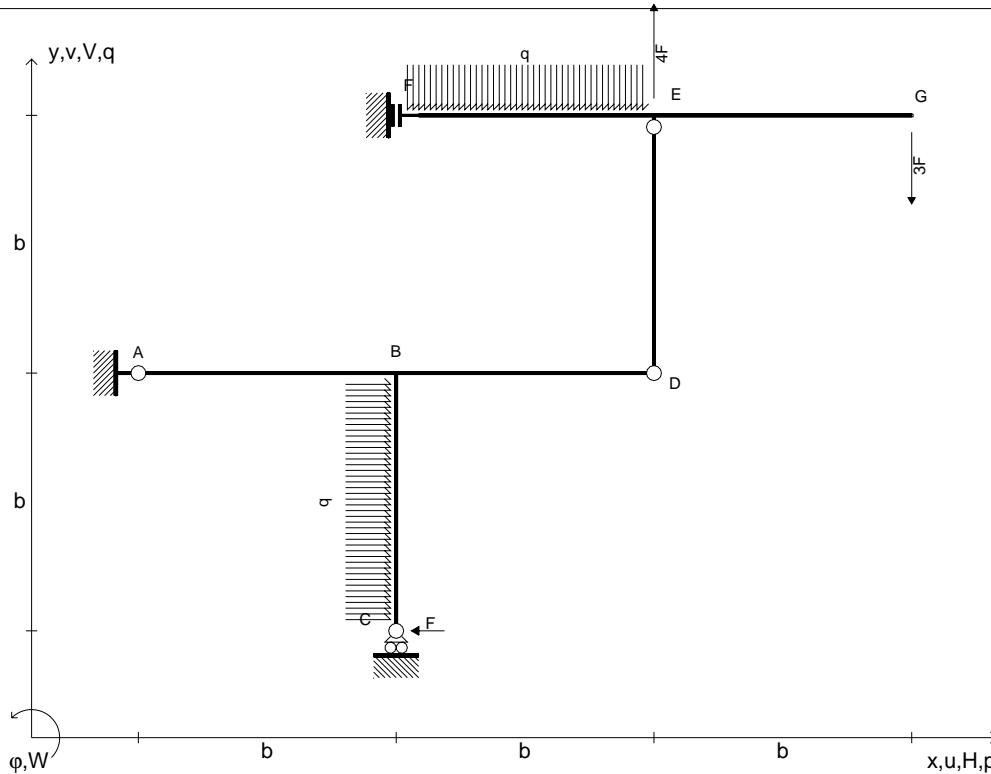
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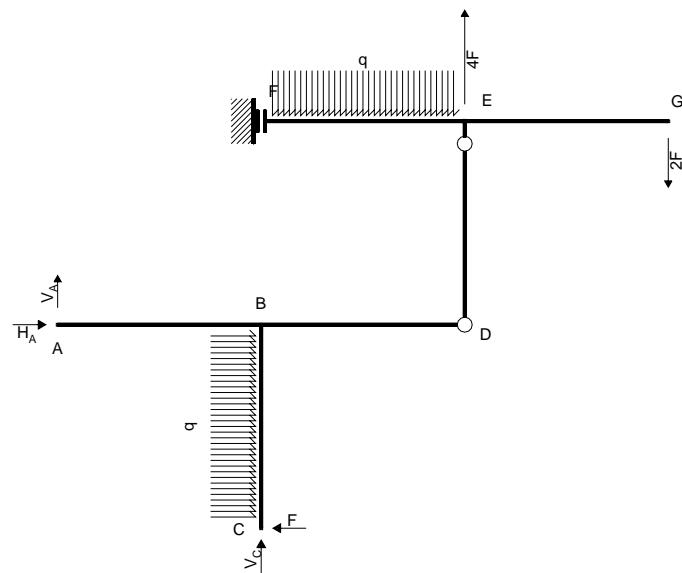
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EQUAZIONI DI EQUILIBRIO

Traslazione verticale globale

$$V_A + V_C = -2F + qb$$

Rotazione intorno a E: aste ED DB BA BC

$$H_A b - 2V_A b - V_C b = 2Fb - 3/2qb^2$$

Rotazione intorno a D: aste DB BA BC

$$-2V_A b - V_C b = Fb - 1/2qb^2$$

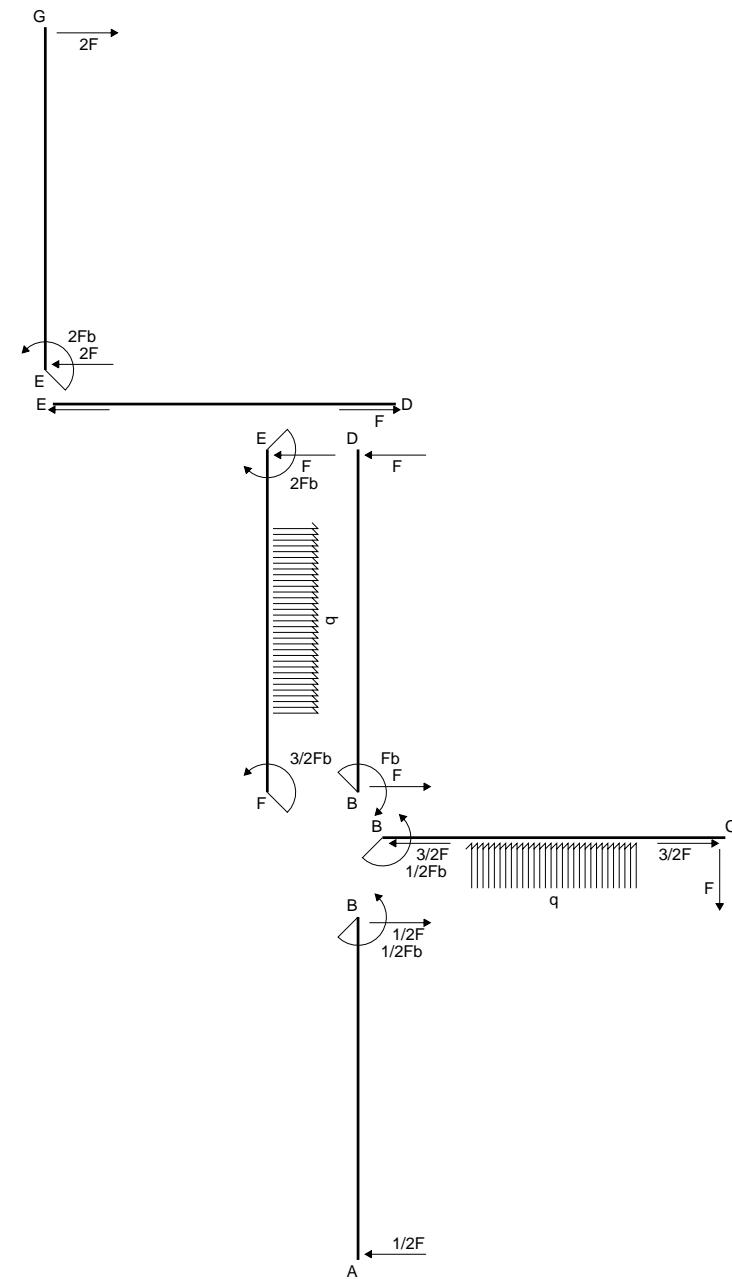
Matrice di equilibrio

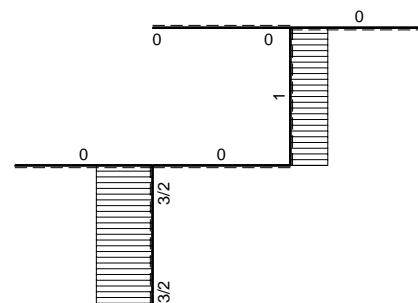
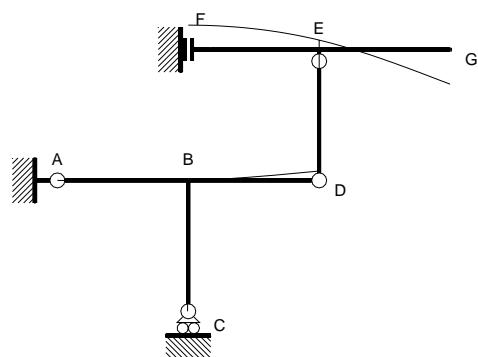
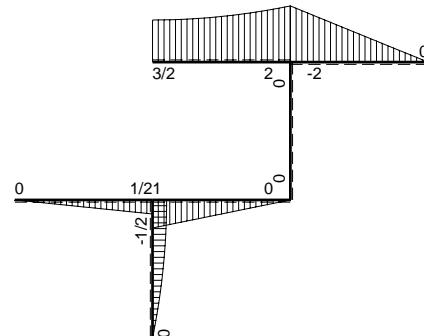
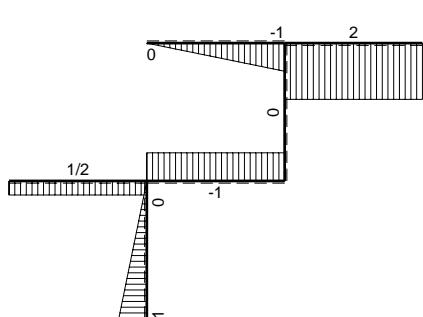
$$\begin{bmatrix} H_A b & V_A b & V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$

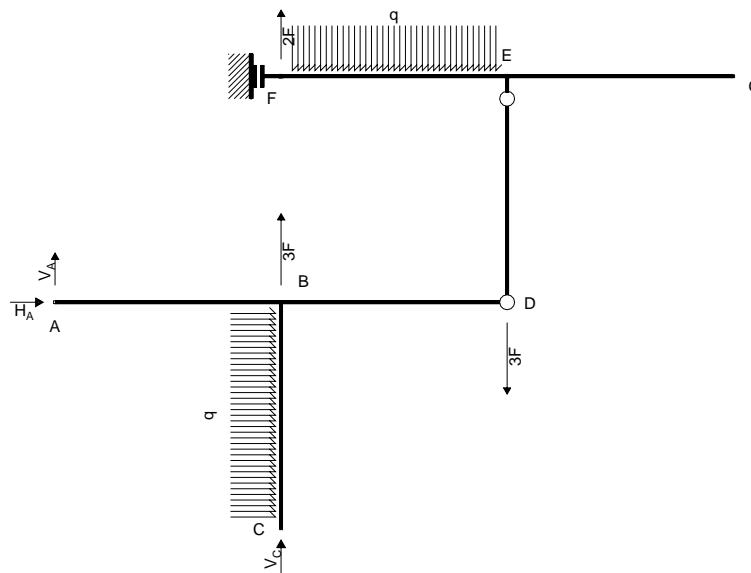
$$\begin{bmatrix} V_A & \\ H_A & \\ \varphi_{ED} & \\ \varphi_{DB} & \end{bmatrix} = \begin{bmatrix} 0 & 1 & 1 \\ 1 & -2 & -1 \\ 0 & -2 & -1 \end{bmatrix} \begin{bmatrix} -2 & 1 \\ 2 & -3/2 \\ 1 & -1/2 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_A & \\ H_A & \\ \varphi_{ED} & \\ \varphi_{DB} & \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 1 & -1/2 \\ 1 & -1 \\ -3 & 3/2 \end{bmatrix}$$




 $\text{---} 4 F b^3 / E J$
 $\leftarrow [+] \rightarrow F$

 $\uparrow [+] \downarrow F$



EQUAZIONI DI EQUILIBRIO

Traslazione verticale globale

$$V_A + V_C = -2F + qb$$

Rotazione intorno a E: aste ED DB BA BC

$$H_A b - 2V_A b - V_C b = 3Fb - 3/2qb^2$$

Rotazione intorno a D: aste DB BA BC

$$-2V_A b - V_C b = 3Fb - 1/2qb^2$$

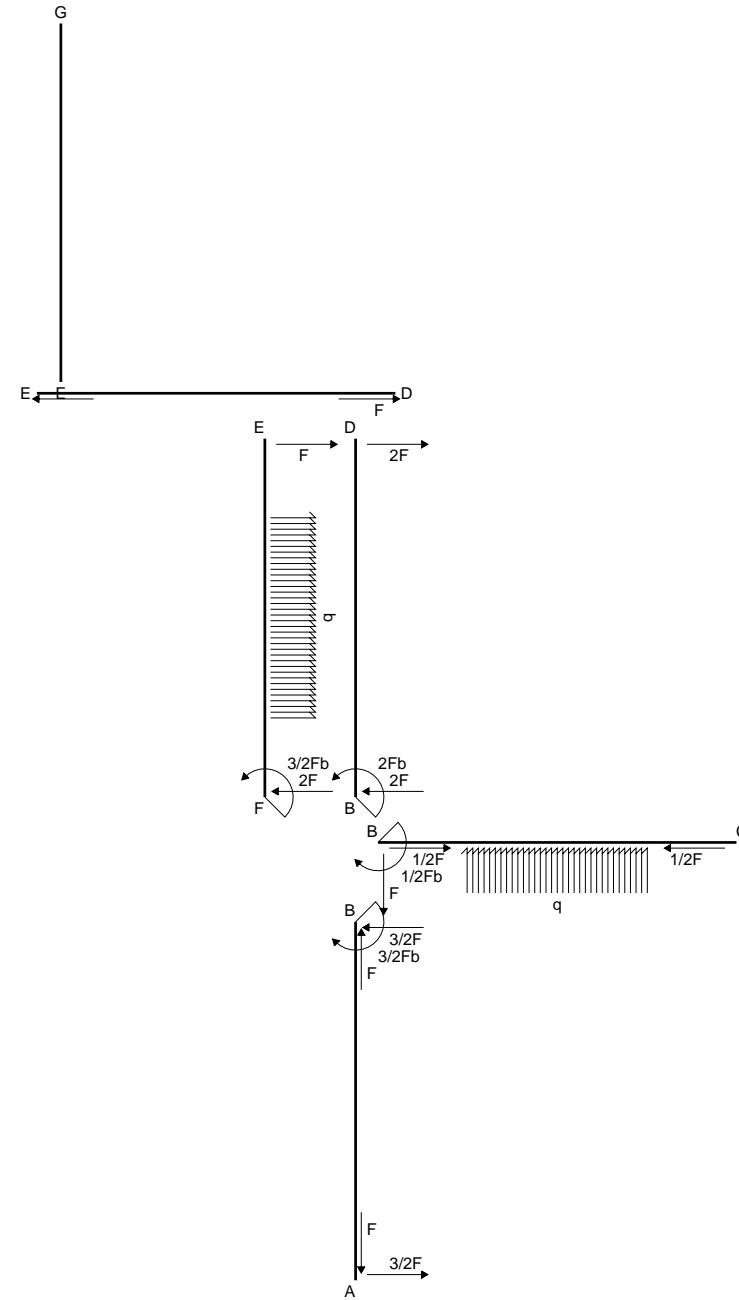
Matrice di equilibrio

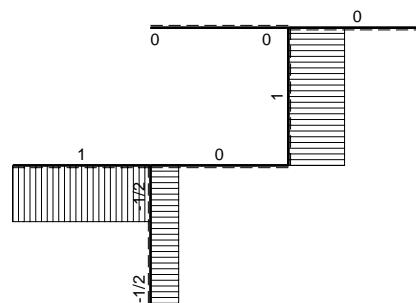
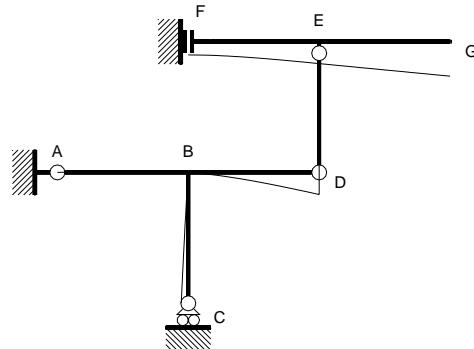
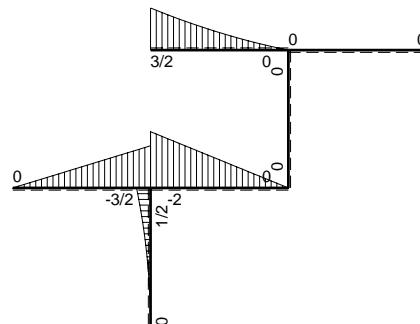
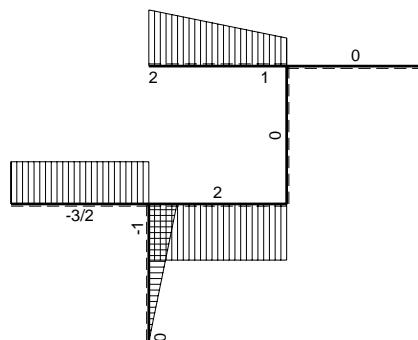
$$\begin{bmatrix} H_A b & V_A b & V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$

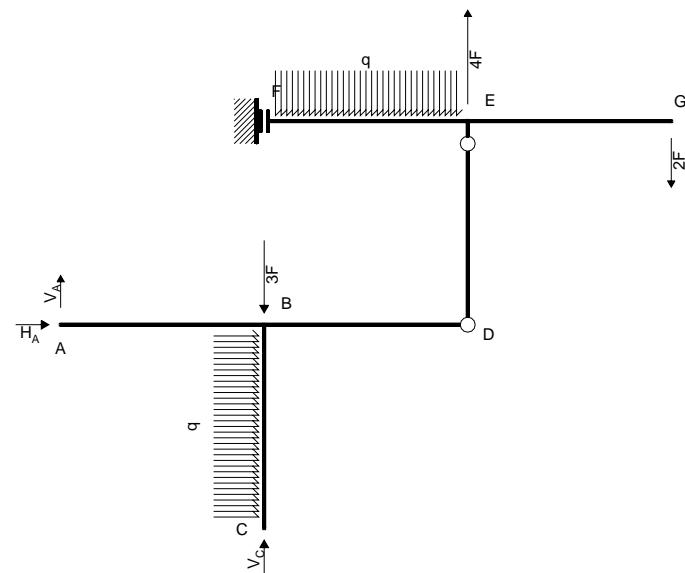
$$\begin{bmatrix} V_F \\ \varphi_{ED} \\ \varphi_{DB} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 1 \\ 1 & -2 & -1 \\ 0 & -2 & -1 \end{bmatrix} \begin{bmatrix} -2 & 1 \\ 3 & -3/2 \\ 3 & -1/2 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_A b \\ H_A b \\ V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -1 & -1/2 \\ 0 & -1 \\ -1 & 3/2 \end{bmatrix}$$




 $\longleftarrow 4 F b^3 / E J$
 $\leftarrow [+] \rightarrow F$

 $\uparrow [+] \downarrow$
 $\curvearrowleft [+] \curvearrowright$



EQUAZIONI DI EQUILIBRIO

Traslazione verticale globale

$$V_A + V_C = F + qb$$

Rotazione intorno a E: aste ED DB BA BC

$$H_A b - 2V_A b - V_C b = -3Fb - 3/2qb^2$$

Rotazione intorno a D: aste DB BA BC

$$-2V_A b - V_C b = -3Fb - 1/2qb^2$$

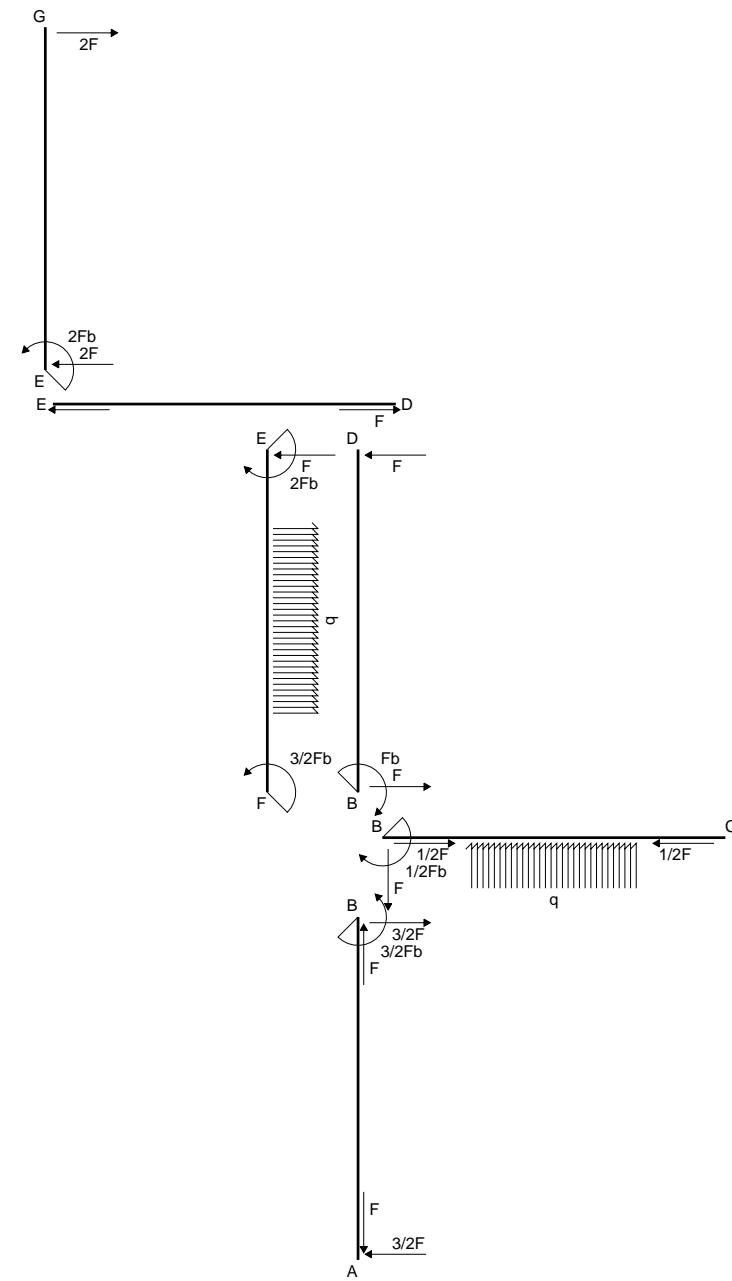
Matrice di equilibrio

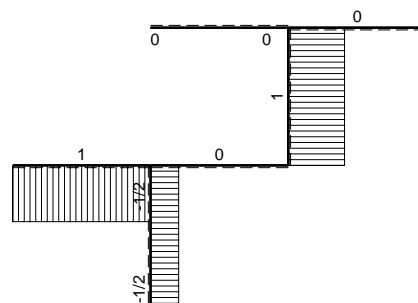
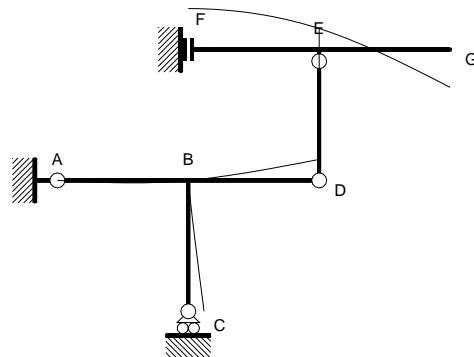
$$\begin{bmatrix} H_A b & V_A b & V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$

$$\begin{bmatrix} V_A & 0 & 1 & 1 \\ \Phi_{ED} & 1 & -2 & -1 \\ \Phi_{DB} & 0 & -2 & -1 \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ -3 & -3/2 \\ -3 & -1/2 \end{bmatrix}$$

Soluzione del sistema

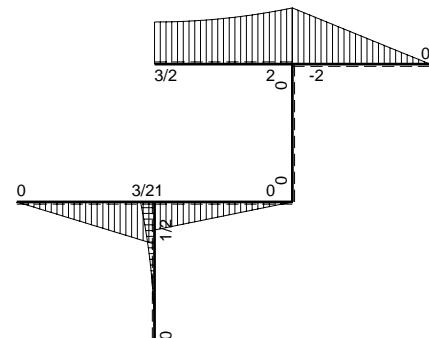
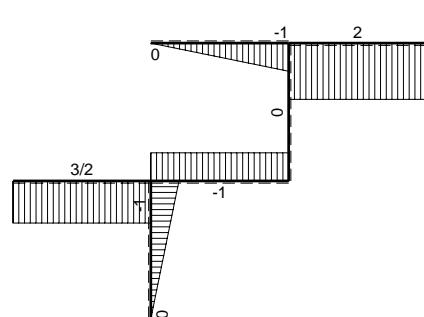
$$\begin{bmatrix} V_A b \\ H_A b \\ V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -1/2 \\ 0 & -1 \\ -1 & 3/2 \end{bmatrix}$$





$\longleftarrow 3 F b^3 / E J$

$\longleftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow$ F

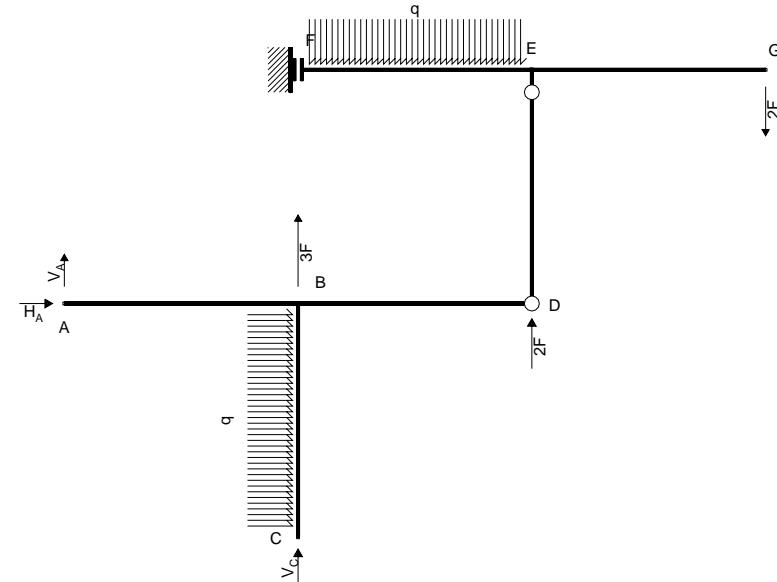
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$\curvearrowleft [+] \curvearrowright$ F_b

03.02.11

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03.02.11



EQUAZIONI DI EQUILIBRIO

Traslazione verticale globale

$$V_A + V_C = -3F + qb$$

Rotazione intorno a E: aste ED DB BA BC

$$H_A b - 2V_A b - V_C b = 3Fb - 3/2qb^2$$

Rotazione intorno a D: aste DB BA BC

$$-2V_A b - V_C b = 3Fb - 1/2qb^2$$

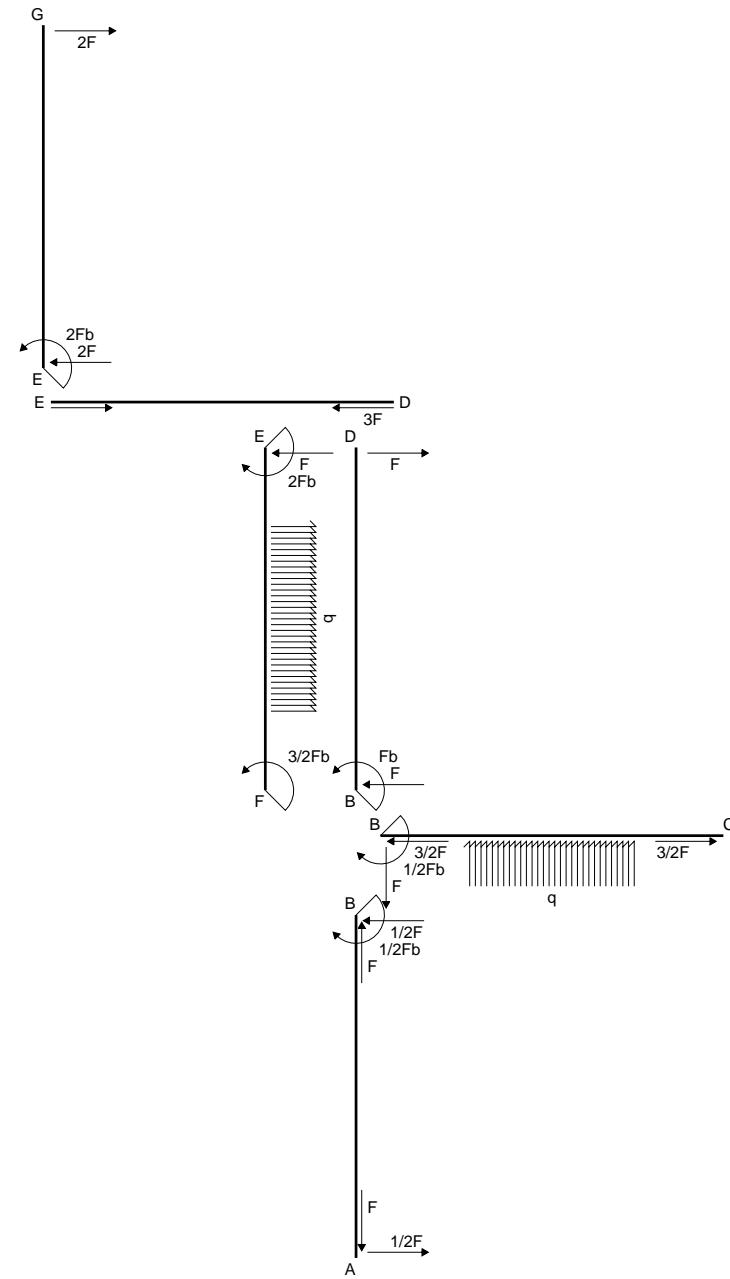
Matrice di equilibrio

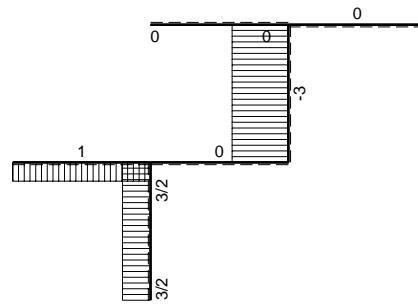
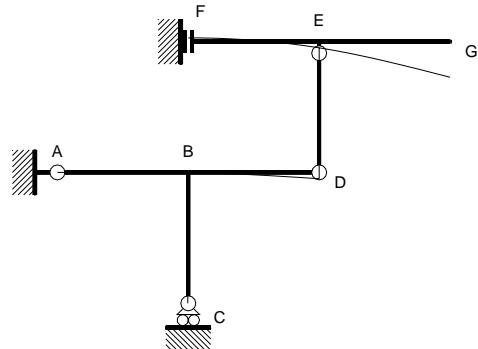
$$\begin{bmatrix} H_A b & V_A b & V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$

$$\begin{bmatrix} V_F \\ \varphi_{ED} \\ \varphi_{DB} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 1 \\ 1 & -2 & -1 \\ 0 & -2 & -1 \end{bmatrix} \begin{bmatrix} -3 & 1 \\ 3 & -3/2 \\ 3 & -1/2 \end{bmatrix}$$

Soluzione del sistema

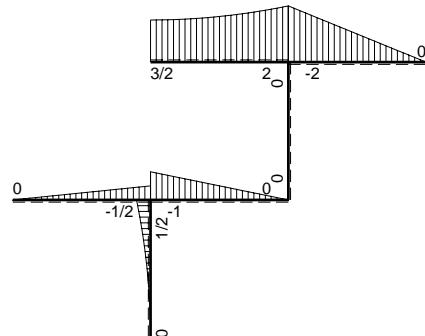
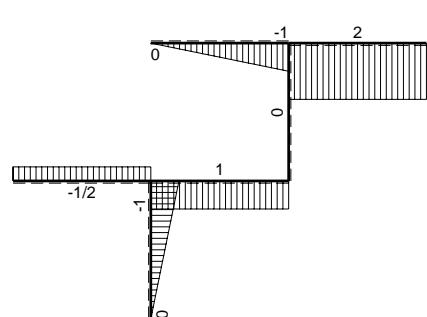
$$\begin{bmatrix} V_A b \\ H_A b \\ V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & -1/2 \\ 0 & -1 \\ -3 & 3/2 \end{bmatrix}$$





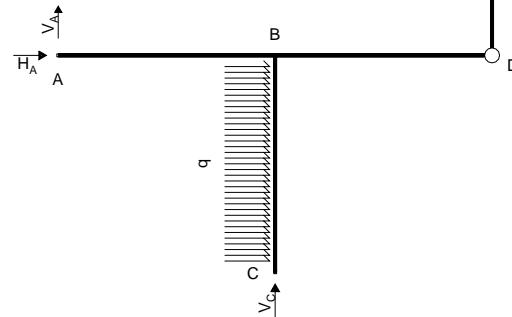
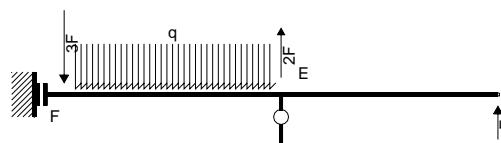
$\longleftarrow 6 F b^3 / E J$

$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow$ F

$\curvearrowleft [+] \curvearrowright$ F_b



EQUAZIONI DI EQUILIBRIO

Traslazione verticale globale

$$V_A + V_C = qb$$

Rotazione intorno a E: aste ED DB BA BC

$$H_A b - 2V_A b - V_C b = -3/2qb^2$$

Rotazione intorno a D: aste DB BA BC

$$-2V_A b - V_C b = -1/2qb^2$$

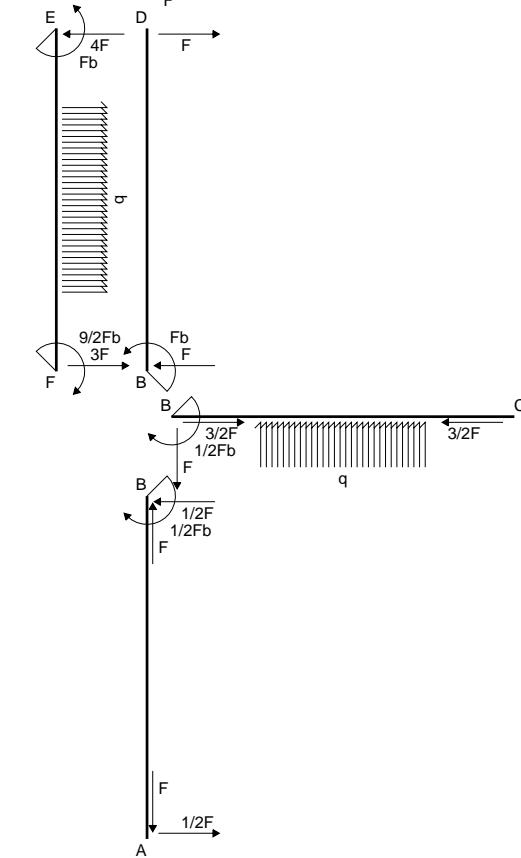
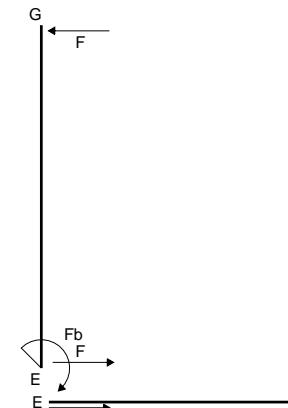
Matrice di equilibrio

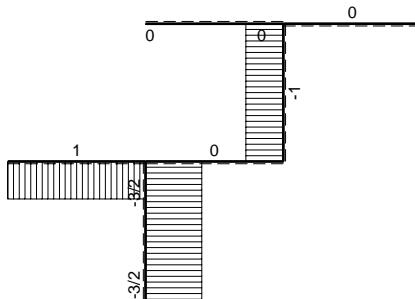
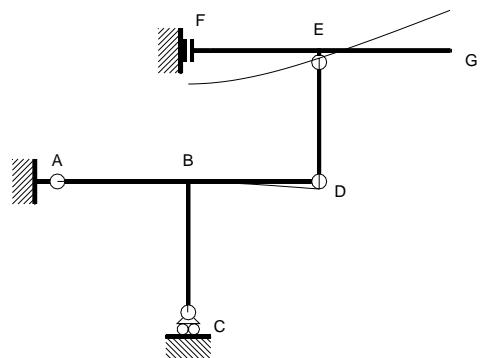
$$\begin{bmatrix} H_A b & V_A b & V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$

$$\begin{bmatrix} V_F \\ \varphi_{ED} \\ \varphi_{DB} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 1 \\ 1 & -2 & -1 \\ 0 & -2 & -1 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 0 & -3/2 \\ 0 & -1/2 \end{bmatrix}$$

Soluzione del sistema

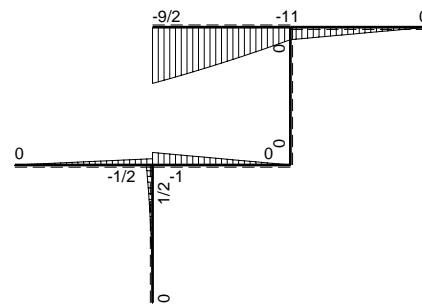
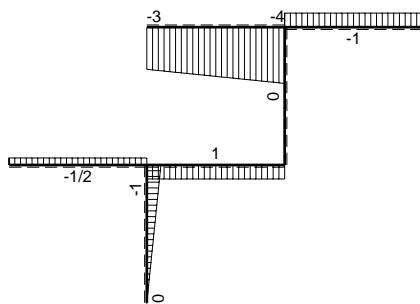
$$\begin{bmatrix} V_A b \\ H_A b \\ V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & -1/2 \\ 0 & -1 \\ 0 & 3/2 \end{bmatrix}$$



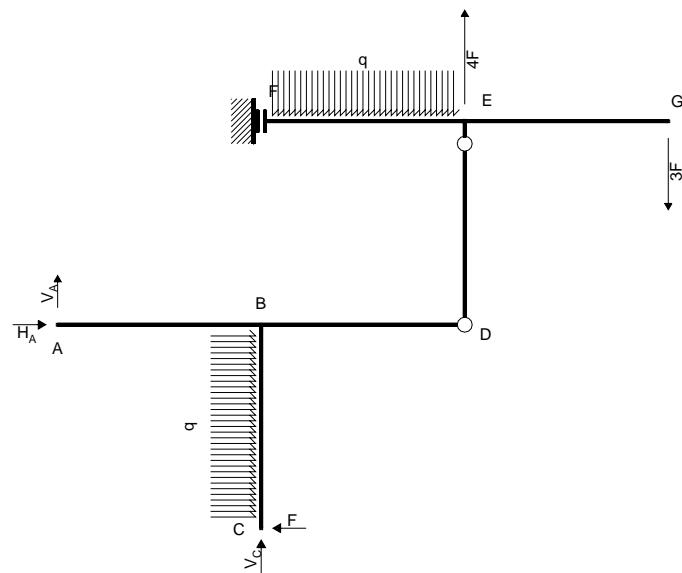


$\longleftarrow 5 Fb^3/EJ$

$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow$ F



EQUAZIONI DI EQUILIBRIO

Traslazione verticale globale

$$V_A + V_C = -F + qb$$

Rotazione intorno a E: aste ED DB BA BC

$$H_A b - 2V_A b - V_C b = 2Fb - 3/2qb^2$$

Rotazione intorno a D: aste DB BA BC

$$-2V_A b - V_C b = Fb - 1/2qb^2$$

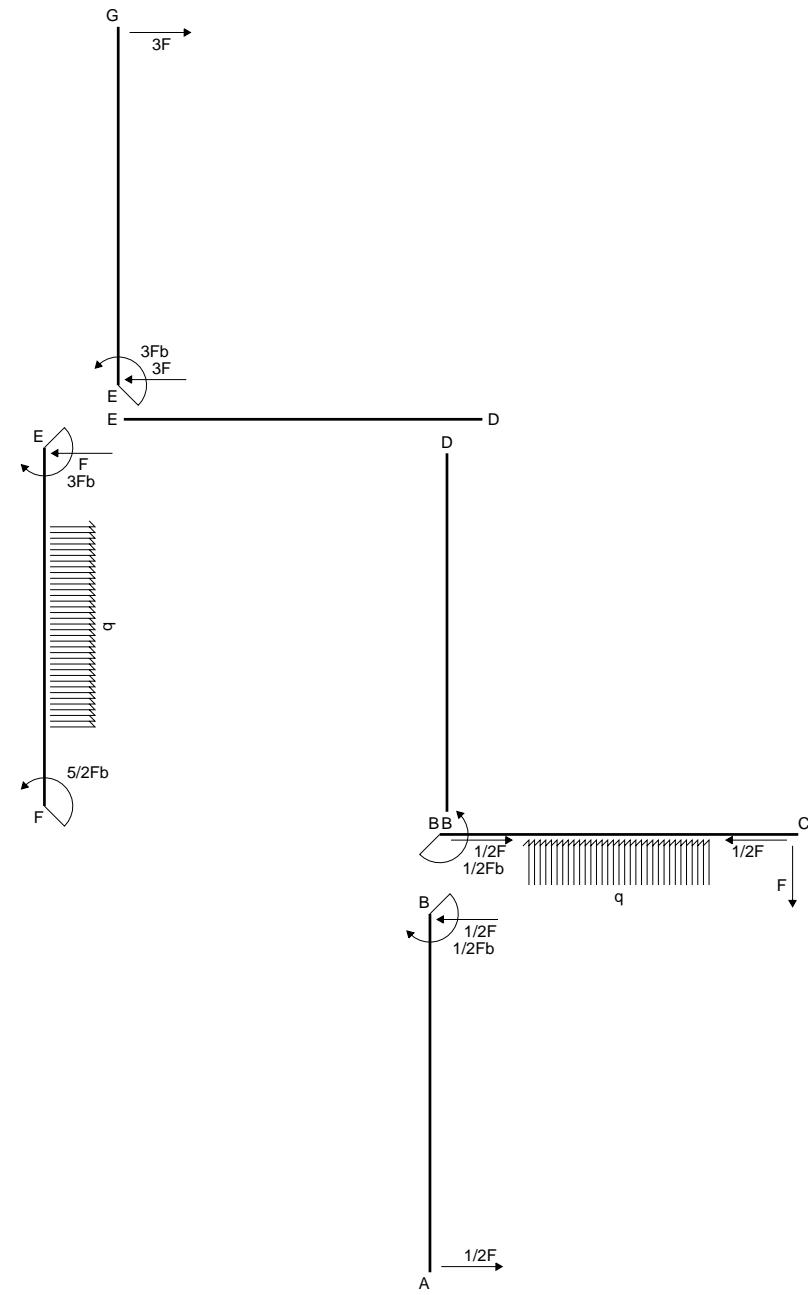
Matrice di equilibrio

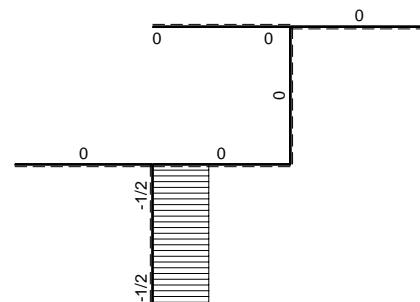
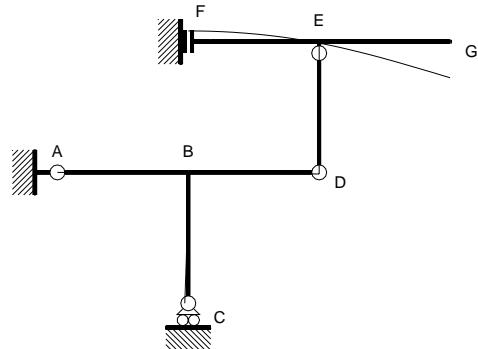
$$\begin{bmatrix} H_A b & V_A b & V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$

$$\begin{bmatrix} V_F \\ \varphi_{ED} \\ \varphi_{DB} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 1 \\ 1 & -2 & -1 \\ 0 & -2 & -1 \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 2 & -3/2 \\ 1 & -1/2 \end{bmatrix}$$

Soluzione del sistema

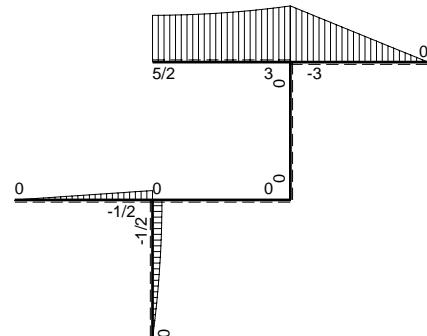
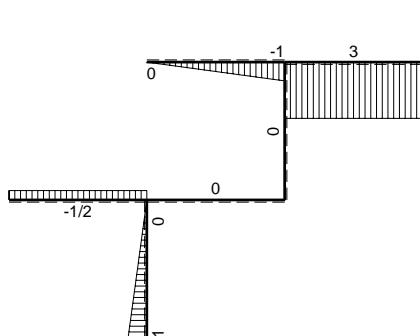
$$\begin{bmatrix} V_A b \\ H_A b \\ V_C b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 0 & -1/2 \\ 1 & -1 \\ -1 & 3/2 \end{bmatrix}$$



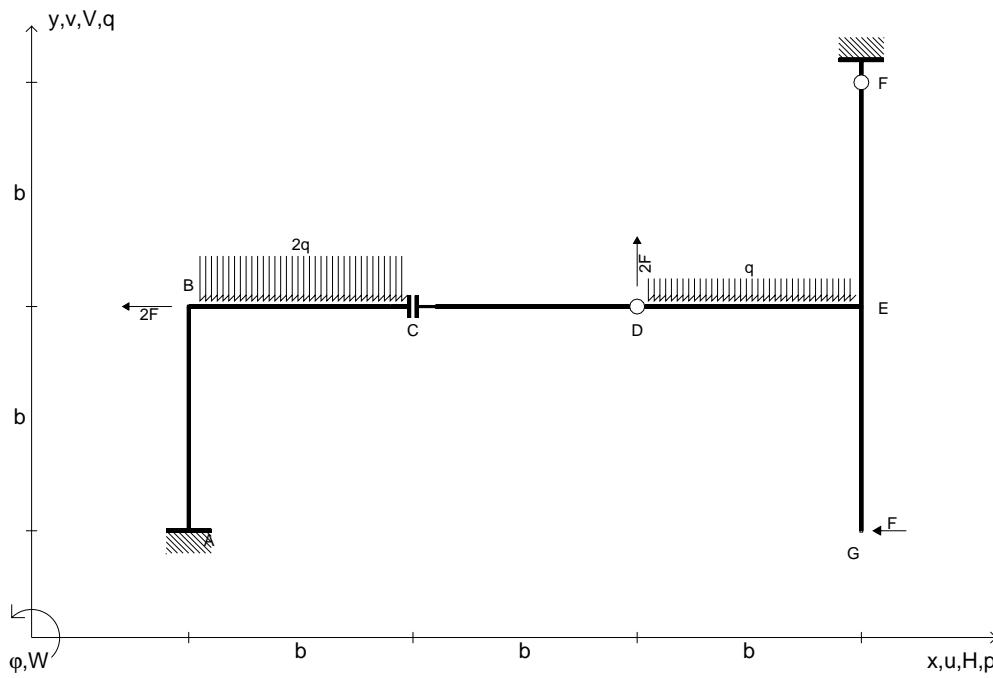


$$\longleftarrow 8 F b^3 / E J$$

$$\longleftrightarrow \boxed{+} \rightarrow F$$



$$\uparrow \boxed{+} \downarrow F$$



$$V_D = 2F$$

$$H_B = -2F$$

$$H_G = -F$$

$$q_{BC} = -2q = -2F/b$$

$$q_{DE} = -q = -F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{CD} = EJ$$

$$EJ_{DE} = EJ$$

$$EJ_{EF} = EJ$$

$$EJ_{EG} = EJ$$

$$EJ_{DF} = EJ$$

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

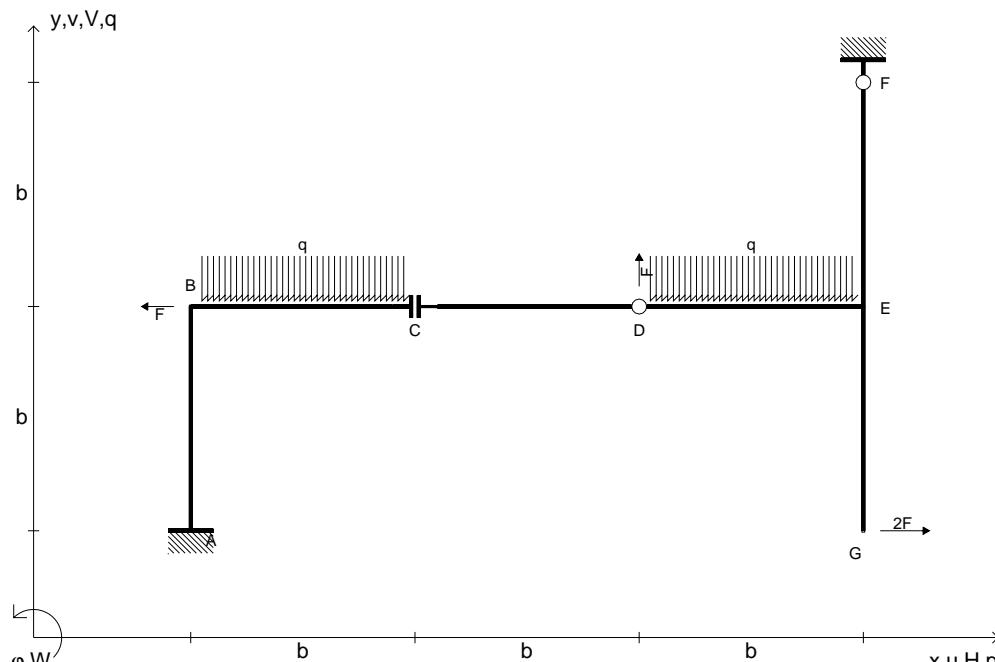
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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04.09.12

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$$\begin{aligned} V_D &= F \\ H_B &= -F \end{aligned}$$

$$\begin{aligned} H_G &= 2F \\ q_{BC} &= -q = -F/b \end{aligned}$$

$$\begin{aligned} q_{DE} &= -q = -F/b \\ EJ_{AB} &= EJ \end{aligned}$$

$$\begin{aligned} EJ_{BC} &= EJ \\ EJ_{CD} &= EJ \end{aligned}$$

$$EJ_{DE} = EJ$$

$$EJ_{EF} = EJ$$

$$EJ_{EG} = EJ$$

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

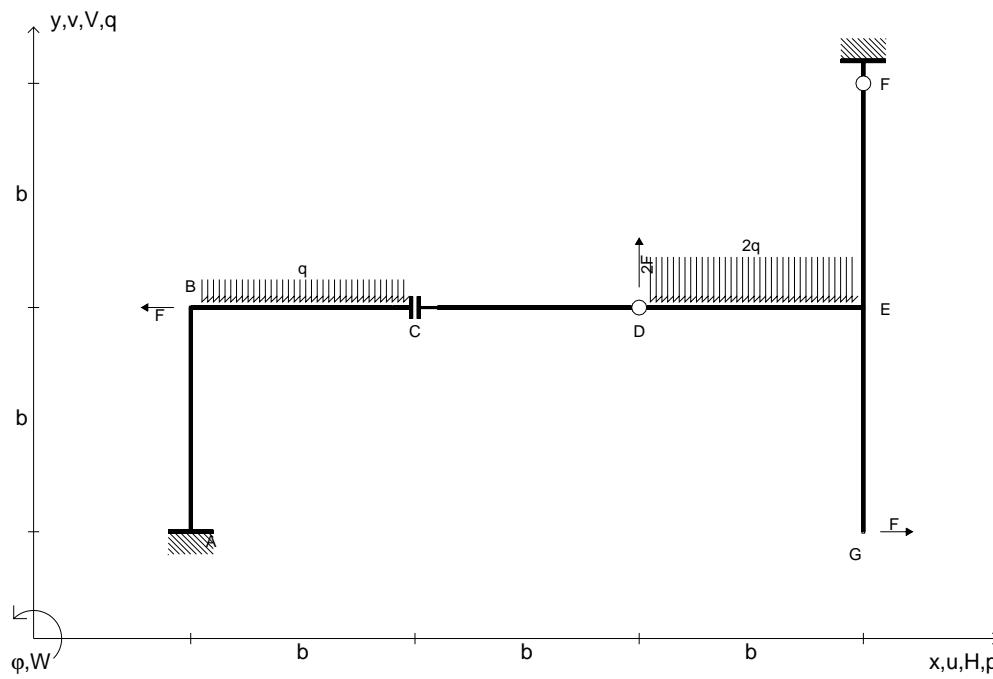
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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$$V_D = 2F$$

$$H_B = -F$$

$$H_G = F$$

$$q_{BC} = -q = -F/b$$

$$q_{DE} = -2q = -2F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{CD} = EJ$$

$$EJ_{DE} = EJ$$

$$EJ_{EF} = EJ$$

$$EJ_{EG} = EJ$$

$$EJ_{DG} = EJ$$

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

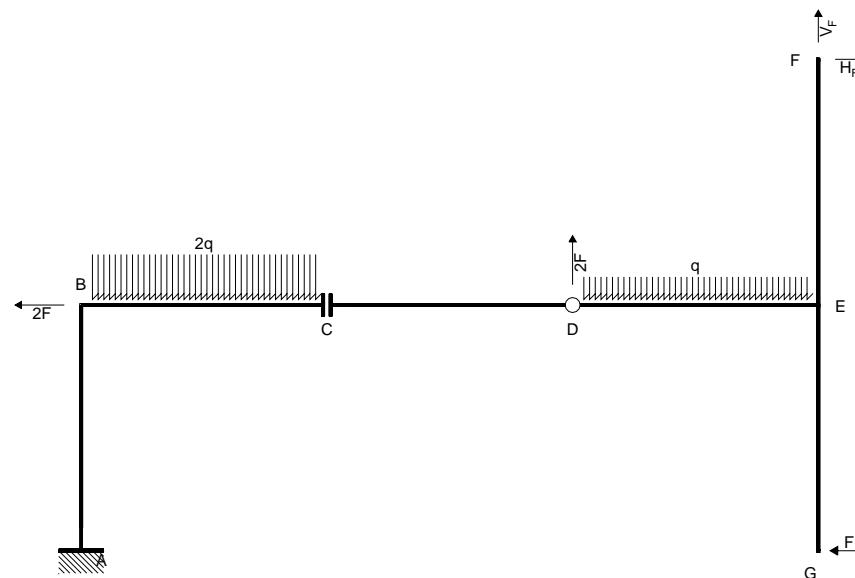
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG

$$V_F = -2F + qb$$

Rotazione intorno a D: aste DE EF EG

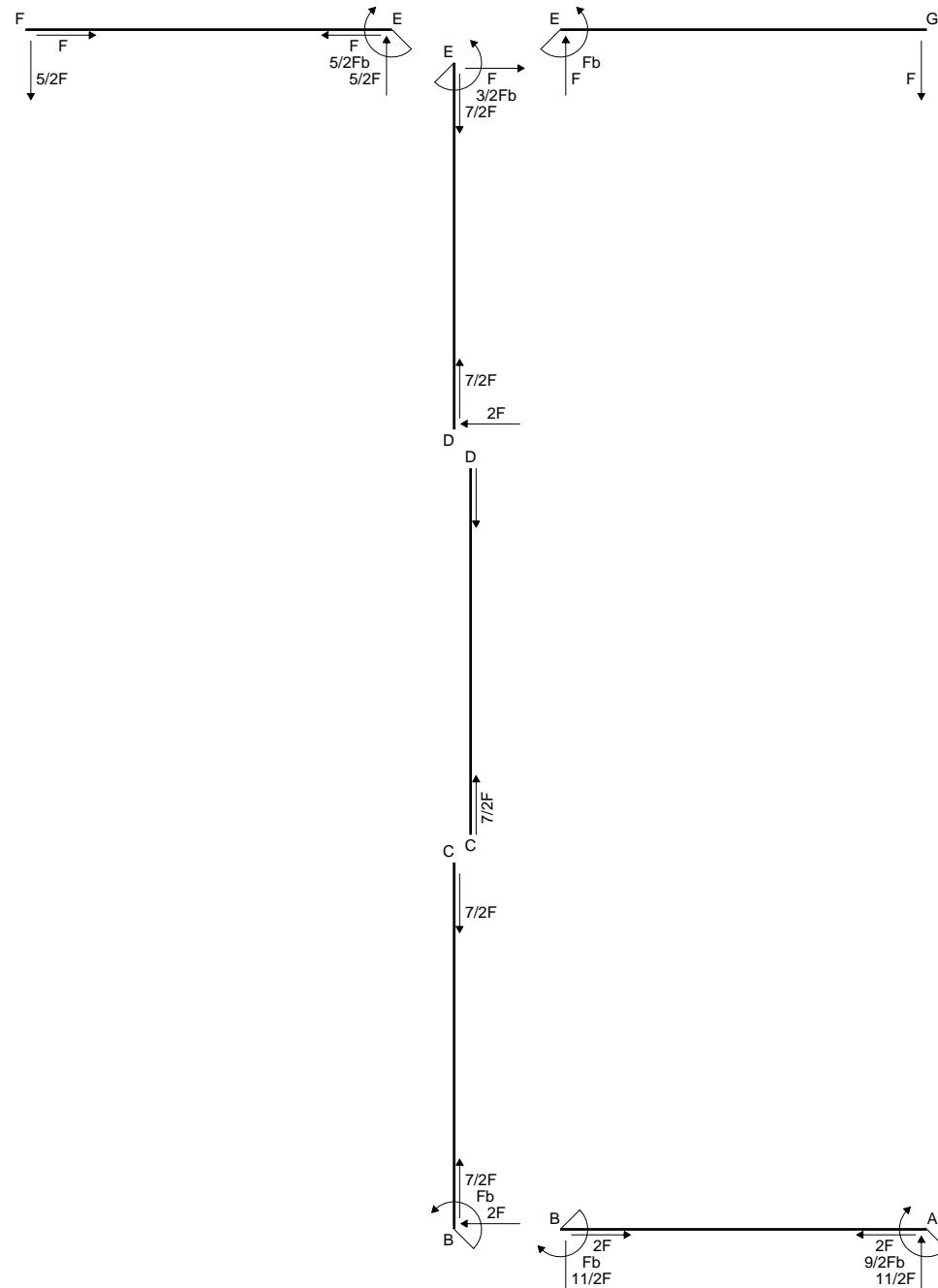
$$-H_F b + V_F b = Fb + 1/2qb^2$$

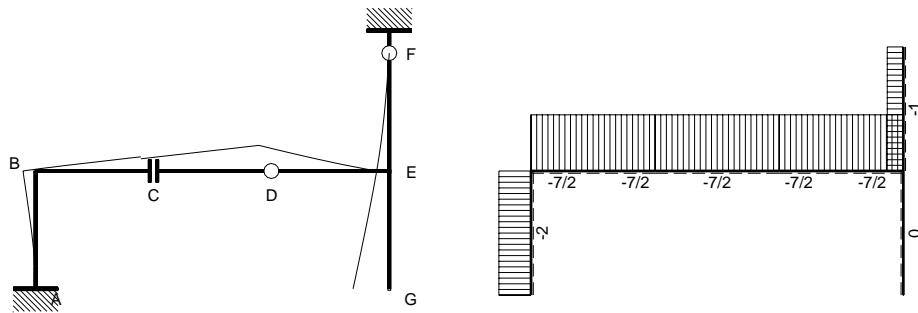
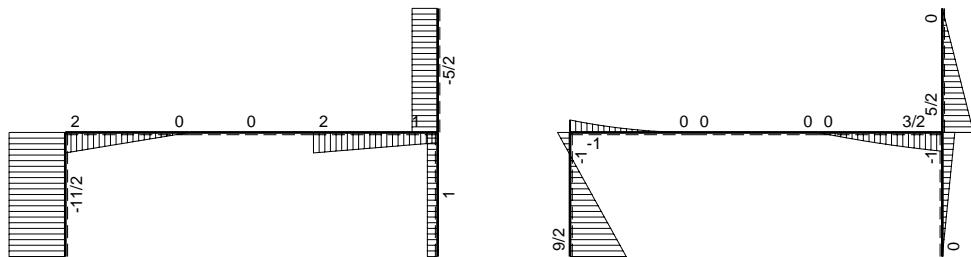
Matrice di equilibrio

$$\begin{bmatrix} H_F b & V_F b \\ V_{CB} & 0 \\ \Phi_{DC} & -1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -2 & 1 \\ 1 & 1/2 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_F b \\ H_F b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -2 & 1 \\ -3 & 1/2 \end{bmatrix}$$




 $\text{---} 8 F b^3 / E J$
 $\leftarrow \square \rightarrow F$

 $\uparrow \square \downarrow F$

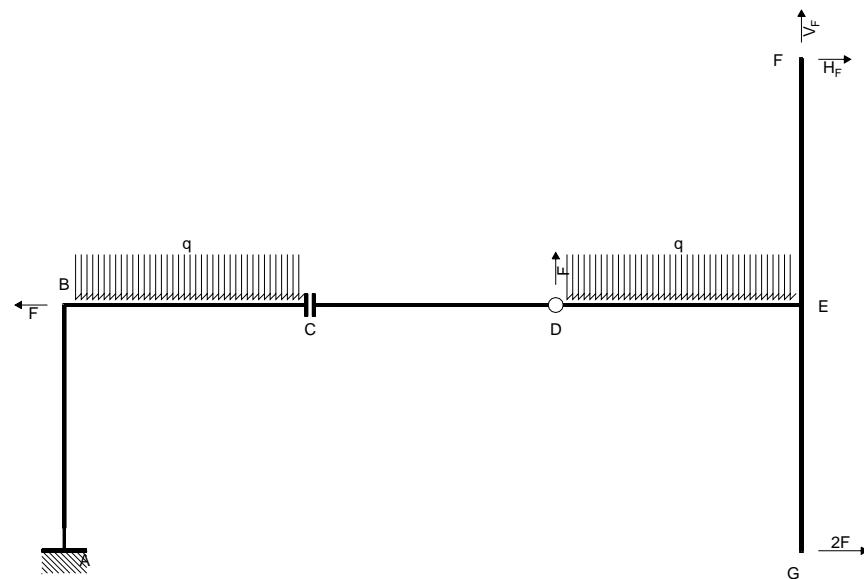
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 $\curvearrowleft \square \curvearrowright F_b$

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EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG

$$V_F = -F + qb$$

Rotazione intorno a D: aste DE EF EG

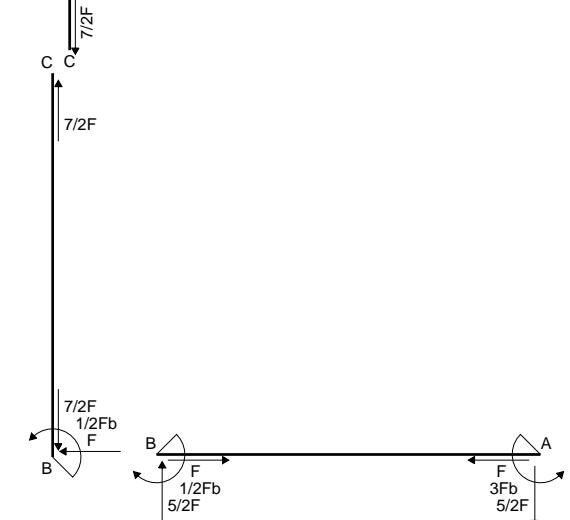
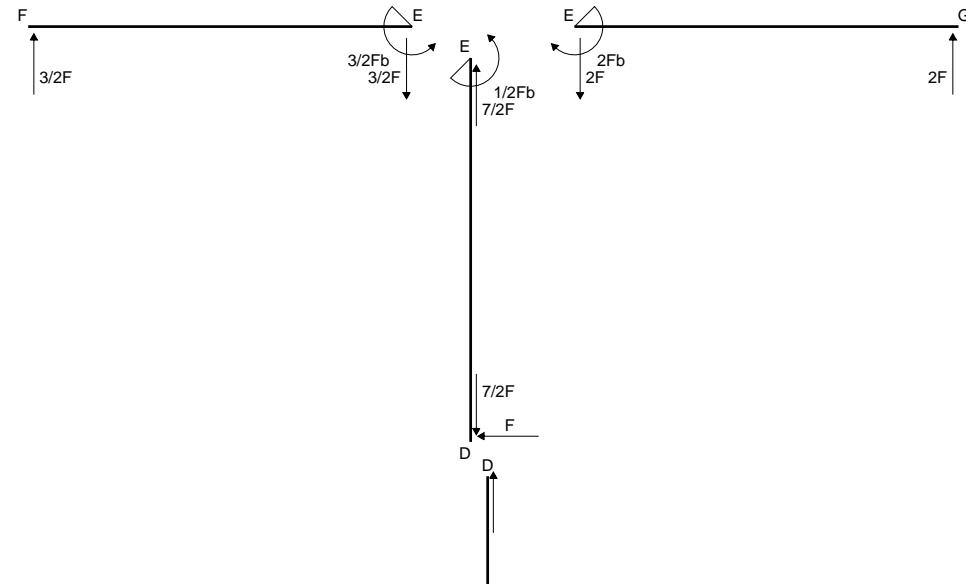
$$-H_F b + V_F b = -2Fb + 1/2qb^2$$

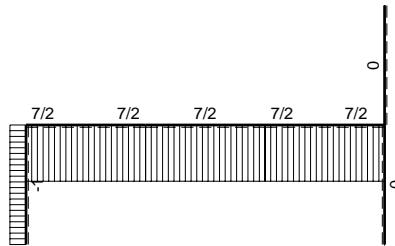
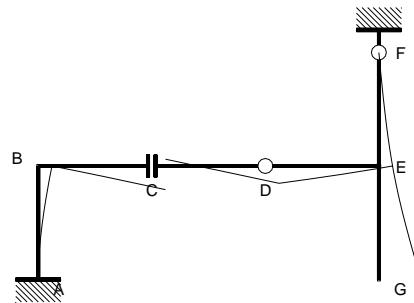
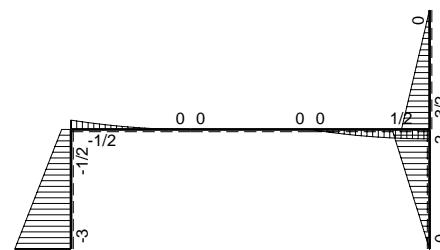
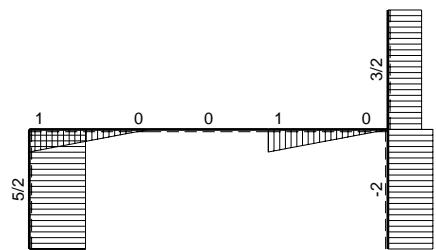
Matrice di equilibrio

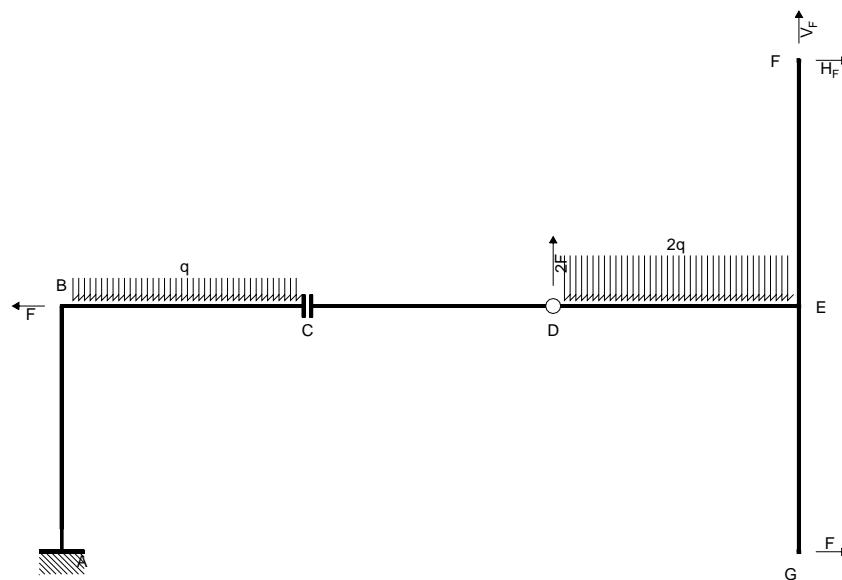
$$\begin{bmatrix} H_F b & V_F b \\ V_{CB} & 0 \\ \Phi_{DC} & -1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -1 & 1 \\ -2 & 1/2 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} V_F b \\ H_F b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -1 & 1 \\ 1 & 1/2 \end{bmatrix}$$




 $\text{---} \quad 6 F b^3 / E J$
 $\leftarrow [+] \rightarrow F$

 $\uparrow [+] \downarrow F$
 $\curvearrowleft [+] \curvearrowright F_b$



EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste CD DE EF EG

$$V_F = -2F + 2qb$$

Rotazione intorno a D: aste DE EF EG

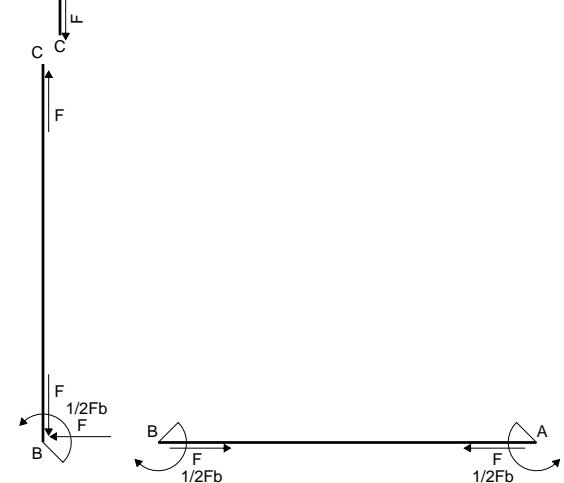
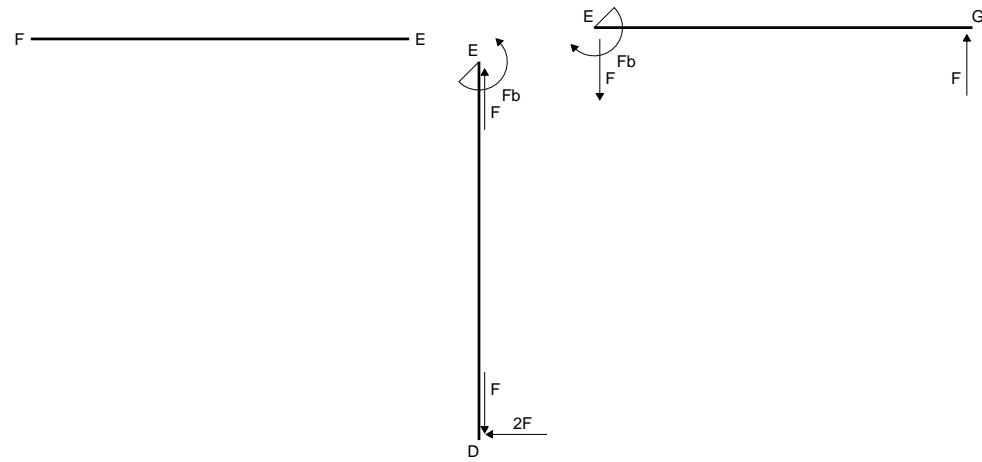
$$-H_F b + V_F b = -Fb + qb^2$$

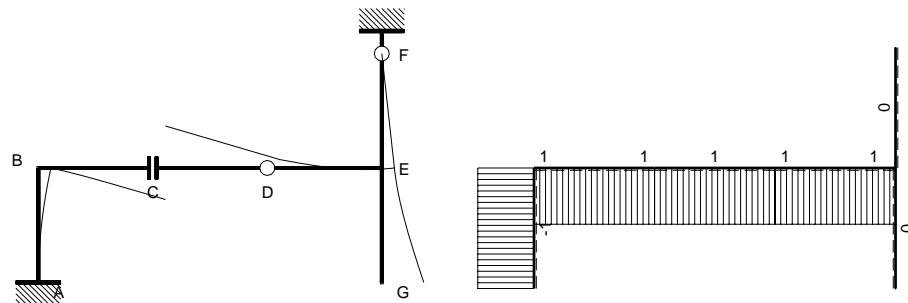
Matrice di equilibrio

$$\begin{bmatrix} H_F b & V_F b \\ V_{CB} & 0 \\ \Phi_{DC} & -1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -2 & 2 \\ -1 & 1 \end{bmatrix}$$

Soluzione del sistema

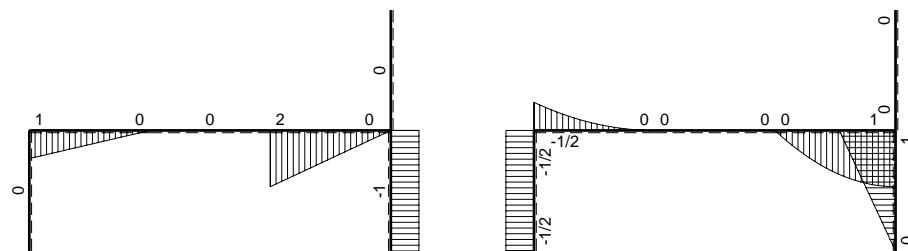
$$\begin{bmatrix} V_F b \\ H_F b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -2 & 2 \\ -1 & 1 \end{bmatrix}$$





$\vdash \dashv 1.5 F b^3 / E J$

$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$

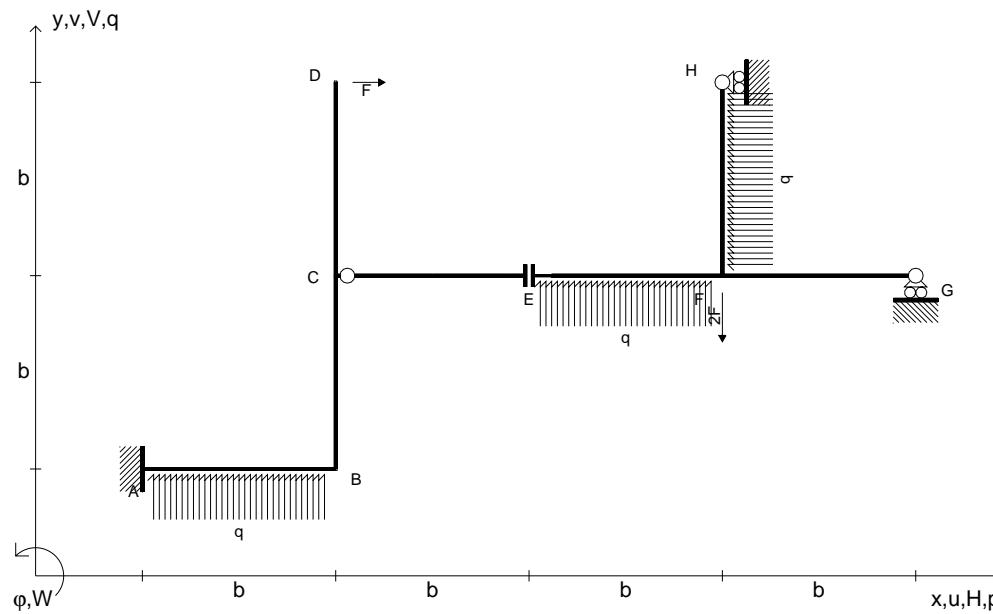
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$\curvearrowleft [+] \curvearrowright F_b$

04.09.12

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04.09.12



$$\begin{cases} V_F = -2F \\ H_D = F \end{cases}$$

$$\begin{cases} q_{AB} = q = F/b \\ p_{FH} = -q = -F/b \end{cases}$$

$$EJ_{AB} = EJ$$

$$\begin{cases} EJ_{BC} = EJ \\ EJ_{CD} = EJ \end{cases}$$

$$\begin{cases} EJ_{CE} = EJ \\ EJ_{EF} = EJ \\ EJ_{FG} = EJ \\ EJ_{FH} = EJ \end{cases}$$

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

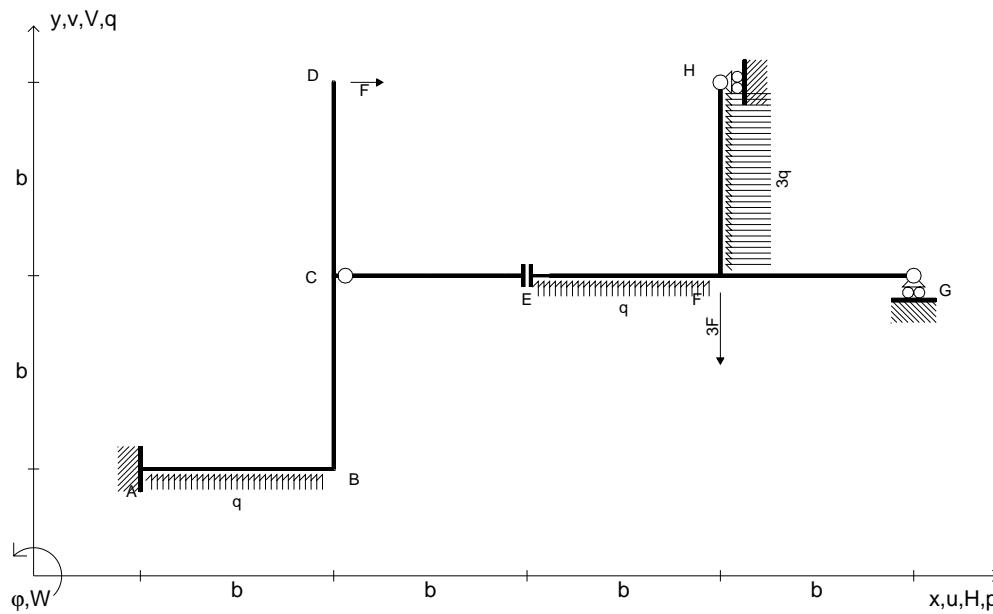
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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28.02.13

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28.02.13



$$\begin{aligned} V_F &= -3F \\ H_D &= F \\ q_{AB} &= q = F/b \end{aligned}$$

$$\begin{aligned} p_{FH} &= -3q = -3F/b \\ q_{EF} &= q = F/b \\ EJ_{AB} &= EJ \end{aligned}$$

$$\begin{aligned} EJ_{BC} &= EJ \\ EJ_{CD} &= EJ \\ EJ_{CE} &= EJ \end{aligned}$$

$$\begin{aligned} EJ_{EF} &= EJ \\ EJ_{FG} &= EJ \\ EJ_{FH} &= EJ \end{aligned}$$

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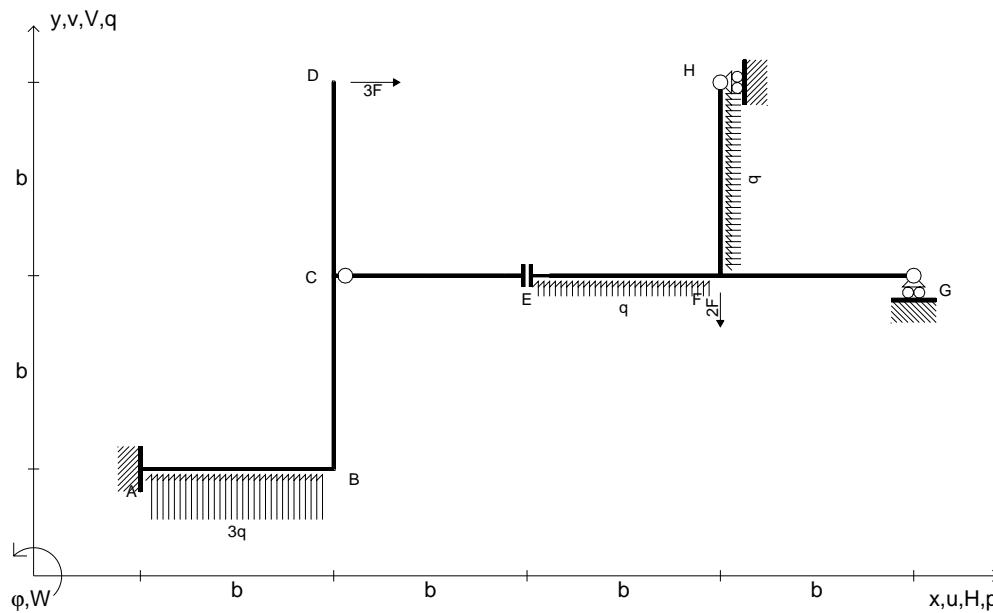
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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28.02.13



$$V_F = -2F$$

$$H_D = 3F$$

$$q_{AB} = 3q = 3F/b$$

$$p_{FH} = -q = -F/b$$

$$q_{EF} = q = F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{CD} = EJ$$

$$EJ_{CE} = EJ$$

$$EJ_{EF} = EJ$$

$$EJ_{FG} = EJ$$

$$EJ_{FH} = EJ$$

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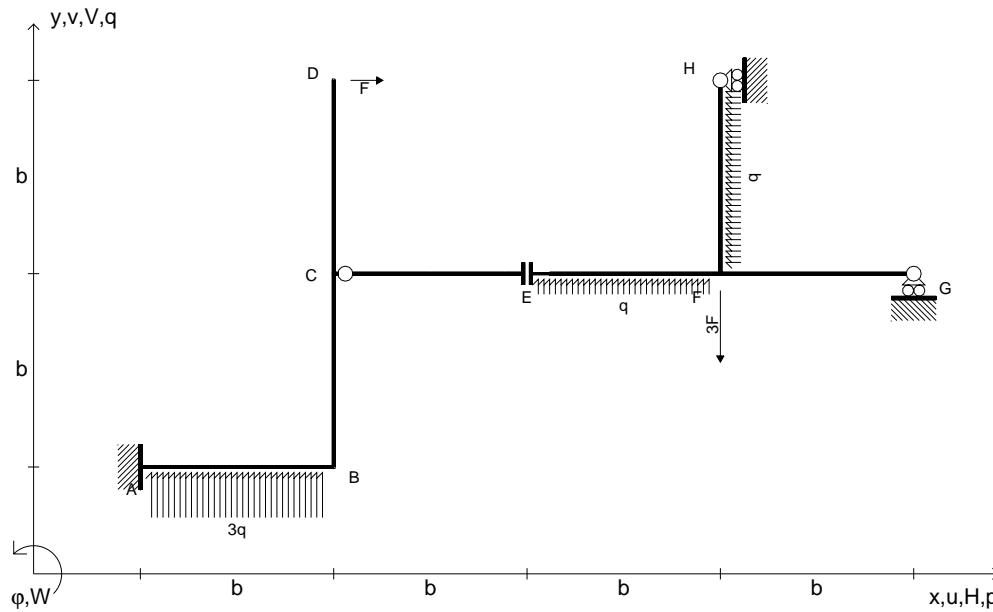
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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$$\begin{aligned}V_F &= -3F \\p_{FH} &= -q = -F/b \\H_D &= F \\q_{AB} &= 3q = 3F/b\end{aligned}$$

$$\begin{aligned}p_{FH} &= -q = F/b \\q_{EF} &= q = F/b \\EJ_{AB} &= EJ\end{aligned}$$

$$\begin{aligned}EJ_{BC} &= EJ \\EJ_{CD} &= EJ \\EJ_{CE} &= EJ \\EJ_{EF} &= EJ \\EJ_{FG} &= EJ \\EJ_{FH} &= EJ\end{aligned}$$

Carichi e deformazioni date hanno verso efficace in disegno.

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Tracciare i diagrammi quotati delle azioni interne nelle aste.

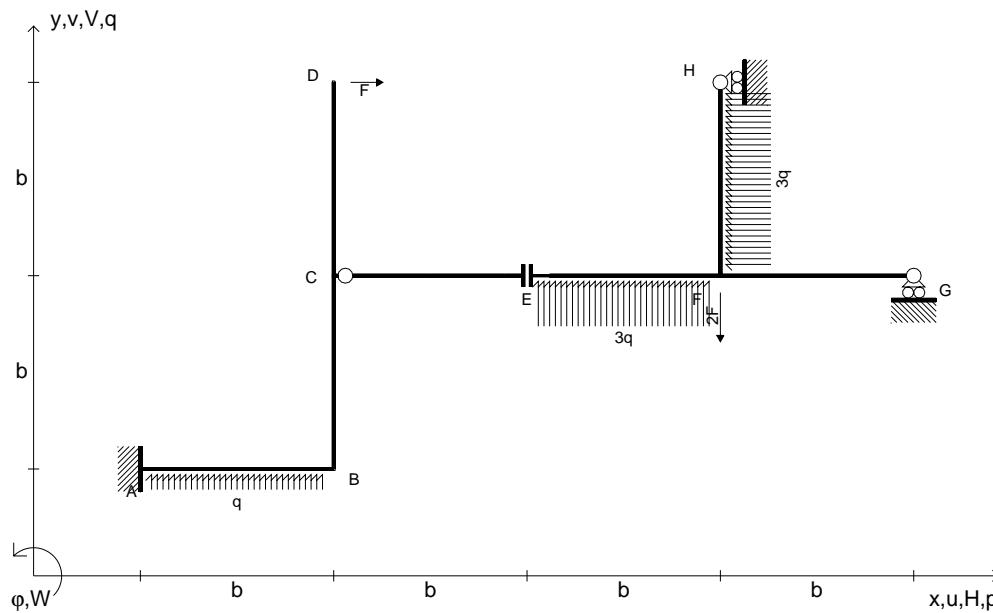
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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$$\begin{aligned}V_F &= -2F \\H_D &= F \\q_{AB} &= q = F/b\end{aligned}$$

$$\begin{aligned}p_{FH} &= -3q = -3F/b \\q_{EF} &= 3q = 3F/b \\EJ_{AB} &= EJ\end{aligned}$$

$$\begin{aligned}EJ_{BC} &= EJ \\EJ_{CD} &= EJ \\EJ_{CE} &= EJ\end{aligned}$$

$$\begin{aligned}EJ_{EF} &= EJ \\EJ_{FG} &= EJ \\EJ_{FH} &= EJ\end{aligned}$$

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Tracciare i diagrammi quotati delle azioni interne nelle aste.

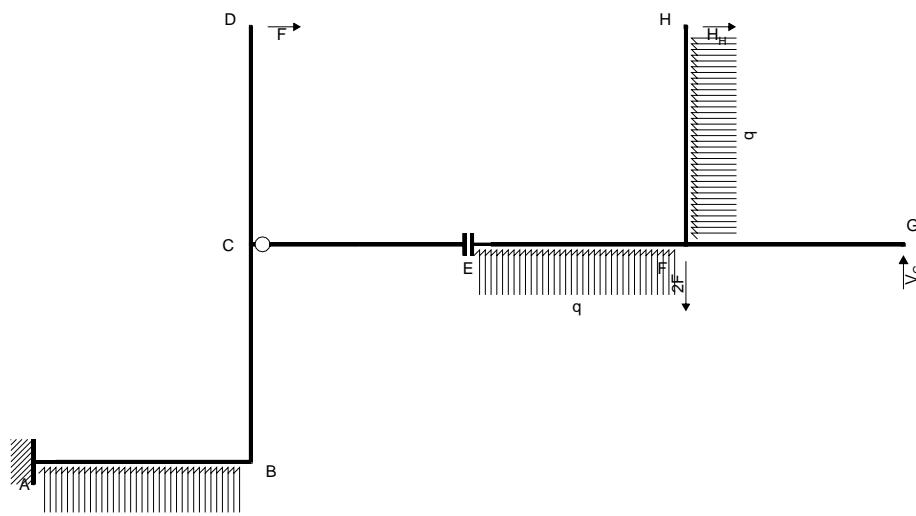
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: aste CE EF FG FH

$$3V_G b - H_H b = 4Fb - 2qb^2$$

Traslazione verticale: aste EF FG FH

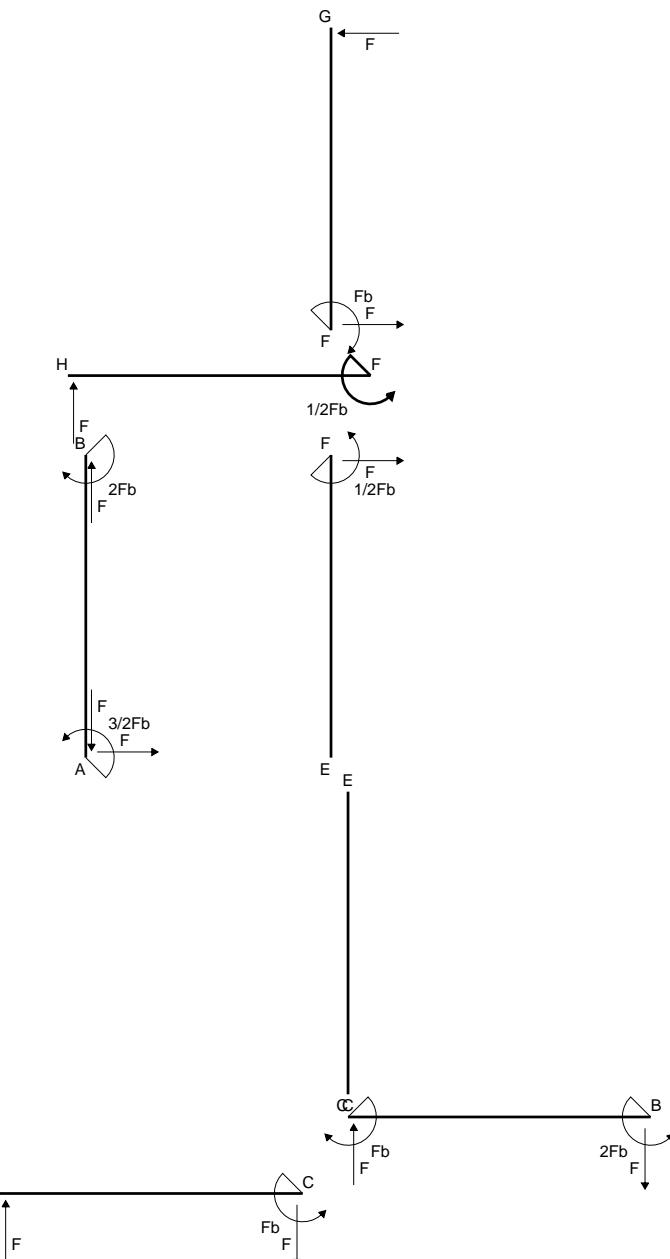
$$V_G = 2F - qb$$

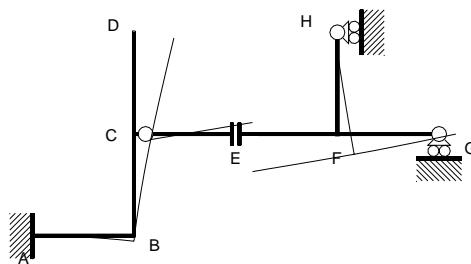
Matrice di equilibrio

$$\begin{bmatrix} V_G b & H_H b \\ \Phi_{CE} & 3 & -1 \\ V_{EC} & 1 & 0 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 4 & -2 \\ 2 & -1 \end{bmatrix}$$

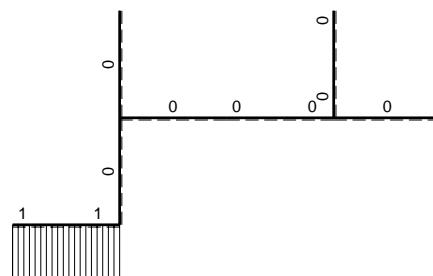
Soluzione del sistema

$$\begin{bmatrix} V_G b \\ H_H b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -1 \\ 2 & -1 \end{bmatrix}$$

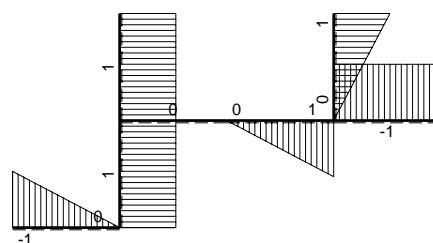




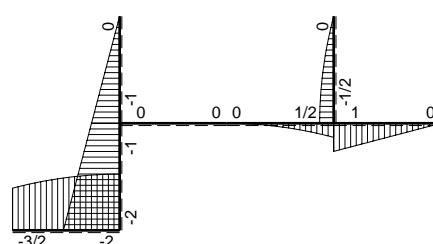
$\vdash \dashv 12 Fb^3/EJ$



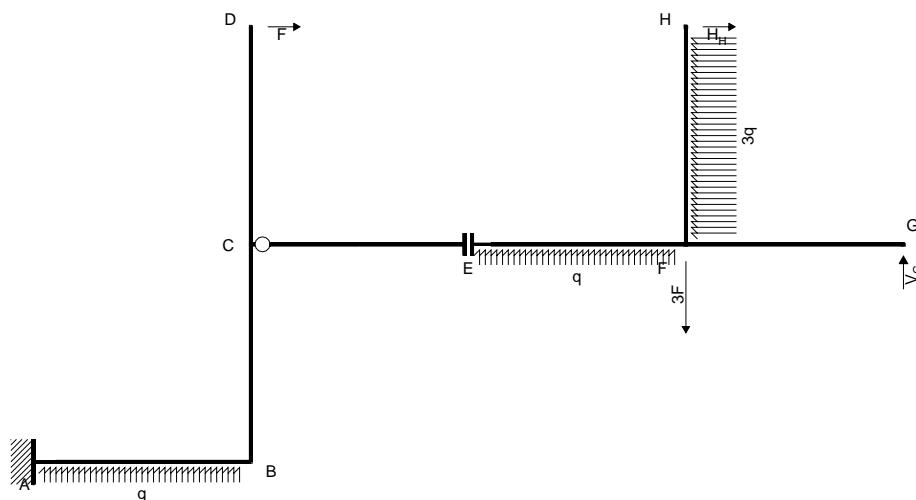
$\leftarrow \boxed{+} \rightarrow F$



$\uparrow \boxed{+} \downarrow F$



$\zeta \boxed{+} \zeta F_b$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: aste CE EF FG FH

$$3V_G b - H_H b = 6Fb - 3qb^2$$

Traslazione verticale: aste EF FG FH

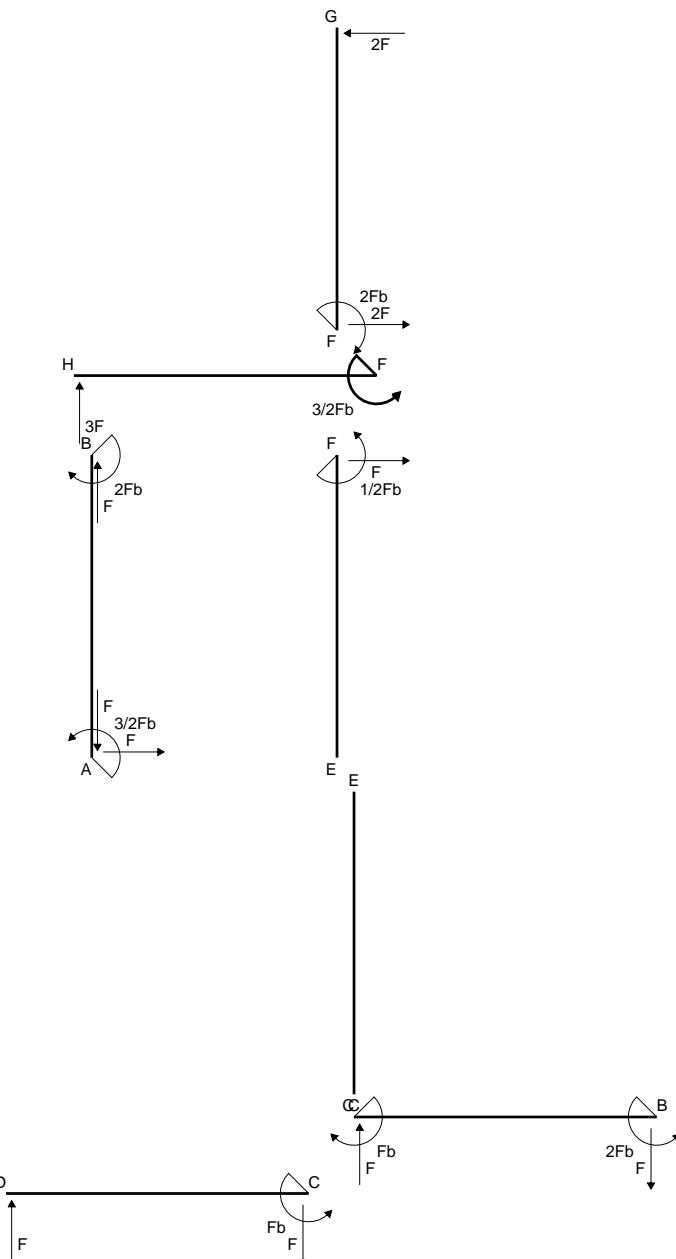
$$V_G = 3F - qb$$

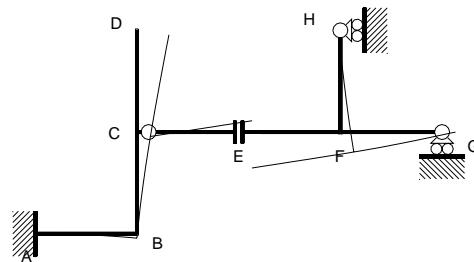
Matrice di equilibrio

$$\begin{bmatrix} V_G b & H_H b \\ \Phi_{CE} & 1 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 3 & -1 \\ 1 & 0 \end{bmatrix}$$

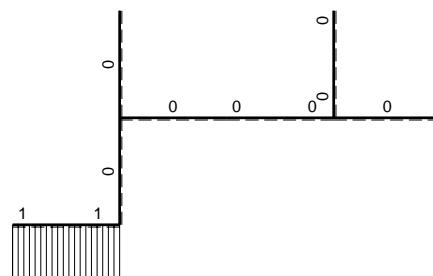
Soluzione del sistema

$$\begin{bmatrix} V_G b \\ H_H b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 3 & -1 \\ 3 & 0 \end{bmatrix}$$

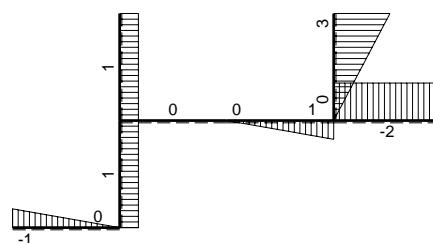




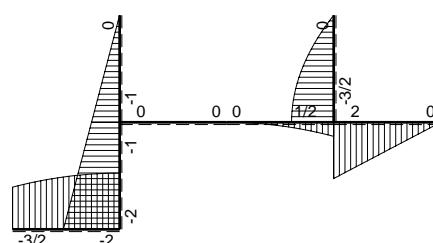
$\vdash \dashv 15 Fb^3/EJ$



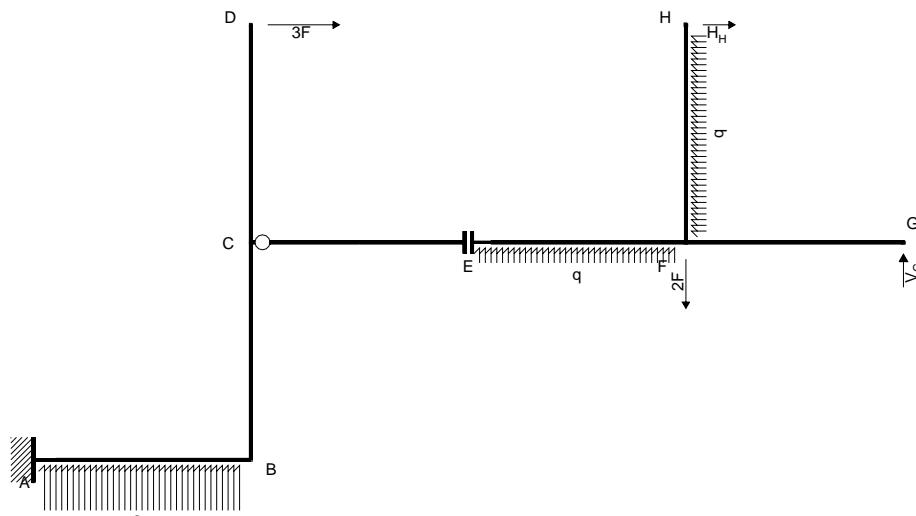
$\leftarrow \boxed{+} \rightarrow F$



$\uparrow \boxed{+} \downarrow F$



$\zeta \boxed{+} \zeta F_b$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: aste CE EF FG FH

$$3V_G b - H_H b = 4Fb - 2qb^2$$

Traslazione verticale: aste EF FG FH

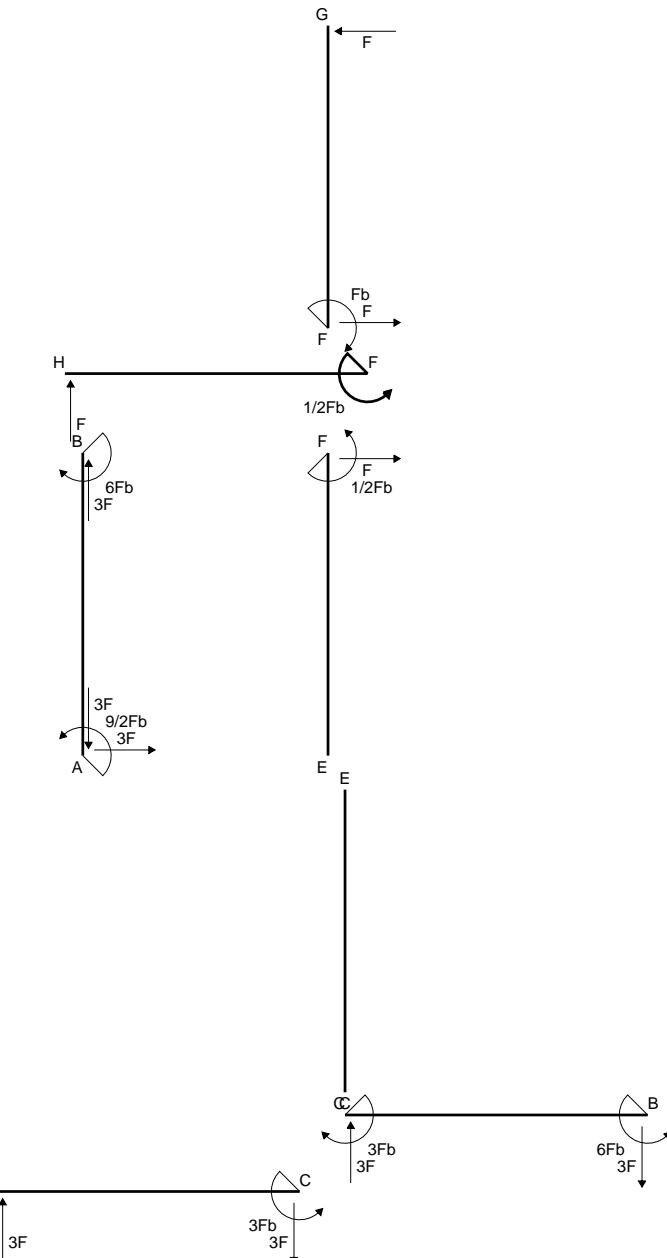
$$V_G = 2F - qb$$

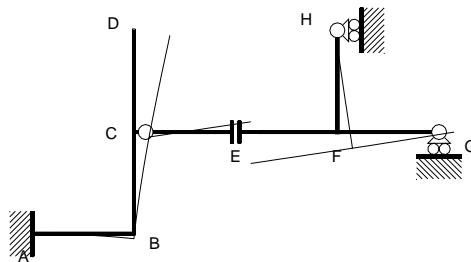
Matrice di equilibrio

$$\begin{bmatrix} V_G b & H_H b \\ \Phi_{CE} & 3 & -1 \\ V_{EC} & 1 & 0 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 4 & -2 \\ 2 & -1 \end{bmatrix}$$

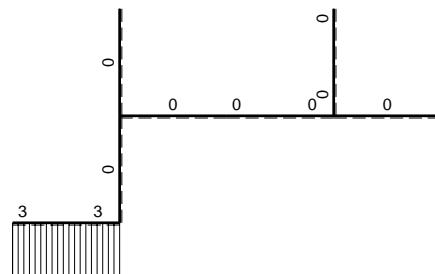
Soluzione del sistema

$$\begin{bmatrix} V_G b \\ H_H b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -1 \\ 2 & -1 \end{bmatrix}$$

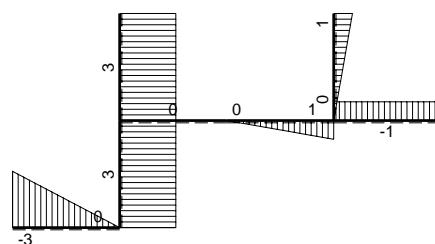




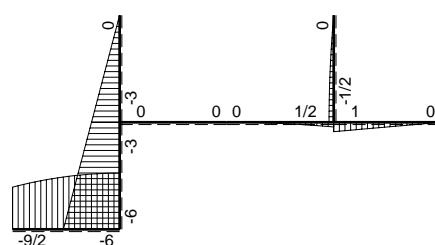
$\rightarrow 40 Fb^3/EJ$



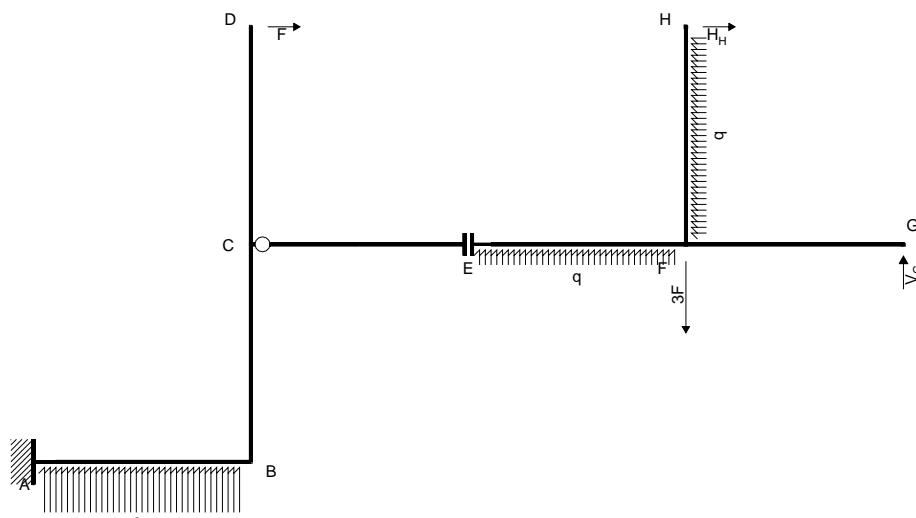
$\leftarrow \boxed{+} \rightarrow F$



$\uparrow \boxed{+} \downarrow F$



$\zeta \boxed{+} \zeta F_b$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: aste CE EF FG FH

$$3V_G b - H_H b = 6Fb - 2qb^2$$

Traslazione verticale: aste EF FG FH

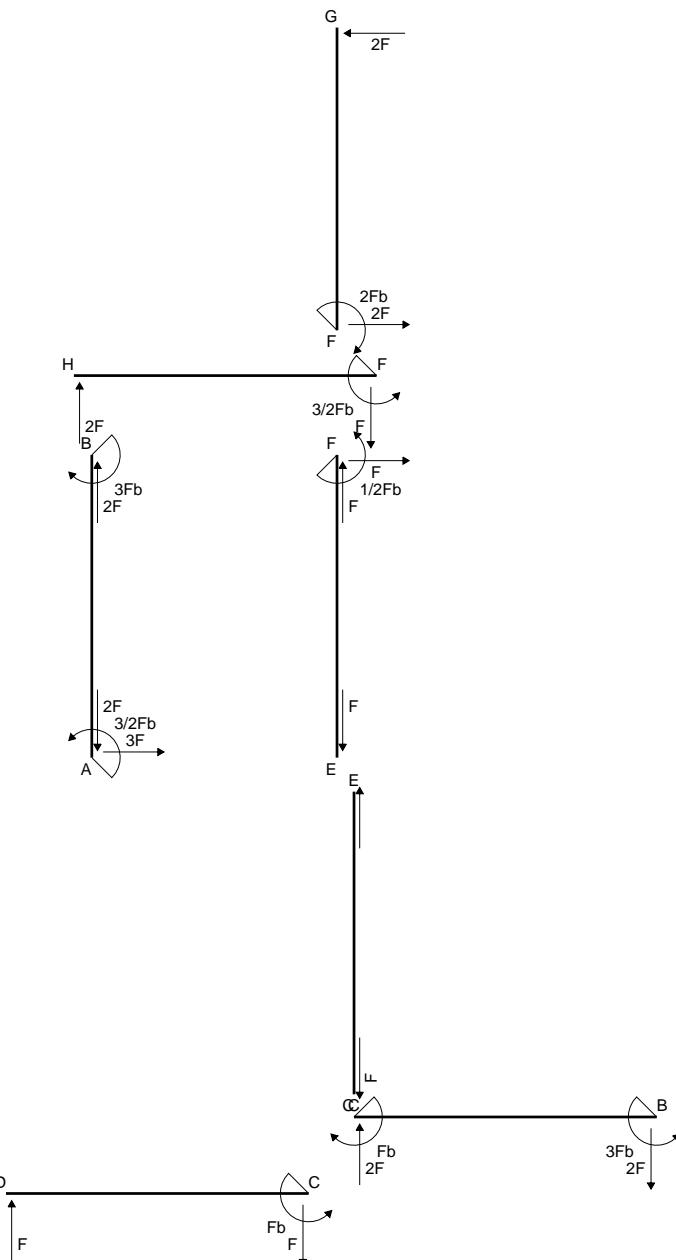
$$V_G = 3F - qb$$

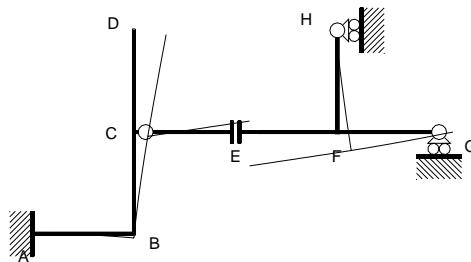
Matrice di equilibrio

$$\begin{bmatrix} V_G b & H_H b \\ \Phi_{CE} & 3 & -1 \\ V_{EC} & 1 & 0 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 6 & -2 \\ 3 & -1 \end{bmatrix}$$

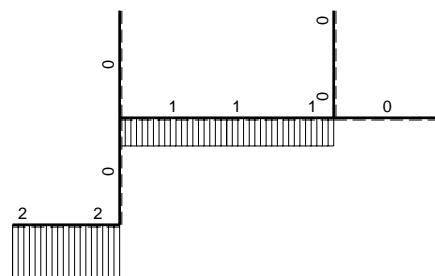
Soluzione del sistema

$$\begin{bmatrix} V_G b \\ H_H b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 3 & -1 \\ 3 & -1 \end{bmatrix}$$

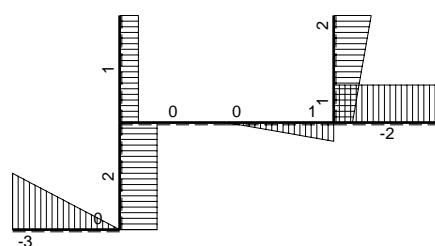




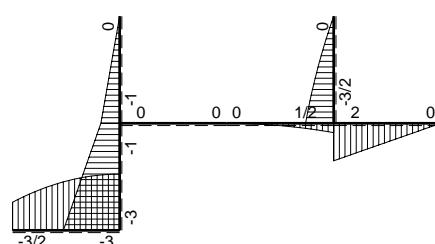
$\rightarrow 20 F_b^3/EJ$



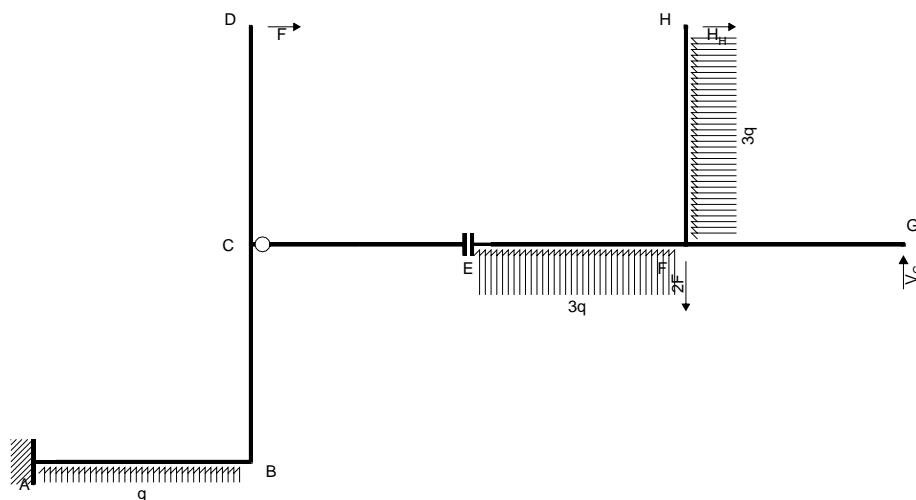
$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$



$\zeta [+] \zeta F_b$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: aste CE EF FG FH

$$3V_G b - H_H b = 4Fb - 6qb^2$$

Traslazione verticale: aste EF FG FH

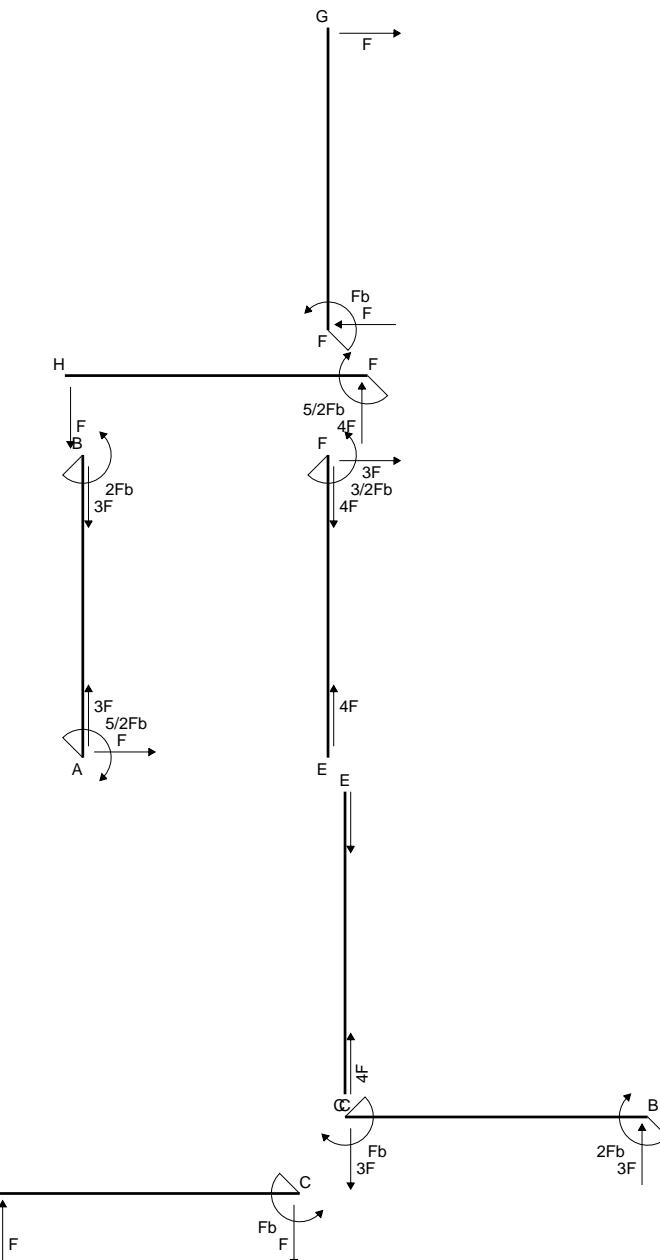
$$V_G = 2F - 3qb$$

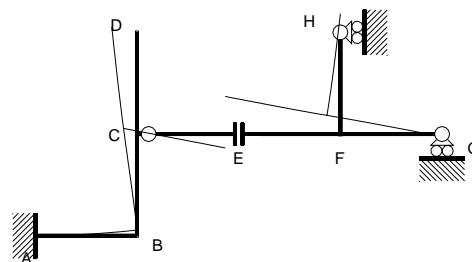
Matrice di equilibrio

$$\begin{bmatrix} V_G b & H_H b \\ \Phi_{CE} & 3 & -1 \\ \Phi_{EC} & 1 & 0 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 4 & -6 \\ 2 & -3 \end{bmatrix}$$

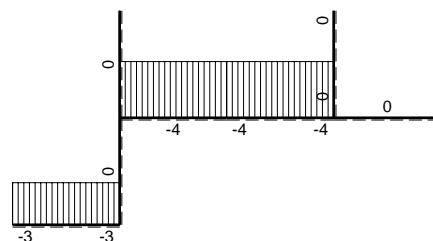
Soluzione del sistema

$$\begin{bmatrix} V_G b \\ H_H b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -3 \end{bmatrix}$$

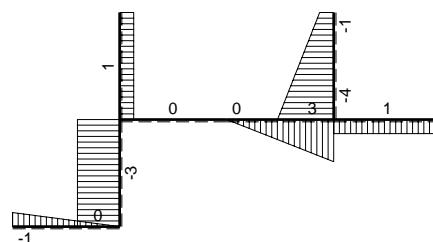




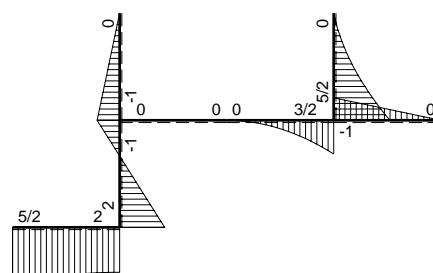
$\vdash 15 Fb^3/EJ$



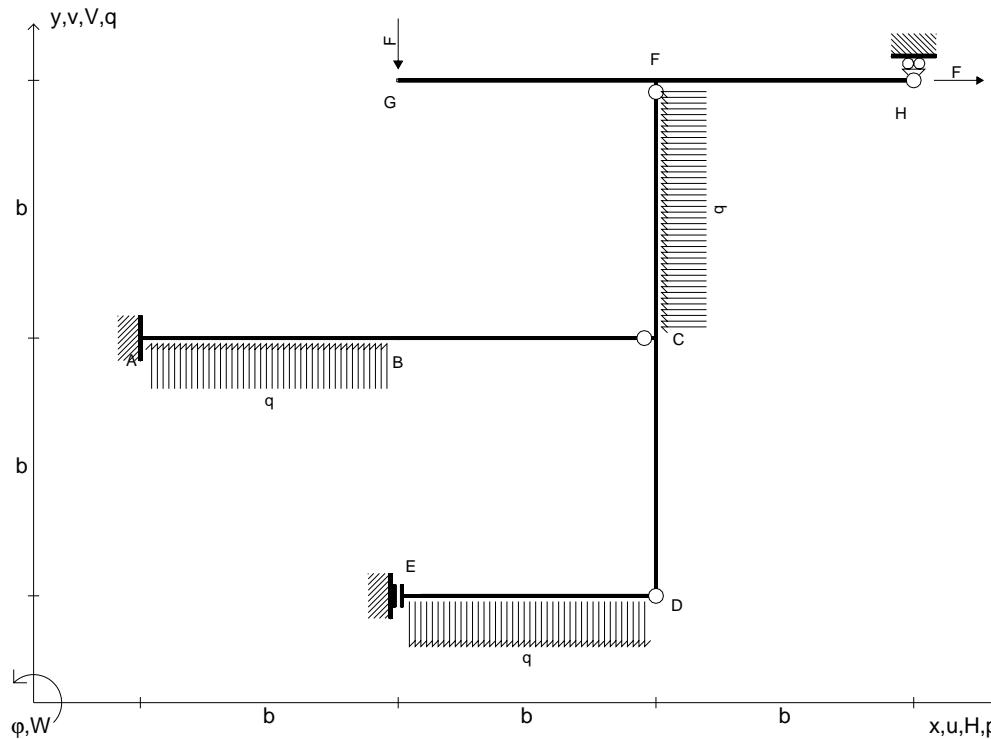
$\leftarrow \boxed{+} \rightarrow F$



$\uparrow \boxed{+} \downarrow F$



$\zeta \boxed{+} \zeta F_b$



$$V_G = -F$$

$$H_H = F$$

$$q_{AB} = q = F/b$$

$$p_{CF} = -q = -F/b$$

$$q_{DE} = -q = -F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{CD} = EJ$$

$$EJ_{DE} = EJ$$

$$EJ_{CF} = EJ$$

$$EJ_{FG} = EJ$$

$$EJ_{FH} = EJ$$

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

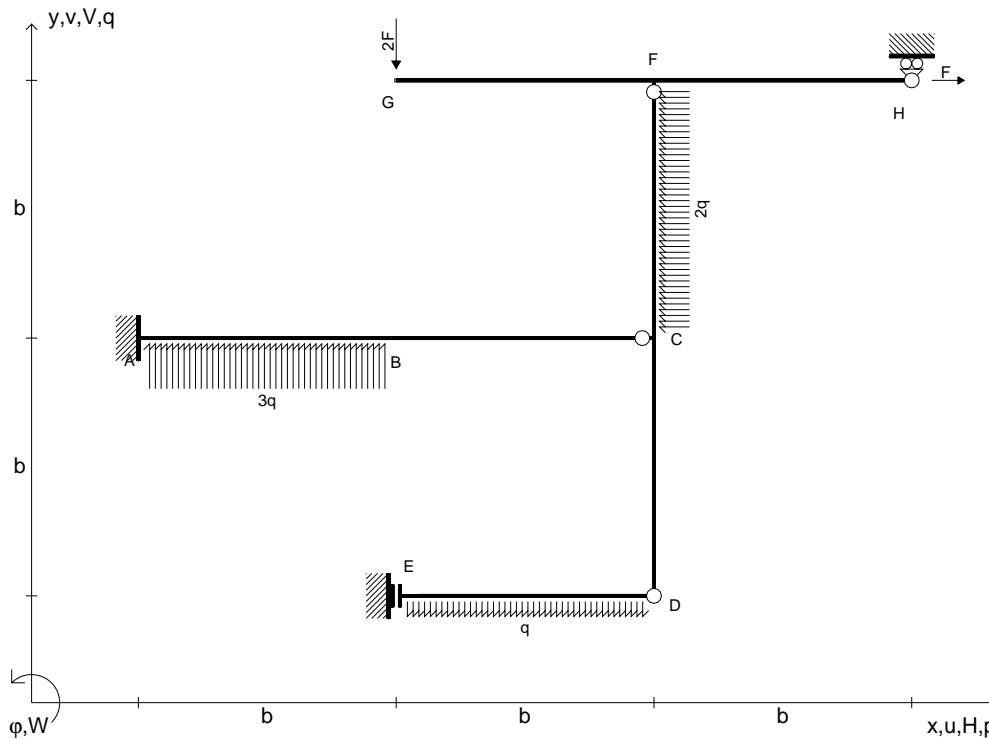
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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08.02.13

@ Adolfo Zavelani Rossi, Politecnico di Milano, vers.28.01.13

08.02.13



$$V_G = -2F$$

$$H_H = F$$

$$q_{AB} = 3q = 3F/b$$

$$p_{CF} = -2q = -2F/b$$

$$q_{DE} = -q = -F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{CD} = EJ$$

$$EJ_{DE} = EJ$$

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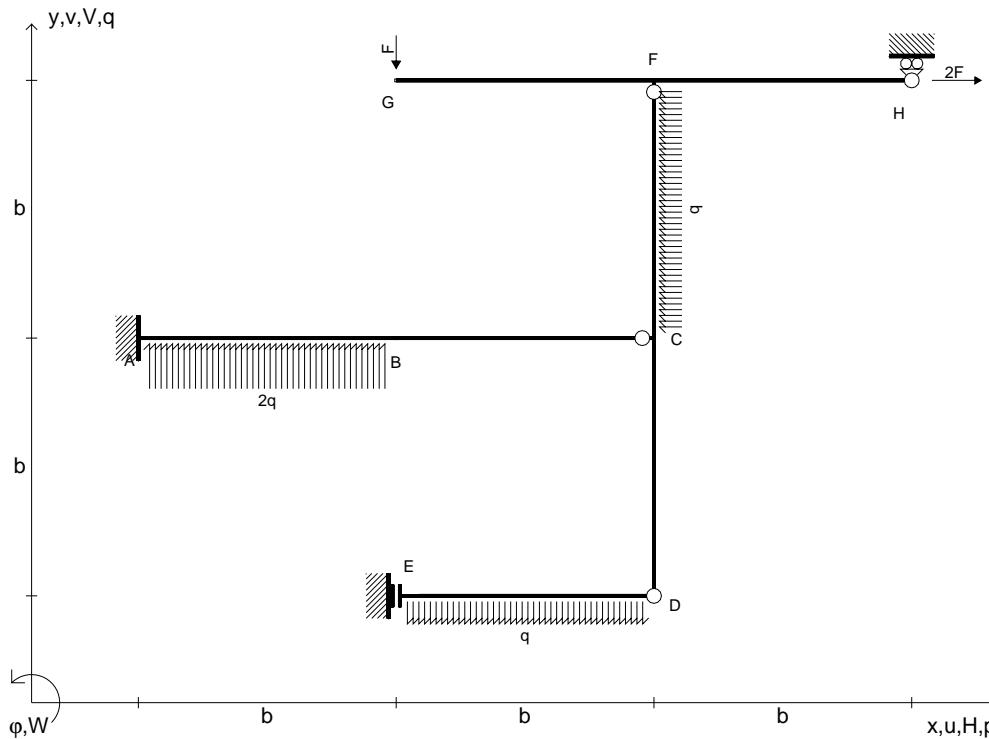
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y .

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08.02.13

@ Adolfo Zavelani Rossi, Politecnico di Milano, vers.28.01.13

08.02.13



$$V_G = -F$$

$$H_H = 2F$$

$$q_{AB} = 2q = 2F/b$$

$$p_{CF} = -q = -F/b$$

$$q_{DE} = -q = -F/b$$

$$q_{AB} = 2q = 2F/b$$

$$EJ_{BC} = EJ$$

$$EJ_{CD} = EJ$$

$$EJ_{AB} = EJ$$

$$EJ_{CF} = EJ$$

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Tracciare i diagrammi quotati delle azioni interne nelle aste.

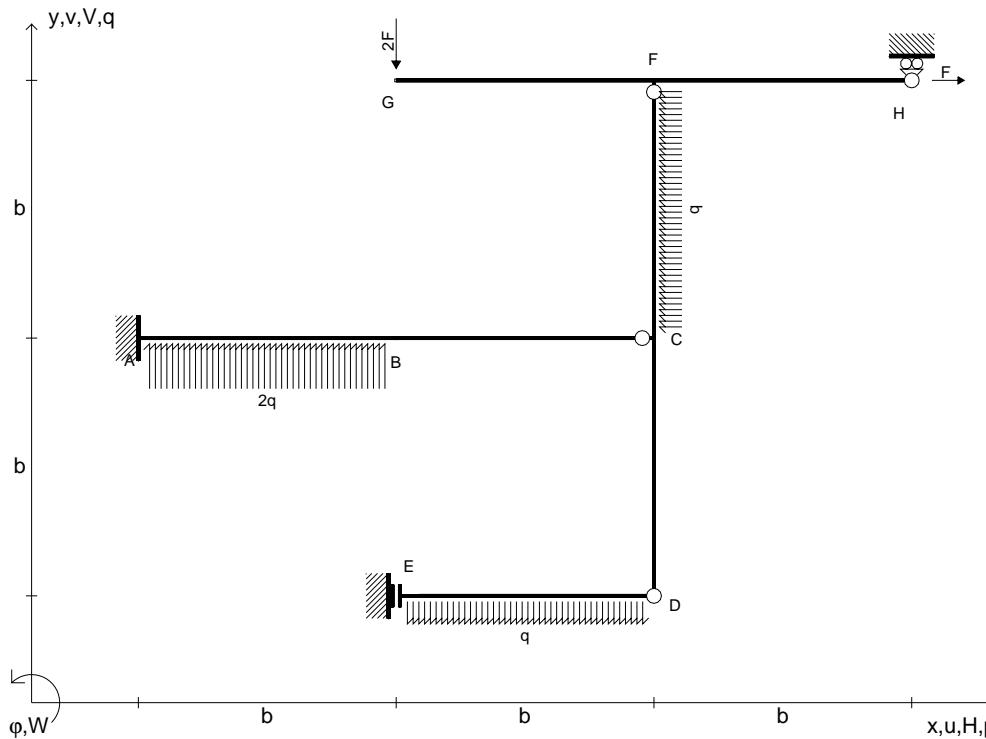
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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$$V_G = -2F$$

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$$q_{AB} = 2q = 2F/b$$

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Tracciare i diagrammi quotati delle azioni interne nelle aste.

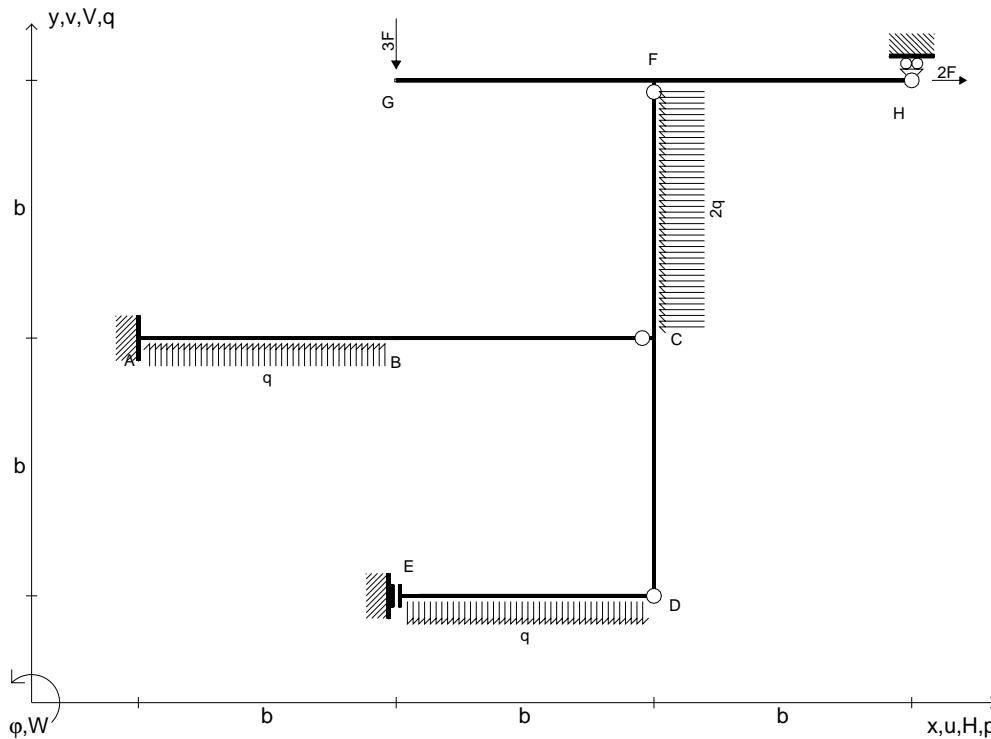
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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08.02.13



$$V_G = -3F$$

$$H_H = 2F$$

$$q_{AB} = q = F/b$$

$$p_{CF} = -2q = -2F/b$$

$$q_{DE} = -q = -F/b$$

$$EJ_{AB} = EJ$$

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Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

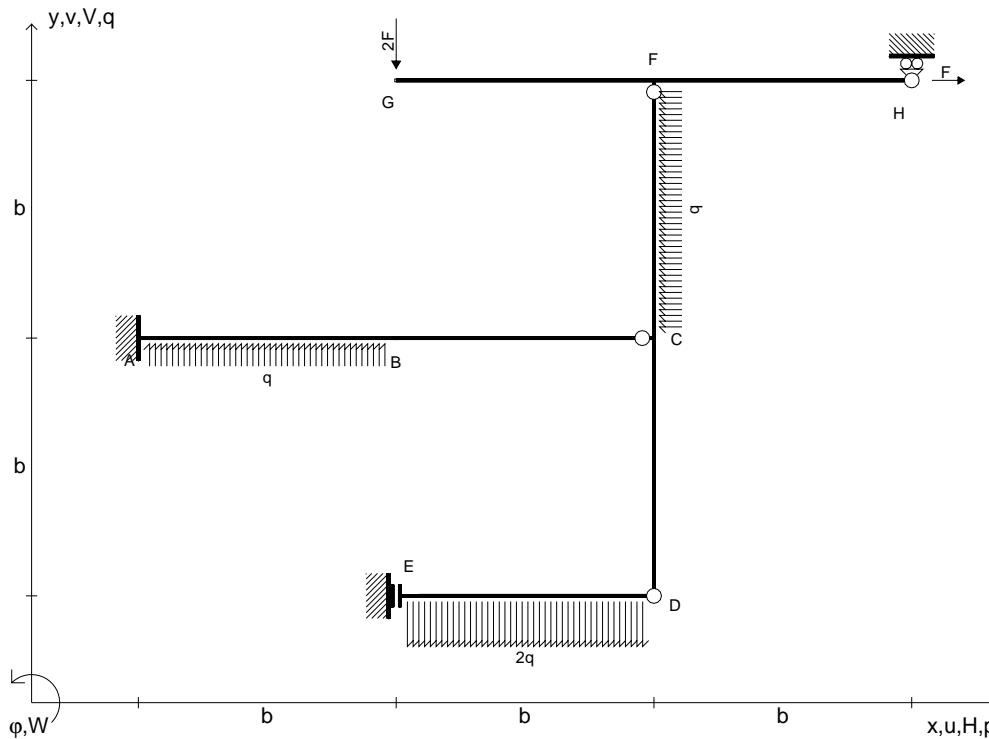
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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$$V_G = -2F$$

$$H_H = F$$

$$q_{AB} = q = F/b$$

$$p_{CF} = -q = -F/b$$

$$q_{DE} = -2q = -2F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{CD} = EJ$$

$$EJ_{DE} = EJ$$

$$EJ_{CF} = EJ$$

$$EJ_{FG} = EJ$$

$$EJ_{FH} = EJ$$

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

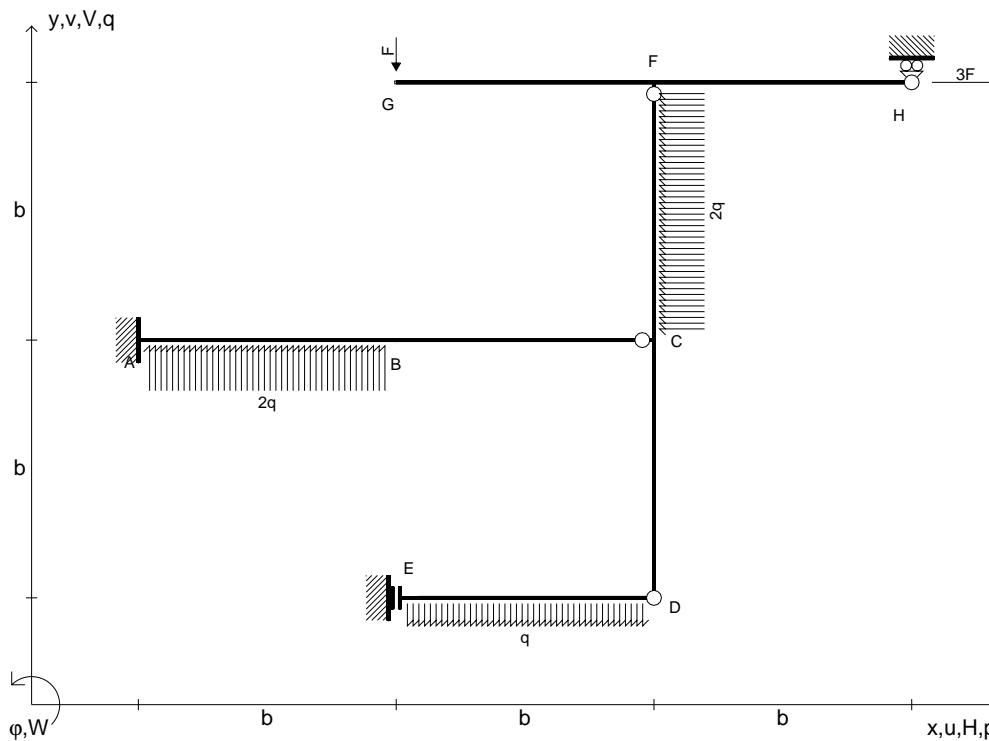
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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$$V_G = -F$$

$$H_H = 3F$$

$$q_{AB} = 2q = 2F/b$$

$$p_{CF} = -2q = -2F/b$$

$$q_{DE} = -q = -F/b$$

$$EJ_{AB} = EJ$$

$$EJ_{BC} = EJ$$

$$EJ_{CD} = EJ$$

$$EJ_{DE} = EJ$$

$$EJ_{CF} = EJ$$

$$EJ_{FG} = EJ$$

$$EJ_{FH} = EJ$$

Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

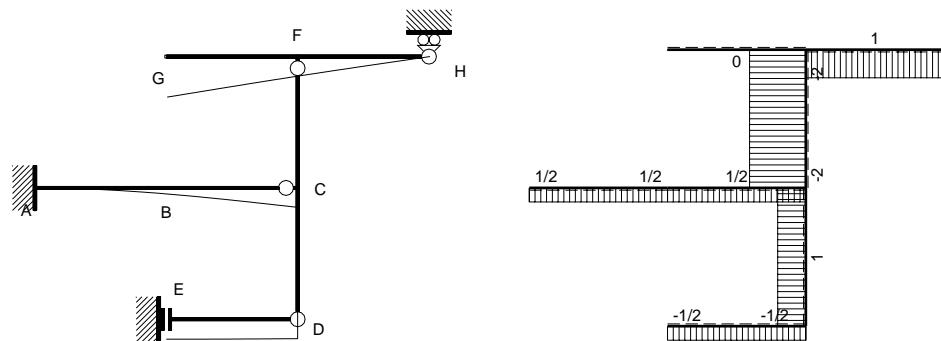
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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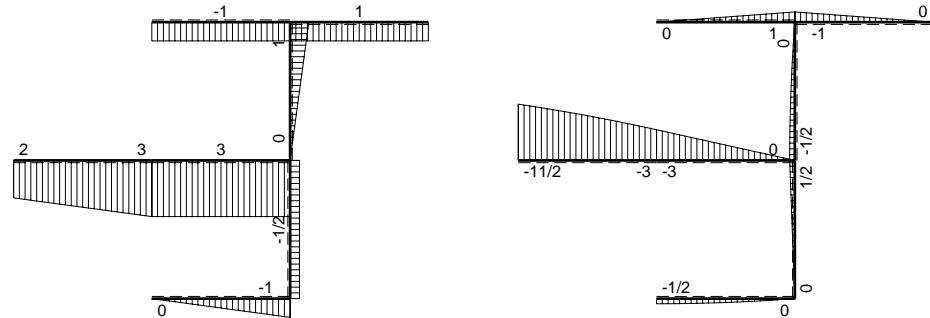
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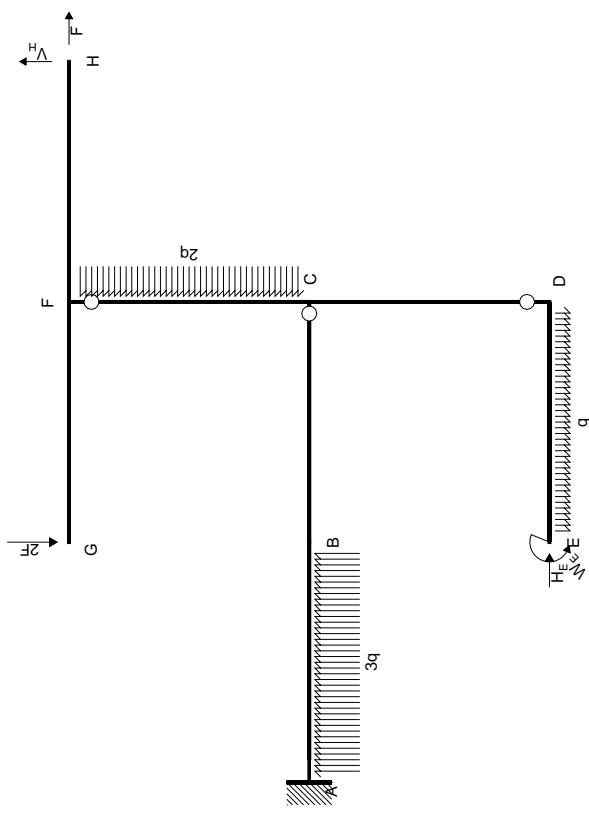
$\vdash \dashv 30 Fb^3/EJ$

$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$

$\curvearrowleft [+] \curvearrowright Fb$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: asta CD CF DE FG FH

$$H_E b + W_E + V_H b = -Fb - 3/2qb^2$$

Rotazione intorno a D: asta DE

$$W_E = -1/2qb^2$$

Rotazione intorno a F: asta FG FH

$$V_H b = -2Fb$$

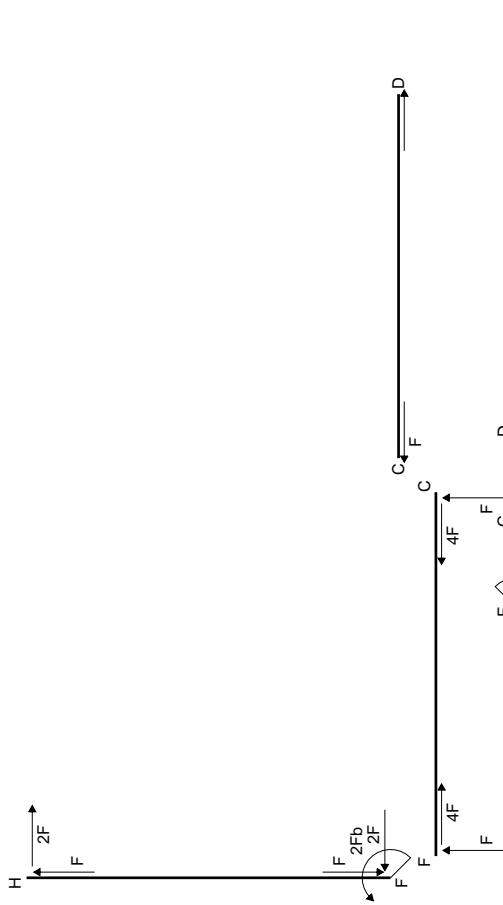
Matrice di equilibrio

$$\begin{bmatrix} H_E b & W_E & V_H b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 1 & -1 \\ 0 & -3/2 \end{bmatrix}$$

$$\begin{bmatrix} \Phi_{CB} \\ \Phi_{DC} \\ \Phi_{FC} \end{bmatrix} = \begin{bmatrix} 0 & -1/2 \\ 0 & 1 \\ -2 & 0 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_E b \\ W_E \\ V_H b \end{bmatrix} = \begin{bmatrix} Fb \\ 1 \\ 0 \end{bmatrix}$$

EQUAZIONI DI EQUILIBRIO
Rotazione intorno a C: asta CD CF DE FG FH

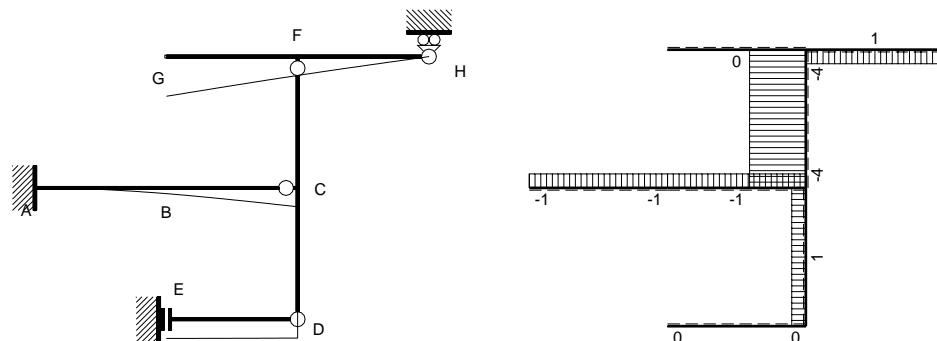
$$H_E b + W_E + V_H b = -Fb - 3/2qb^2$$

Rotazione intorno a D: asta DE

$$W_E = -1/2qb^2$$

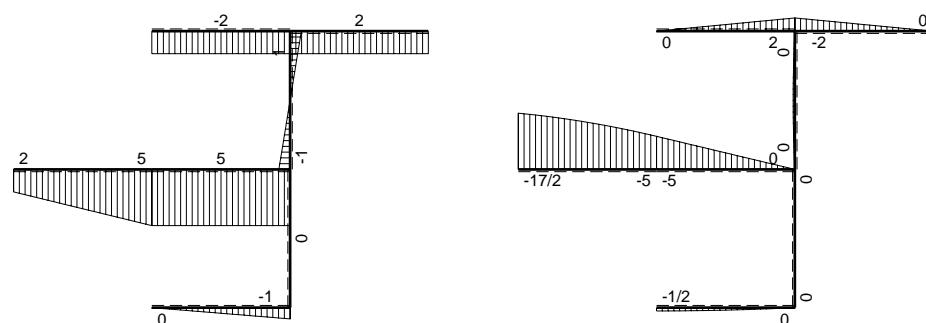
Rotazione intorno a F: asta FG FH

$$V_H b = -2Fb$$



$\vdash \dashv 50 F b^3 / E J$

$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$

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$\curvearrowleft [+] \curvearrowright F_b$

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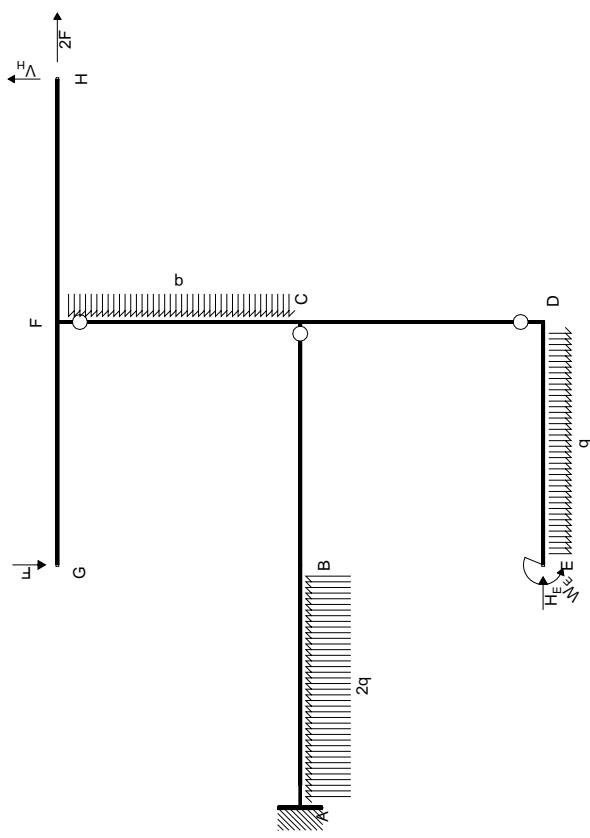
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EQUILIBRIO Nome:

REAZIONI Nome:

Struttura Isostatica.003

Struttura Isostatica.003



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: asta CD CF DE FG FH

$$H_E b + W_E + V_H b = F_b - q b^2$$

Rotazione intorno a D: asta DE

$$W_E = -1/2 q b^2$$

Rotazione intorno a F: asta FG FH

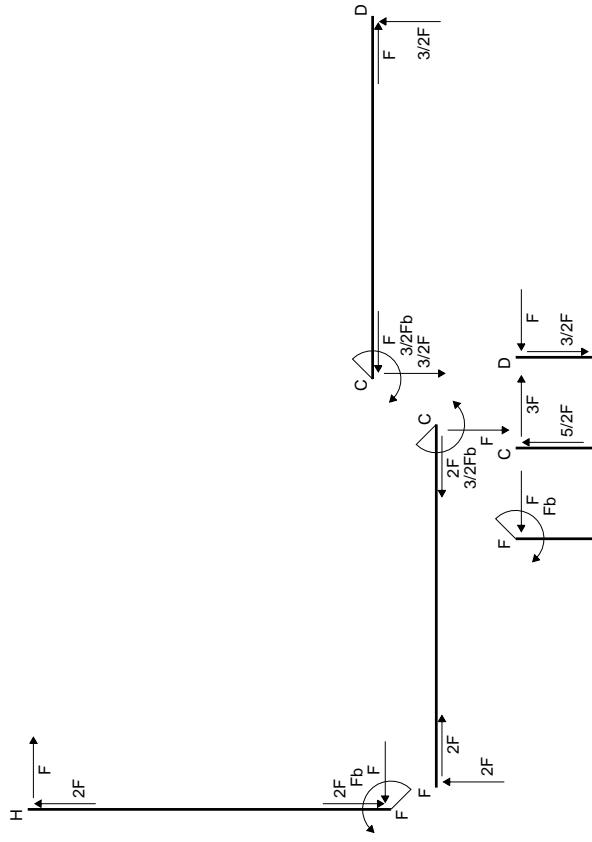
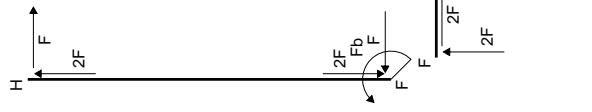
$$V_H b = -F_b$$

Matrice di equilibrio

$$\begin{bmatrix} H_E b & W_E & V_H b \end{bmatrix} = \begin{bmatrix} F_b & q b^2 \\ 1 & 1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} F_b & q b^2 \\ 1 & -1 \\ 0 & -1/2 \\ 0 & 1 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_E b \\ W_E \\ V_H b \end{bmatrix} = \begin{bmatrix} F_b \\ 2 \\ 0 \\ -1/2 \\ -1 \\ 0 \end{bmatrix}$$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: asta CD CF DE FG FH

$$H_E b + W_E + V_H b = F_b - q b^2$$

Rotazione intorno a D: asta DE

$$W_E = -1/2 q b^2$$

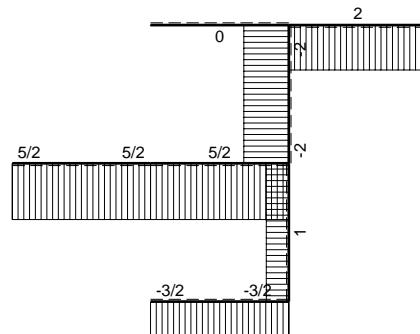
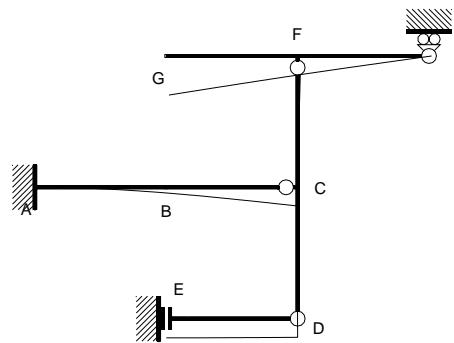
Rotazione intorno a F: asta FG FH

$$V_H b = -F_b$$

Soluzione del sistema

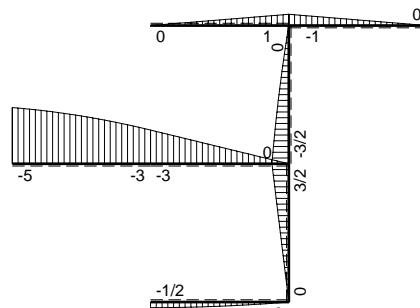
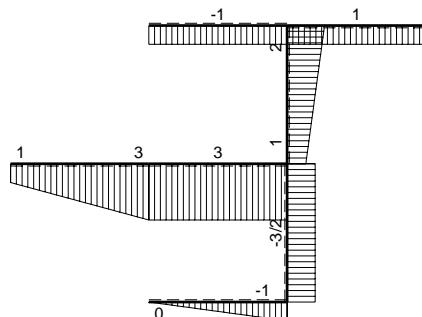
$$\begin{bmatrix} H_E b \\ W_E \\ V_H b \end{bmatrix} = \begin{bmatrix} F_b \\ 2 \\ 0 \\ -1/2 \\ -1 \\ 0 \end{bmatrix}$$





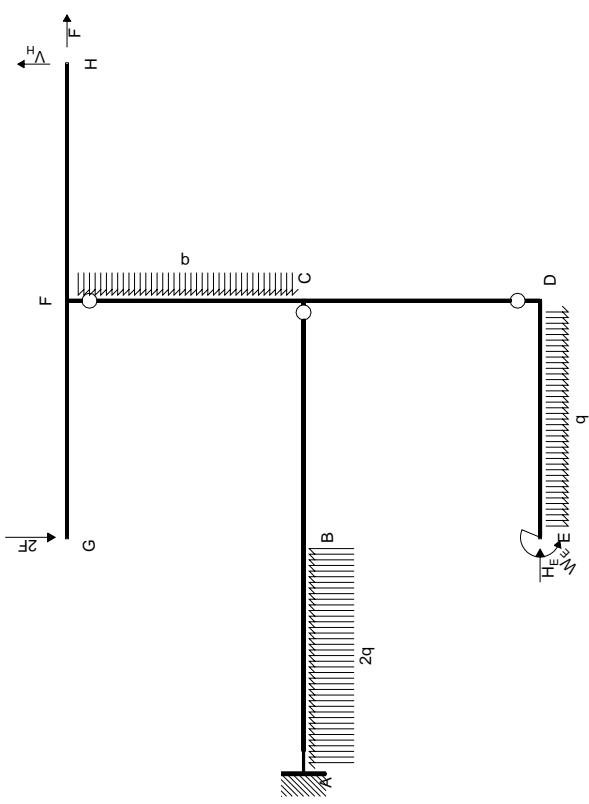
$\text{---} 30 \frac{\text{Fb}^3}{\text{EJ}}$

$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$

$\curvearrowleft [+] \curvearrowright F_b$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: aste CD CF DE FG FH

$$H_E b + W_E + V_H b = -Fb - qb^2$$

Rotazione intorno a D: aste DE

$$W = -1/2gh^2$$

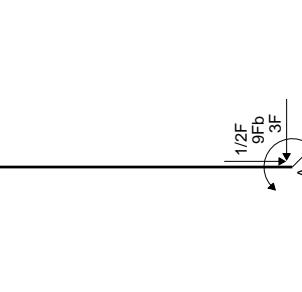
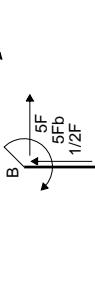
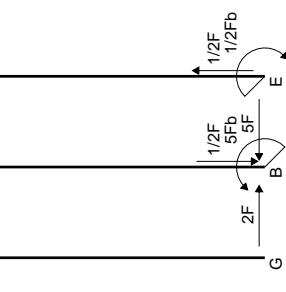
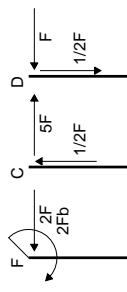
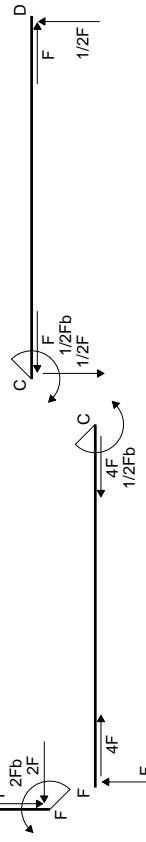
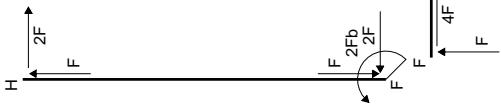
$$W_E = -1/2q\beta$$

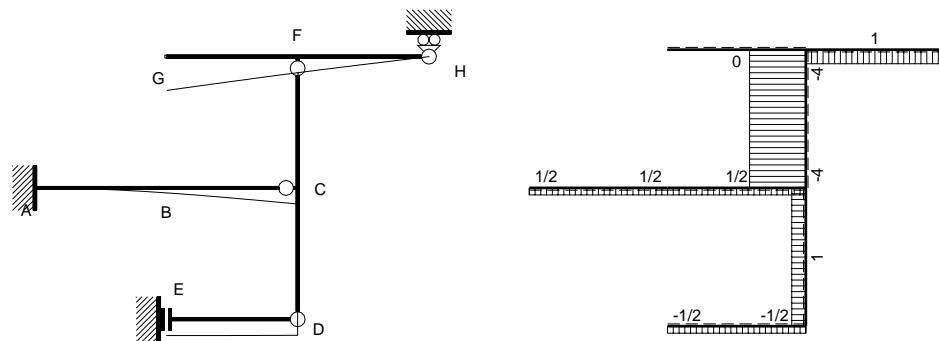
Rutazzi (1990) a F. asté FG FH

Matrice di equilibrio

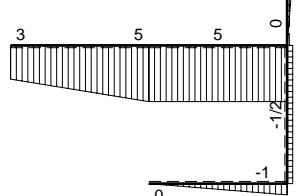
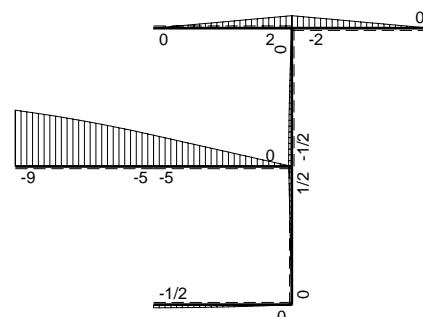
$$\begin{bmatrix} \Phi_{CB} \\ \Phi_{DC} \\ \Phi_{FC} \end{bmatrix} = \begin{bmatrix} \mathbf{v}_E & \mathbf{v}_H \\ \mathbf{v}_H & \mathbf{v}_B \end{bmatrix}^{-1} \begin{bmatrix} \mathbf{f}_B \\ \mathbf{q}_B \end{bmatrix}$$

$$\text{Soluzione del sistema} \quad \begin{bmatrix} F_B & qB^2 \\ 1 & -1/2 \\ 1 & 0 & -1/2 \\ V_H B & -2 & 0 \end{bmatrix} = \begin{bmatrix} H_E \\ W_E \end{bmatrix}$$





$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$

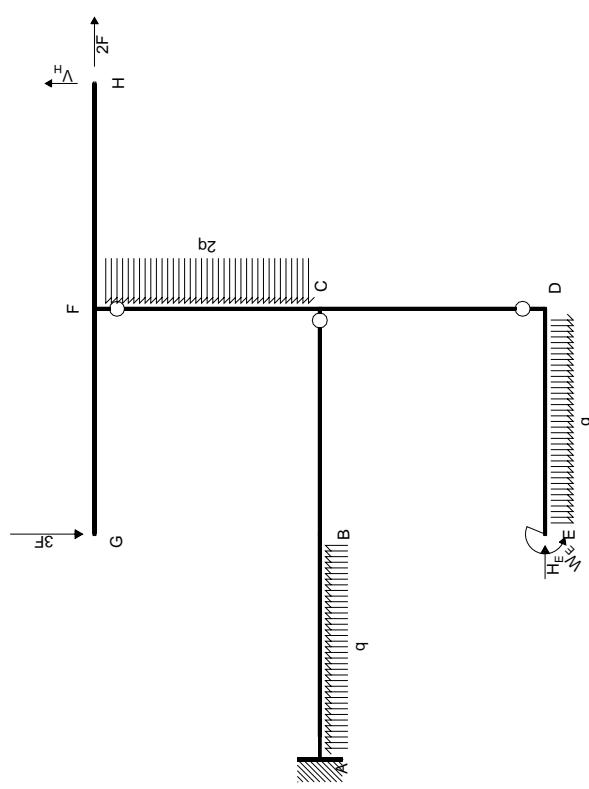
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$\curvearrowleft [+] \curvearrowright F_b$

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EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: asta CD CF DE FG FH

$$H_E b + W_E + V_H b = -Fb - 3/2qb^2$$

Rotazione intorno a D: asta DE

$$W_E = -1/2qb^2$$

Rotazione intorno a F: asta FG FH

$$V_H b = -3Fb$$

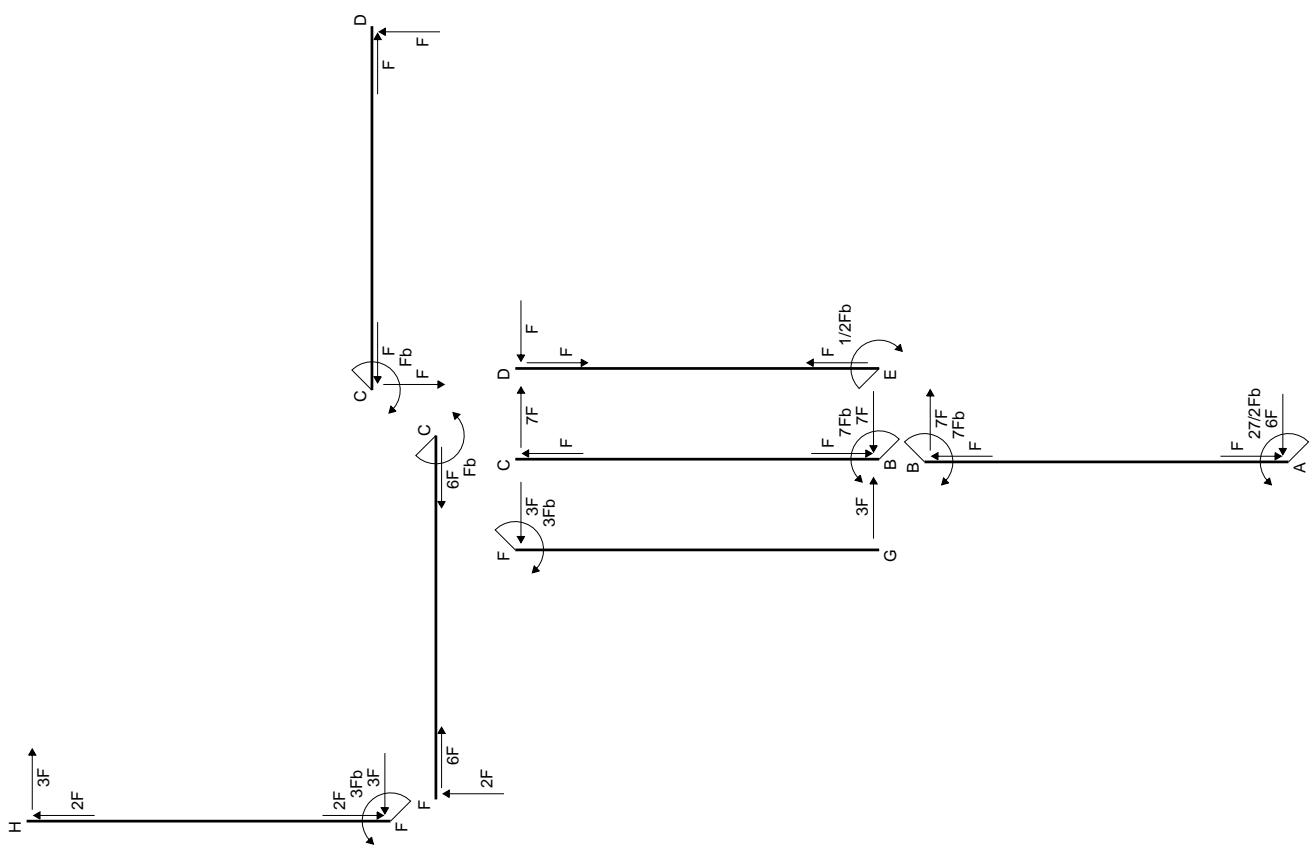
Matrice di equilibrio

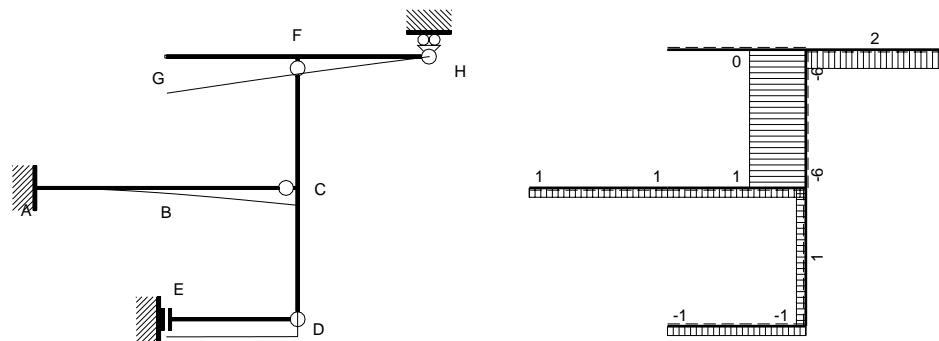
$$\begin{bmatrix} H_E b & W_E & V_H b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 1 & 1 \\ 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} \Phi_{CB} \\ \Phi_{DC} \\ \Phi_{FC} \end{bmatrix} = \begin{bmatrix} -1 & -3/2 \\ 0 & -1/2 \\ 0 & 0 \end{bmatrix}$$

Soluzione del sistema

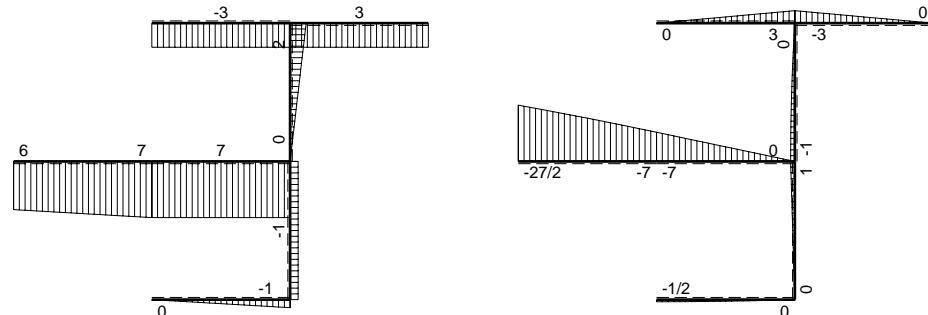
$$\begin{bmatrix} H_E b \\ W_E \\ V_H b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 2 & -1 \\ 0 & -1/2 \\ -3 & 0 \end{bmatrix}$$





$\vdash \dashv 80 F b^3 / E J$

$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$

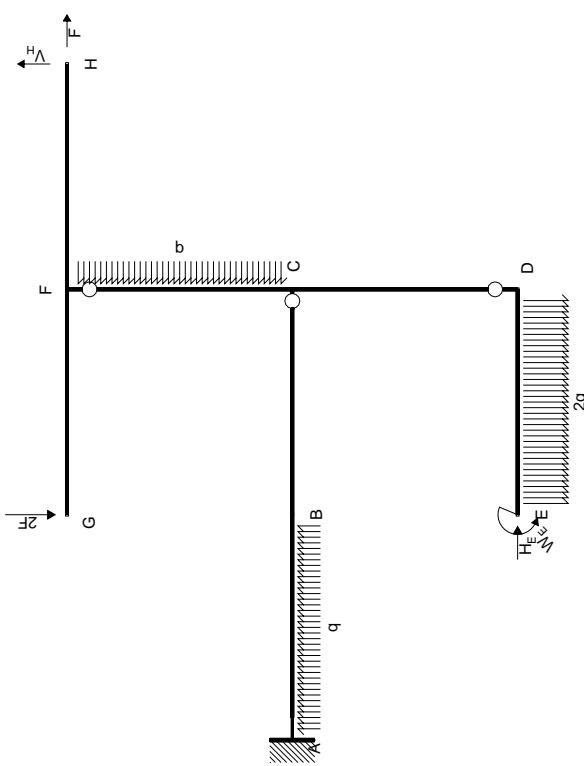
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$\curvearrowleft [+] \curvearrowright F_b$

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EQUAZIONI DI EQUILIBRIO
Rotazione intorno a \hat{z} : aste CD CE DE EG EH

$H_E b + W_E + V_H b = -F_b - 3/2 q b^2$

Rotazione intorno a D: aste DE

$$W = -gh^2$$

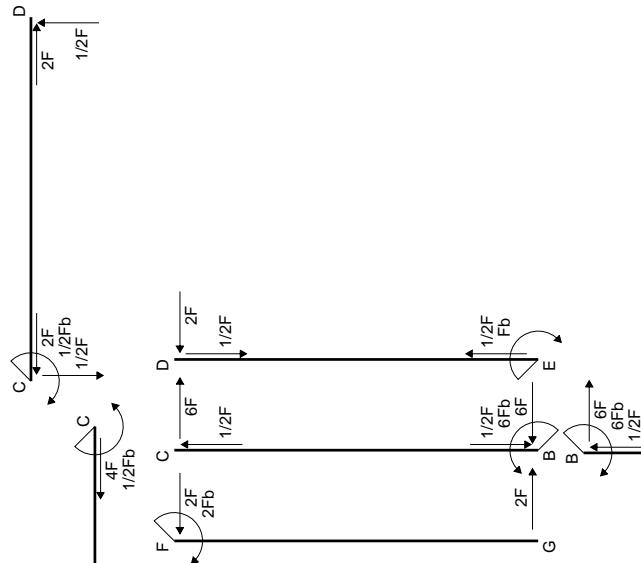
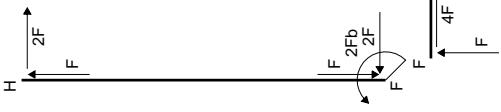
Rotazione intorno a F: aste FG F

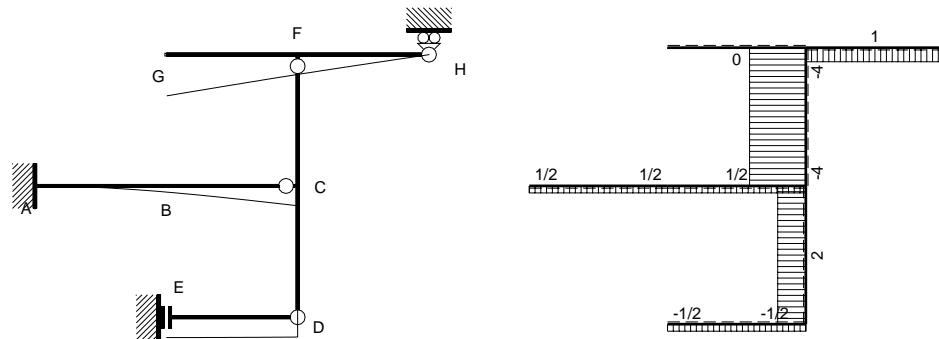
$$V_H b = -2Fb$$

Matrice di equilibrio

$$\begin{bmatrix} H_E b \\ W_E \\ V_H b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -1 & -3/2 \\ 0 & -1 \end{bmatrix} = \begin{bmatrix} 0 \\ -2 \\ 0 \end{bmatrix}$$

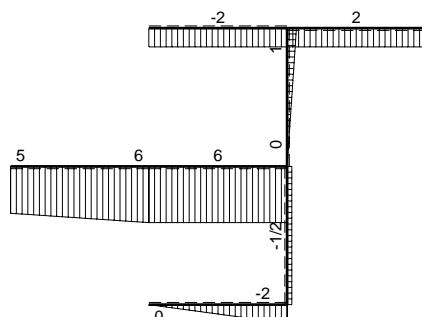
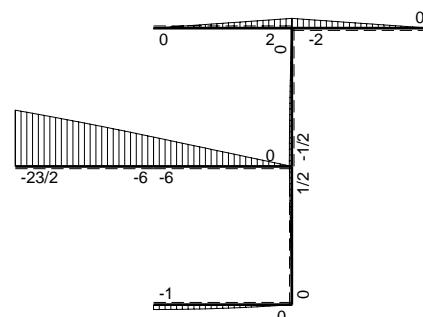
$$\text{Soluzione del sistema} \quad \begin{bmatrix} F_B & qB^2 \\ 1 & -1/2 \\ 1 & 0 & -1 \\ H_E b & W_E & V_H b \end{bmatrix} = \begin{bmatrix} 1 & -2 & 0 \end{bmatrix}$$





$\vdash \dashv 60 F b^3 / E J$

$\leftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$

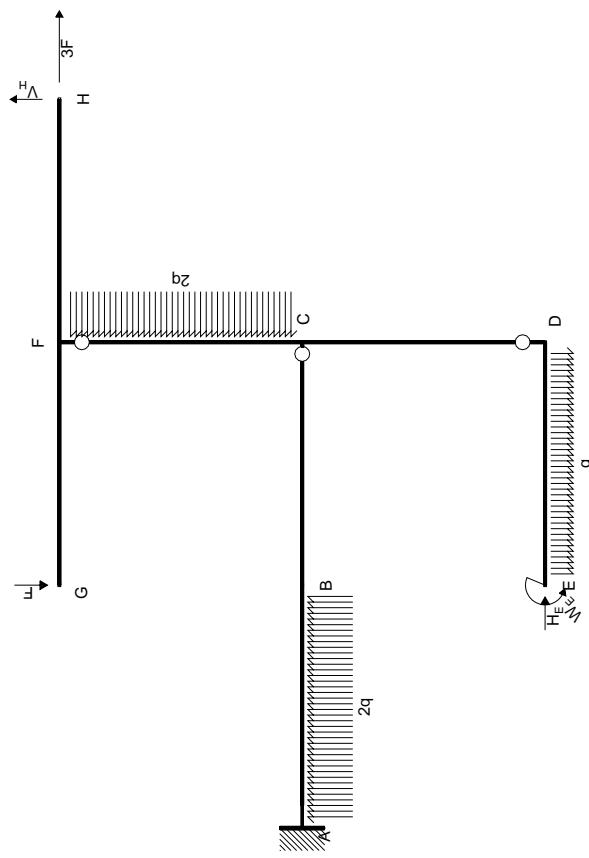
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$\curvearrowleft [+] \curvearrowright F_b$

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EQUAZIONI DI EQUILIBRIO

Rotazione intorno a C: asta CD CF DE FG FH

$$H_E b + W_E + V_H b = 2Fb - 3/2qb^2$$

Rotazione intorno a D: asta DE

$$W_E = -1/2qb^2$$

Rotazione intorno a F: asta FG FH

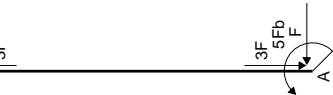
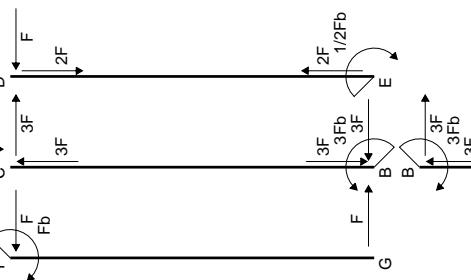
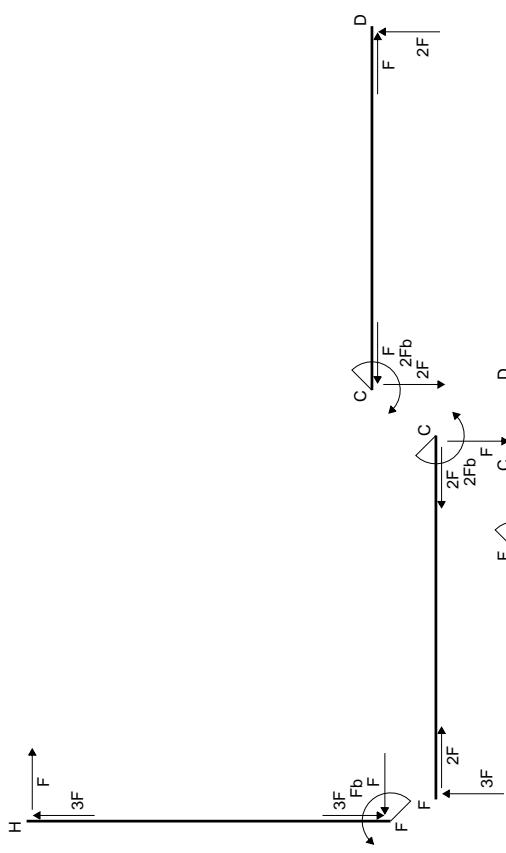
$$V_H b = -Fb$$

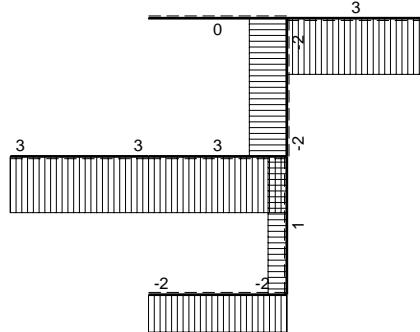
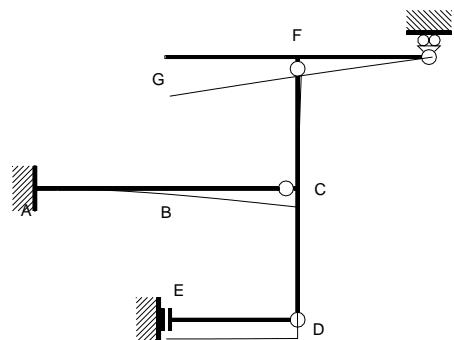
Matrice di equilibrio

$$\begin{bmatrix} H_E b & W_E & V_H b \end{bmatrix} \begin{bmatrix} Fb & qb^2 \\ 2 & -3/2 \\ 0 & -1/2 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 3 & -1 \\ 0 & -1/2 \\ -1 & 0 \end{bmatrix}$$

Soluzione del sistema

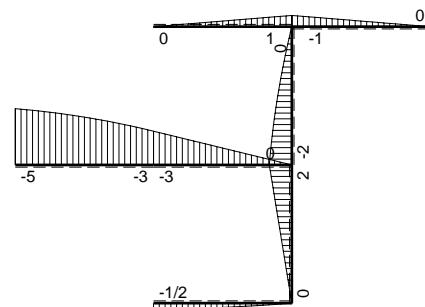
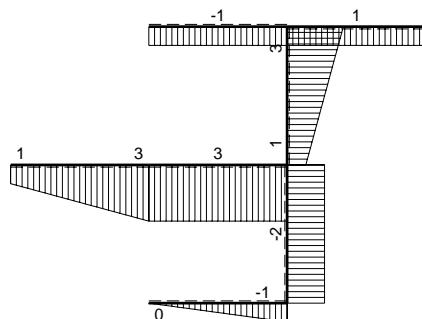
$$\begin{bmatrix} H_E b \\ W_E \\ V_H b \end{bmatrix} = \begin{bmatrix} Fb \\ qb^2 \\ 3 \\ 0 \\ -1/2 \\ -1 \end{bmatrix}$$





$\longleftarrow 30 F b^3 / E J$

$\longleftarrow [+] \rightarrow F$



$\uparrow [+] \downarrow F$

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$\curvearrowleft [+] \curvearrowright F_b$

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