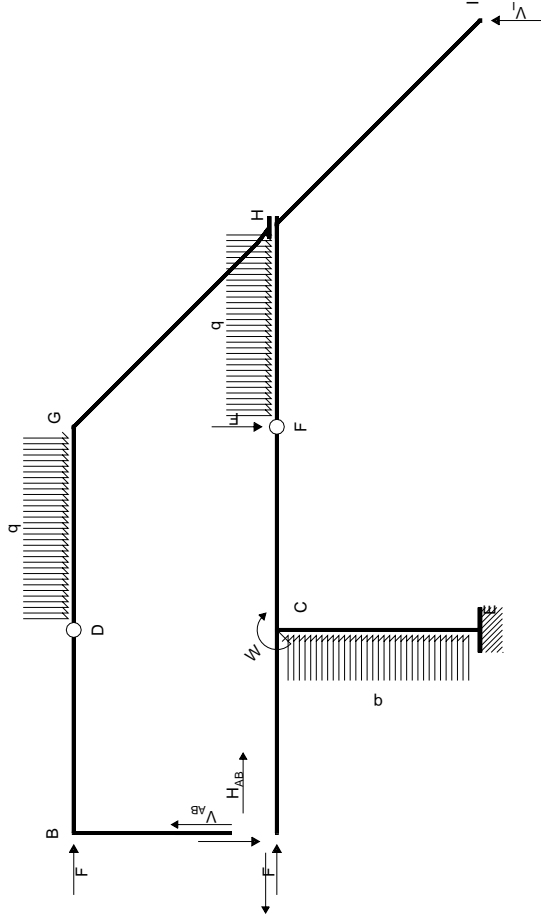


Carichi e deformazioni date hanno verso efficace in disegno.
Calcolare reazioni vincolari della struttura e delle aste.
Tracciare i diagrammi quotati delle azioni interne nelle aste.
 $J_{YZ} - X_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.
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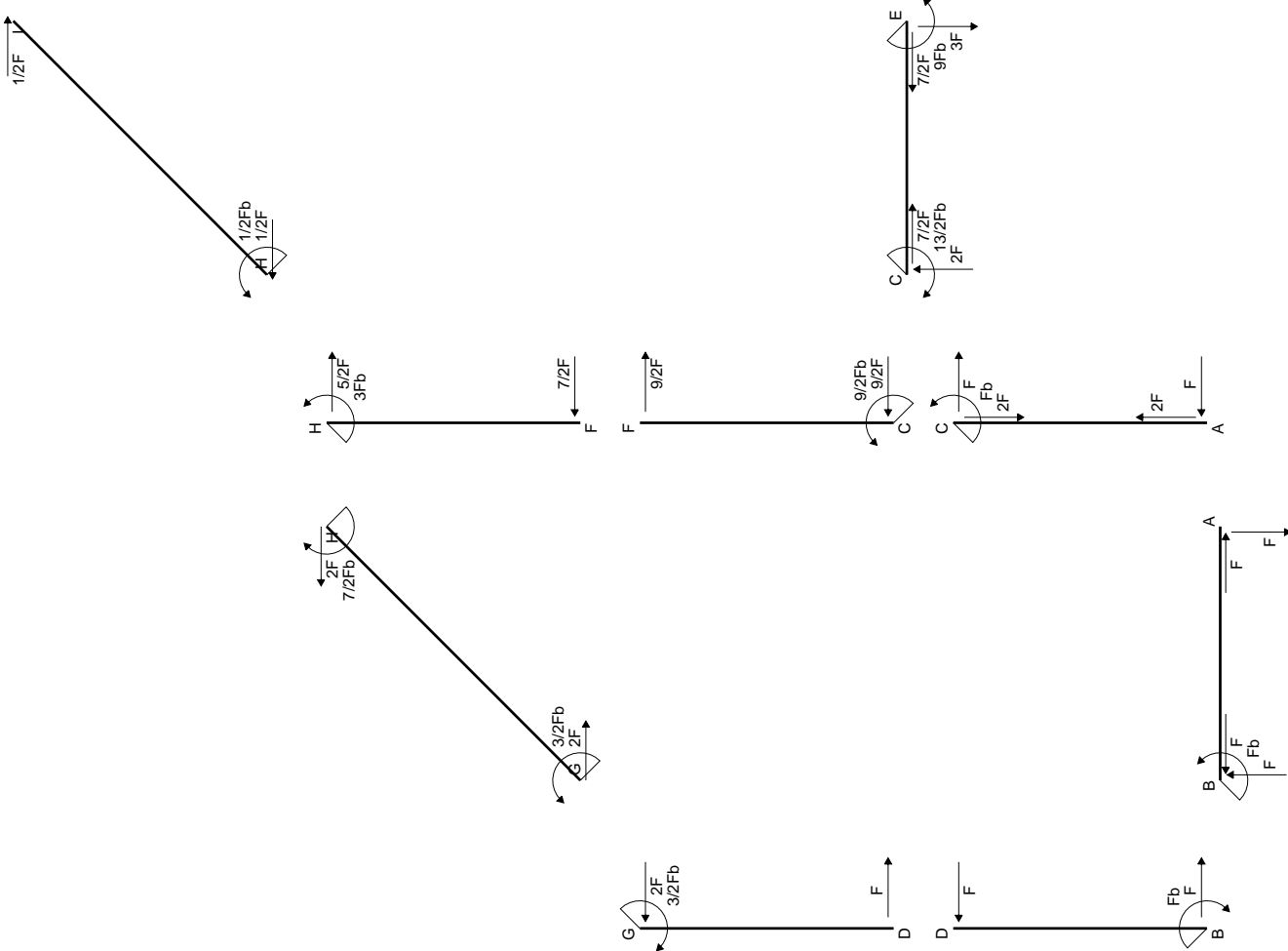
EQUAZIONI DI EQUILIBRIO
Rotazione intorno a F: aste FH HG HI GD DB BA
 $2V_b - 2V_{AB}b = Fb$
Traslazione orizzontale: aste HG GD DB BA
 $H_{AB} = -F$
Rotazione intorno a D: aste DB BA
 $H_{AB}b - V_{AB}b = 0$

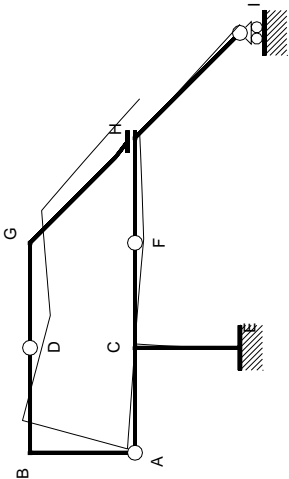
Matrice di equilibrio

$$\begin{bmatrix} V_b & H_{AB}b & V_{AB}b \end{bmatrix} \begin{bmatrix} Fb & W & qb^2 \end{bmatrix}$$
$$\varphi_{FC} \begin{bmatrix} 2 & 0 & -2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$$
$$u_{HG} \begin{bmatrix} 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 \end{bmatrix}$$
$$\varphi_{DB} \begin{bmatrix} 0 & 1 & -1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix}$$

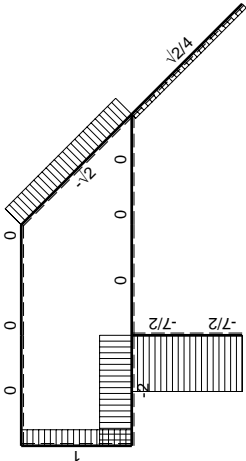
Soluzione del sistema

$$\begin{bmatrix} V_b \\ H_{AB}b \\ V_{AB}b \end{bmatrix} = \begin{bmatrix} Fb \\ -1/2 & 0 & 0 \\ -1 & 0 & 0 \\ -1 & 0 & 0 \end{bmatrix} \begin{bmatrix} Fb \\ W \\ qb^2 \end{bmatrix}$$

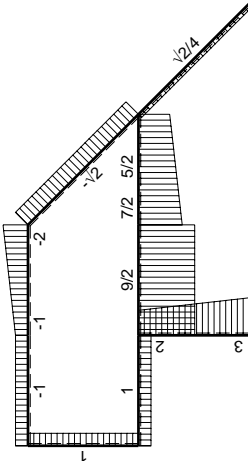




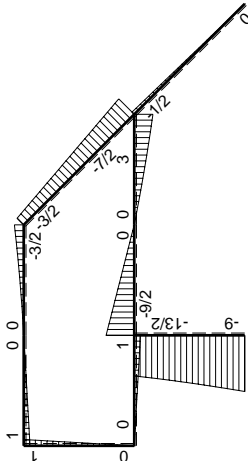
$\frac{1}{180} \frac{Fb^3}{EJ}$



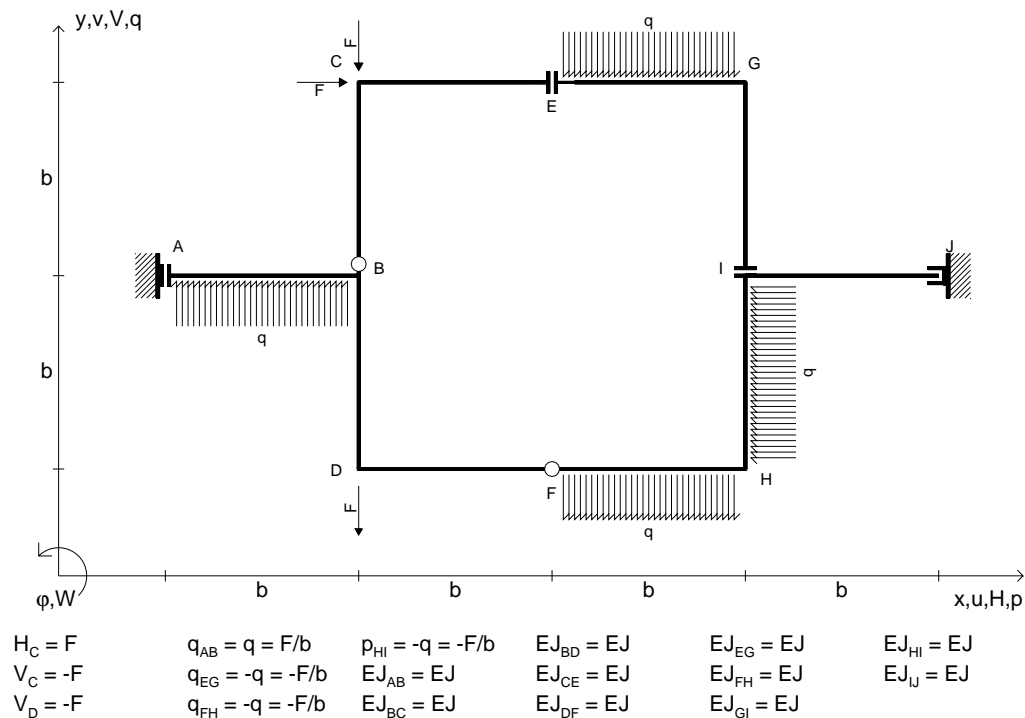
$\frac{1}{180} \frac{Fb^3}{EJ}$



$\frac{1}{180} \frac{Fb^3}{EJ}$



$\frac{1}{180} \frac{Fb^3}{EJ}$



Carichi e deformazioni date hanno verso efficace in disegno.

Calcolare reazioni vincolari della struttura e delle aste.

Tracciare i diagrammi quotati delle azioni interne nelle aste.

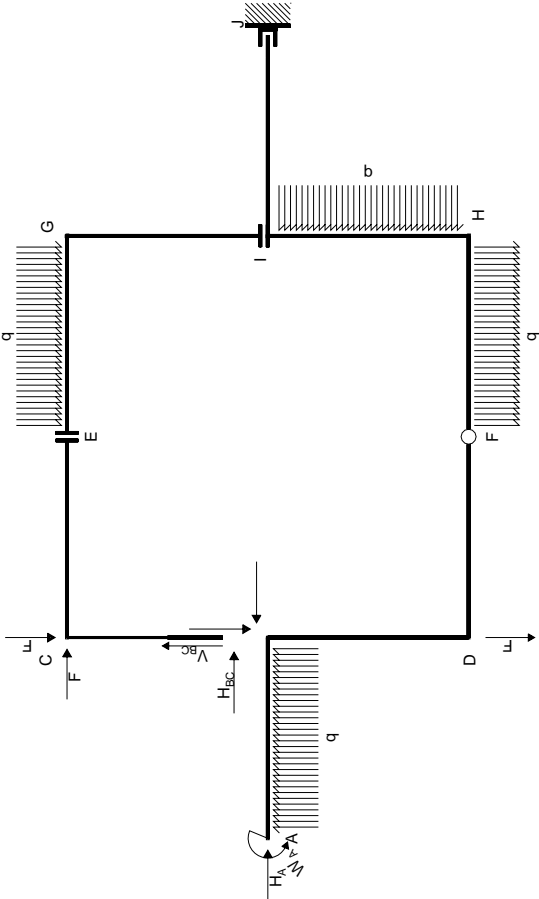
$J_{YZ} - x_{YZ} - \theta_{YZ}$ riferimento locale asta YZ con origine in Y.

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09.02.16

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09.02.16



EQUAZIONI DI EQUILIBRIO

Traslazione orizzontale globale

$H_A = -F + qb$

Traslazione orizzontale: aste IG GE EC CB

$H_{BC} = -F$

Traslazione verticale: aste EC CB

$V_{BC} = F$

Rotazione intorno a F: aste FD DB BA

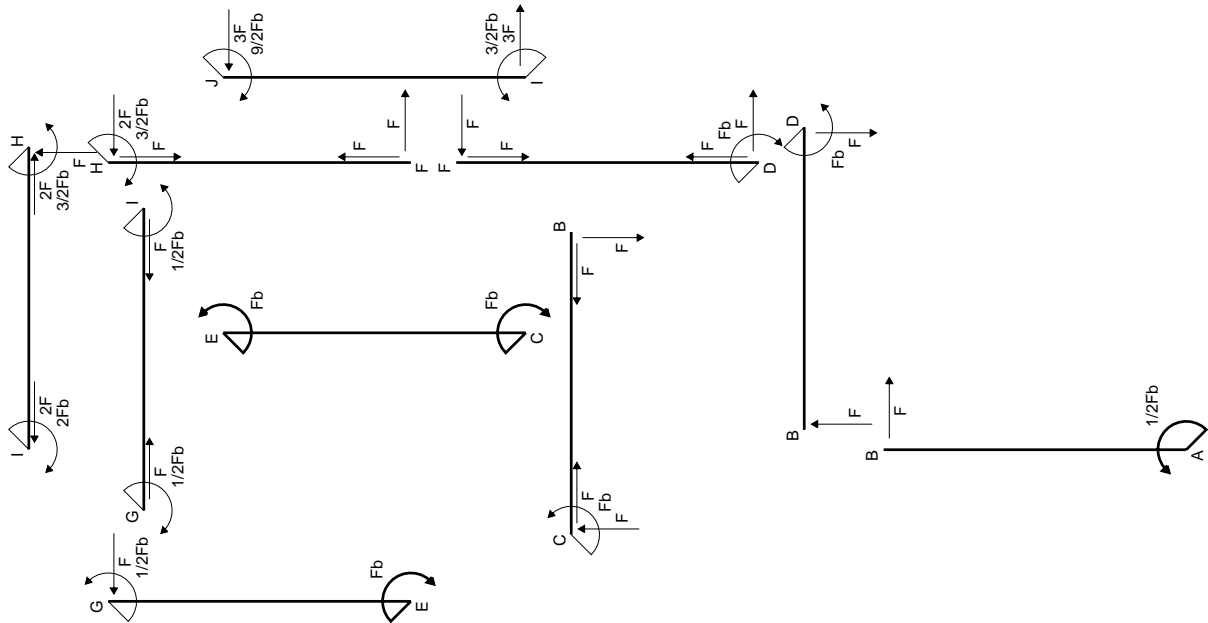
$-H_A b + W_A + H_{BC} b + V_{BC} b = -Fb + 3/2qb^2$

Matrice di equilibrio

$$\begin{bmatrix} H_A b & W_A & H_{BC} b & V_{BC} b \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$
$$u_j \begin{bmatrix} 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} -1 & 1 \end{bmatrix}$$
$$u_{IG} \begin{bmatrix} 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} -1 & 0 \end{bmatrix}$$
$$V_{EC} \begin{bmatrix} 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \end{bmatrix}$$
$$\theta_{FD} \begin{bmatrix} -1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} -1 & 3/2 \end{bmatrix}$$

Soluzione del sistema

$$\begin{bmatrix} H_A b \\ H_{BC} b \\ V_{BC} b \\ W_A \end{bmatrix} = \begin{bmatrix} -1 & 1 \\ -1 & 0 \\ 1 & 0 \\ -2 & 5/2 \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$

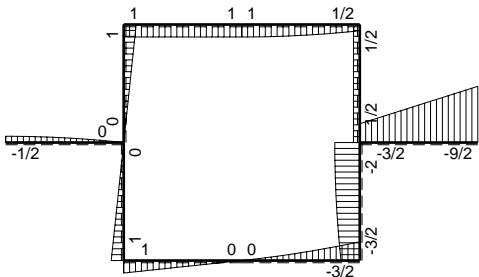
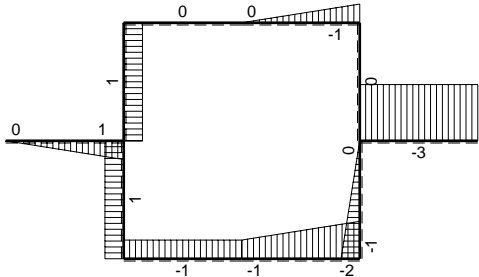
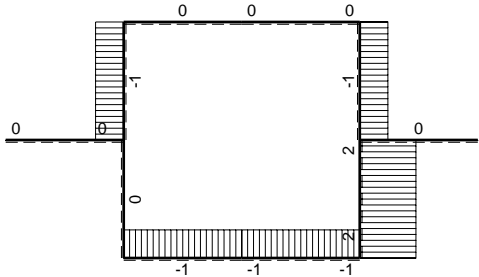
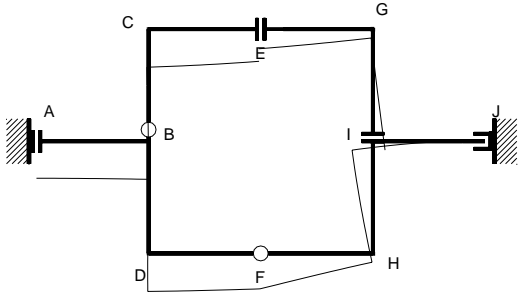


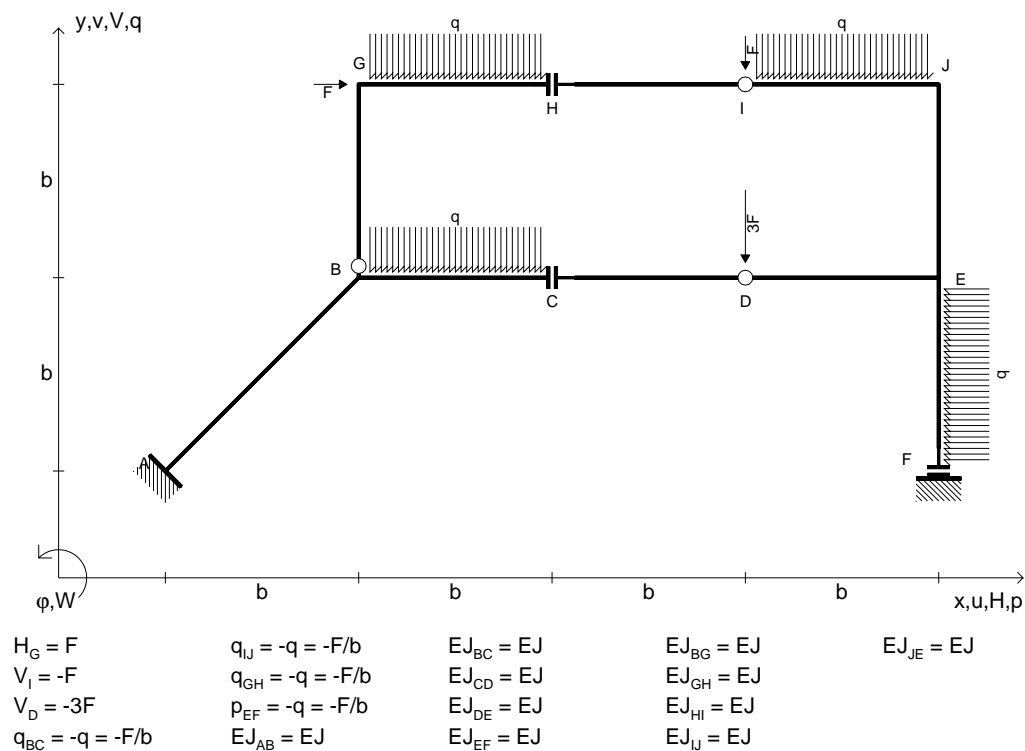
$15 Fb^3/EJ$

F

F

Fb





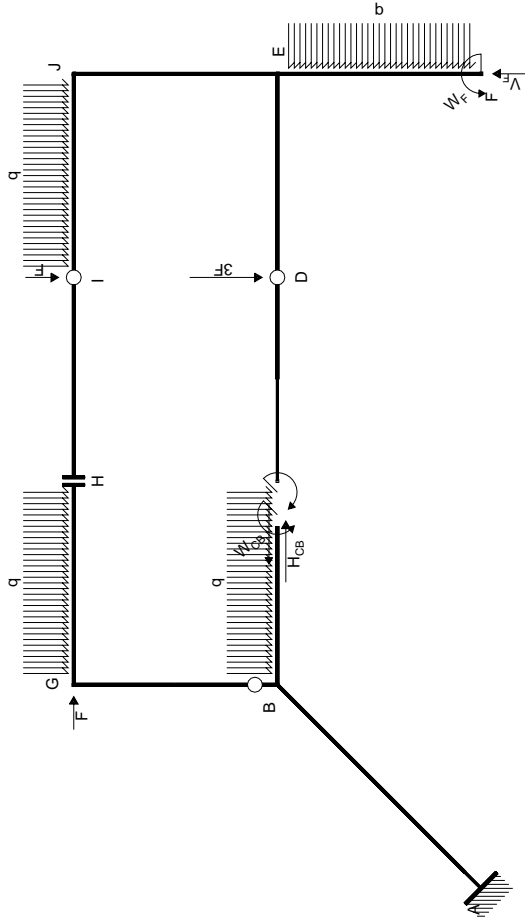
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EQUAZIONI DI EQUILIBRIO

Rotazione intorno a B: aste BG GH HI IJ JE ED EF DC

$3V_F b + W_F - W_{CB} = 9Fb + 7/2qb^2$

Traslazione verticale: aste HI IJ JE DE EF DC

$V_F = 4F + qb$

Rotazione intorno a I: aste IJ JE ED EF DC

$V_F b + W_F - H_{CB} b - W_{CB} = 2qb^2$

Rotazione intorno a D: aste DC

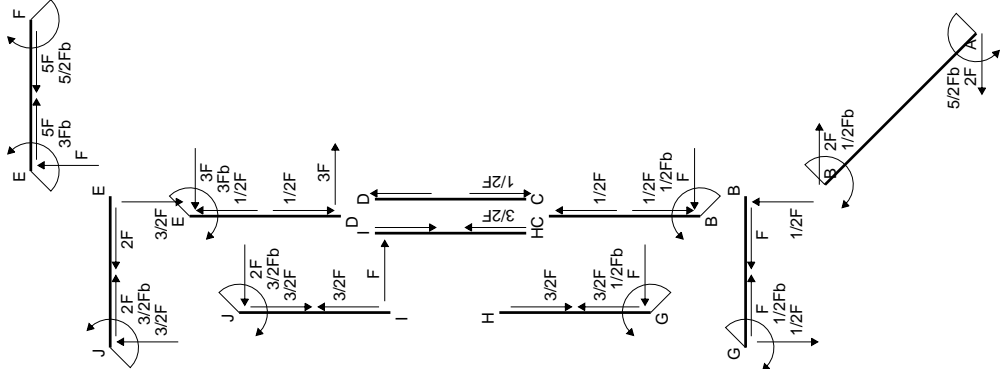
$-W_{CB} = 0$

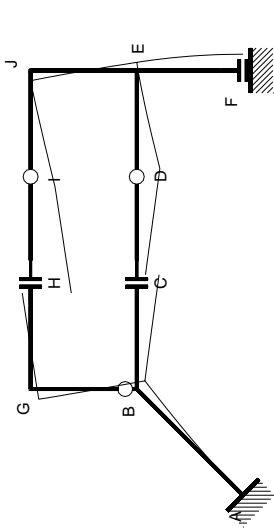
Matrice di equilibrio

$$\begin{bmatrix} V_F b & W_F & H_{CB} b & W_{CB} \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$
$$\begin{bmatrix} \varphi_{BG} \\ \varphi_{HG} \\ \varphi_{IH} \\ \varphi_{DC} \end{bmatrix} \begin{bmatrix} 3 & 1 & 0 & -1 \\ 1 & 0 & 0 & 0 \\ 1 & 1 & -1 & -1 \\ 0 & 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} 9 & 7/2 \\ 4 & 1 \\ 0 & 2 \\ 0 & 0 \end{bmatrix} =$$

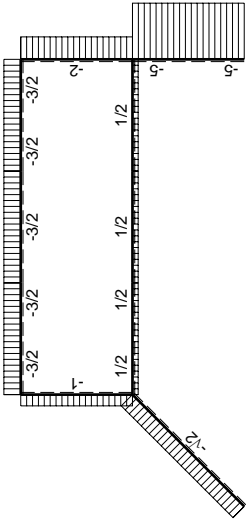
Soluzione del sistema

$$\begin{bmatrix} V_F b \\ W_F \\ H_{CB} b \\ W_{CB} \end{bmatrix} \begin{bmatrix} Fb & qb^2 \end{bmatrix}$$
$$\begin{bmatrix} 4 & 1 \\ -3 & 1/2 \\ 1 & -1/2 \\ 0 & 0 \end{bmatrix} =$$

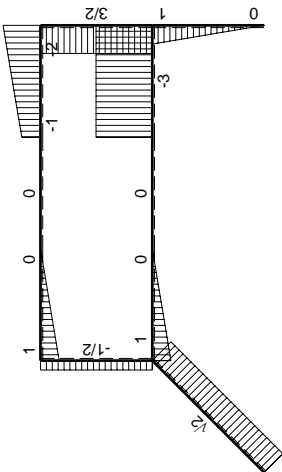




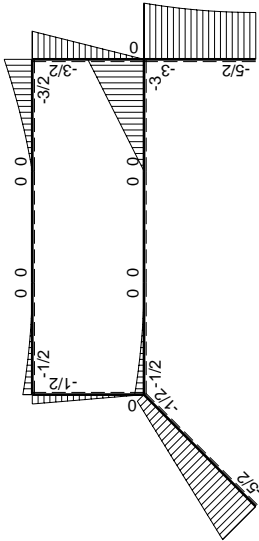
$\text{---} 12 Fb^3/EJ$



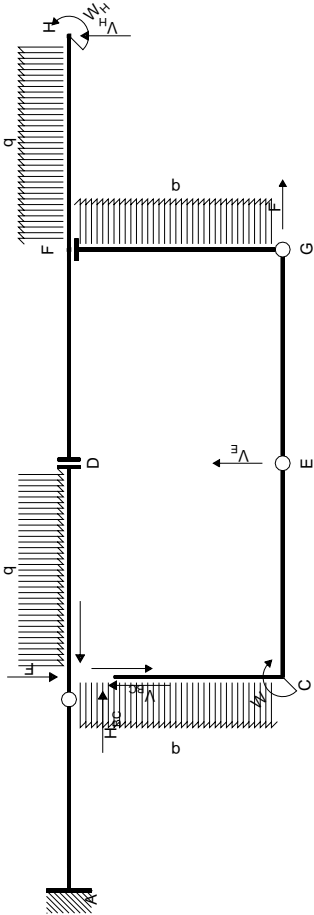
$\left[\begin{smallmatrix} + \\ - \end{smallmatrix} \right] \rightarrow F$



$\uparrow \left[\begin{smallmatrix} + \\ - \end{smallmatrix} \right] \downarrow F$



$\curvearrowleft \left[\begin{smallmatrix} + \\ - \end{smallmatrix} \right] \curvearrowright Fb$



EQUAZIONI DI EQUILIBRIO

Rotazione intorno a B: aste BD DF FG FH GE EC CB

$V_E b + 3V_H b + W_H = -Fb + W - 2qb^2$

Traslazione verticale: aste DF FG FH GE EC CB

$V_E + V_H + V_{BC} = -qb$

Traslazione orizzontale: aste FG GE EC CB

$H_{BC} = -F$

Rotazione intorno a G: aste GE EC CB

$-V_E b - H_{BC} b - 2V_{BC} b = W - 1/2qb^2$

Rotazione intorno a E: aste EC CB

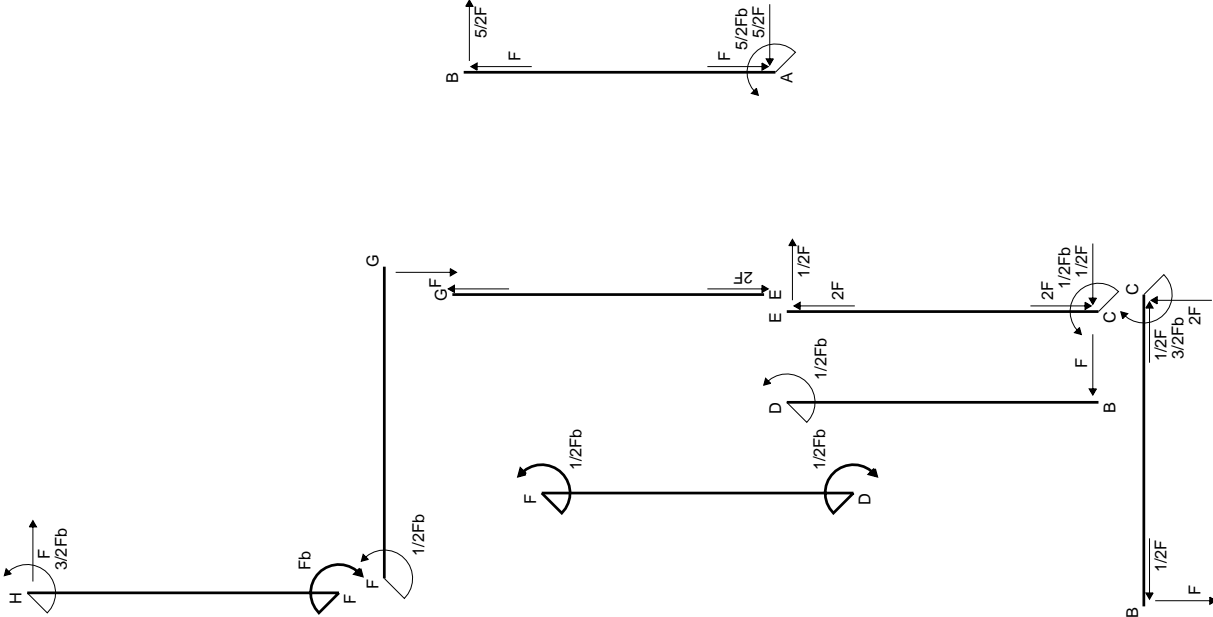
$-H_{BC} b - V_{BC} b = W - 1/2qb^2$

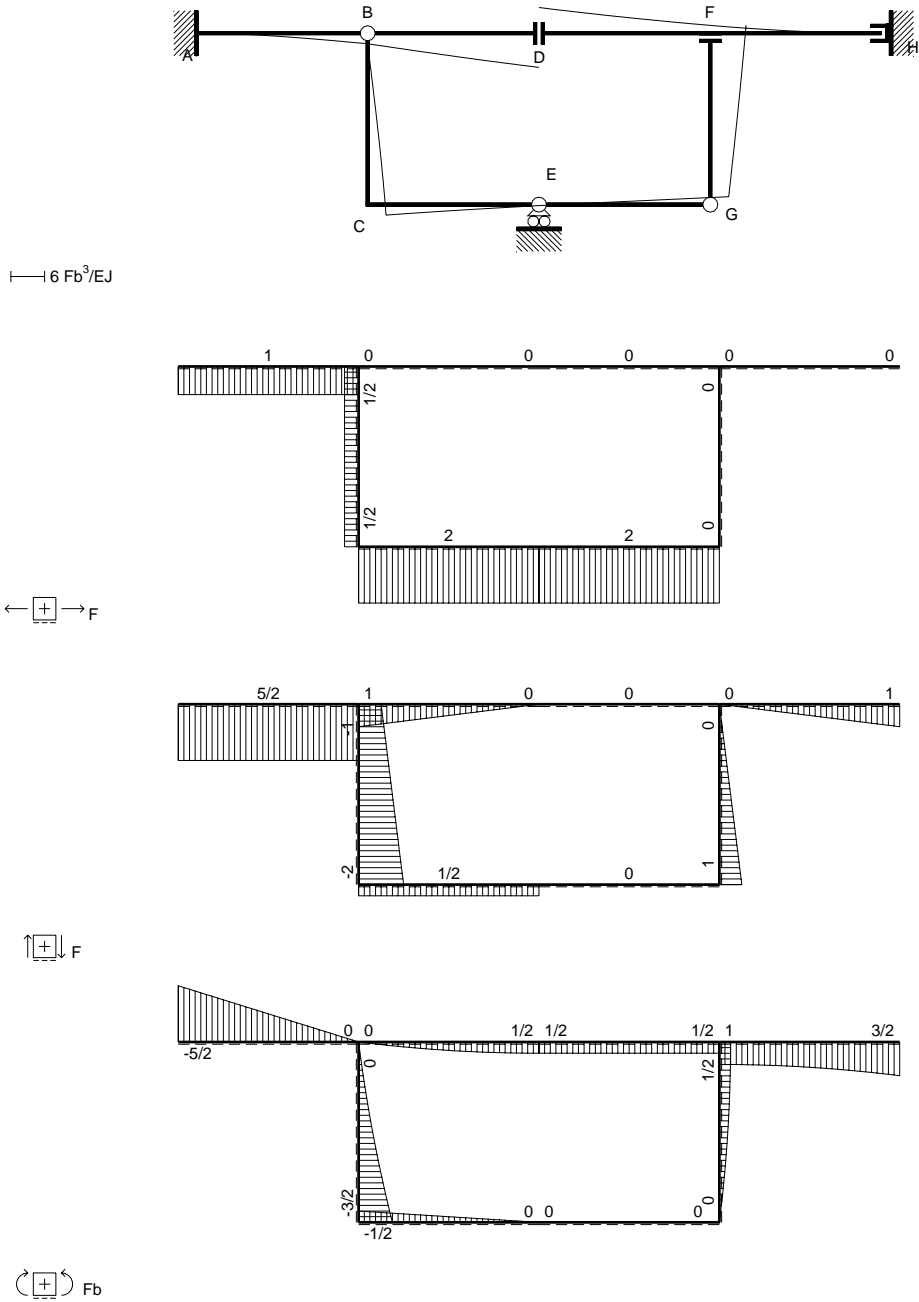
Matrice di equilibrio

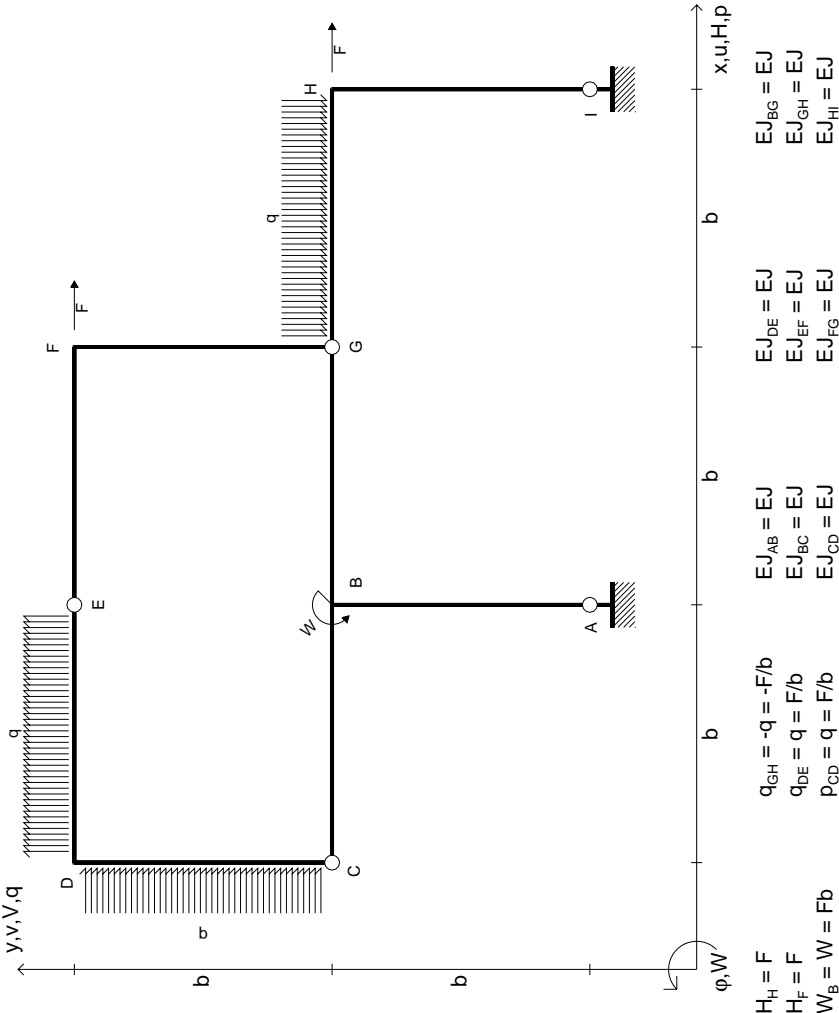
$$\begin{bmatrix} \Phi_{BA} \\ \Phi_{DB} \\ U_{FG} \\ \Phi_{GE} \\ \Phi_{EC} \end{bmatrix} \begin{bmatrix} V_E b & V_H b & W_H & H_{BC} b & V_{BC} b \end{bmatrix} \begin{bmatrix} Fb & W & qb^2 \end{bmatrix} = \begin{bmatrix} -1 & 1 & -2 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & -2 \\ 0 & 0 & -1 \end{bmatrix}$$

Soluzione del sistema

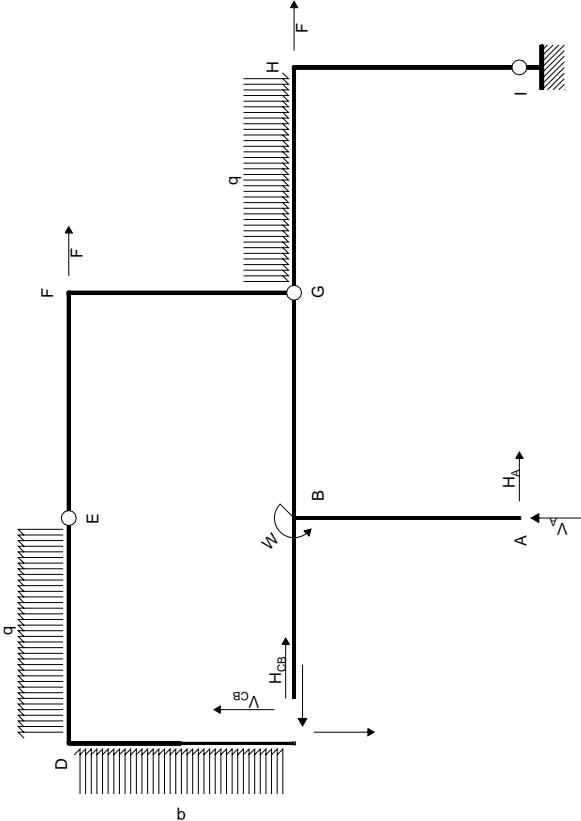
$$\begin{bmatrix} V_E b \\ V_H b \\ H_{BC} b \\ W_H \\ V_{BC} b \end{bmatrix} \begin{bmatrix} Fb & W & qb^2 \end{bmatrix} = \begin{bmatrix} -1 & 1 & -1/2 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & 0 & 3/2 \\ 1 & -1 & 1/2 \end{bmatrix}$$







Carichi e deformazioni date hanno verso efficace in disegno.
Calcolare reazioni vincolari della struttura e delle aste.
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@ Adolfo Zavelani Rossi, Politecnico di Milano, vers.27.03.13



EQUAZIONI DI EQUILIBRIO

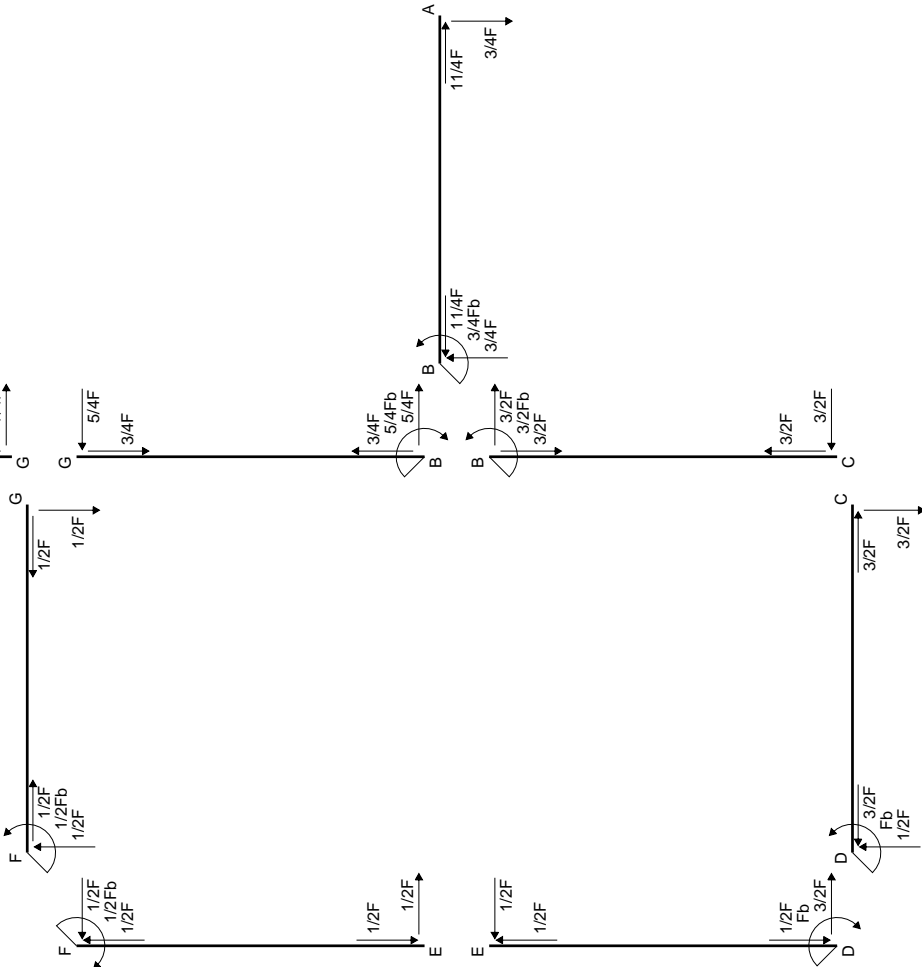
- Rotazione globale intorno a I
- $-2V_{Ab} = 3Fb - W + 7/2qb^2$
- Rotazione intorno a G: aste GF FE ED DC
- $2V_{Cgb} = Fb + 2qb^2$
- Rotazione intorno a G: aste GB BA BC
- $H_{Ab} - V_{Ab} - 2V_{Cgb} = -W$
- Rotazione intorno a E: aste ED DC
- $-H_{Cgb} + V_{Cgb} = 0$

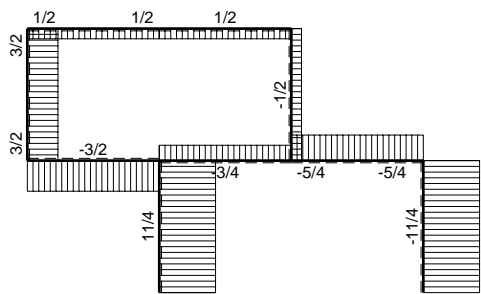
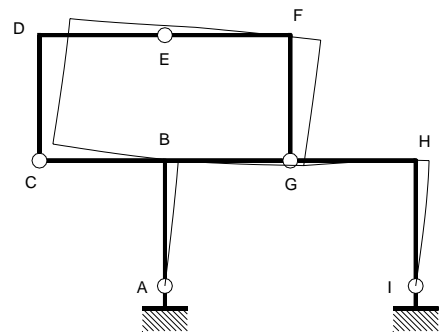
Matrice di equilibrio

$$\begin{bmatrix} H_{Ab} & V_{Ab} & H_{Cgb} & V_{Cgb} \end{bmatrix} \begin{bmatrix} Fb & W & qb^2 \end{bmatrix} \\ \begin{bmatrix} 0 & -2 & 0 & 0 \\ 0 & 0 & 0 & 2 \\ 1 & -1 & 0 & -2 \\ 0 & 0 & -1 & 1 \end{bmatrix} \begin{bmatrix} 3 & -1 & 7/2 \\ 1 & 0 & 2 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{bmatrix} =$$

Soluzione del sistema

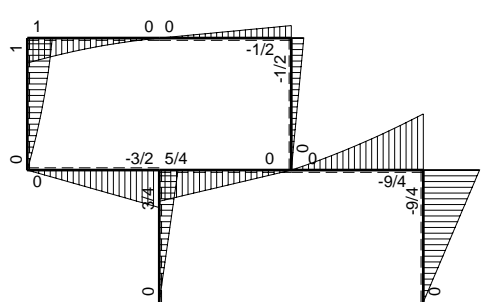
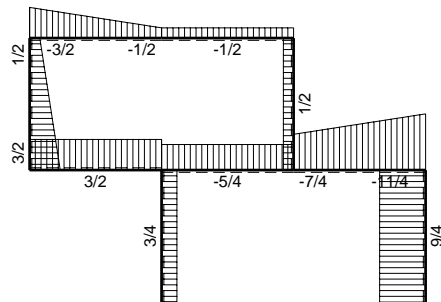
$$\begin{bmatrix} V_{Ab} \\ V_{Cgb} \\ H_{Ab} \\ H_{Cgb} \end{bmatrix} = \begin{bmatrix} -3/2 & 1/2 & -7/4 \\ 1/2 & 0 & 1 \\ -1/2 & -1/2 & 1/4 \\ 1/2 & 0 & 1 \end{bmatrix} \begin{bmatrix} Fb & W & qb^2 \end{bmatrix}$$





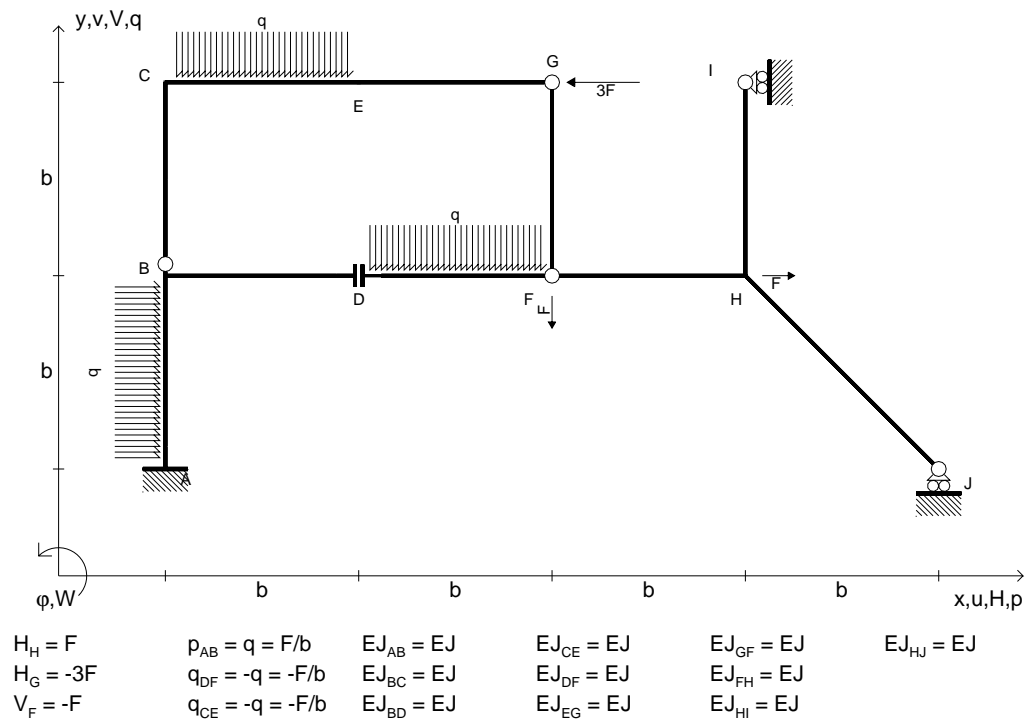
$\delta = 6 F b^3 / EJ$

$\leftarrow \boxed{+} \rightarrow F$



$\uparrow \boxed{+} \downarrow F$

$\curvearrowright \boxed{+} \curvearrowleft F_b$



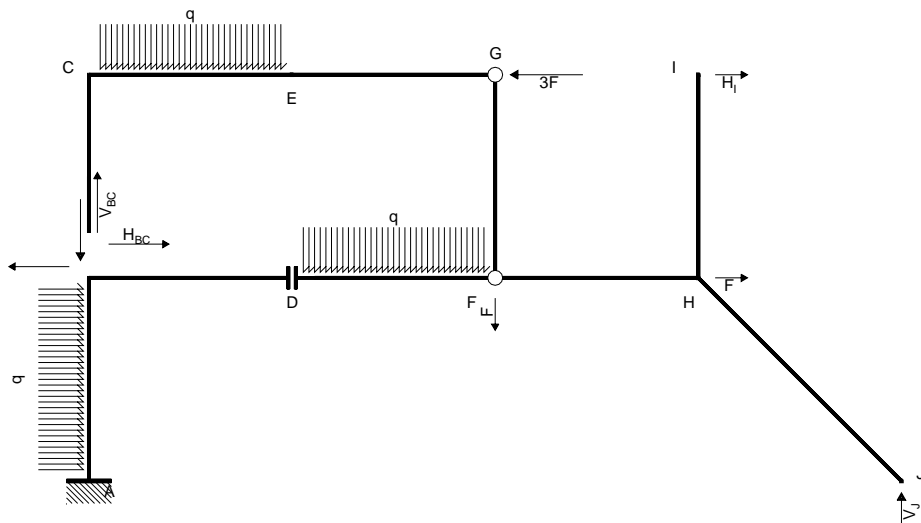
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EQUAZIONI DI EQUILIBRIO

Traslazione verticale: aste DF FG FH GE HI HJ EC CB

$$V_J + V_{BC} = F + 2qb$$

Rotazione intorno a F: aste FG FH GE HI HJ EC CB

$$-H_1b + 2V_Jb - 2V_{BC}b = -3Fb - 3/2qb^2$$

Rotazione intorno a F: aste FG GE EC CB

$$-2V_{BC}b = -3Fb - 3/2qb^2$$

Rotazione intorno a G: aste GE EC CB

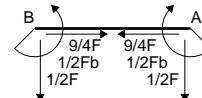
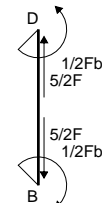
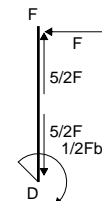
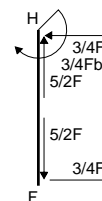
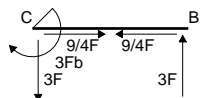
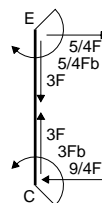
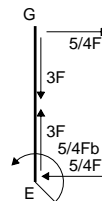
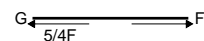
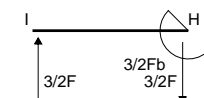
$$H_{BC}b - 2V_{BC}b = -3/2qb^2$$

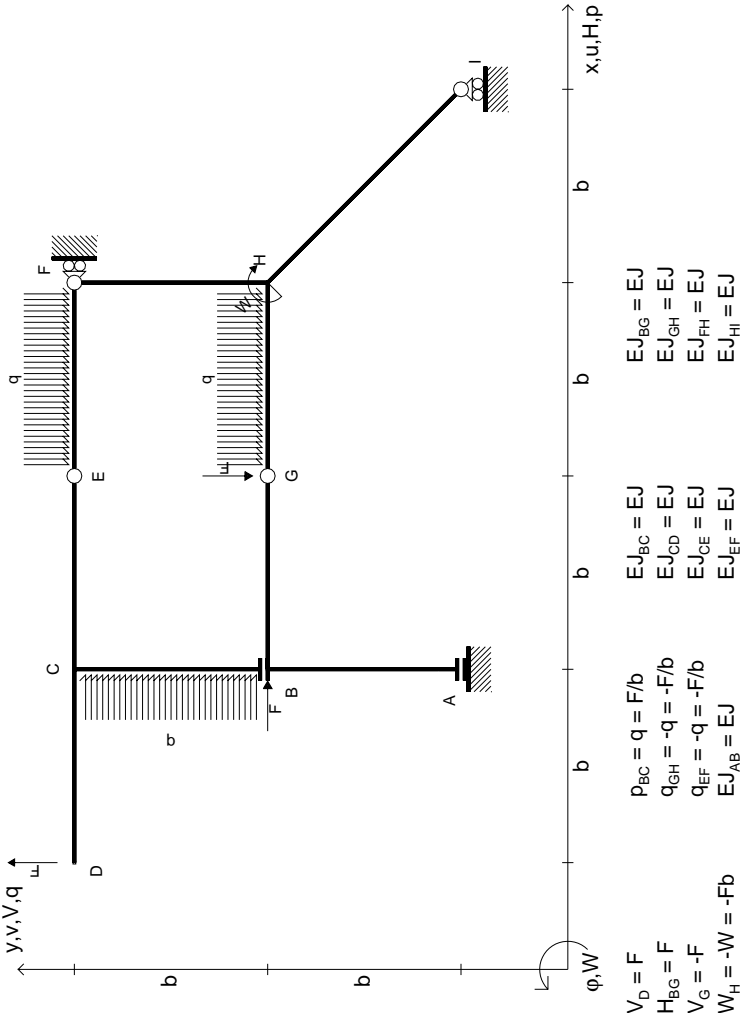
Matrice di equilibrio

$$\begin{bmatrix} H_1b & V_Jb & H_{BC}b & V_{BC}b \\ \phi_{FD} & -1 & 2 & 0 & -2 \\ \phi_{FG} & 0 & 0 & 0 & -2 \\ \phi_{GE} & 0 & 0 & 1 & -2 \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ 1 & 2 \\ -3 & -3/2 \\ -3 & -3/2 \\ 0 & -3/2 \end{bmatrix}$$

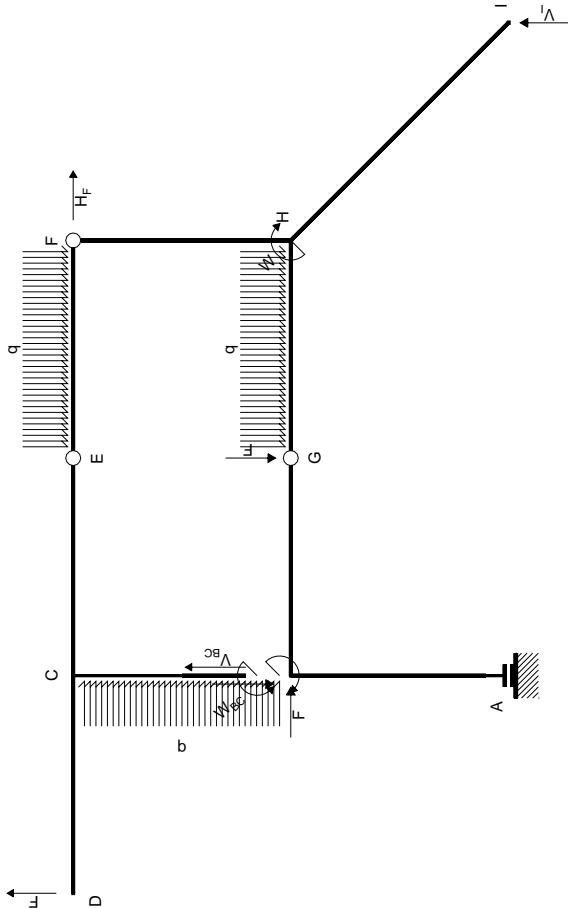
Soluzione del sistema

$$\begin{bmatrix} V_Jb \\ H_1b \\ V_{BC}b \\ H_{BC}b \end{bmatrix} = \begin{bmatrix} Fb & qb^2 \\ -1/2 & 5/4 \\ -1 & 5/2 \\ 3/2 & 3/4 \\ 3 & 0 \end{bmatrix}$$





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EQUAZIONI DI EQUILIBRIO

Traslazione orizzontale globale

$H_F = -F - qb$

Rotazione intorno a G: aste GH HF HI FE EC CB CD

$-H_F b + 2V_F b - V_{BC} b + W_{BC} = 2Fb + W + 3/2qb^2$

Rotazione intorno a F: aste FE EC CB CD

$-2V_{BC} b + W_{BC} = 3Fb - qb^2$

Rotazione intorno a E: aste EC CB CD

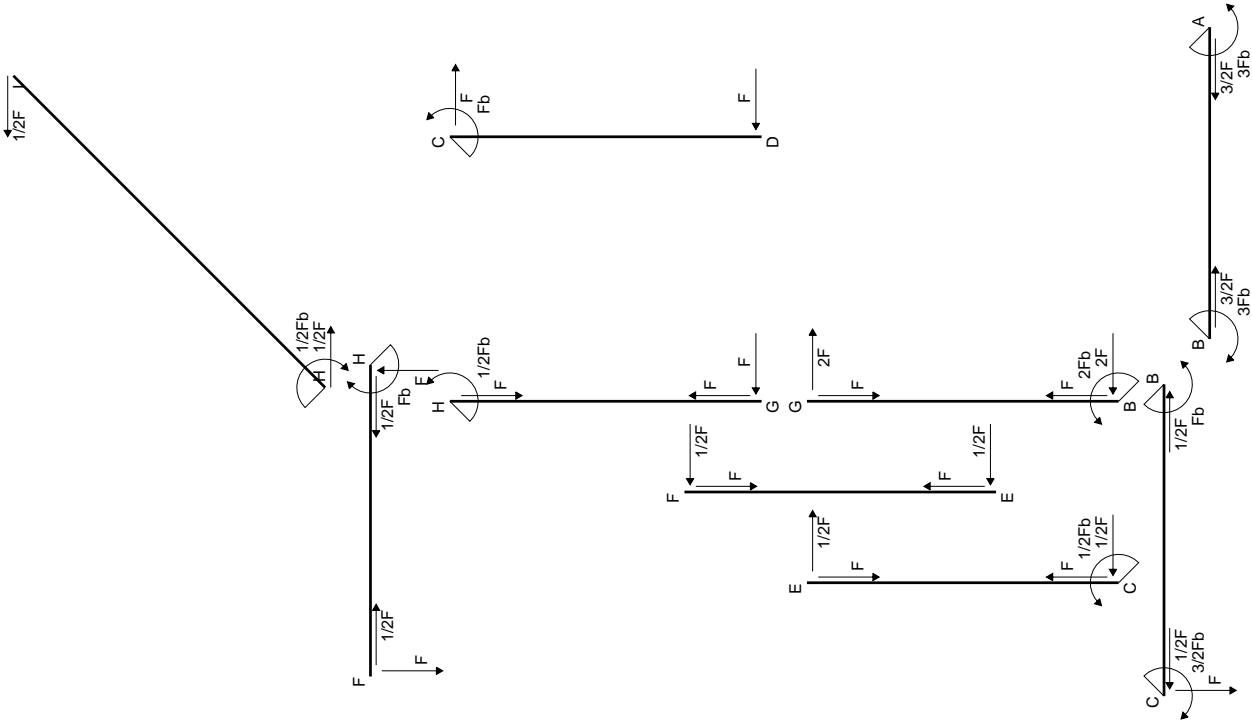
$-V_{BC} b + W_{BC} = 2Fb - 1/2qb^2$

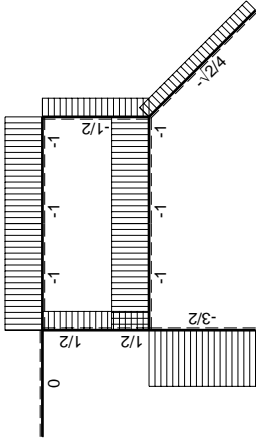
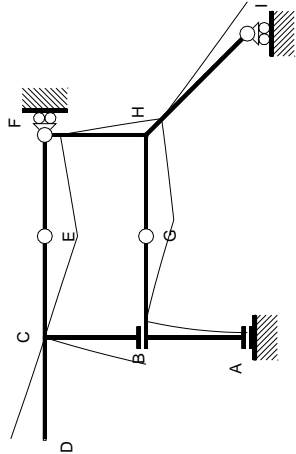
Matrice di equilibrio

$$\begin{bmatrix} H_F b & V_F b & V_{BC} b & W_{BC} \end{bmatrix} \begin{bmatrix} Fb & W & qb^2 \end{bmatrix}$$
$$u_A \begin{bmatrix} 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} -1 & 0 & -1 \end{bmatrix}$$
$$\varphi_{GB} \begin{bmatrix} -1 & 2 & -1 & 1 \end{bmatrix} = \begin{bmatrix} 2 & 1 & 3/2 \end{bmatrix}$$
$$\varphi_{FE} \begin{bmatrix} 0 & 0 & -2 & 1 \end{bmatrix} = \begin{bmatrix} 3 & 0 & -1 \end{bmatrix}$$
$$\varphi_{EC} \begin{bmatrix} 0 & 0 & -1 & 1 \end{bmatrix} \begin{bmatrix} 2 & 0 & -1/2 \end{bmatrix}$$

Soluzione del sistema

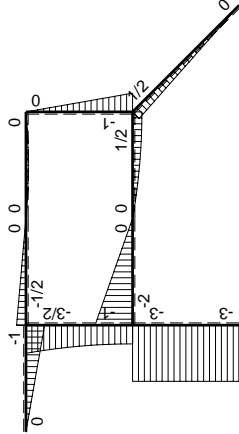
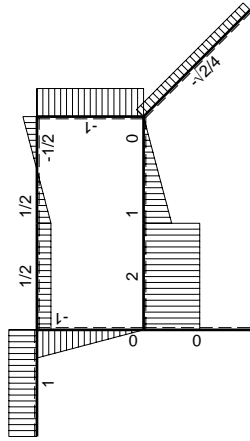
$$\begin{bmatrix} H_F b \\ V_F b \\ V_{BC} b \\ W_{BC} \end{bmatrix} = \begin{bmatrix} Fb & W & qb^2 \end{bmatrix} \begin{bmatrix} -1 & 0 & -1 \\ -1/2 & 1/2 & 1/2 \\ -1 & 0 & 1/2 \\ 1 & 0 & 0 \end{bmatrix}$$





10 Fb³/EJ

F



F

Fb