

* sequential system

4 flip flops:

- D FF $\begin{cases} \text{equation. (Characteristic eqn.)} \\ = \text{Next state eqn.} \end{cases}$
- SR FF - Transition Table
- T FF - Characteristic Table
- JK FF - Excitation Table
- State Diagram



Equations

$$\underline{\underline{D \text{ ff}}} \quad Q^* = Q(t+1) = D$$

S R FF

$$\underline{\underline{Q^* = S + R'Q}}$$

T FF

$$Q^* = T \oplus Q$$

JK FF

$$Q^* = JQ + K'Q$$

①

* Convert between 2 flip flops:

Construct a \triangle using \equiv .

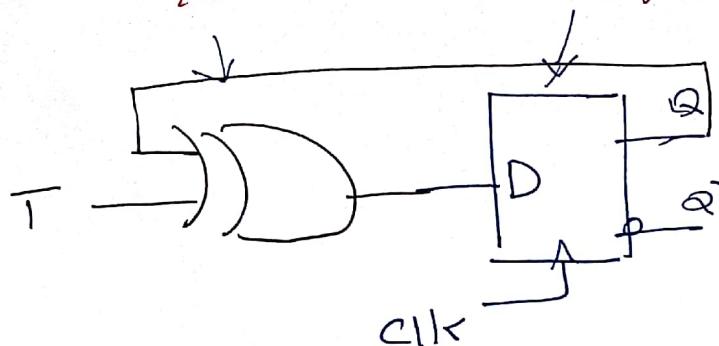


* Ex:

* Design a T^3FF using DFF ?

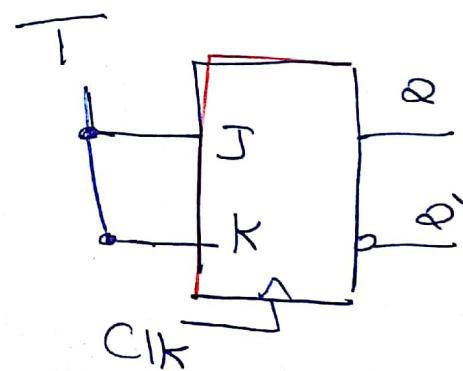
equ.

Design



A diagram consisting of two parts. The first part shows a rectangle with a horizontal arrow pointing to its right. The second part is a wavy line.

* Design a T flip-flop using JK flip-flop?



equ. of TFF $\Rightarrow Q^* =$

equ of Jkff \Rightarrow

$$T' = k' \Rightarrow T = k$$

$$T = \overline{J}$$

$$\boxed{T = K - J}$$

$$P^* = \underbrace{\int P'_r}_{\text{Part 1}} + \lambda,$$

$$Q^* = \textcircled{J} Q' + K' Q$$

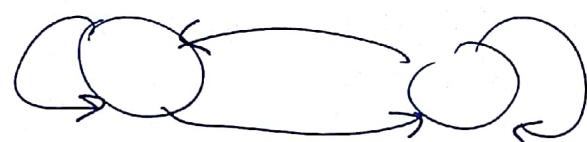
$$Q^* = JQ' + KQ$$

$$= \boxed{KQ} + JQ'$$

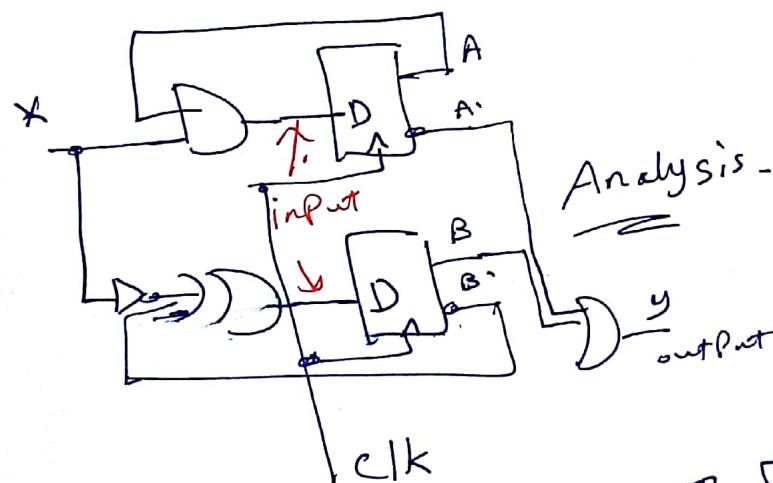
① \Rightarrow State Table

input	Current state		next state	output
	Q_1	Q_2		
x	Q_1	Q_2	Q_1^*	Q_2^*

② \Rightarrow State Diagram



③ \Rightarrow Block diagram.



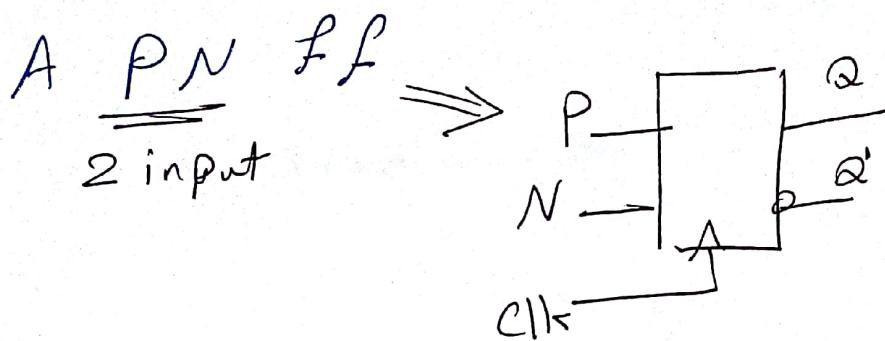
④ \Rightarrow equations
 → input equations
 → output eqn.
 → Next state equations.

ز ... ایجاد موجات و جعل جمله کوئی فکر نہیں دیجیں

③

⇒ How to build new FF?

↳ From "Revision file" Q 29



* Four operations:

	P	N
① clear to 0	0	0
② no change	0	1
③ complement	1	0
④ set to 1	1	1

a) Tabulate the Characteristic Table:

P	N		Q^*
0	0		0
0	1		Q
1	0		\bar{Q}
1	1		①

b) Derive Characteristic equation:

$$Q^* = \overline{Q} PN + \overline{Q} \overline{P} \overline{N} + P \overline{N}$$

↑ K-map

(4)

After
K-map

$$Q^* = PQ' + NQ$$

c) Tabulate the excitation Table:

Q	Q^*	P	N
0	0	0 X	①
0	1	1 X	②
1	0	X 0	③
1	1	X 1	④

①	Q	Q^*	P	N	
	0	0	0 0	0 0	Clear to 0
			0 1	1 0	No Change

0 X

②	Q	Q^*	P	N	
	0	1	1 1	1 1	Set to 1
			1 0	0 1	Complement

1 X

③	Q	Q^*	P	N	
	1	0	0 0	0 0	Clear to 0
			1 0	0 1	Complement

X 0

⑤

④

Q Q*

|

|

P N

o · |

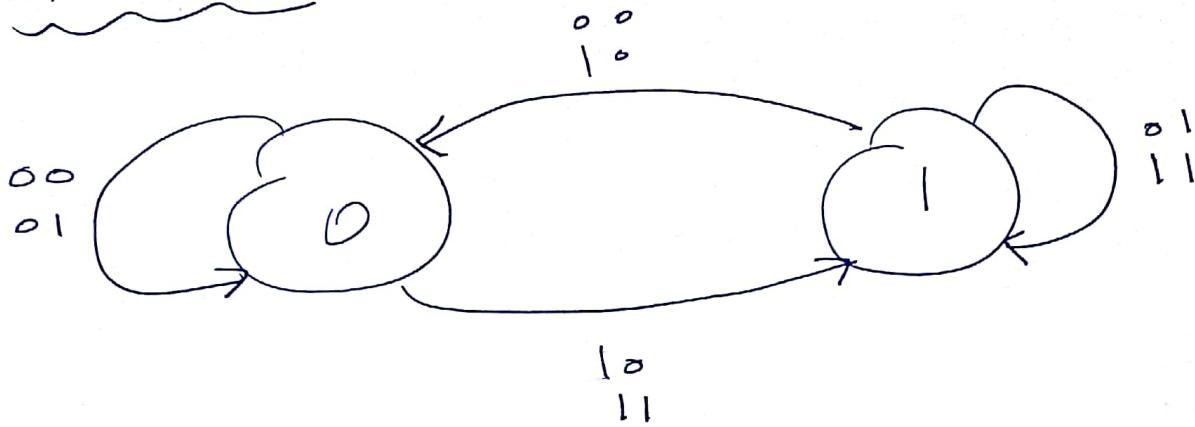
No charge

| |

set t_0

X I

* State Diagram

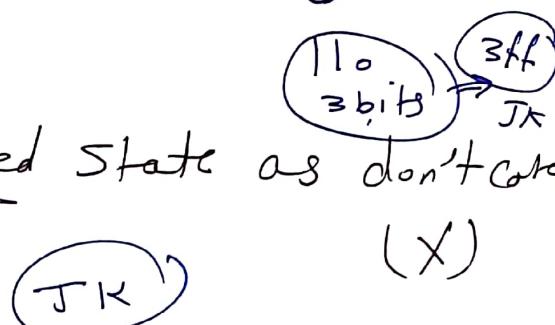


⑤

⇒ Counters with unused state? ex:

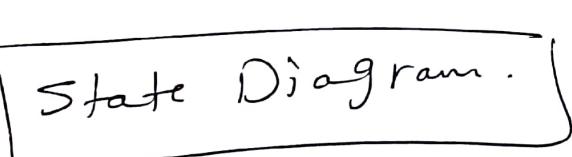
Ex.  → in "Revision file"

↳ sequence $0 \rightarrow 1 \rightarrow 2 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 0$

Manipulate the unused state as don't care
= 

Requirements ~~① Draw~~

② logic diagram.

③  to show the

effect of unused state.

Counter \Rightarrow M S T T
Modified State Transition Table

⑦

① Modified State Transition Table (MSTT)

input	current state			next state			flip flops inputs.					
	A	B	C	A*	B*	C*	J _A	K _A	J _B	K _B	J _C	K _C
0 → 0	0	0	0	0	0	1	0	x	0	x	1	x
0 → 0	0	0	1	0	1	0	0	x	1	x	x	1
0 → 1	0	1	0	1	0	0	1	x	x	0	x	
unused	0	1	1	x	x	x	x	x	x	x	x	x
	1	0	0	1	0	1	x	0	0	x	1	x?
	1	0	1	1	1	0	x	0	1	x	x	1
	1	1	0	0	0	0	x	1	x	x	0	x
	x	x	x	x	x	x	x	x	x	x	x	x
7 → 111												
unused												

↓

0 → 1 → 2 → 4 → 5 → 6 → 0

↑

② equation

$$J_A = \Sigma m(2) + \Sigma d(3-4, 5, 6, 7)$$

K_A

J_B

K_B

J_C

K_C

③ on K-map -

Excitation Table

		Q	Q*	JK.
0	0	0	x	0
0	1	1	x	1
1	0	x	1	0
1	1	x	0	0



After K-map

$$\rightarrow J_A = K_A = B$$

$$\rightarrow J_B = C$$

$$\rightarrow K_B = 1$$

$$\rightarrow J_C = B'$$

$$\rightarrow K_C = 1$$

(ii) next state equ. $Q_{JK}^* = J\bar{Q} + K\bar{Q}$

$$A^* = J_A \bar{A} + K_A A$$
$$= B \bar{A} + B' A$$

$$\boxed{A^* = B \oplus A}$$

$$B^* = J_B \bar{B} + K_B B$$
$$= C \bar{B}' + 0$$

$$\boxed{B^* = C B'}$$

$$C^* = J_C \bar{C} + K_C C$$
$$= B' \bar{C} + 0$$

$$\boxed{C^* = B' \bar{C}}$$

⑨

$$A^* = B \oplus A$$

$$B^* = CB'$$

$$C^* = B'C'$$

2 unused state.

	A^*	B^*	C^*	
$3 \rightarrow 011$	1	0	0	(4)
$7 \rightarrow 111$	0	0	0	(0)

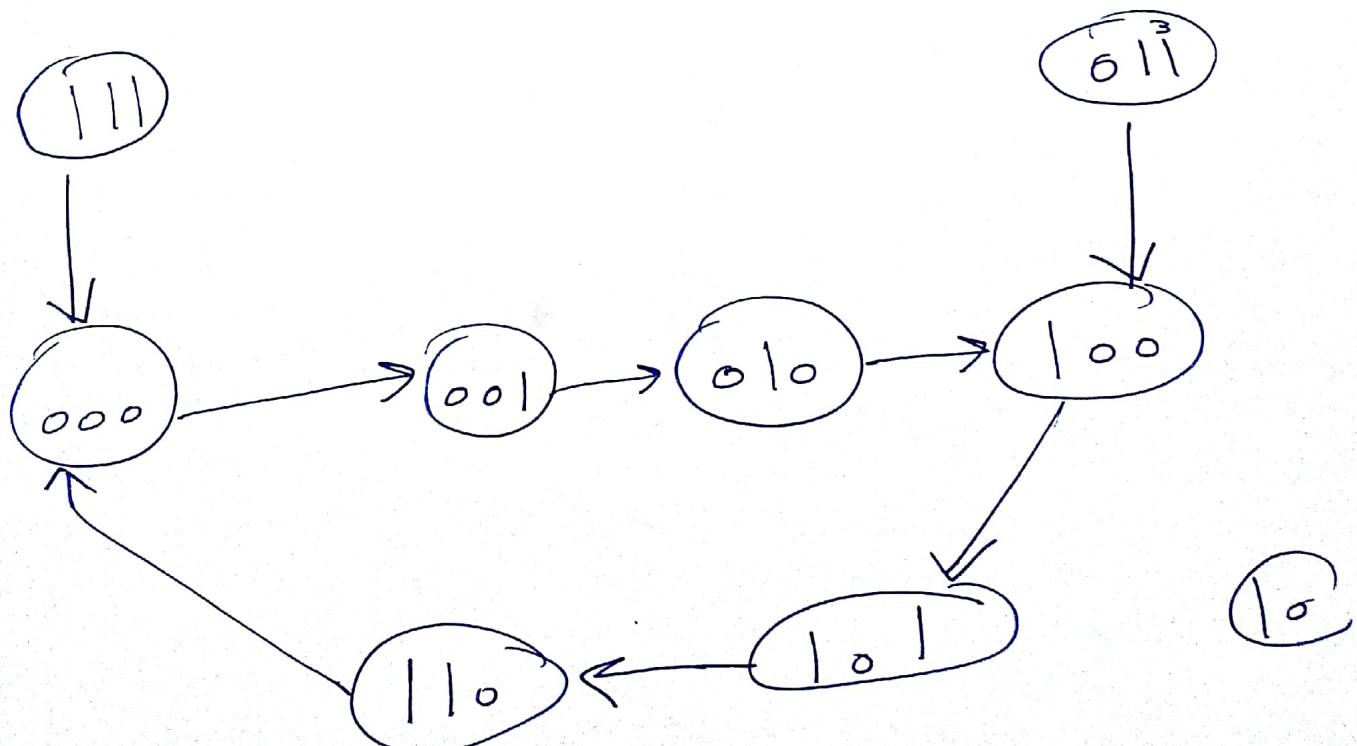
next state of $3 \rightarrow 4$ self ✓

next state of $7 \rightarrow 0$ ✓

self correcting.



* State Diagram.



* Logic Diagram or Block diagram

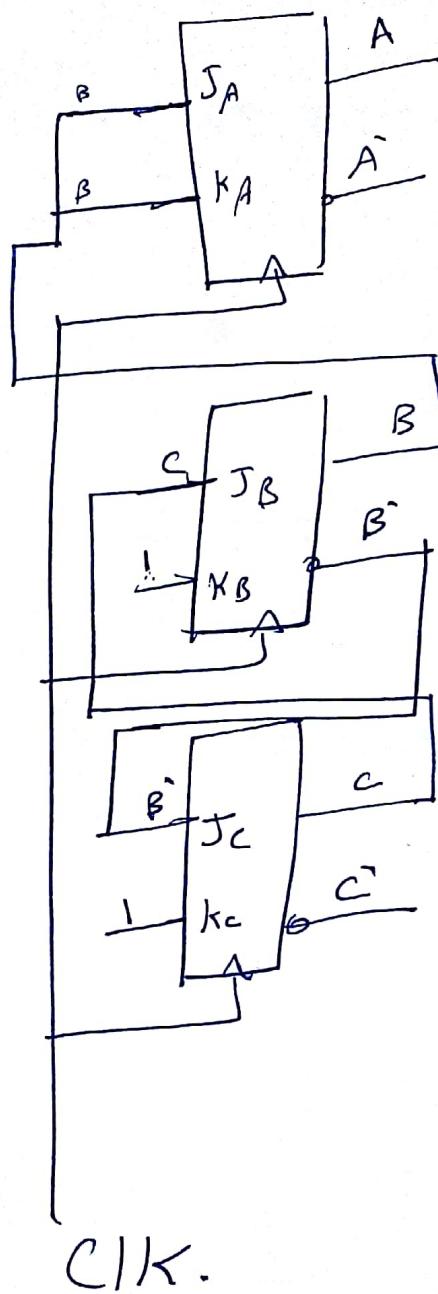
$$\rightarrow J_A = k_A = B$$

$$\rightarrow J_B = C$$

$$\rightarrow k_B = 1$$

$$\rightarrow J_C = \bar{B}$$

$$\rightarrow k_C = 1$$



Q33)

2 Tff A & B input X_{in}

① MSTT

input X_{in}	current state		next state $A^* B^*$	flip flops input	
	A	B		T_A	T_B
0	0	0	0 0	0	0
0	0	1	0 1	0	0
0	1	0	1 0	0	0
0	1	1	1 1	0	0
1	0	0	0 1	1	0
1	0	1	1 1	1	0
1	1	0	0 0	1	0
1	1	1	1 0	0	1

$\overbrace{00 \rightarrow 01 \rightarrow 11 \rightarrow 10}^A$ excitation Table of T

② equations.

$$T_A = \Sigma_m () = X(\bar{A}B + A\bar{B}) = X(A \oplus B)$$

$$T_B = \Sigma_m () = X(\bar{A}\bar{B} + A\bar{B}) + X(A \oplus B)$$

③ K-map - X

④ next state eqn.

$$A^* = T_A \oplus A$$

Q	Q^*	T
0	0	0
0	1	1
1	0	1
1	1	0

\Rightarrow logic Diagram
 \Rightarrow State diagram

⑫

Q 34)

Fib

* State Diagram (Given)

input

X

3 FF

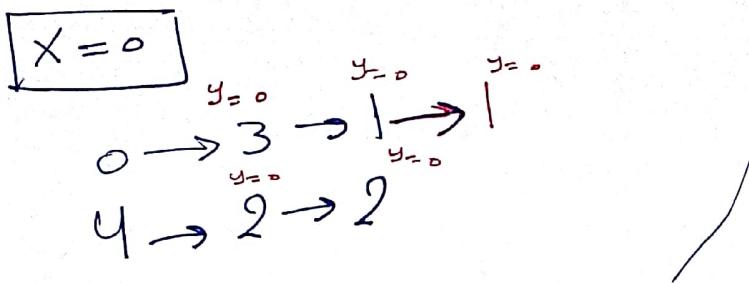
Toggle

3 TFF

output

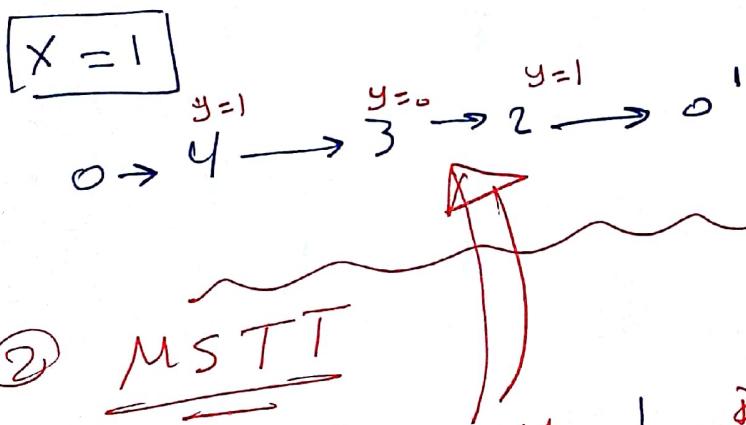
Y

① Sequence - From state diagram.



1, 2, 3, 4)

5, 6, 7
unused states.



wave excitation Table.

② MSTT

input x	current A B C			next A* B* C*			input of ff T ₁ T ₂ T ₃	FF	output y

T₁ T₂ T₃
en en en
↳ K.mel.

13

* From K-map:

$$T_A = A + X\bar{B}$$

$$T_B = A + \bar{X}\bar{B}\bar{C} + \bar{X}\bar{B}C + X\bar{B}\bar{C}$$

$$T_C = A + \bar{X}\bar{B}\bar{C} + XC$$

$$A^* = T_A \oplus A$$

$$(A + X\bar{B}) \oplus A$$

$$B^* = T_B \oplus B$$

$$= (\bar{A} + \bar{X}\bar{B}\bar{C} + \bar{X}\bar{B}C + X\bar{B}\bar{C}) \oplus B$$

$$C^* = T_C \oplus C$$

$$= (\bar{A} + \bar{X}\bar{B}\bar{C} + XC) \oplus C$$

⇒ The effect of unused states. (5, 6, 7)

	unused State			next state.		
	A	B	C	A^*	B^*	C^*
5 →	1	0	1	0	0	0
6 →	1	1	0	0	0	1
7 →	1	1	1	0	0	0

$$5 \rightarrow 2 \checkmark$$

$$6 \rightarrow 1 \checkmark$$

$$7 \rightarrow 0 \checkmark$$

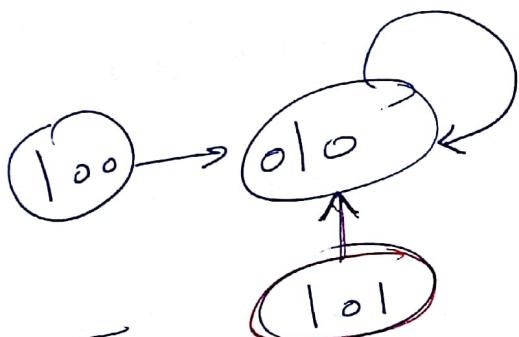
self correcting.

(14)

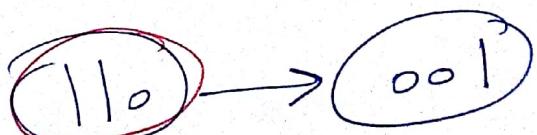
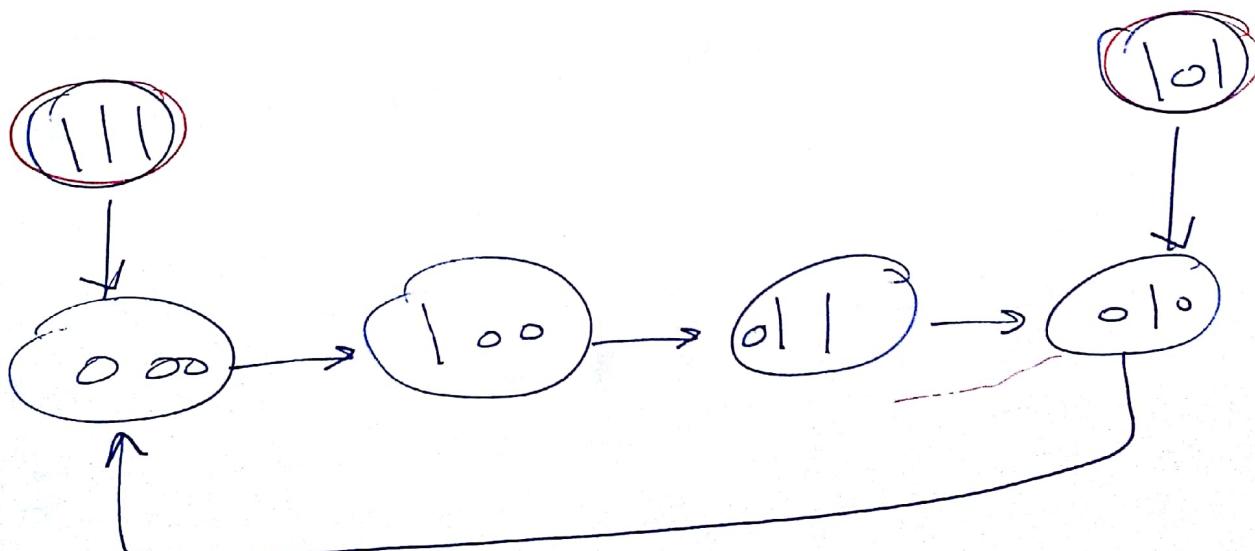
* State Diagram

$$X = 0$$

Meally State & Input
A, B, C & X
Moore
only on State
A, B, C



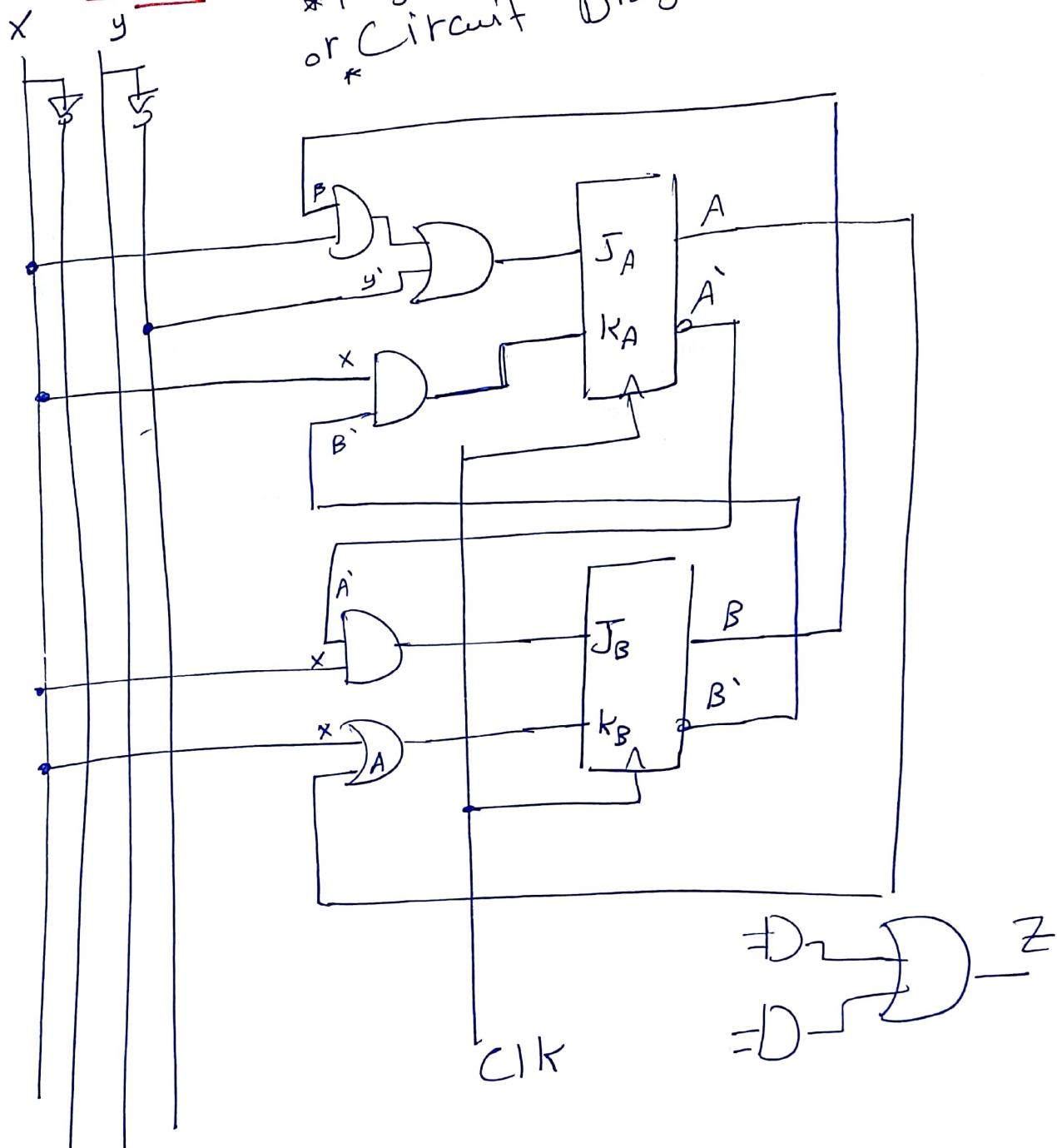
$$X = 1$$



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Q 35

① * logic Diagram
or Circuit Diagram / Block Diagram



② State Table

$$A^* = \bar{J}_A \bar{A}' + \bar{K}_A A$$

$$A^* = (\bar{B}x + y')\bar{A}' + (\bar{B}'x) \cdot A$$

B*

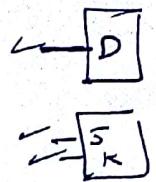
~~Q35~~

The solution is
in
"revision file"
Q 35.

⑯

Q6 in Final 2015:

* State Table is given:



- Find the input equations when using a D ff for A, JK ff for B.
- Find system output equ. (Z)
- Implement Design

↳ Block diagram

A NS.

a) MSTT (Modified State Transition Table)

input x	Current State		Next state		ff-input		output Z
	A	B	A*	B*	$Q^* = D_A$ $= A^*$	$J_B K_B$	
0	0	0	1	0	1	0 X	0
0	0	1	0	0	0	X 1	1
0	1	0	0	1	0	1 X	1
0	1	1	1	0	1	X 1	1
0	1	1	0	0	0	0 X	0
1	0	0	0	0	1	X 0	1
1	0	1	1	1	1	1 X	1
1	1	0	1	0	0	X 0	1
1	1	1	0	1	1	X 1	1

From excitation table.

* Excitation Table for JK:

Q	Q^*	JK	
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

Equations

$$DA = \Sigma_m(0, 3, 5, 6)$$

$$JB = \Sigma_m(2, 6) + \Sigma_d(1, 3, 5, 7)$$

$$KB = \Sigma_m(1, 3) + \Sigma_d(0, 2, 4, 6)$$

$$Z = \Sigma_m(1, 2, 3, 5, 6, 7)$$

PA

	X_A	\bar{X}_A	X_A	\bar{X}_A	X_A	\bar{X}_A
B	0	1	2	3	4	5
\bar{B}	1	0	1	0	1	0

$$\begin{aligned}
 DA &= X_A \bar{B} + \bar{X}_A B + X_A B + \bar{X}_A \bar{B} \\
 &= X(A \oplus B) + X(A \oplus B) \\
 &= (X \oplus A \oplus B)
 \end{aligned}$$

$$[J_B] = A$$

	X_A	X_A'	X_A	X_A	X_A'
B	0	2	6	1	4
B'					
B	X	X	X	X	X
	1	3	7	5	8

$K_B = X'$

	X_A	X_A'	X_A	X_A	X_A'
B	0	2	6	4	
B'					
B	X	X	X	X	X
	1	3	7	5	8

$$Z = B + A$$

	X_A	X_A'	X_A	X_A	X_A'
B	0	2	6	1	4
B'					
B	X	X	X	X	X
	1	3	7	1	5



* input equations.

$$PA = \underline{X \oplus A \oplus B}$$

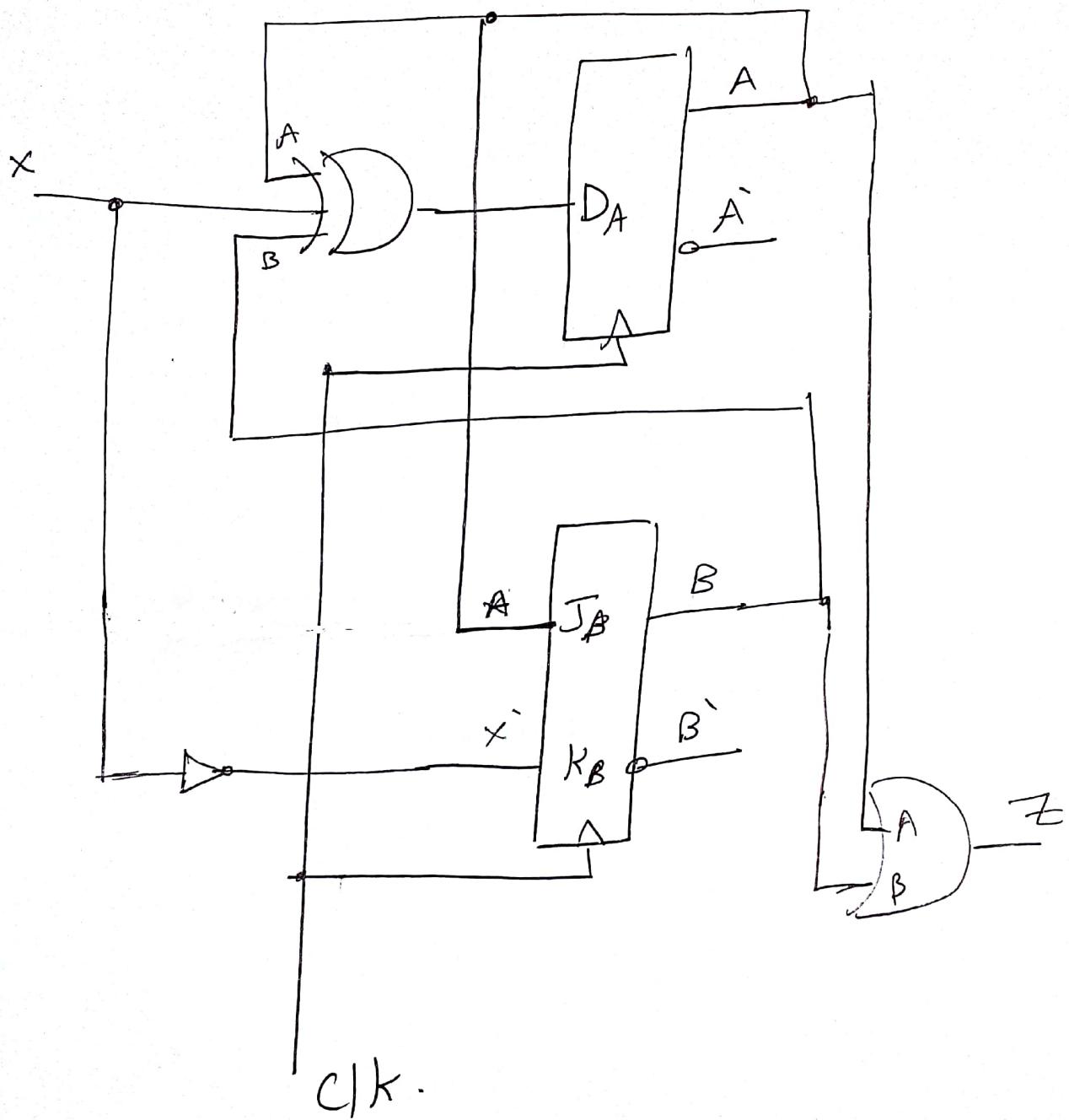
$$K_B = \underline{X'}$$

$$J_B = \underline{A}$$

* output equations.

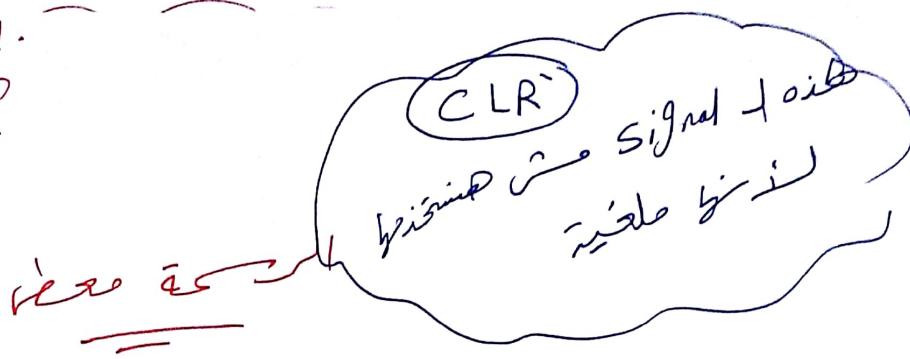
$$Z = B + A$$

* Block diagram:



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Q6) 2016



a) Build State Table.

b) Complete ^{The} Timing diagram. (A & B are initially zero)

① State Table.

$$J_A = \bar{X} A' \quad , \quad K_A = B' \\ J_B = A \quad , \quad K_B = (A' \oplus X)'$$

$$A^* = J_A \bar{A}' + K_A A \\ = \bar{X} \bar{A}' + B A$$

$$B^* = J_B \bar{B}' + K_B B \\ = A \bar{B}' + (A' \oplus X) B$$

$$\begin{array}{c} X = 0 \\ \hline A^* = \bar{A}' + B A \\ = \boxed{\bar{A}' + B} \end{array}$$

$$B^* = A \bar{B}' + A B \\ = \boxed{A \oplus B}$$

$$\begin{array}{c} X = 1 \\ \hline A^* = \boxed{A B} \end{array}$$

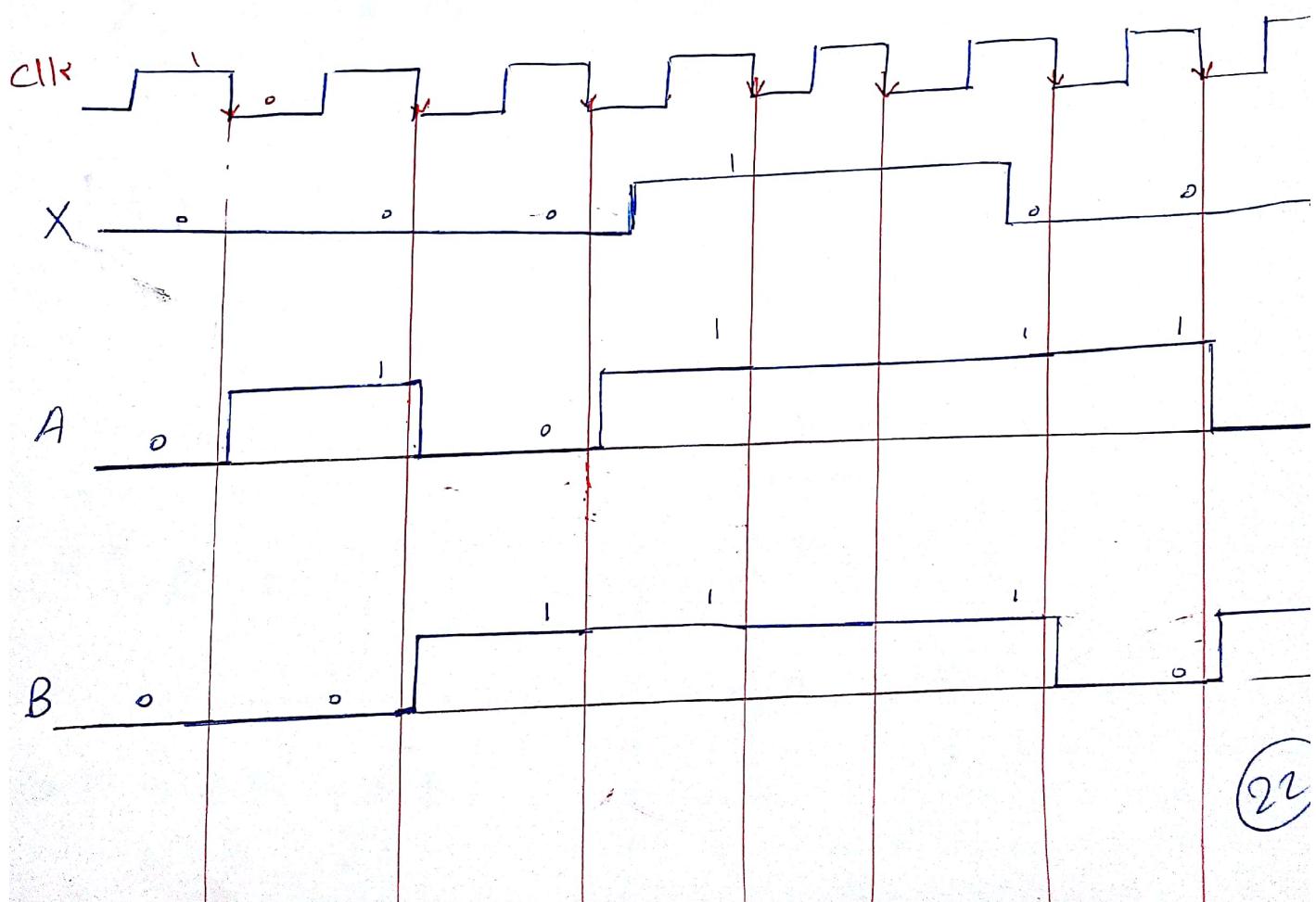
$$\begin{aligned} B^* &= A \bar{B}' + A B \\ &= A(B' + B) \\ &= \boxed{A} \end{aligned}$$

(21)

* State Table

Input X	Current State		Next state	
	A	B	A*	B*
0	0	0	1	0
0	0	1	1	1
0	1	0	0	1
0	1	1	1	0
0	0	0	0	0
0	1	0	0	0
1	0	0	0	1
1	1	1	1	1

⇒ Timing Diagram



Q6) Final 2017

Block diagram is given

⇒ Complete Timing Diagram

(Positive edge)

$Q_a \rightarrow$ (enabled), $Q_b \rightarrow$ edge trigger high.



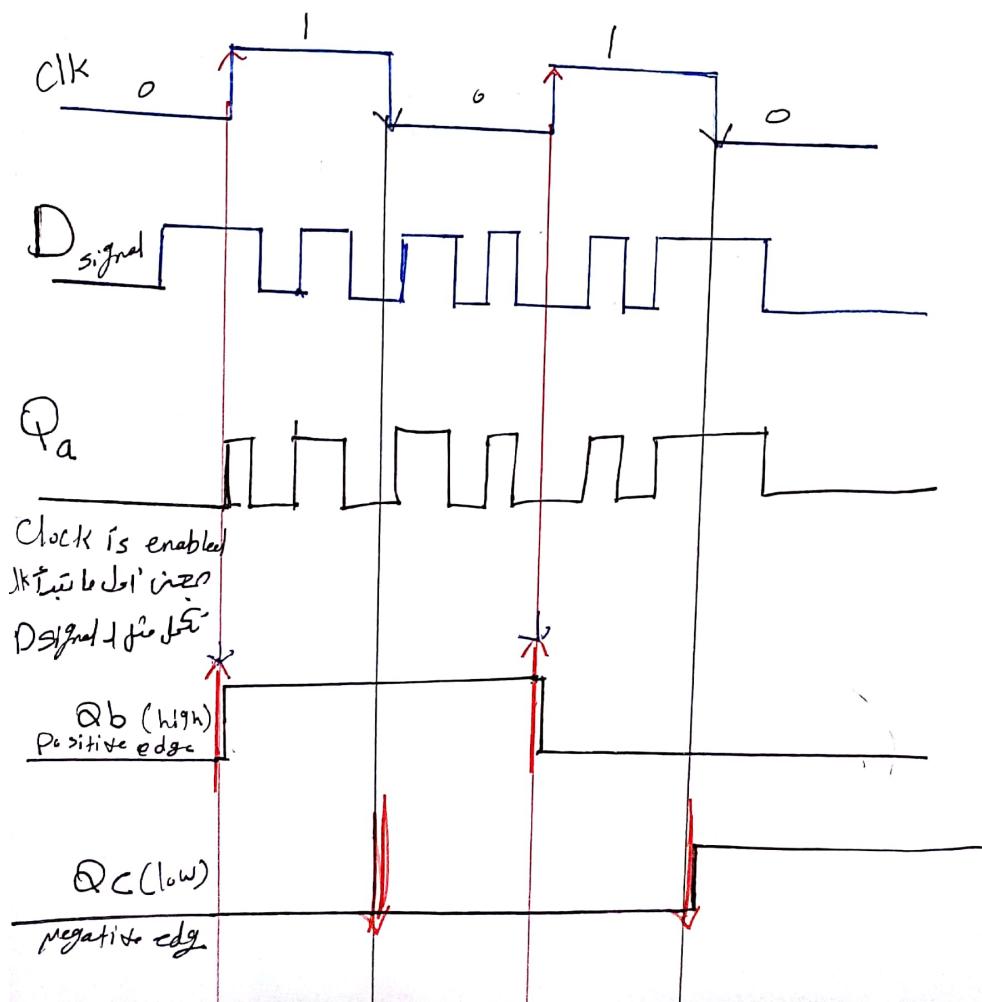
$Q_c \rightarrow$ edge trigger low



(Negative edge)

$$Q^* = D$$

* Timing Diagram



23

Q5) 2017)

→ the sequence $2 \rightarrow 6 \rightarrow 1 \rightarrow 7 \rightarrow 5$ & Repeat

using Tff

$7 \Rightarrow 111$
3 bits
3 Tff

① is it self-started?

M S T T Inputs of ff

Current			next			flip flop inputs		
A	B	C	A^*	B^*	C^*	T_A	T_B	T_C
0	0	0	x	x	x	x	x	x
0	0	1	1	1	1	1	1	0
0	1	0	1	1	0	1	0	0
0	1	1	x	x	x	x	x	x
0	1	1	x	x	x	x	x	x
1	0	0	x	x	x	1	1	1
1	0	1	0	1	0	1	1	1
1	1	0	0	0	1	1	1	1
1	1	1	1	0	1	0	1	0

$$T_A = \sum_m (1, 2, 5, 6) + \sum_d (0, 3, 4)$$

$$T_B = \sum_m (1, 5, 6, 7) + \sum_d (0, 3, 4)$$

$$T_C = \sum_m (5, 6, 7) + \sum_d (0, 3, 4)$$

(24)

on k.m.

$$T_A = \bar{B} + \bar{C}$$

	$A\bar{B}$	$\bar{A}\bar{B}$	$\bar{A}B$	$A\bar{B}$	$A\bar{B}'$
C	0	2	3	4	
\bar{C}	X	1	1	X	
C	1	3	X	7	5

$$T_B = C + A$$

X		1	X
1	X	1	1

$$T_C = A\bar{C} + A\bar{B}$$

X		1	X
	X		1

$$\begin{aligned} A^* &= T_A \oplus A \\ &= (\bar{B} + \bar{C}) \oplus A \end{aligned}$$

$$\begin{aligned} B^* &= T_B \oplus B \\ &= (C + A) \oplus B \end{aligned}$$

$$\begin{aligned} C^* &= T_C \oplus C \\ &= (A\bar{C} + A\bar{B}) \oplus C \\ &= [A(\bar{C} + \bar{B})] \oplus C \end{aligned}$$

(B)

* unused state

	A	B	C		A*	B*	C*
0 →	0	0	0		1	0	0 →
3 →	0	1	1		0	0	1
4 →	1	0	0		0	1	1

0 → 4 X
3 → 1 ✓
4 → 3 X

isn't self started

(25)

A)
⇒ Design a synchronous Counter

Q5
2017

Ans

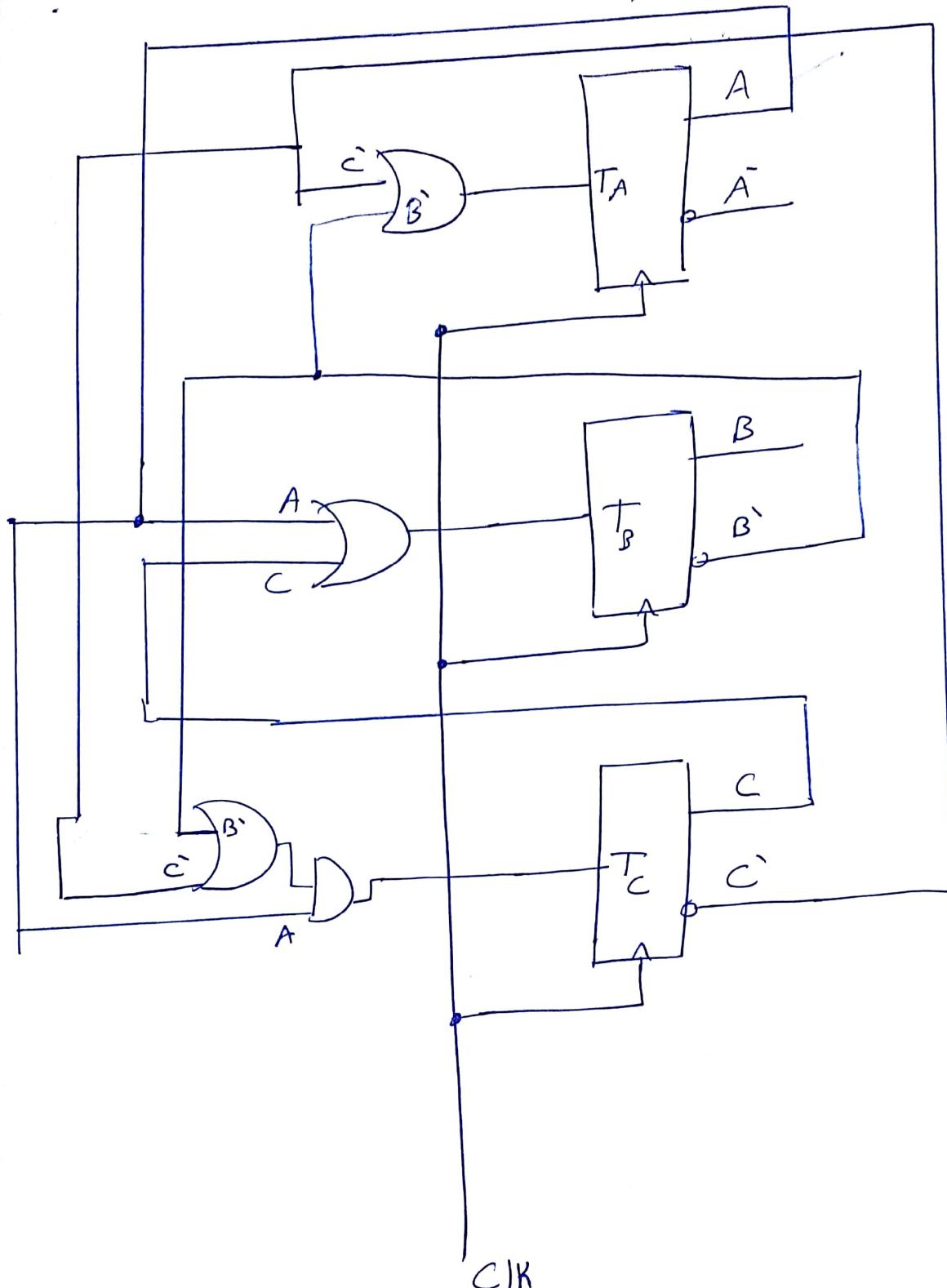
2 6 1 7 5

$$A = \overline{B} + \overline{C}$$

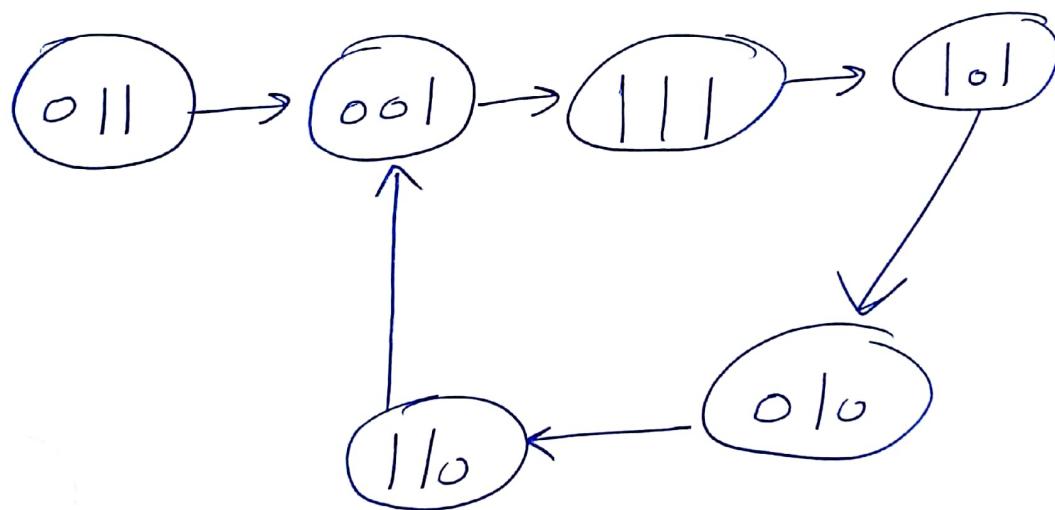
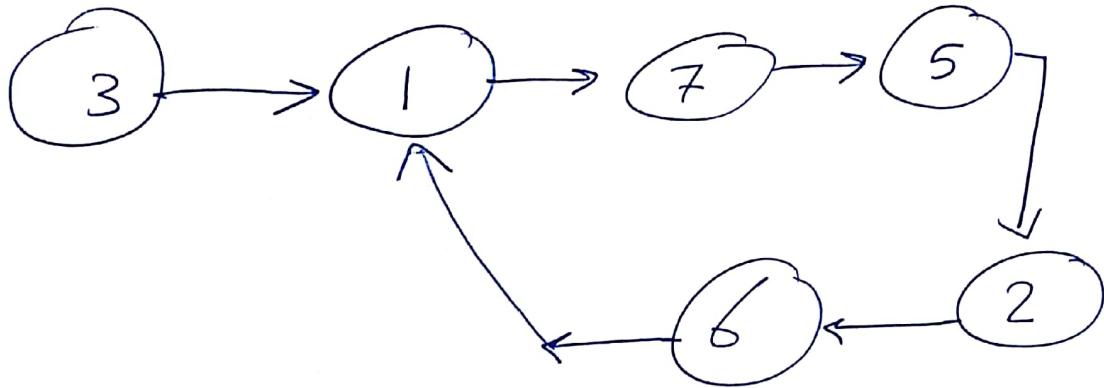
$$T_A = \overline{B} + \overline{C}$$

$$T_B = C + A$$

$$T_C = A(C + \overline{B})$$



(26)



c) State Diagram

(27)