

Calcolare

$$\int_0^1 \frac{1}{\sqrt{x+x}} dx \quad \ln 4$$

$$\int_0^1 \ln x dx \quad -1$$

$$\int_0^{+\infty} \frac{1}{1+x^2} dx \quad \frac{\pi}{2}$$

$$\int_1^{+\infty} e^{-x} dx \quad \frac{1}{e}$$

$$\int_0^{+\infty} e^{-2x} \sin(e^{-x}) dx \quad \cos(1) - \sin(1)$$

$$\int_{-\infty}^0 \frac{1}{cosh^2 x} dx \quad 1$$

Stabilire se convergono

$$\int_0^1 \frac{\sin x}{x^3 \sqrt{x}} dx \quad \text{converge}$$

$$\int_0^{+\infty} \frac{\ln x}{(1+x)^2} dx \quad \text{converge}$$

$$\int_{-\infty}^0 \sin^2 x dx \quad \text{diverge}$$

$$\int_0^1 \frac{\sqrt{e^x - 1}}{(1+x)^3 \sqrt{x^2}} dx \quad \text{converge}$$

$$\int_0^1 \frac{\cosh x}{x^2} dx \quad \text{diverge}$$

$$\int_0^1 \frac{\ln(\cos x)}{x} dx \quad \text{converge}$$

$$\int_0^{+\infty} \tanh(x) dx \quad \text{diverge}$$

$$\int_1^{+\infty} e^{-x^2} dx \quad \text{converge}$$

$$\int_0^1 e^{x^{-1}} dx \quad \text{diverge}$$

$$\int_1^{+\infty} \frac{\cos x}{2\sqrt{x}} dx \quad \text{converge}$$

$$\int_1^{+\infty} \frac{1}{\sinh x} dx \quad \text{converge}$$

stabilire per quali valori del parametro $k > 0$ converge

$$\text{l'integrale improprio } \int_1^{+\infty} \frac{1}{\sqrt[5]{e^x - e}(x-1)^k} dx$$

converge se $k < \frac{4}{5}$

Considerata la funzione $f_k(x) = \frac{\sqrt{1+x} - \sqrt{x}}{x} e^{kx}$ stabilire per quali valori del parametro reale k converge $\int_1^{+\infty} f_k(x) dx$.

converge se $k \leq 0$

Considerata la funzione $f_k(x) = \frac{(\sinh x)^k}{e^{2x}-1}$ stabilire per quali valori del parametro reale k converge $\int_0^1 df_k(x)x$

converge se $k > 0$

Considerata la funzione $f_k(x) = \frac{e^{-x} + x - 1}{x^k (\sqrt{1+x^k} - 1)}$ stabilire per quali valori del parametro reale k converge $\int_0^{+\infty} f_k(x) dx$

converge se $\frac{4}{3} < k < \frac{3}{2}$