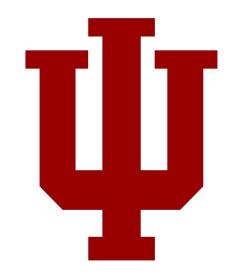
15: Hardware Pipelining II

ENGR 315: Hardware/Software CoDesign

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Indiana University

Some material taken from: https://github.com/trekhleb/homemade-machine-learning/tree/master/homemade/neural_network-http://cs231n.github.io/neural-networks-1/



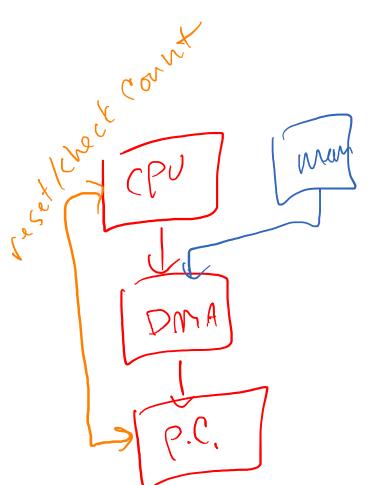
Announcements

• P5 is out

P6 is out (I think)

• Exam in 3 weeks

P5: Adds DMA + AXI-Stream to Popcount



• DMA

 Add DMA engine to move data via AXI4-Full to AXI-Stream interface

Popcount.sv:

- Add AXI-Stream Interface
- Keep AXI4-Lite Interface to read result

Example DMA

https://pynq.readthedocs.io/en/v2.6.1/pynq_libraries/dma.html

```
import numpy as np
from pynq import allocate
from pynq import Overlay
overlay = Overlay('example.bit')
dma = overlay.axi_dma
                                                                       Count (muto)
input_buffer = allocate(shape=(5,), dtype=np.uint32)
output buffer = allocate(shape-(5,), dtype-np.uint32)
for i in range(5):
   input_buffer[i] = i
dma.sendchannel.transfer(input_buffer)
dma-recychannel_transfer(output_buffer)
dma.sendchannel.wait()
-dma.recvchannel.wait()
Output buffer will contain: [0 1 2 3 4]
```

P6 – DMA from C

Start the MM2S channel running by setting the run/stop bit to 1 (MM2S_DMACR.RS =

 The halted bit (DMASR.Halted) should deassert indicating the MM2S channel is running.

2. Skip

- 3. Write a valid source address to the MM2S_SA register.
- 4. Write the number of bytes to transfer in the MM2S_LENGTH register.

 The MM2S_LENGTH register must be written last.
- 5. Poll MM2S_DMASR.Idle bit for completion wat until MM25_DMASR. Tale = (

P7+ Accelerate Machine Learning

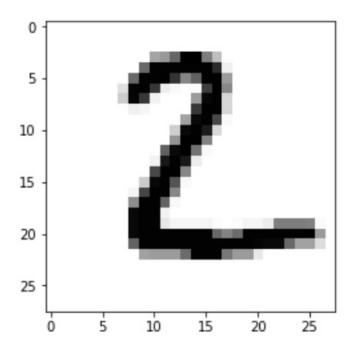
• Goal: Accelerate reference neural network

Harder, more open-ended projects

Groups of 2 allowed.

Simple Neural Network

Index: 0
Image:



ML Classification Result: 2

Real Value: 2

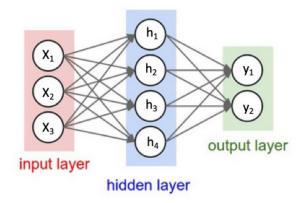
Correct Result: True

Takes in image of number

Returns integer value

• How? artificial neural network

Why Dot Product?



```
# forward-pass of a 3-layer neural network:
f = lambda x: 1.0/(1.0 + np.exp(-x)) # activation function (use sigmoid)
x = np.random.randn(3, 1) # random input vector of three numbers (3x1)
h1 = f(np.dot(W1, x) + b1) # calculate first hidden layer activations (4x1)
h2 = f(np.dot(W2, h1) + b2) # calculate second hidden layer activations (4x1)
out = np.dot(W3, h2) + b3 # output neuron (1x1)
```

Matrix Multiplication (Dot Product)

$$\begin{bmatrix} i_0 & i_1 \end{bmatrix} \times \begin{bmatrix} \omega_{00} & \omega_{10} & \omega_{20} \\ \omega_{01} & \omega_{11} & \omega_{21} \end{bmatrix} = \begin{bmatrix} 0_0 & 0_1 & 0_2 \end{bmatrix}$$

$$\begin{bmatrix} 0_0 & i_0 & \omega_{10} & \omega_{11} \\ 0_0 & i_0 & \omega_{11} & \omega_{21} \end{bmatrix}$$

$$\begin{bmatrix} 0_0 & i_0 & \omega_{10} & i_0 \\ 0_1 & i_0 & \omega_{10} & i_0 \end{bmatrix}$$

$$\begin{bmatrix} 0_1 & i_0 & \omega_{10} & i_0 \\ 0_2 & i_0 & \omega_{20} & i_0 \end{bmatrix}$$

$$\begin{bmatrix} 0_1 & i_0 & \omega_{10} & \omega_{21} \\ 0_0 & i_0 & \omega_{21} \end{bmatrix}$$

Alternative Dot Computations

$$\begin{bmatrix}
0.1 & 0.2 \end{bmatrix} \times \begin{bmatrix}
1 & 2 & 3 \\
4 & 5 & 6
\end{bmatrix} = \begin{bmatrix}
0.9 & 1.2 & 1.5
\end{bmatrix}$$

$$0.1 \cdot 1 & 0.1 \cdot 2 & 0.1 \cdot 3 = \begin{bmatrix}
0.1 & 0.2 & 0.3
\end{bmatrix}$$

$$0.2 \cdot 4 & 0.2 \cdot 5 & 0.2 \cdot 6 = \begin{bmatrix}
0.8 & 1.0 & 1.2
\end{bmatrix}$$

Alternative Dot Computations

$$\begin{bmatrix}
0.1 & 0.2
\end{bmatrix} \times \begin{bmatrix}
1 & 2 & 3\\
4 & 5 & 6
\end{bmatrix} = \begin{bmatrix}
0.9 & 1.2 & 1.5
\end{bmatrix}$$

$$\begin{bmatrix}
0 & 1.1 & 0.1.2 & 0.1.3
\end{bmatrix} + \begin{bmatrix}
0 & 0 & 0
\end{bmatrix} = \begin{bmatrix}
0.1 & 0.2 & 0.3
\end{bmatrix}$$

$$\begin{bmatrix}
0.2.4 & 0.2.5 & 0.2.6 + \begin{bmatrix}
0.1 & 0.2 & 0.3
\end{bmatrix} = \begin{bmatrix}
0.9 & (.2 & 1.5)
\end{bmatrix}$$

11

```
Input Weights Output
[[0.1 0.2 0.3]] . [1. 2. 3. 4.] = [3.8000002 4.4
[5. 6. 7. 8.]
[9. 10. 11. 12.]
```

Alternative Dot

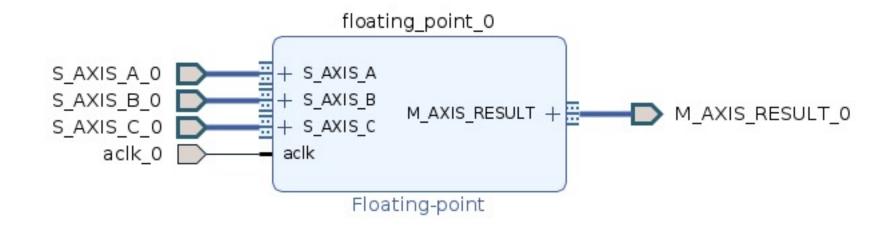
```
# how its done in dot.sv

def pydot(inputs, weights):
    inputs = inputs[0] # remove outer nesting
    outs = np.zeros(weights.shape[1], dtype=np.float32)
    for i in range(weights.shape[0]): # input length
        for j in range(weights.shape[1]): # output length
            outs[j] = outs[j] + weights[i][j] * inputs[i]
    return outs
```

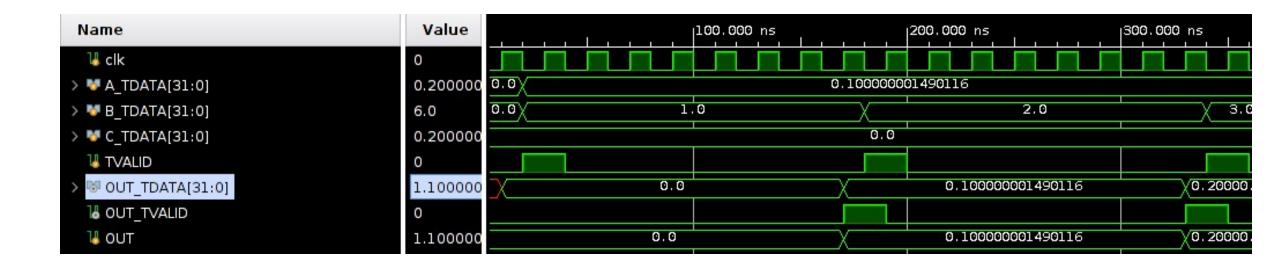
5. 5.6000004]

```
Inputs (Shape):
  (1, 3)
Output (Shape):
  (1, 4)
Weights (Shape):
  (3, 4)
```

Hardware Dot Product



Demo Time



Floating-Point Multiply-Accumulate (FMAC)

• Math: a * b + c 8 cycles

Floating-Point math takes 8 cycles.

Floating-Point is complicated.

How do we work around an 8 cycle latency?

Pipelining!

Pipelining

- FMAC takes 8 cycles for 1 value
- But can accept a new value every cycle.

- Latency: 8 cycles / value
- Throughput: 1 value / cycle

Latency vs. Throughput

 Latency: How long does an individual operation take?

• Throughput: How many operations can you complete in a given time?

Pipelining

Pipelined Dot Computations

$$[0.1 \ 0.2] \times [1 \ 2 \ 3] = [0.9 \ 1.2 \ (.5]$$

Problems with Pipelined FMAC

Latency!

Latency on Pipelined FMAC

• Solution: Stall at the end of a row.

• Drain the pipeline.

Hardware Parallelism

```
• CPU: 1 Floating-Point Unit
• FPGA? (1) Floating-Point Units?
20?
100?
```

Finding Parallelism

 Some some computation that doesn't depend on other computation's results

Shared Inputs are OK.

Next Time: Can we use 2+ FMACs?

reset por count in Hw?

-) reset w/ mmTo

$$\begin{bmatrix}
0.1 & 0.2 & 0.3
\end{bmatrix}
\begin{bmatrix}
1 & 2 & 3 & 4 \\
9 & 10 & 11 & 12
\end{bmatrix}
= \begin{bmatrix}
3.8 & 4.4 & 5 & 5.6
\end{bmatrix}$$

$$\begin{bmatrix}
0.1 & . & [2 & 3 & 4] + [0 & 0 & 0 & 0] = [0.1 & 0.2 & 0.3 & 0.4]
\end{bmatrix}$$

$$0.2 - [5 & 6 & 78] + [0.1 & 0.2 & 0.3 & 0.4] = [1.1 & 1.4 & 1.7 & 2.0]$$

$$0.3 - [9 & 10 & 11 & 1.4 & 1.7 & 2.0] = [3.8 & 4.4 & 5 & 5.6]$$

Parallize Alternative Dot Computations?

[0.1 0.2]
$$\times$$
 [1 2 3] = [0.9 1.2 (.5]
[0 , 0 , 0] c_result
0.1 \cdot [1 23] + [0 0 0] =
[0.1 0.2 03] + [0 0 0] = [0.1 0.2 0.3] = femp
[0.2 \cdot [45 6] + [0.1 0.2 0.3] = [0.9 (.2 (.5])] = [0.

Can we parallelize Dot?

TOIL 0.2 0.3] [1 2 3 4] = [3.8 4.4 5 5.6]
9 WH 12

$$\begin{bmatrix}
 0.1 & 0.2 & 0.3 \\
 5 & 6.7 & 8 \\
 9 & 10 & 11 & 12
 \end{bmatrix} = \begin{bmatrix}
 3.8 & 4.4 & 5 & 5.6 \\
 9 & 10 & 11 & 12
 \end{bmatrix}$$

$$\begin{bmatrix}
6.1 & 0.3 \\
9.101112
\end{bmatrix} = \begin{bmatrix}
2.8 & 3.2 & 3.6 & 4
\end{bmatrix}$$

$$\begin{bmatrix}
6.1 & 0.3 \\
9.101112
\end{bmatrix} = \begin{bmatrix}
1.2 & 1.4 & 1.6
\end{bmatrix}$$

Can we parallelize Dot?

Can we parallelize Dot?

19: Hardware Acceleration III

Engr 315: Hardware / Software Codesign Andrew Lukefahr Indiana University

