

Version here does not optimize the Dij Alg with a heap or a priority queue.

```
function dijkstra(DirectedGraph graph) {  
    visited <- a set of visited vertices      k0  
    unvisited <- a set of unvisited vertices  
  
    copy every vertex into the unvisited  O(V)  
  
    relax[] <- an array with length of V, used for relaxing vertices      k1  
    prev[] <- an array keeping the previous vertex to record the route, length = V  
  
    initialize 2 arrays, relax[every index] = infinity, prev[every index] = -1      O(V)  
  
    minRoute(source, target)      O(V^2) see below  
}
```

Conclusion:

$O(V + V^2) = O(V^2)$

```
function minRoute(int source, int target) {  
    boolean found = false;  
    int node = source;      k2  
    relax[source] = 0;  // set source to 0, all others infinity by default  
    prev[source] = -1;  
  
    while(!found)  
    {  
        node = findNextNode(node);      O(V) see below  
  
        if(node == target)  // quit when reaches the target      k8  
            found = true;  
  
        visited.add(graph.getLabel(node));  // add the current node to Set: visited      k9  
  
        relaxEdge(node);  // relax the edges      O(V) see below  
  
        unvisited.remove(graph.getLabel(node));  // remove the node from Set: unvisited, means it's done  
        O(V) in worst based on the set implementation  
  
        if(unvisited.isEmpty()) {      k10  
            System.out.println("No route");  // if all nodes are visited and still in the loop, means there is no route  
            break;  
        }  
    }  
}
```

In the worst case, every vertex in the graph is visited until it reach the target.

So the loop runs V times, and complexitiy ->  $O(V * (V + k8 + k9 + V + k10)) = O(V^2)$

```
function findNextNode(node) {  
    int min = Integer.MAX_VALUE;  // default value      k3
```

```

for(int i = 0; i < relax.length; i++)      O(V)
    if(relax[i] < min && unvisited.contains(graph.getLabel(i)) && relax[i] > 0) // get the next smallest relaxation
        value, and make sure it is in the unvisited Set
        min = relax[i];      k4

for(int i = 0; i < relax.length; i++)      O(V)
    if(min == relax[i] && min != Integer.MAX_VALUE && unvisited.contains(graph.getLabel(i)))
        node = i;    // when you get it, get the index      k5

return node;
}

```

$O(k3 + V(k4) + V(k5)) = O(V)$

Assume  $E = V - 1$  for every vertex in the worst case, which means every vertex has a path to every other vertex, so the edge for the whole graph will reach the maximum  $= V^2$

```

function relaxEdge(current <- currentNode) {
    for(int i = 0; i < relax.length; i++) {      O(V)
        if((graph.getEdge())[current][i] && !visited.contains(graph.getLabel(i))) {      k6
            if(relax[i] == Integer.MAX_VALUE || (relax[current] + graph.getWeight(current, i)) < relax[i]) {      k7
                relax[i] = graph.getWeight(current, i) + relax[current];
                prev[i] = current;    // relax algorithm of Dijkstra
            }
        }
    }
}
}
O(V * (k6 + k7)) = O(V)

```