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function mergeSort(Array arr, Array tempArr, int first, int last) {
    mid = (first + last) / 2 // initial condition    k0

    if (first < last) {
        mid = (first + last) / 2    k1
        mergeSort(arr, tempArr, first, mid)    log(n) / 2 calls
        mergeSort(arr, tempArr, mid + 1, last)    log(n) / 2 calls
    }
    merge(arr, tempArr, first, mid, last)    O(n), see below
}

```

Conclusion:

mergeSort() contains b calls, which $2^b = n$, $b = \log(n)$ base 2, consider as $O((k_0 + k_1) * \log n) = O(\log n)$, this is always true no matter the best case or the worst case.

worst case complexity = $O(n * \log(n)) = O(n \log n)$

```

function merge(Array arr, Array tempArr, int first, int mid, int last) {
    // arr1 & arr2 means 2 part in the arr to be merged together
    int beginHalf1 = first;
    int endHalf1 = mid;
    int beginHalf2 = mid + 1;    k0
    int endHalf2 = last;
    int index = 0;

    while((beginHalf1 <= endHalf1) && (beginHalf2 <= endHalf2))    iterate 2 arrays ->  $O(2 * n) = O(n)$ 
    {
        if(array[beginHalf1].compareTo(array[beginHalf2]) < 1)    k1
        {
            tempArray[index] = array[beginHalf1];
            beginHalf1++;
        }
        else    k2
        {
            tempArray[index] = array[beginHalf2];
            beginHalf2++;
        }
        index++;
    }

    // when arr1 is empty, but arr2 is not
    while((beginHalf1 >= endHalf1) && (beginHalf2 <= endHalf2))    Worst case: arr1 empty, arr2 full ->  $O(n)$ 
    {
        tempArray[index] = array[beginHalf2];    k3
        beginHalf2++;
        index++;
    }

    // when the right part has completely copied to tempArray
    while((beginHalf2 >= endHalf2) && (beginHalf1 <= endHalf1))    Worst case: arr2 empty, arr1 full ->  $O(n)$ 
    {
        tempArray[index] = array[beginHalf1];    k4
        beginHalf1++;
    }
}

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    index++;
}

index = 0    // copy back to the original
for(int i = first; i <= last; i++)    iterate the whole array -> O(n)
{
    if(tempArray[index] != null)    k5
    array[i] = tempArray[index];
    index++;
}
}

```

$O(k_0 + 2n(k_1 + k_2) + n(k_3) + n(k_4) + n(k_5)) = O(n)$