

Logical Operations

3 operation.

AND

OR

XOR

AND (فرب)

$$\begin{array}{r} 00 \\ \text{AND } 00 \\ \hline 00 \end{array}$$

$$\begin{array}{r} 01 \\ \hline 00 \end{array}$$

$$\begin{array}{r} 10 \\ \hline 00 \end{array}$$

$$\begin{array}{r} 11 \\ \hline 11 \end{array}$$

فرب = فرب

OR

(+ كذا)

$$\begin{array}{r} 00 \\ \text{OR } 00 \\ \hline 00 \end{array}$$

$$\begin{array}{r} 01 \\ \hline 01 \end{array}$$

$$\begin{array}{r} 10 \\ \hline 10 \end{array}$$

$$\begin{array}{r} 11 \\ \hline 11 \end{array}$$

أى واحد = 1

XOR

(Complement)

$$\begin{array}{r} \boxed{00} \\ \text{XOR } \boxed{00} \\ \hline 00 \end{array}$$

$$\begin{array}{r} 01 \\ \hline 10 \end{array}$$

$$\begin{array}{r} 10 \\ \hline 01 \end{array}$$

$$\begin{array}{r} \boxed{11} \\ \hline 00 \end{array}$$

المختلف = 1
المساوي = 0

~~XOR~~
AND

$$\begin{array}{r} \text{AND} \\ \begin{array}{cccccccc} 1 & 1 & 0 & 0 & 1 & 0 & 1 & 1 \\ 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 \end{array} \\ \hline 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{array}$$

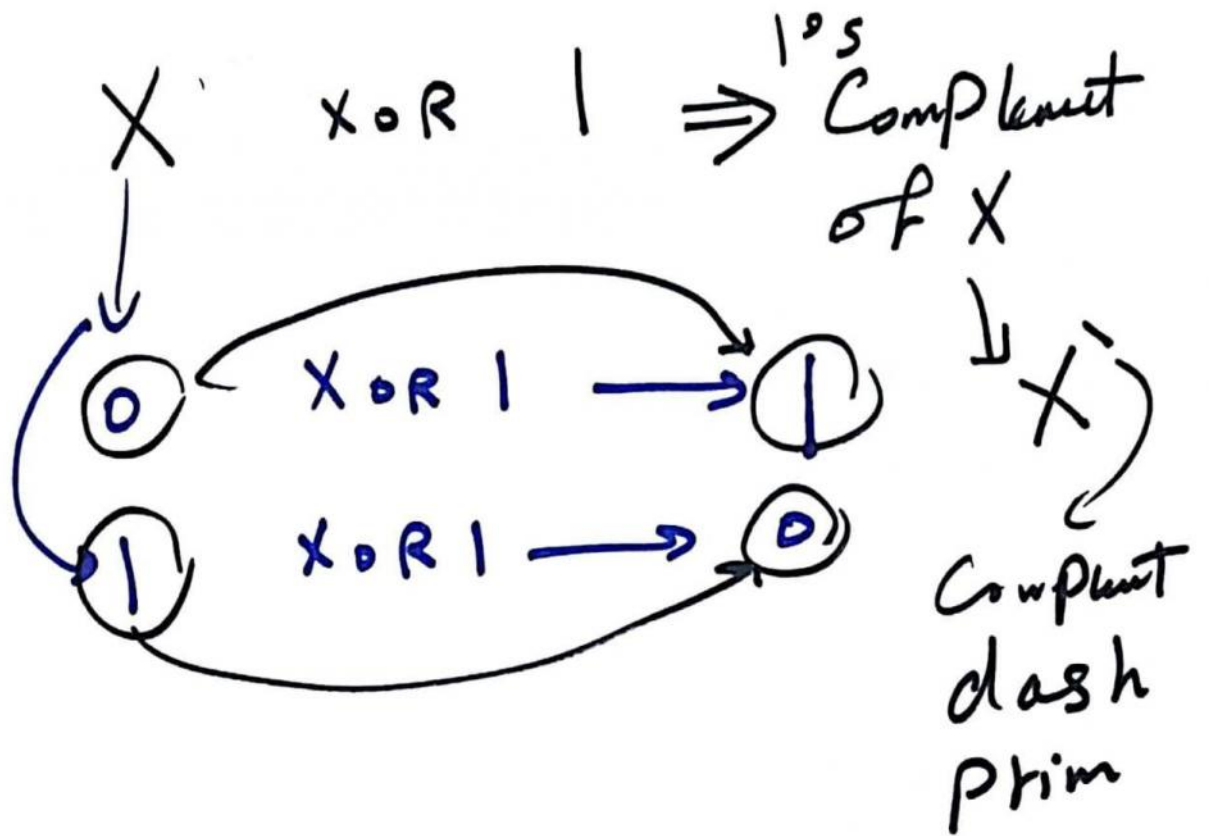
~~~~~

$$\begin{array}{r} \text{OR} \\ \text{OR} \\ \begin{array}{cccccccc} 1 & 1 & 0 & 0 & 1 & 0 & 1 & 1 \\ 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 \end{array} \\ \hline 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \end{array}$$

~~~~~

$$\begin{array}{r} \text{XOR} \\ \text{XOR} \\ \begin{array}{cccccccc} 1 & 1 & 0 & 0 & 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 \end{array} \\ \hline 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 \end{array}$$

المساوية = 0
المتفاوتة = 1



$$\begin{aligned}
 Y \text{ XOR } 1 &\rightarrow Y' \\
 Z \text{ XOR } 1 &\rightarrow Z'
 \end{aligned}$$

X	XOR	0
1	XOR 0	1
0	XOR 0	0

AND

8
AND

R R R
0 1 2
↓

$$R_0 = R_1 \text{ AND } R_2$$

OR

7
OR

R R R
1 2 4
↓

$$R_1 = R_2 \text{ OR } R_4$$

XOR

9
XOR

R R R
3 5 6
↓

$$R_3 = R_5 \text{ XOR } R_6$$

logical masks. / filters.

X X X X y y y y ← 8 bits

AND F 0
 | | | | 0 0 0 0
 └──────────┘
 mask

← Operation
X X X X 0 0 0 0 ← Result

The operation will be AND with
the mask (11110000) = (F0)₁₆

X X X X y y y y
XOR 0 0 0 0 y y y y

X X X X 0 0 0 0

← 4 bits
The first 4 bits = 0

$$\begin{array}{r}
 \begin{array}{ccccccccc}
 \underline{x} & \underline{x} & & \underline{x} & \underline{x} & & \underline{y} & \underline{y} & \underline{y} & \underline{y} \\
 & & & \underbrace{\hspace{1cm}} & & & & & \underbrace{\hspace{1cm}} & \\
 & & & 3 & & & & & c & \\
 \text{OR} & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & \\
 \hline
 \underline{x} & \underline{x} & 1 & 1 & 1 & 1 & y & y & &
 \end{array}
 \end{array}$$

operation \Rightarrow OR with the mask $(3c)_{16}$

the middle four bits = 1

most significant

$$\begin{array}{ccccccccc}
 \boxed{xx} & x & x & y & y & \boxed{yy} & & & \text{least signif.} \\
 \hline
 \text{XOR} & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 1 \\
 \hline
 \underline{x} & \underline{\cancel{x}} & \underline{\cancel{x}} & x & y & y & \underline{y} & \underline{y} &
 \end{array}$$

The most significant 2 bits & the least significant 2 bits are complemented.

x x x x y y y y

AND

1 1 1 0 0 1 1 1

x x x 0 0 y y y

0 1 1 0 0 1 1 0

x 1 1 0 0 1 1 y

XOR

1 0 0 0 0 0 0 1

x' 1 1 0 0 1 1 y'

	x	x	x	x	y	y	y	y
OR	0	1	1	1	1	1	1	0

x	1	1	1	1	1	1	1	y
--------------	---	---	---	---	---	---	---	---

XOR	1	0	0	0	1	0	0	1
-----	---	---	---	---	---	---	---	---

x'	1	1	0	0	1	1	y'
----	---	---	---	---	---	---	----

(x')	1	1	0	0	1	1	(y')
------	---	---	---	---	---	---	------

1 ← OR - *مجموع*

EX:

a) What is the mask with what operation that must be used to make the middle 4 bits of eight bits string as it & the other bits are 0's?

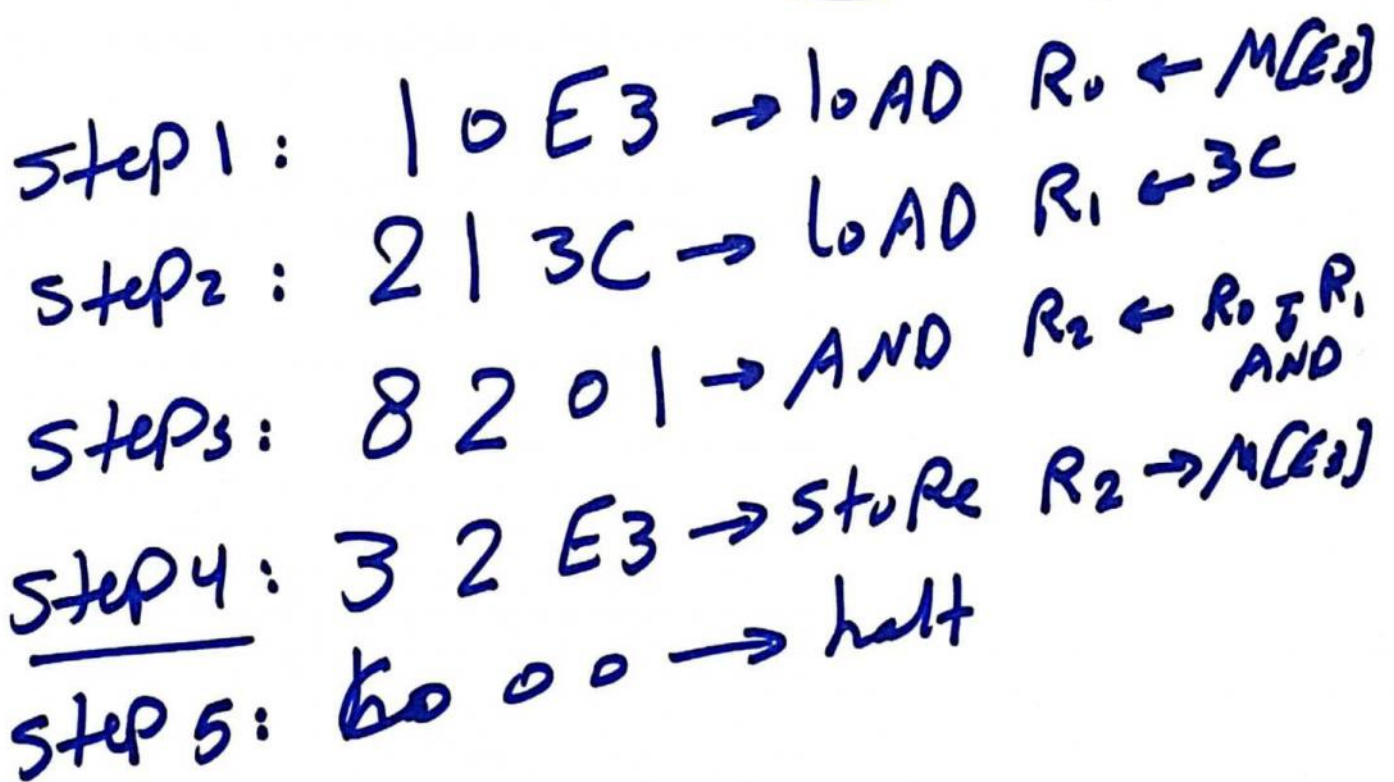
AND operation

	X	X	X	X	Y	Y	Y	Y	$\leftrightarrow R_0$
				1	1	1	1	0	$\leftrightarrow R_1$
	0	0							
	0	0	X	X	Y	Y	0	0	

→ We will use "AND" operation with the mask $\rightarrow (3c)_{16}$

b) Write the program that make this if the number is in

$M[E3]$



Step 1: 10E5 → LOAD R₁ ← 3C
Step 2: 213C → LOAD R₂ ← R₁

step₂: 213C → CONT
step₃: 8201 → AND $R_2 \leftarrow R_0 \text{ AND } R_1$
step₄: 4000 → M[0] $R_2 \rightarrow M[0]$

steps: 0 2 1
step 4: 3 2 E3 → store R2 → M[E3]
halt

step 4: 3 2 1
step 5: 0 0 0 → halt

*Write a machine Language Program That:
 Combines the most Significant four
 bits of the memory cell whose address
 is B_1 with the low significant
 4 bits of the memory cell B_2 and
 put the Result in memory cell whose
 Address is B_3 ?

$M[B_1] \rightarrow$	<u>most signi.</u>	<u>yyyy</u>
	<u>xxxx</u>	
$M[B_2] \rightarrow$	aaaa	<u>low sign.</u>
		<u>bbbb</u>
$M[B_3] \leftarrow$	xxxx	bbbb

$M[B_1]$ $\boxed{X\ X\ X\ X}$ $y\ y\ y\ y \leftarrow R_0$
 AND $\begin{array}{cccc|c} 1 & 1 & 1 & 1 & F \end{array}$ $0\ 0\ 0\ 0 \leftarrow R_1$

 $R_2 \leftarrow X\ X\ X\ X\ 0\ 0\ 0\ 0 \leftarrow$

$M[B_2]$ $a\ a\ a\ a$ $b\ b\ b\ b \leftarrow R_3$
 AND $\begin{array}{cccc|c} 0 & 0 & 0 & 0 & F \end{array}$ $1\ 1\ 1\ 1 \leftarrow R_4$

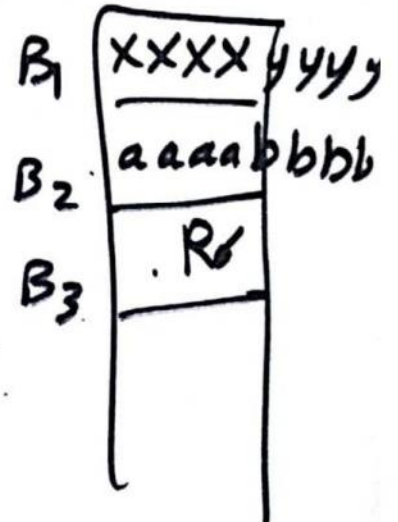
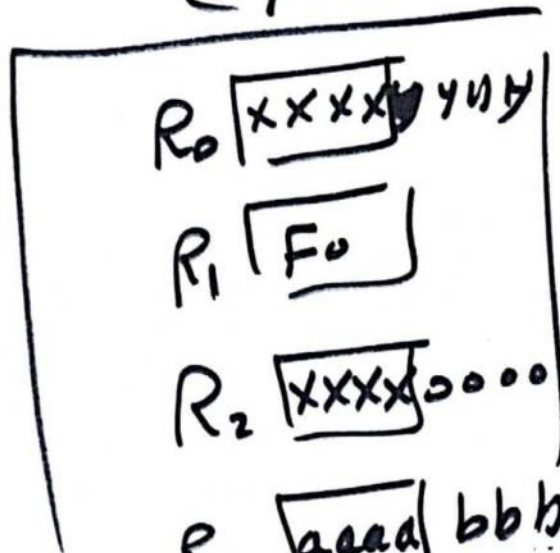
 $R_5 \leftarrow 0\ 0\ 0\ 0\ b\ b\ b\ b \leftarrow$

$R_2 \rightarrow X\ X\ X\ X\ 0\ 0\ 0\ 0 \leftarrow$
 OR $0\ 0\ 0\ 0\ b\ b\ b\ b \leftarrow$

 $R_5 \rightarrow$

$M[B_3]$ $X\ X\ X\ X\ b\ b\ b\ b$

CPU



- 1) load $R_0 \leftarrow M[B_1] \rightarrow$ | 0 B1
 - 2) load $R_1 \leftarrow F_0 \rightarrow$ 2 | F0
 - 3) AND $R_2 \leftarrow R_0, R_1 \rightarrow$ 8 201
 - 4) load $R_3 \leftarrow M[B_2] \rightarrow$ | 3 B2
 - 5) load $R_4 \leftarrow 0F \rightarrow$ 2 40F
 - 6) AND $R_5 \leftarrow R_3, R_4 \rightarrow$ 8 534
 - 7) OR $R_6 \leftarrow R_2, R_5 \rightarrow$ 7 625
 - 8) store $R_6 \rightarrow M[B_3] \rightarrow$ 3 6 B3
 - 9) halt \rightarrow
- C o o o

Shifting.

Shift to Right
(\div)

EX. shift (100) to the Right

1. Location.

$$\begin{array}{r} 4 \qquad 2 \\ 100 \div 10 \\ \hline = 10 = (2)_{10} \end{array}$$

1- Location means $2^1 \div 2$

2- location means $2^2 \Rightarrow 4 \div 4$

3- location means $2^3 \Rightarrow 8 \div 8$

Examples:

EX1

shift to Right (3- location)

$$1000 \div 1000 = 10$$

EX2

shift to Right (2- location)

$$10100 \div 100 = 101$$

Shift to Left
(\times)

EX. shift (101) to the left
1. location.

$$\begin{array}{r} 101 \\ \leftarrow 5 \times 10^2 \\ = 10100 = (10)_{10} \end{array}$$

1. location means $2^1 \times 2$

2. Location means $2^2 \times 4$

3. Location means $2^3 \times 8$

EX3

shift to left (2- locat)

$$100 \times 100 = 10000$$

EX4

shift to left (3 Location)

$$1110 \times 1000 = 1110000$$

EX5

Shift to Right

$$100.10 \div 10$$

↓
(1-location)

$$= 10.0$$

EX6

Shift to Right (2-location)

$$1100.100 \div 100$$

↓ ↘
(2-location)

$$= 11.00$$

EX7

Shift to left

$$11.10 \times 100$$

↓ ↙
(2-Location)

$$= 1110.00$$

Rotate operation\$

Left Rotate

Called Circular Left shift

EX:

Perform a rotation operation 2-Location to the left for the number :

(10110110)

نحن أننا نحرك (2 bits) من اليمين ونضعهم بنفس الترتيب.

⇒ 11011010

Right Rotate

Called Circular Right shift

EX:

Perform a rotation operation 3-Locations to the Right

For (11101001)

نحن أننا نحرك (3 bits) من اليمين

من اليسار ونضعهم بنفس الترتيب في أماكنهم.

⇒ 00111101

The Rotate instruction \Rightarrow "A"

Right Rotate \leftarrow A 5 0 1
 \nwarrow \swarrow
 R₅ (1-Location)

\hookrightarrow This instruction makes Right Rotate \Rightarrow (1-bit)
For the Content* in Register 5.
and Puts the Result in the same Register (R₅)

EX

\hookrightarrow If R₅ = E3

\hookrightarrow After execution of the ~~the~~ instruction A501,
What is the ^{Value} Content in R₅?

Ans.

R₅ = (E3)₁₆ \leftarrow Right Rotate (1-Location)

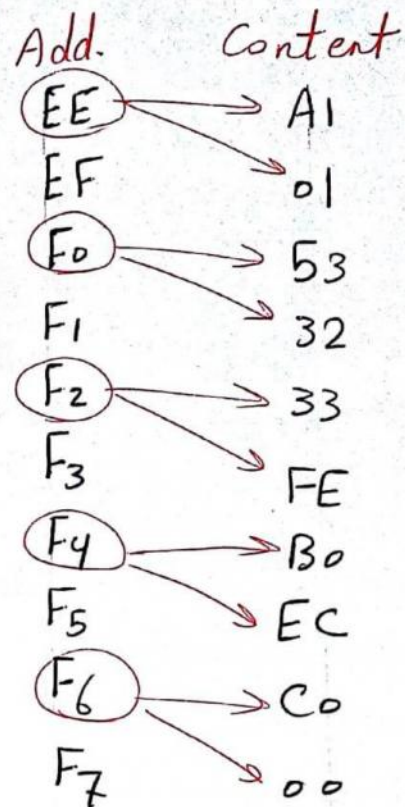
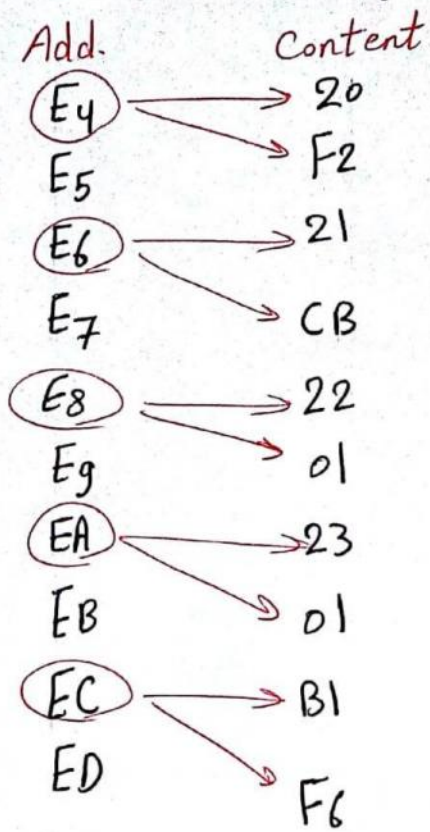
\Downarrow
A 1 1 1 0 0 0 1 1

1 1 1 1 0 0 0 1

F 1

R₅ will have the Value (F1)

* Suppose the memory cells at addresses (E4) to (F7) contain the following program:



Instruction Table

Start Address	Instruction	Meaning.
E4	20F2	LOAD $R_0 \leftarrow F2$
E6	21CB	LOAD $R_1 \leftarrow CB$
E8	2201	LOAD $R_2 \leftarrow 01$
EA	2301	LOAD $R_3 \leftarrow 01$
EC	B1F6	JUMP to M[F6] if $R_1 \leq R_0$
EE	A101	Right Rotate for R_1 (1-location)
F0	5332	Add $R_3 \leftarrow R_3 + R_2$
F2	33FE	Store $R_3 \rightarrow M[FE]$
F4	B0EC	JUMP to M[EC] if $R_0 = R_0$ (unconditional jump)
F6	C000	halt/stop.

Trace Table

Start Address	Trace	M[FE] <u>02</u> <u>03</u>	R ₀ F ₂	R ₁ CB E5 F ₂	R ₂ 01	R ₃ <u>01</u> <u>02</u> 03
E ₄	R ₀ = F ₂					
E ₆	R ₁ = CB					
E ₈	R ₂ = 01					
E _A	R ₃ = 01					
E _C	if ^{CB} R ₁ = ^{F₂} R ₀ X					
E _E (Rotate)	R ₁ = CB = $\begin{array}{ccccccc} 1 & 1 & 0 & 0 & 1 & 0 & 1 \\ \hline 1 & 1 & 0 & 0 & 1 & 0 & 1 \end{array}$					
F ₀	R ₃ = ⁰¹ R ₃ + ⁰¹ R ₂ = 02					
F ₂	M[FE] = R ₃ = 02					
F ₄	R ₀ = R ₀ ✓					
EC	if ^{E5} R ₁ = ^{F₂} R ₀ X					
E _E (Rotate)	R ₁ = E5 = $\begin{array}{ccccccc} 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ \hline 1 & 1 & 1 & 0 & 0 & 1 & 0 \end{array}$					
F ₀	R ₃ = ⁰² R ₃ + ⁰¹ R ₂ = 03					
F ₂	M[FE] = R ₃ = 03					
F ₄	R ₀ = R ₀ ✓					
EC	if ^{F₂} R ₁ = ^{F₂} R ₀ ✓					
F ₆	halt / stop.					

بعد ذلك اجاب على اسئلة المطلوبة
→

- 1) What is the content of Register 1 after the first time the instruction EE is executed?

$$R_1 = E5$$

- 2) What is the content of R_1 after the second time the instruction EE is executed?

$$R_1 = F2$$

- 3) How many times the instruction at address EC is executed before the machine halts?

3 times

- 4) What is the content of R_3 after the Program Termination?

$$R_3 = 03$$

- 5) What will happen if the Program starts execution with Replacing the contents at address EF to be 08?

لن يكون! إذا غيرنا قيمة محتويات $M[EF]$ إلى (08) في جدول التعليمات

Add	content
EE	A1
EF	08

أمر ال Rotate سيصبح $[A108]$

ومعنا! أننا نعمل Rotate بـ مقدار (08)

لن يكون مفسد أي تغيير هيجعل بين البرنامج هيكو غير مفسد أبداً

⇒ After the Rotate instruction the number at R_1 will be as it each time, and the Jump operation at (EC) won't be true so, it will be (infinite Loop)


Ex. (From the book P.160)

⇒ Write a machine language Program that Copies the middle four bits from memory cell E_0 into the least significant four bits of memory cell E_1 , while placing 0's in the most significant four bits of the same cell.

Ans.

مثال توضیحي

→ If $M[E_0]$ has (a a b b b b a a)
→ We need to change the number in $M[E_0]$ to be
most significant least significant
0 0 0 0 b b b b

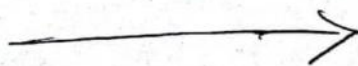
Then, put the new number  in $M[E_1]$

① We will make "Rotate" operation for (a a b b b b a a)
to be
(a a a a b b b b)

② We will make "AND" operation with (0F) Mask

	a	a	a	a	b	b	b	b
AND	0	0	0	0	1	1	1	1
	<hr/>				<hr/>			
	0	0	0	0	b	b	b	b

→ Then store this number in $M[E_1]$



* لحل البرنامج ← لابد من التحليل كل القيم التي سوف تستخدم داخل (R)

Steps	Symbolic Form	Instruction Form
Step 1 →	LOAD $R_0 \leftarrow M[E_0]$	10E0
Step 2 →	Rotate R_0 , 2-Location	A002
Step 3 →	LOAD R_1 , of "ANDmask"	210F
Step 4 →	AND $R_2 \leftarrow R_0 \text{ AND } R_1$	8201
Step 5 →	STORE $R_2 \rightarrow M[E_1]$	32E1
Step 6 →	halt/stop.	C000



EX:

* It is Required to Change the Content of Memory Cell C_2 From $(b_7 b_6 b_5 b_4 b_3 b_2 b_1 b_0)$ to be $(b_3 \circ b_1 \mid \mid b_6 \circ b_4)$

* Determine the Required masks and logical operations to make such a change, then Write a machine Program to perform the above operations?

ANS.



للحصول من المخرج
 (b₇ b₆ b₅ b₄ b₃ b₂ b₁ b₀)
 الب (b₃ 0 b₁ 1 1 b₆ 0 b₄)

① نحتاج أولًا لعمل (Rotate) بمقدار أربع حركات لكي يصبح الرقم

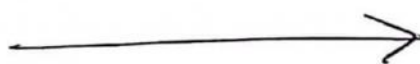
$$\begin{array}{ccccccc} b_7 & b_6 & b_5 & b_4 & b_3 & b_2 & b_1 & b_0 \\ \hline b_3 & b_2 & b_1 & b_0 & b_7 & b_6 & b_5 & b_4 \end{array}$$

② نستخدم (OR mask) لجعل البتات التي نحتاجها في الناتج صفراً وذلك
 بعلامة (1) كالآتي .

	b ₃	b ₂	b ₁	b ₀	b ₇	b ₆	b ₅	b ₄
OR	0	1	5	1	1	0	1	0
<hr/>								
	b ₃	1	b ₁	1	1	b ₆	1	b ₄
XOR	0	1	1	0	0	1	1	0
<hr/>								
	b ₃	0	b ₁	1	1	b ₆	0	b ₄

ونضع (1)
 في البتات التي نحتاجها
 صفراً و complement

خطوات عمل البرنامج

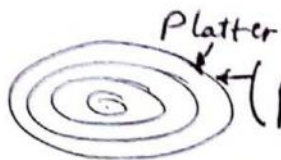
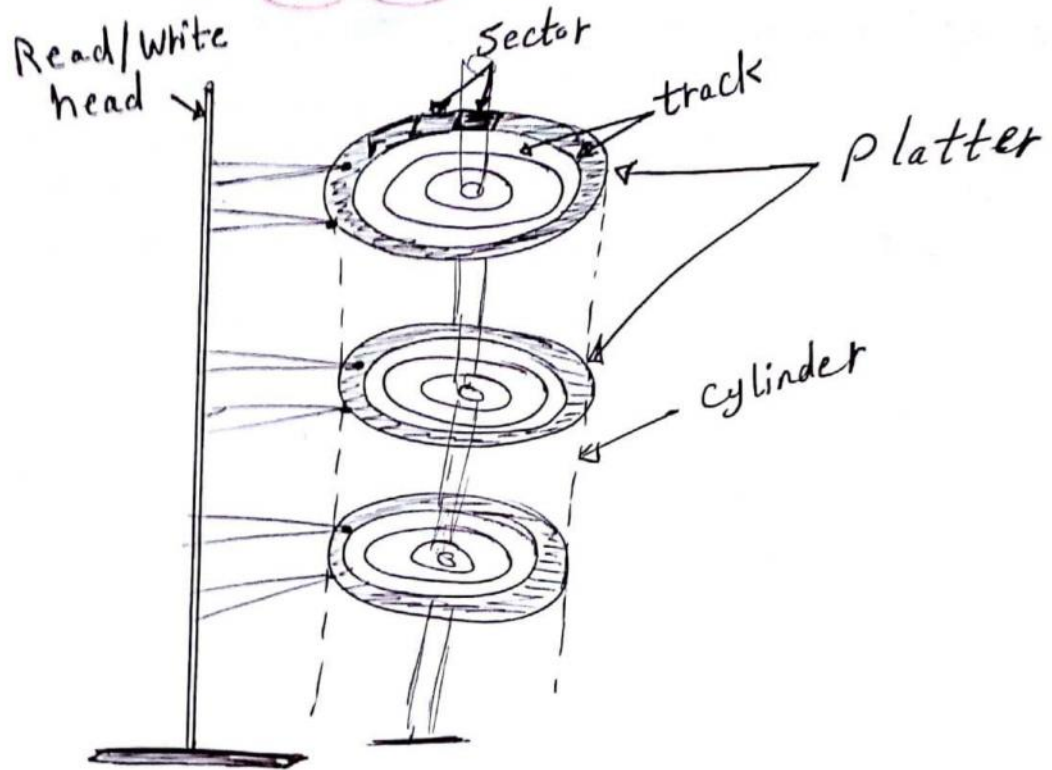


خطوات عمل البرنامج ..

- ① نأخذ الرقم المراد تحويله واسمونه $M[C2]$ داخل R_0
- ② نأخذ Rotate لهذا الرقم بمقدار 4 بتات (4 bits) ونخزنه في R_0
- ③ ~~نأخذ (OR mask) للرقم الموجود في R_0~~
- ④ نأخذ ال (OR mask) والذي قيمته (5A) داخل R_1
- ⑤ نأخذ (OR operation) بين R_0 و R_1 ونضع الناتج في R_2
- ⑥ نأخذ (XOR mask) والذي قيمته (66) داخل R_3
- ⑦ نأخذ (XOR operation) بين R_2 و R_3 ونضع الناتج داخل R_4
- ⑧ نخزنه (R_4) داخل $M[C2]$
- ⑨ نغلق البرنامج .

steps	Symbolic form	Instruction form
step1:	LOAD $R_0 \leftarrow M[C2]$	1 0 C2
step2:	Rotate R_0 , 4-Location	A 0 0 4
step3:	LOAD $R_1 \leftarrow 5A$	2 1 5A
step4:	OR $R_2 \leftarrow R_1 \text{ OR } R_0$	7 2 1 0
step5:	LOAD $R_3 \leftarrow 66$	2 3 6 6
step6:	XOR $R_4 \leftarrow R_2, R_3$	9 4 2 3
step7:	STORE $R_4 \rightarrow M[C2]$	3 4 C2
step8:	halt/stop.	C 0 0 0

Hard disk

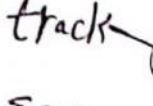


Platter

* ال (hard disk) يتكون من عدد من (Platters)

* كل (platter) له وجهين لتخزين البيانات (2 sides)

* كل (side) عليه عدد من ال (tracks)



track

* كل (track) مقسم لمجموعة من ال (sectors) كل واحد



Sectors

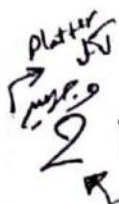
حجم ال track الواحد = حجم ال Sector \times عدد ال

* ال (Cylinder) هو مجموع لنفس ال (track) من كل ال (platters) الموجودين (sides وجهين)



حجم ال Cylinder = حجم ال track \times 2 \times عدد ال Platter

* حجم ال hard يتكون من مجموع بطرق حسب المعطيات:



Platter

track

sector

س

2

ال

Platter

ال

ال

$$\text{حجم ال hard} = \text{حجم ال track} \times \text{عدد ال tracks} \times \text{عدد ال Platter} \times 2$$

$$\text{حجم ال hard} = \text{حجم ال Cylinder} \times \text{عدد ال cylinders} \quad (14) \quad (15)$$

Ex:

- * If the size of sector = 512 B / ^{per} sector
- * No. of sector / track = 63 sector / track.
- * No. of platters = 8

- a) Find the size of cylinder.
- b) If the hard disk has 100 cylinders find the size of the hard disk.

Ans.

a) The size of cylinder = size of track $\times 2 \times$ No. of platters

$$\begin{aligned}\text{Size of track} &= \text{No. of sector} \times \text{size of one sector} \\ &= 63 \times 512 \\ &= \boxed{32256} \text{ Bytes}\end{aligned}$$

\rightarrow

$$\begin{aligned}\text{The size of cylinder} &= \text{size of track} \times 2 \times \text{No. of platter.} \\ &= 32256 \times 2 \times 8 \\ &= \boxed{516096} \text{ Bytes.}\end{aligned}$$

b) If the hard disk has 100 cylinders \Rightarrow

$$\begin{aligned}\text{The hard disk size} &= \text{Cylinder size} \times \text{No. of cylin} \\ &= 516096 \times 100 \\ &= \boxed{51609600} \text{ B} \approx 49 \text{ MB} \quad (15)\end{aligned}$$

المواضيع التي ندرست بالسبج

① Number systems.

→ التحويل من وإلى (decimal)
 → التحويل المباشر إلى ()
 4 bits → 2 bits
 8 bits → 4 bits
 16 bits → 8 bits

② Addition & subtraction.

→ ولطرح ثلاثة أنواع :-
 → Direct → verified by decimal
 → 1's Comp. → " " ()
 → 2's Comp. → " " 10's Comp.

③ Signed Numbers:

From $(-)_10 \rightarrow (?)_2$ From $(-)_2 \rightarrow (?)_{10}$
 محتاجين ان نكتب اثنان لاننا
 لنعرف هل الرقم ايجابي او سالب
 فنكتبه اولا

- unsign method
- Signed magnitude
- 1's Complement
- 2's Complement
- EXcess notation.

④ Signed 2's complement subtraction

في هذه النوعية من الحسابات بنقل الرقم لعدد
 ال bits المعطاة في رأس السؤال ثم نحول الى
 اثنان سالب () 2's Comp.

⑤ Floating point Representation

→ IEEE (المعيار)
 → نوعية اشارة الرسالة التي يمكن تجربتها :-
 } Code } Decode.

⑥ Memory Capacity

Memory Capacity = no. of cell X cell size
 For Address line
 = $2^n \times$

⑦ Machine manipulating.

- * How to Write machine language Program.
- * Jump.
- * masks (AND, OR, XOR)
- * Rotate, Shift (\div , \times)

⑧ Hard disk.