Lecture 9 Relational Algebra

Agenda



Unary Relational Operations



Relational Algebra Operations From Set Theory



Binary Relational Operators



Additional Relational Operations



Examples of Queries in Relational Algebra

- Two formal languages for the relational model are: the relational algebra and the relational calculus.
- They form the basis of the *practical language* for the relational model, namely the SQL standard.
- We will focus in this lecture on *relational algebra*.

Relational algebra is the basic set of operations for the relational model.

- These operations enable a user to specify basic Retrieval Requests (or Queries)
- The result of an operation is a <u>new relation:</u>
 - The new relations can be further manipulated using operations of the relational algebra

- A sequence of relational algebra operations forms a **Relational Algebra Expression**
 - The result of a relational algebra expression is also a relation that represents the result of a database query (or retrieval request).
- The relational algebra is very important for several reasons:
 - It provides a formal foundation for relational model operations.
 - It is used as a basis for implementing and optimizing queries in the query processing and optimization modules that are integral parts of relational database management systems.

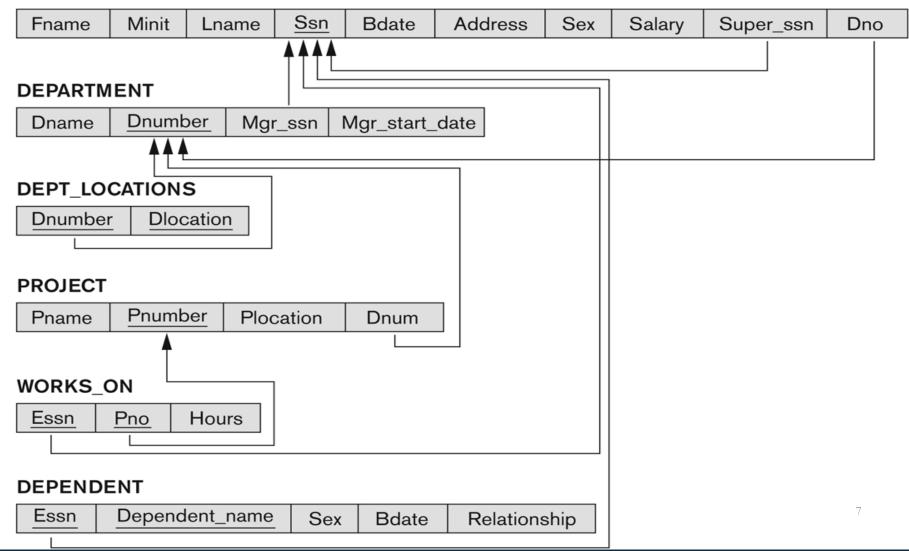
- > Relational Algebra consists of several groups of operations
 - Unary Relational Operations
 - SELECT (symbol: σ (sigma))
 - PROJECT (symbol: π (pi))
 - RENAME (symbol: ρ (rho))
 - Relational Algebra Operations From Set Theory
 - UNION (∪), INTERSECTION (∩), DIFFERENCE (or MINUS, −)
 - CARTESIAN PRODUCT (x)
 - Binary Relational Operations
 - JOIN (several variations of JOIN exist)
 - DIVISION
 - Additional Relational Operations
 - AGGREGATE FUNCTIONS
 - (These compute summary of information: for example, SUM, COUNT, AVG, MIN, MAX)
 - OUTER JOINS

All examples discussed refer to the COMPANY DB shown here

Figure 5.7

Referential integrity constraints displayed on the COMPANY relational database schema.

EMPLOYEE



4

5

5

4

1

Dnum

5

5

Spouse

One possible database state for the COMPANY relational database schema.

EMPLOYEE

EMPLOTE									
Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4

Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Ho
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle,

Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX
Ahmad	>	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX
lames	F	Borg	888665555	1937-11-10	450 Stone Houston TX

		-		
ENT				
me	Dnumber	Mar ssn	Mar start date	

DEPARTMENT							
Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date				
Research	5	333445555	1988-05-22				
Administration	4	987654321	1995-01-01				
Headquarters	1	888665555	1981-06-19				

DEPT_LOCATIONS

Plocation

Sugarland

Bellaire

NULL

43000

38000

25000

25000

55000

M

F

M

M

Pnumber

1

2

Dnumber_	Dlocation		
1	Houston		
4	Stafford		
5	Bellaire		
5	Sugarland		
5	Houston		

888665555

333445555

333445555

987654321

453453453

333445555

333445555

333445555

333445555 999887777

999887777

987987987 987987987

987654321

987654321

888665555

WORKS_ON			
Essn	<u>Pno</u>	Hours	
123456789	1	32.5	
123456789	2	7.5	
666884444	3	40.0	
453453453	1	20.0	

2

2

3

10

20

30

10

10

30

30

20

20

20.0

10.0

10.0

10.0

10.0

30.0

10.0

35.0

20.0

15.0

NULL

5.0

DEPENDENT	

123456789

ProductZ		3		Houston	
Computerization	า 1	10	Stafford		4
Reorganization	2	20	Houston		1
Newbenefits	3	30 Stafford		t	4
	·				
endent_name_	Sex	Bdate		Relat	ionship

1967-05-05

	DEPENDENT				
	Essn	Dependent_name	Sex	Bdate	Relationshi
	333445555	Alice	F	1986-04-05	Daughter
╛	333445555	Theodore	М	1983-10-25	Son
4	333445555	Joy	F	1958-05-03	Spouse
	987654321	Abner	М	1942-02-28	Spouse
╛	123456789	Michael	М	1988-01-04	Son 8
	123456789	Alice	F	1988-12-30	Daughter
- 1	 				

PROJECT

ProductX

ProductY

Elizabeth

Pname



Unary Relational Operators:

SELECT σ PROJECT π RENAME ρ

Unary Relational Operations: SELECT

- The SELECT operation (denoted by **G** (sigma)) is used to select a *subset* of the tuples from a relation based on a **selection condition**.
 - The selection condition acts as a **filter**
 - Keeps only those tuples that satisfy the qualifying condition
 - Tuples satisfying the condition are <u>selected</u> whereas the other tuples are <u>discarded</u> (*filtered out*)
- >Examples:
 - Select the EMPLOYEE tuples whose department number is 4:

$$\sigma_{\text{DNO}=4}$$
 (EMPLOYEE)

• Select the employee tuples whose salary is greater than \$30,000:

$$\sigma_{SALARY > 30,000}$$
 (EMPLOYEE)

Unary Relational Operations: SELECT

• In general, the *select* operation is denoted by

σ_{<selection condition>}(R) where

- The symbol **o** (sigma) is used to denote the *select* operator
- The selection condition is a Boolean (conditional) expression specified on the attributes of relation R
- Tuples that make the condition true are selected
 - appear in the result of the operation
- Tuples that make the condition **false** are filtered out
 - discarded from the result of the operation

Unary Relational Operations: SELECT

- SELECT Operation Properties
 - The SELECT operation $\sigma_{\text{selection condition}}(R)$ produces a relation S that has the same schema (same attributes) as R
 - SELECT σ is commutative:
 - $\sigma_{\text{condition1}}(\sigma_{\text{condition2}}(R)) = \sigma_{\text{condition2}}(\sigma_{\text{condition1}}(R))$
 - Because of commutativity property, a cascade (sequence) of SELECT operations may be applied in any order:
 - σ_{cond1} (σ_{cond2} (σ_{cond3} (R)) = σ_{cond2} (σ_{cond3} (σ_{cond1} (R))
 - A cascade of SELECT operations may be replaced by a single selection with a conjunction of all the conditions:
 - $\sigma_{< cond1>}(\sigma_{< cond2>} (\sigma_{< cond3>}(R)) = \sigma_{< cond1> AND < cond2> AND < cond3>}(R)$
 - The number of tuples in the result of a SELECT is less than (or equal to) the number of tuples in the input relation R

Unary Relational Operations: PROJECT

- \triangleright PROJECT Operation is denoted by π (pi)
- This operation keeps certain *columns* (attributes) from a relation and discards the other columns.
 - PROJECT creates a vertical partitioning
 - The list of specified columns (attributes) is kept in each tuple
 - The other attributes in each tuple are discarded
- Example: To list each employee's first and last name and salary, the following is used:

 $\pi_{\text{LNAME, FNAME,SALARY}}(\text{EMPLOYEE})$

Unary Relational Operations: PROJECT

The general form of the *project* operation is:

 $\pi_{\text{<attribute list>}}(R)$

- π is the symbol used to represent the *project* operation
- <attribute list> is the desired list of attributes from relation R.
- The project operation removes any duplicate tuples
 - This is because the result of the *project* operation must be a *set of tuples*
 - Mathematical sets *do not allow* duplicate elements.

Unary Relational Operations: PROJECT

- ➤ PROJECT Operation Properties
 - The number of tuples in the result of projection $\pi_{< list>}(R)$ is always less or equal to the number of tuples in R
 - If the list of attributes includes a *key* of R, then the number of tuples in the result of PROJECT is *equal* to the number of tuples in R
 - PROJECT is *not* commutative
 - $\pi_{< \text{list}1>}$ ($\pi_{< \text{list}2>}$ (R)) = $\pi_{< \text{list}1>}$ (R) as long as tist2> contains the attributes in tist1>

Examples: .

Figure 8.1

Results of SELECT and PROJECT operations. (a) $\sigma_{\text{(Dno=4 AND Salary}>25000)}$ OR (Dno=5 AND Salary>30000) (EMPLOYEE). (b) $\pi_{\text{Lname, Fname, Salary}}$ (EMPLOYEE). (c) $\pi_{\text{Sex, Salary}}$ (EMPLOYEE).

(a)

Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX	М	38000	333445555	5

(b)

Lname	Fname	Salary
Smith	John	30000
Wong	Franklin	40000
Zelaya	Alicia	25000
Wallace	Jennifer	43000
Narayan	Ramesh	38000
English	Joyce	25000
Jabbar	Ahmad	25000
Borg	James	55000

(c)

Sex	Salary
М	30000
М	40000
F	25000
F	43000
М	38000
М	25000
М	55000

Duplicate Removed

Relational Algebra Expressions

- We may want to apply several relational algebra operations one after the other
 - Either we can write the operations as a single **Relational Algebra Expression** by nesting the operations, or
 - We can apply one operation at a time and create **Intermediate Result Relations**.
- In the latter case, we must give names to the relations that hold the intermediate results.

Single expression *versus* sequence of relational operations (Example)

- To retrieve the *first name, last name, and salary* of all employees who work in *department number 5*, we must apply a select and a project operation
- We can write a single relational algebra expression as follows:
 - $\pi_{\text{FNAME, LNAME, SALARY}}(\sigma_{\text{DNO}=5}(\text{EMPLOYEE}))$
- ➤OR We can explicitly show the *sequence of operations*, giving a name to each intermediate relation:
 - DEP5_EMPS $\leftarrow \sigma_{\text{DNO}=5}(\text{EMPLOYEE})$
 - RESULT $\leftarrow \pi_{\text{FNAME, LNAME, SALARY}}$ (DEP5_EMPS)

Unary Relational Operations: RENAME

- The RENAME operator is denoted by ρ (rho)
- In some cases, we may want to *rename* the attributes of a relation or the relation name or both
 - Useful when a query requires multiple operations
 - Necessary in some cases (see JOIN operation later)

Unary Relational Operations: RENAME

- The general RENAME operation ρ can be expressed by any of the following forms:
 - $\bullet \rho_{S (B1, B2, ..., Bn)}(R)$ changes both:
 - the relation name to S, and
 - the column (attribute) names to B1, B2,Bn
 - $\rho_{S}(R)$ changes:
 - the relation name only to S
 - $\rho_{(B1, B2, ..., Bn)}(R)$ changes:
 - the column (attribute) names only to B1, B2,Bn

Unary Relational Operations: RENAME

- For convenience, we also use a *shorthand* for renaming attributes in an intermediate relation:
 - If we write:
 - RESULT $\leftarrow \pi_{\text{FNAME, LNAME, SALARY}}$ (DEP5_EMPS)
 - RESULT will have the *same attribute names* as DEP5_EMPS (same attributes as EMPLOYEE)
 - If we write:
 - R (First_name, Last_name, Salary) ← π _{FNAME, LNAME, SALARY}(DEP5_EMPS)

(a)

Fname	Lname	Salary
John	Smith	30000
Franklin	Wong	40000
Ramesh	Narayan	38000
Joyce	English	25000

(b) **TEMP**

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston,TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston,TX	М	40000	888665555	5
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble,TX	М	38000	333445555	5
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5

R

First_name	Last_name	Salary
John	Smith	30000
Franklin	Wong	40000
Ramesh	Narayan	38000
Joyce	English	25000

Figure 8.2

Results of a sequence of operations. (a) $\pi_{Fname, Lname, Salary}$ ($\sigma_{Dno=5}$ (EMPLOYEE)). (b) Using intermediate relations and renaming of attributes.



Relational Algebra Operators from Set Theory:

UNION (∪), INTERSECTION (∩), DIFFERENCE (or MINUS, -) CARTESIAN PRODUCT (x)

Relational Algebra Operations from Set Theory: UNION

>UNION Operation

- Binary operation, denoted by ∪
- The result of $R \cup S$, is a relation that includes all tuples that are either in R or in S or in both R and S
- Duplicate tuples are eliminated
- The two operand relations R and S must be "type compatible" (or UNION compatible)
 - R and S must have same number of attributes
 - Each pair of corresponding attributes must be type compatible (have same or compatible domains)

Relational Algebra Operations from Set Theory: UNION

- >Example:
 - Retrieve the social security numbers of all employees who either <u>work in department 5</u> (RESULT1 below) or <u>directly supervise an employee who works in department 5</u> (RESULT2 below)
 - We can use the UNION operation as follows:

DEP5_EMPS
$$\leftarrow \sigma_{\text{DNO=5}}$$
 (EMPLOYEE)

RESULT1 $\leftarrow \pi_{\text{SSN}}$ (DEP5_EMPS)

RESULT2(SSN) $\leftarrow \pi_{\text{SUPERSSN}}$ (DEP5_EMPS)

RESULT \leftarrow RESULT1 \cup RESULT2

• The union operation produces the tuples that are in either RESULT1 or RESULT2 or both

Example of the result of a UNION operation

EMPLOYEE

Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
Т	Wong	333445555	1955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX	М	38000	333445555	5
Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5
V	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX	М	25000	987654321	4
E	Borg	888665555	1937-11-10	450 Stone, Houston, TX	М	55000	NULL	1
	B T J S K A	B Smith T Wong J Zelaya S Wallace K Narayan A English V Jabbar	B Smith 123456789 T Wong 333445555 J Zelaya 999887777 S Wallace 987654321 K Narayan 666884444 A English 453453453 V Jabbar 987987987	B Smith 123456789 1965-01-09 T Wong 333445555 1955-12-08 J Zelaya 999887777 1968-01-19 S Wallace 987654321 1941-06-20 K Narayan 666884444 1962-09-15 A English 453453453 1972-07-31 V Jabbar 987987987 1969-03-29	B Smith 123456789 1965-01-09 731 Fondren, Houston, TX T Wong 333445555 1955-12-08 638 Voss, Houston, TX J Zelaya 999887777 1968-01-19 3321 Castle, Spring, TX S Wallace 987654321 1941-06-20 291 Berry, Bellaire, TX K Narayan 666884444 1962-09-15 975 Fire Oak, Humble, TX A English 453453453 1972-07-31 5631 Rice, Houston, TX U Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX	B Smith 123456789 1965-01-09 731 Fondren, Houston, TX M T Wong 333445555 1955-12-08 638 Voss, Houston, TX M J Zelaya 999887777 1968-01-19 3321 Castle, Spring, TX F S Wallace 987654321 1941-06-20 291 Berry, Bellaire, TX F K Narayan 666884444 1962-09-15 975 Fire Oak, Humble, TX M A English 453453453 1972-07-31 5631 Rice, Houston, TX F V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M	B Smith 123456789 1965-01-09 731 Fondren, Houston, TX M 30000 T Wong 333445555 1955-12-08 638 Voss, Houston, TX M 40000 J Zelaya 999887777 1968-01-19 3321 Castle, Spring, TX F 25000 S Wallace 987654321 1941-06-20 291 Berry, Bellaire, TX F 43000 K Narayan 666884444 1962-09-15 975 Fire Oak, Humble, TX M 38000 A English 453453453 1972-07-31 5631 Rice, Houston, TX F 25000 V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M 25000	B Smith 123456789 1965-01-09 731 Fondren, Houston, TX M 30000 333445555 T Wong 333445555 1955-12-08 638 Voss, Houston, TX M 40000 888665555 J Zelaya 999887777 1968-01-19 3321 Castle, Spring, TX F 25000 987654321 S Wallace 987654321 1941-06-20 291 Berry, Bellaire, TX F 43000 888665555 K Narayan 666884444 1962-09-15 975 Fire Oak, Humble, TX M 38000 333445555 A English 453453453 1972-07-31 5631 Rice, Houston, TX F 25000 333445555 V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M 25000 987654321

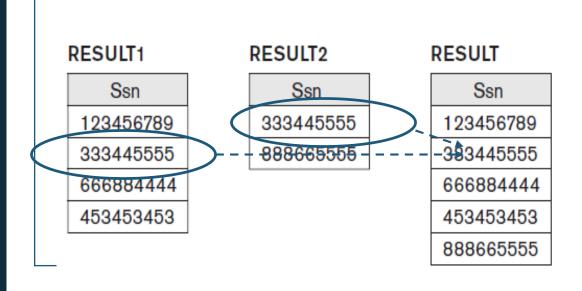


Figure 8.3 Result of the UNION operation RESULT ← RESULT1 ∪ RESULT2.

Relational Algebra Operations from Set Theory

- Type Compatibility of operands is required for the binary set operation UNION \cup , (also for INTERSECTION \cap , and SET DIFFERENCE -)
- ➤R1(A1, A2, ..., An) and R2(B1, B2, ..., Bn) are type compatible if:
 - They have the same number of attributes, and
 - The <u>domains</u> of corresponding attributes are <u>type</u> compatible (i.e. dom(Ai)=dom(Bi) for i=1, 2, ..., n).
- The resulting relation for R1 \cup R2 (also for R1 \cap R2, or R1-R2) has the same attribute names as the *first* operand relation R1 (by convention)

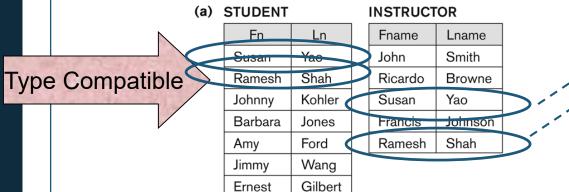
Relational Algebra Operations from Set Theory: INTERSECTION

- ➤INTERSECTION is denoted by ∩
- The result of the operation $R \cap S$, is a relation that includes all tuples that are in both R and S
 - The attribute names in the result will be the same as the attribute names in R
- The two operand relations R and S must be "type compatible"

Relational Algebra Operations from Set Theory: SET DIFFERENCE

- SET DIFFERENCE (also called **MINUS** or **EXCEPT**) is denoted by –
- The result of R S, is a relation that includes all tuples that are in R but not in S
 - The attribute names in the result will be the same as the attribute names in R
- The two operand relations R and S must be "type compatible"





	Fn	Ln
•	Susan	Yao
	Ramesh	Shah
	Johnny	Kohler
	Barbara	Jones
	Amy	Ford
	Jimmy	Wang
	Ernest	Gilbert
	John	Smith
	Ricardo	Browne
	Francis	Johnson

UNION

INTERSECT

Fn	Ln			
Susan	Yao			
Ramesh	Shah			

DIFFERENCE

(c)

Fn	Ln
Johnny	Kohler
Barbara	Jones
Amy	Ford
Jimmy	Wang
Ernest	Gilbert

(e)

(b)

Fname	Lname
John	Smith
Ricardo	Browne
Francis	Johnson

DIFFERENCE

Figure 8.4

The set operations UNION, MTERSECTION, and MINUS. (a) Two union-compatible relations.

- (b) STUDENT \cup INSTRUCTOR. (c) STUDENT \cap INSTRUCTOR. (d) STUDENT INSTRUCTOR.
- (e) INSTRUCTOR STUDENT.

Some properties of UNION, INTERSECT, and DIFFERENCE

- Notice that both union and intersection are *commutative* operations; that is
 - $R \cup S = S \cup R$, and $R \cap S = S \cap R$
- Both union and intersection can be treated as **n-ary** operations applicable to any number of relations as both are *associative* operations; that is
 - $R \cup (S \cup T) = (R \cup S) \cup T$
 - $(R \cap S) \cap T = R \cap (S \cap T)$
- The minus operation is **not commutative**; that is, in general
 - $R S \neq S R$

Relational Algebra Operations from Set Theory: CARTESIAN PRODUCT

>CARTESIAN (or CROSS) PRODUCT Operation

- This operation is used to combine tuples from two relations in a combinatorial fashion.
- Denoted by R(A1, A2, . . ., An) x S(B1, B2, . . ., Bm)
- Result is a relation Q with degree n + m attributes:
 - Q(A1, A2, . . ., An, B1, B2, . . ., Bm), in that order.
- The resulting relation state has one tuple for each combination of tuples—one from R and one from S.
- Hence, if R has n_R tuples (denoted as $|R| = n_R$), and S has n_S tuples, then R x S will have $\underline{n_R} * \underline{n_S}$ tuples.
- The two operands DO NOT have to be "type compatible"

Relational Algebra Operations from Set Theory: CARTESIAN PRODUCT

- Generally, CROSS PRODUCT is not a meaningful operation
 - Can become meaningful when followed by other operations
- Example (not meaningful):
 - FEMALE_EMPS $\leftarrow \sigma_{\text{SEX='F'}}(\text{EMPLOYEE})$
 - EMPNAMES $\leftarrow \pi_{\text{FNAME, LNAME, SSN}}$ (FEMALE_EMPS)
 - EMP_DEPENDENTS ← EMPNAMES x DEPENDENT
- ➤ EMP_DEPENDENTS will contain every combination of EMPNAMES and DEPENDENT
 - whether or not they are actually related

Relational Algebra Operations from Set Theory: CARTESIAN PRODUCT

- To keep only combinations where the DEPENDENT is related to the EMPLOYEE, we add a SELECT operation as follows
- Example (meaningful):
 - FEMALE_EMPS $\leftarrow \sigma_{\text{SEX='F'}}(\text{EMPLOYEE})$
 - EMPNAMES $\leftarrow \pi_{\text{FNAME, LNAME, SSN}}$ (FEMALE_EMPS)
 - EMP_DEPENDENTS ← EMPNAMES x DEPENDENT
 - ACTUAL_DEPS $\leftarrow \sigma_{SSN=ESSN}(EMP_DEPENDENTS)$
 - RESULT $\leftarrow \pi_{\text{FNAME, LNAME, DEPENDENT_NAME}}$ (ACTUAL_DEPS)
- > RESULT will now contain the name of female employees and their dependents

Dno

5

Super_ssn

333445555

888665555

One possible database state for the COMPANY relational database schema.

731 Fondren, Houston, TX

Sex

М

M

Salary

30000

40000

Address

1955-12-08 | 638 Voss, Houston, TX

EMPLOYEE Fname

John

Franklin

Minit

В

Т

Lname

Smith

Wong

	11011	, 000 .	.000	5 1000 12 00 000 1000, 11000ton, 17				 							
J	Zelay	a 9998	87777	1968-01	01-19 3321 Castle, Spring, TX		F	25	25000		987654321				
s	Walla	ce 9876	54321	1941-06-20 291 Berry, Bellaire, TX			F	43	43000 888		665555	4			
K	Naray	an 6668	84444	1962-09	-15	975 Fi	re Oak, H	lumble, T	X M	38	38000 333		445555	5	
Α	Englis	h 4534	53453	1972-07-	31	5631 l	Rice, Hou	ıston, TX	F	25	000	3334	445555	5	
V	Jabba	r 98798	37987	1969-03	-29	980 D	allas, Hοι	uston, TX	М	25	000	9876	554321	4	
E	Borg	8886	65555	1937-11	-10	450 S	tone, Hou	ıston, TX	М	55	000	NUL	L	1	
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789	2	7.5	_				Produc	tY		2	Sugar				
444	3	40.0					Produc	tZ		3	Ho	ousto	n	5	
453	1	20.0	_						1	10	St	afforc	1	4	
453		20.0	_						2	20 Hou				1	
555	2	10.0	_				Newbei	nefits	3	30 Staffor		afforc	<u> </u>	4	
	3	10.0	\perp												
555	10	10.0	_ D	EPENDE	NT										
555	20	10.0		Essn		De	pendent_	name	Sex	Е	Bdate		Relatio	nship	
777	30	30.0	_ [3334455	55	Alic	е		F	198	1986-04-05		Daugh	nter	
777	10	10.0	\bot	333445555 The		odore		М	198	33-10	-25	Son			
987	10	35.0	\bot	3334455	333445555 Joy				F	195	8-05	-03	Spous	se	
987	30	5.0	_	98765432	21	Abr	er		М	194	1942-02-28		Spous		
321	30	20.0		12345678	39	Mic	chael		М	198	1988-01-04		Son 35		
	00	15.0		19345678	8456789 Alice		e		F	198	1988-12-30		Daughter		
321	20	15.0		12040070	23456789 Elizabeth			-		1988-12-30		Daag.	1101		
	S K A V E IENT me ch stration arters ON 789 789 444 453 453 555 555 555 777 777 987 987	S Walla K Naray A Englis V Jabba E Borg IENT me Dr ch stration arters DN Pno 789 1 789 2 444 3 453 1 453 2 555 2 555 3 555 10 555 10 555 20 777 30 777 10 987 10 987 30 987 30	S Wallace 98768 K Narayan 6668 A English 45348 V Jabbar 98798 E Borg 8886 IENT The Dnumber of the stration 4 stration 4 straters 1 TON Pno Hours 789 1 32.5 789 2 7.5 789 2 7.5 444 3 40.0 453 1 20.0 453 1 20.0 453 2 20.0 555 2 10.0 555 3 10.0 555 10 10.0 555 10 10.0 777 30 30.0 777 10 10.0 777 10 10.0 777 10 10.0 777 30 35.0 777 10 35.0 787 30 5.0	S Wallace 987654321 K Narayan 666884444 A English 453453453 V Jabbar 987987987 E Borg 888665555 IENT Me	S Wallace 987654321 1941-06 K Narayan 666884444 1962-09 A English 453453453 1972-07 V Jabbar 987987987 1969-03 E Borg 888665555 1937-11 IENT me Dnumber Mgr_ssn stration 4 987654321 earters 1 888665555 ON Pno Hours 789 1 32.5 789 2 7.5 444 3 40.0 453 1 20.0 453 2 20.0 555 2 10.0 555 3 10.0 555 2 10.0 655 2 10.0 655 2 10.0 655 2 10.0 655 2 10.0 677 10 10.0 687 </td <td>S Wallace 987654321 1941-06-20 K Narayan 666884444 1962-09-15 A English 453453453 1972-07-31 V Jabbar 987987987 1969-03-29 E Borg 888665555 1937-11-10 IENT </td> <td> S Wallace 987654321 1941-06-20 291 Bd K Narayan 6668844444 1962-09-15 975 Fin A English 453453453 1972-07-31 5631 Fin V Jabbar 987987987 1969-03-29 980 D E Borg 888665555 1937-11-10 450 St S S S S S S S S S</td> <td>S Wallace 987654321 1941-06-20 291 Berry, Bella K Narayan 666884444 1962-09-15 975 Fire Oak, H A English 453453453 1972-07-31 5631 Rice, Hou V Jabbar 987987987 1969-03-29 980 Dallas, Hou E Borg 888665555 1937-11-10 450 Stone, Hou IENT Me</td> <td> S Wallace 987654321 1941-06-20 291 Berry, Bellaire, TX K Narayan 666884444 1962-09-15 975 Fire Oak, Humble, T A English 453453453 1972-07-31 5631 Rice, Houston, TX V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX E Borg 888665555 1937-11-10 450 Stone, Houston, TX IENT </td> 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Humble, TX M 38000 3334 A English 453453453 1972-07-31 5631 Rice, Houston, TX F 25000 9876 </td> <td> Section Sect</td>	S Wallace 987654321 1941-06-20 K Narayan 666884444 1962-09-15 A English 453453453 1972-07-31 V Jabbar 987987987 1969-03-29 E Borg 888665555 1937-11-10 IENT	S Wallace 987654321 1941-06-20 291 Bd K Narayan 6668844444 1962-09-15 975 Fin A English 453453453 1972-07-31 5631 Fin V Jabbar 987987987 1969-03-29 980 D E Borg 888665555 1937-11-10 450 St S S S S S S S S S	S Wallace 987654321 1941-06-20 291 Berry, Bella K Narayan 666884444 1962-09-15 975 Fire Oak, H A English 453453453 1972-07-31 5631 Rice, Hou V Jabbar 987987987 1969-03-29 980 Dallas, Hou E Borg 888665555 1937-11-10 450 Stone, Hou IENT Me	S Wallace 987654321 1941-06-20 291 Berry, Bellaire, TX K Narayan 666884444 1962-09-15 975 Fire Oak, Humble, T A English 453453453 1972-07-31 5631 Rice, Houston, TX V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX E Borg 888665555 1937-11-10 450 Stone, Houston, TX IENT	S 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1972-07-31 5631 Rice, Houston, TX F 25000 9876	Section Sect	

Ssn

123456789

333445555

Bdate

1965-01-09

Figure 8.5

The CARTESIAN PRODUCT (CROSS PRODUCT) operation.

FEMALE_EMPS

Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
Alicia	J	Zelaya	999887777	1968-07-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	291Berry, Bellaire, TX	F	43000	888665555	4
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5

EMPNAMES

Fname	Lname	Ssn
Alicia	Zelaya	999887777
Jennifer	Wallace	987654321
Joyce	English	453453453

EMP_DEPENDENTS

Fname	Lname	Ssn	Essn	Dependent_name	Sex	Bdate	
Alicia	Zelaya	999887777	333445555	Alice	F	1986-04-05	
Alicia	Zelaya	999887777	333445555	Theodore	М	1983-10-25	
Alicia	Zelaya	999887777	333445555	Joy	F	1958-05-03	
Alicia	Zelaya	999887777	987654321	Abner	М	1942-02-28	
Alicia	Zelaya	999887777	123456789	Michael	М	1988-01-04	
Alicia	Zelaya	999887777	123456789	Alice	F	1988-12-30	
Alicia	Zelaya	999887777	123456789	Elizabeth	F	1967-05-05	
Jennifer	Wallace	987654321	333445555	Alice	F	1986-04-05	
Jennifer	Wallace	987654321	333445555	Theodore	М	1983-10-25	
Jennifer	Wallace	987654321	333445555	Joy	F	1958-05-03	
Jennifer	Wallace	987654321	987654321	Abner	М	1942-02-28	
Jennifer	Wallace	987654321	123456789	Michael	М	1988-01-04	
Jennifer	Wallace	987654321	123456789	Alice	F	1988-12-30	
Jennifer	Wallace	987654321	123456789	Elizabeth	F	1967-05-05	
Joyce	English	453453453	333445555	Alice	F	1986-04-05	
Joyce	English	453453453	333445555	Theodore	М	1983-10-25	
Joyce	English	453453453	333445555	Joy	F	1958-05-03	
Joyce	English	453453453	987654321	Abner	М	1942-02-28	
Joyce	English	453453453	123456789	Michael	М	1988-01-04	
Joyce	English	453453453	123456789	Alice	F	1988-12-30	
Joyce	English	453453453	123456789	Elizabeth	F	1967-05-05	

ACTUAL_DEPENDENTS

Fname	Lname	Ssn	Essn	Dependent_name	Sex	Bdate	
Jennifer	Wallace	987654321	987654321	Abner	М	1942-02-28	

RESULT

Fname	Lname	Dependent_name
Jennifer	Wallace	Abner



Binary Relational Operators:

JOIN DIVISION

Binary Relational Operations: JOIN

►JOIN Operation (denoted by ⋈)

- The sequence of <u>CARTESIAN PRODECT followed by</u> SELECT is used quite commonly to identify and select related tuples from two relations
- A special operation, called JOIN combines this sequence into a single operation
- This operation is very important for any relational database with more than a single relation, because it allows us to combine related tuples from various relations
- The general form of a join operation on two relations R(A1, A2, ..., An) and S(B1, B2, ..., Bm) is:

 $\begin{array}{c|c} R \bowtie_{\leq_{join\ condition}>} S \\ \hline \bullet \ \text{where}\ R \ \text{and}\ S \ \text{can}\ \text{be}\ \text{any}\ \text{relations}\ \text{that}\ \text{result}\ \text{from}\ \text{general} \\ \end{array}$ relational algebra expressions.

Binary Relational Operations: JOIN

- Example: Suppose that we want to retrieve the name of the manager of each department.
 - To get the manager's name, we need to combine each DEPARTMENT tuple with the EMPLOYEE tuple whose SSN value matches the MGRSSN value in the department tuple.
 - We do this by using the join operation.
 - DEPT_MGR ← DEPARTMENT MGRSSN=SSN EMPLOYEE
- ➤ MGRSSN=SSN is the join condition
 - Combines each department record with the employee who manages the department
 - The join condition can also be specified as DEPARTMENT.MGRSSN = EMPLOYEE.SSN

Example of applying the JOIN operation

Figure 8.6

Result of the JOIN operation DEPT_MGR \leftarrow DEPARTMENT $\bowtie_{Mgr_ssn=Ssn} EMPLOYEE.$

DEPT_MGR

Dname	Dnumber	Mgr_ssn	 Fname	Minit	Lname	Ssn	
Research	5	333445555	 Franklin	Т	Wong	333445555	
Administration	4	987654321	 Jennifer	S	Wallace	987654321	•••
Headquarters	1	888665555	 James	Е	Borg	888665555	•••

Binary Relational Operations: EQUIJOIN

- The most common use of join involves join conditions with *equality comparisons* only
- Such a join, where the only comparison operator used is =, is called an EQUIJOIN.
 - In the result of an EQUIJOIN we always have one or more pairs of attributes (whose names need not be identical) that have identical values in every tuple.
 - The JOIN seen in the previous example was an EQUIJOIN.

Binary Relational Operations: NATURAL JOIN

- NATURAL JOIN Operation
 - Another variation of JOIN called NATURAL JOIN denoted by * was created to get rid of the second (extra) attribute in an EQUIJOIN condition.
 - because one of each pair of attributes with identical values is extra
 - The standard definition of natural join <u>requires that the two join attributes</u>, or each pair of <u>corresponding join attributes</u>, <u>have the same name</u> in both <u>relations</u>
 - If this is not the case, a renaming operation is applied first.

Binary Relational Operations: NATURAL JOIN

- Example: To apply a natural join on the DNUMBER attributes of DEPARTMENT and DEPT_LOCATIONS, it is sufficient to write:
 - DEPT_LOCS ← DEPARTMENT * DEPT_LOCATIONS
- ➤ Only attribute with the same name is DNUMBER
- An implicit join condition is created based on this attribute: DEPARTMENT.DNUMBER=DEPT_LOCATIONS.DNUMBER
- Another example: $Q \leftarrow R(A,B,C,D) * S(C,D,E)$
 - The implicit join condition includes *each pair* of attributes with the same name, "AND" ed together:
 - R.C=S.C AND R.D=S.D
 - Result keeps only one attribute of each such pair:
 - \bullet Q(A,B,C,D,E)

Example of NATURAL JOIN operation

(a)

PROJ_DEPT

Pname	Pnumber	Plocation	Dnum	Dname	Mgr_ssn	Mgr_start_date
ProductX	1	Bellaire	5	Research	333445555	1988-05-22
ProductY	2	Sugarland	5	Research	333445555	1988-05-22
ProductZ	3	Houston	5	Research	333445555	1988-05-22
Computerization	10	Stafford	4	Administration	987654321	1995-01-01
Reorganization	20	Houston	1	Headquarters	888665555	1981-06-19
Newbenefits	30	Stafford	4	Administration	987654321	1995-01-01

(b)

DEPT_LOCS

Dname	Dnumber	Mgr_ssn	Mgr_start_date	Location
Headquarters	1	888665555	1981-06-19	Houston
Administration	4	987654321	1995-01-01	Stafford
Research	5	333445555	1988-05-22	Bellaire
Research	5	333445555	1988-05-22	Sugarland
Research	5	333445555	1988-05-22	Houston

Figure 8.7

Results of two natural join operations. (a) proj_dept ← project * dept. (b) dept_locs ← department * dept_locations.

Binary Relational Operations: DIVISION

- ➤DIVISION Operation
 - The division operation is applied to two relations
 - $T(Y) = R(Z) \div S(X)$, where:
 - X subset of Z.
 - \bullet Y = Z X
 - For a tuple t to appear in the result **T** of the DIVISION, the values in t must appear in **R** in combination with *every* tuple in S.

Figure 8.8 The DIVISION operation. (a) Dividing SSN_PNOS by SMITH_PNOS. (b) $T \leftarrow R \div S$.

(a) SSN_PNOS

Essn	Pno
123456789	1
123456789	2
666884444	3
453453453	1
453453453	2
333445555	2
333445555	3
333445555	10
333445555	20
999887777	30
999887777	10
987987987	10
987987987	30
987654321	30
987654321	20
888665555	20

SMITH_PNOS

Pno
1
2
2

SSNS

Ssn
123456789
453453453

(b)

_	
-	

Α	В
a1	b1
a2	b1
a3	b1
a4	b1
a1	b2
a3	b2
a2	b3
a3	b3
a4	b3
a1	b4

b4

b4

a2

аЗ

_

Α
a1
a2
a3

Т

В
b1
b4

Table 8.1 Operations of Relational Algebra

OPERATION	PURPOSE	NOTATION
SELECT	Selects all tuples that satisfy the selection condition from a relation R .	$\sigma_{< selection\ condition>}(R)$
PROJECT	Produces a new relation with only some of the attributes of <i>R</i> , and removes duplicate tuples.	$\pi_{< ext{attribute list}>}(R)$
THETA JOIN	Produces all combinations of tuples from R_1 and R_2 that satisfy the join condition.	$R_1 \bowtie_{< \text{join condition}>} R_2$
EQUIJOIN	Produces all the combinations of tuples from R_1 and R_2 that satisfy a join condition with only equality comparisons.	$R_1 \bowtie_{< \text{join condition}>} R_2$, OR $R_1 \bowtie_{(< \text{join attributes 1}>)}$, R_2
NATURAL JOIN	Same as EQUIJOIN except that the join attributes of R_2 are not included in the resulting relation; if the join attributes have the same names, they do not have to be specified at all.	$R_1*_{<\text{join condition}>} R_2$, OR $R_1*_{<\text{join attributes 1>}}$, (<join 2="" attributes="">) R_2 OR R_1*_R2</join>
UNION	Produces a relation that includes all the tuples in R_1 or R_2 or both R_1 and R_2 ; R_1 and R_2 must be union compatible.	$R_1 \cup R_2$
INTERSECTION	Produces a relation that includes all the tuples in both R_1 and R_2 ; R_1 and R_2 must be union compatible.	$R_1 \cap R_2$
DIFFERENCE	Produces a relation that includes all the tuples in R_1 that are not in R_2 ; R_1 and R_2 must be union compatible.	$R_1 - R_2$
CARTESIAN PRODUCT	Produces a relation that has the attributes of R_1 and R_2 and includes as tuples all possible combinations of tuples from R_1 and R_2 .	$R_1 \times R_2$
DIVISION	Produces a relation $R(X)$ that includes all tuples $t[X]$ in $R_1(Z)$ that appear in R_1 in combination with every tuple from $R_2(Y)$, where $Z = X \cup Y$.	$R_1(Z) \div R_2(Y)$



Additional Relational Operations:

AGGREGARE FUNCTIONS
OUTER JOIN

Aggregate Function Operation

- ➤ Use of the Aggregate Functional operation F
 - $\mathscr{F}_{MAX \; Salary} \; (EMPLOYEE)$
 - retrieves the maximum salary value from the EMPLOYEE relation
 - $\mathscr{F}_{MIN \; Salary} \; (EMPLOYEE)$
 - retrieves the minimum Salary value from the EMPLOYEE relation
 - $\mathcal{F}_{\text{SUM Salary}}$ (EMPLOYEE)
 - retrieves the sum of the Salary from the EMPLOYEE relation
 - FCOUNT SSN, AVERAGE Salary (EMPLOYEE)
 - computes the count (number) of employees and their average salary
 - Note:
 - Count just counts the number of rows, without removing duplicates
 - Aggregate functions ignore NULL values

Using Grouping with Aggregation

- The previous examples all summarized one or more attributes for a set of tuples
 - Maximum Salary or Count (number of) Ssn
- ➤ Grouping can be combined with Aggregate Functions
- >Example:
 - For <u>each department</u>, retrieve the DNO, COUNT SSN, and AVERAGE SALARY
- A variation of aggregate operation Fallows this:
 - Grouping attribute placed to left of symbol
 - Aggregate functions to right of symbol
 - DNO FCOUNT SSN, AVERAGE Salary (EMPLOYEE)
- Above operation groups employees by DNO (department number) and computes the count of employees and average salary per department

Examples of applying aggregate functions and grouping

R

(a)	Dno	No_of_employees	Average_sal
	5	4	33250
	4	3	31000
	1	1	55000

b)	Dno Count_ssn		Average_salary	
	5	4	33250	
	4	3	31000	
	1	1	55000	

(c)	Count_ssn	Average_salary
	8	35125

Figure 8.10

The aggregate function operation.

- a. $\rho_{R(Dno,\ No_of_employees,\ Average_sal)}(Dno\ \Im\ COUNT\ Ssn,\ AVERAGE\ Salary\ (EMPLOYEE)).$
- b. $_{\text{Dno}}\ \Im$ COUNT Ssn, AVERAGE Salary(EMPLOYEE).
- c. 3 COUNT Ssn, AVERAGE Salary (EMPLOYEE).

Additional Relational Operations: OUTER JOIN

- The OUTER JOIN Operation
 - In NATURAL JOIN and EQUIJOIN, tuples without a *matching* (or *related*) tuple are eliminated from the join result
 - Tuples with null in the join attributes are also eliminated
 - This amounts to loss of information.
 - A set of operations, called OUTER joins, can be used when we want to keep all the tuples in R, or all those in S, or all those in both relations in the result of the join, regardless of whether or not they have matching tuples in the other relation.

Additional Relational Operations: OUTER JOIN

- The **left outer join** operation keeps <u>every tuple</u> in the first or left relation R in R \supset S; if no matching tuple is found in S, then the attributes of S in the join result are filled or "padded" with null values.
- A similar operation, **right outer join**, keeps every tuple in the second or right relation S in the result of R S.
- A third operation, **full outer join**, denoted by keeps all tuples in both the left and the right relations when no matching tuples are found, padding them with null values as needed.

Additional Relational Operations: OUTER JOIN

- <u>Example:</u> list all employee names and also the name of departments they manage if they happen to manage a department. If they do not manage one, use NULL value.
- π FNAME, Minit, LNAME, Dname (EMPLOYEE Ssn=Mgr_ssn DEPARTMENT)

Figure 8.12
The result of a LEFT
OUTER JOIN operation.

RESULT

Fname	Minit	Lname	Dname
John	В	Smith	NULL
Franklin	Т	Wong	Research
Alicia	J	Zelaya	NULL
Jennifer	S	Wallace	Administration
Ramesh	K	Narayan	NULL
Joyce	Α	English	NULL
Ahmad	V	Jabbar	NULL
James	E	Borg	Headquarters



Examples of Queries in Relational Algebra

Examples of Queries in Relational Algebra

 Q1: Retrieve the name and address of all employees who work for the 'Research' department.

```
RESEARCH_DEPT \leftarrow \sigma dname='research' (DEPARTMENT)

RESEARCH_EMPS \leftarrow (RESEARCH_DEPT) \rightarrow dnumber= dno EMPLOYEE)

RESULT \leftarrow \pi fname, lname, address (RESEARCH_EMPS)
```

Q2: Retrieve the names of employees who have no dependents.

```
ALL_EMPS \leftarrow \pi \text{ ssn}(\text{EMPLOYEE})

EMPS_WITH_DEPS(SSN) \leftarrow \pi \text{ essn}(\text{DEPENDENT})

EMPS_WITHOUT_DEPS \leftarrow (\text{ALL\_EMPS - EMPS\_WITH\_DEPS})

RESULT \leftarrow \pi \text{ lname}, fname (EMPS_WITHOUT_DEPS * EMPLOYEE)
```

Examples of Queries in Relational Algebra

As a single expression, these queries become:

• Q1: Retrieve the name and address of all employees who work for the 'Research' department.

```
π Fname, Lname, Address (σ Dname= 'Research' (DEPARTMENT Dnumber=Dno(EMPLOYEE))
```

Q2: Retrieve the names of employees who have no dependents.

```
π Lname, Fname((π Ssn (EMPLOYEE) – ρ Ssn (π Essn(DEPENDENT))) * EMPLOYEE)
```

