

```

function heapSort(Array arr) {
    copy the arr into a new array heap with the 0 index empty
    int firstIndex = 1 // assume the first index is 1 for easier calculation    k0
    int lastIndex = arr.length - 1

    // do reheap() on every non-leaf nodes. The last leaf is at lastIndex, so the last non-leaf is at lastIndex / 2
    for(int rootIndex = lastIndex / 2; rootIndex > 0; rootIndex--)    O(n/2) = O(n)
        reheap(arr, rootIndex);    O(log(n)), see below
}

```

Conclusion:

Worst case complexity  $\rightarrow O(n * \log(n)) = O(n \log n)$

```

function reheap(Array heap, rootIndex) {
    boolean done = false;
    T orphan = heap[rootIndex]; // start from root    k2
    int leftChildIndex = rootIndex * 2;

    while(!done && (leftChildIndex <= lastIndex)) {
        int largerChildIndex = leftChildIndex; // assume left is larger    k3
        int rightChildIndex = leftChildIndex + 1;

        if((rightChildIndex <= lastIndex) && heap[rightChildIndex].compareTo(heap[largerChildIndex]) > 0)    k4
            largerChildIndex = rightChildIndex; // get the larger child

        if(orphan.compareTo(heap[largerChildIndex]) < 0)
        {
            heap[rootIndex] = heap[largerChildIndex];
            rootIndex = largerChildIndex; // swap root and larger, and repeat the process    k5
            leftChildIndex = rootIndex * 2;
        }

        else
            done = true; // end the loop    k6
        }

    heap[rootIndex] = orphan; // put this last piece onto the root    k7
    }
}

```

In the worst case:

It will have maximum number of swaps

The second if statement in the while loop "leftChildIndex = rootIndex \* 2" will be called again and again until leftChildIndex >= lastIndex

Since every time the leftChildIndex is doubled, it will reach the lastIndex in  $\log(n)$  times.

$O(k2 + \log(n) * (k3 + k4 + k5 + k6 + k7)) = O(\log(n))$