

## Assignment 2, 2018

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### Challenge 5 Answer

Let  $DFA(Q, \Sigma, \delta, q_0, F)$  and  $PDA(Q', \Sigma', \Gamma, \delta', q'_0, F')$

The goal is to translate our  $DFA$  to a 3-state  $PDA$ . This can be accomplished by creating a  $PDA$  similar to that of a naive search or graph traversal.

This process is possible as there are only two cases to account for:

- The current state is *not* an accept state
- The current state is an accept state

This results in a translation from any  $DFA$  to a 3-state  $PDA$ ; the first state of the  $PDA$  being the *initialisation state* ( $q_I$ ), followed by the *searching state* ( $q_R$ ) and the *accept state* ( $q_A$ ).

First we start by defining our variables:

#### DFA:

Let  $Q$  be a set of DFA states.

Let  $\Sigma$  be a valid alphabet for our DFA.

Let  $\delta$  be a valid set of transition functions for moving between states with a given input.

Let  $q_0$  be the initial state of our DFA.

Let  $F$  be a set of valid accept states for our DFA.

#### PDA:

Let  $Q' = \{q_I, q_R, q_A\}$

Let  $\Sigma' = \Sigma_\epsilon$

Let  $\Gamma$  be a stack alphabet where  $\Gamma = Q$

Let  $\delta'$  be the three transition functions between  $q_I$ ,  $q_R$ , and  $q_A$

(following the form described in lecture 18  $\delta : Q \times \Sigma_\epsilon \times \Gamma_\epsilon \rightarrow \mathcal{P}(Q \times \Gamma_\epsilon)$ ;

$\delta : \{(q_I, \epsilon, \epsilon, \rightarrow q_R, q_0), (q_R, a, b, \rightarrow q_R, \delta(b, a)), (q_R, \epsilon, f \rightarrow q_A, \epsilon)\}$

Let  $q'_0$  be the starting state  $\{q_I\}$

Let  $F'$  be the accept state  $\{q_A\}$

Let  $a$  be a string input where  $a \in \Sigma$

Let  $b$  be a state where  $b \in Q$

Let  $f$  be an accept state where  $f \in F$

Now we may draw a PDA:

