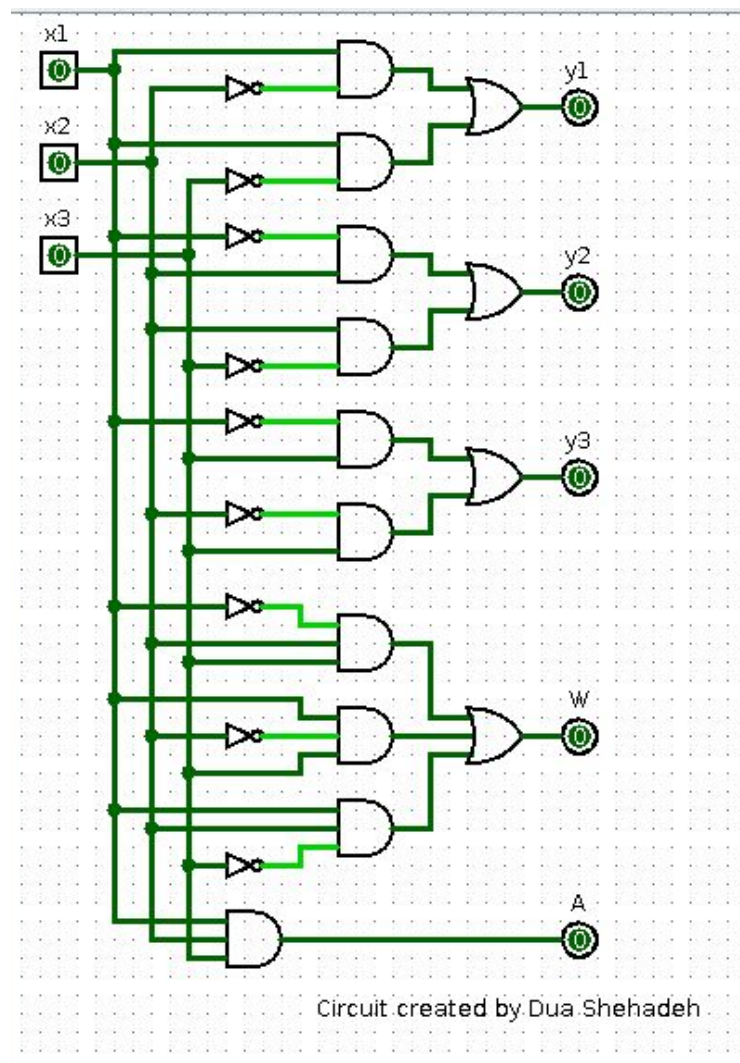


Design Restrictions:

Definition of Y_1 , Y_2 , Y_3 , W , A in terms of X_1 , X_2 and X_3 :

- $Y_n = X_n$ and $W = A = 0$ when one or fewer input signals are high (normal condition, at most one lock is open);
- $Y_n = X_n$, $W = 1$ and $A = 0$ when exactly two input signals are high (warning condition, 2 locks are open);
- $Y_n = 0$, $W = 0$ and $A = 1$ when the river lock operator had moved switches intending for all three locks to open (causing all locks to close and sounding an alarm).

x_1	x_2	x_3	y_1	y_2	y_3	W	A
0	0	0	0	0	0	0	0
0	0	1	0	0	1	0	0
0	1	0	0	1	0	0	0
0	1	1	0	1	1	1	0
1	0	0	1	0	0	0	0
1	0	1	1	0	1	1	0
1	1	0	1	1	0	1	0
1	1	1	0	0	0	0	1



Boolean Functions derived for outputs based on the scenario's specifications:

$$Y_1 = x_1x_2' + x_1x_2x_3'$$

$$Y_2 = x_1'x_2 + x_1x_2x_3'$$

$$Y_3 = x_1'x_3 + x_1x_2x_3'$$

$$W = x_1'x_2x_3 + x_1x_2'x_3 + x_1x_2x_3'$$

$$A = x_1x_2x_3$$

Boolean Function format used: SOP (Sum of product) where ' represents low (0)