

	Bansilal Ramnath Agarwal Charitable Trust's Vishwakarma Institute of Information Technology	
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<b>Semester:</b> V		<b>Academic Year:</b> 2022-23
<b>Subject Name &amp; Code:</b> Design and Analysis of Algorithms		
<b>Title of Assignment:</b> <b>Implement All Pair Shortest paths problem using Floyd's Algorithm.</b>		
<b>Date of Performance:</b>		<b>Date of Submission:</b>

## Aim:

**Implement All Pair Shortest paths problem using Floyd's Algorithm.**

## Problem Statement:

Implement All Pair Shortest paths problem using Floyd's Algorithm.

## Software Requirements:

Text Editor: VSCode, Neovim, etc

Environment: Python 3.10

Terminal Emulator

## Background Information:

### The Floyd Warshall Algorithm:

The Floyd Warshall Algorithm is for solving all pairs shortest path problems. The problem is to find the shortest distances between every pair of vertices in a given edge-weighted directed Graph.

## Algorithm:

- Initialize the solution matrix same as the input graph matrix as a first step.
- Then update the solution matrix by considering all vertices as an intermediate vertex.
- The idea is to one by one pick all vertices and updates all shortest paths which include the picked vertex as an intermediate vertex in the shortest path.
- When we pick vertex number  $k$  as an intermediate vertex, we already have considered vertices  $\{0, 1, 2, \dots, k-1\}$  as intermediate vertices.
- For every pair  $(i, j)$  of the source and destination vertices respectively, there are two possible cases.
- $k$  is not an intermediate vertex in shortest path from  $i$  to  $j$ . We keep the value of  $\text{dist}[i][j]$  as it is.
- $k$  is an intermediate vertex in shortest path from  $i$  to  $j$ . We update the value of  $\text{dist}[i][j]$  as  $\text{dist}[i][k] + \text{dist}[k][j]$  if  $\text{dist}[i][j] > \text{dist}[i][k] + \text{dist}[k][j]$

## Code:

```
main.py
21
20     for k in range(V):
19         for i in range(V):
18             for j in range(V):
17                 dist[i][j] = min(dist[i][j], dist[i][k] + dist[k][j])
16     printSolution(dist)
15
14
13 def printSolution(dist):
12     print(
11         "Following matrix shows the shortest distances between every pair of vertices"
10     )
9     for i in range(V):
8         for j in range(V):
7             if dist[i][j] == INF:
6                 print("%7s" % ("INF"), end=" ")
5             else:
4                 print("%7d\t" % (dist[i][j]), end=" ")
3                 if j == V - 1:
2                     print()
1
30
1 if __name__ == "__main__":
2     graph = [[0, 5, INF, 10], [INF, 0, 3, INF], [INF, INF, 0, 1], [INF, INF, INF, 0]]
3     floydWarshall(graph)
```

## Output:

```
2. Design and Analysis of Algorithm/Assignments/04. All Pair Shortest Path via v3.10.7
> python main.py
Following matrix shows the shortest distances between every pair of vertices
  0      5      3      8      4      9
INF      0      3      1      4
INF     INF      0      1
INF     INF     INF      0

2. Design and Analysis of Algorithm/Assignments/04. All Pair Shortest Path via v3.10.7
> 
```

## Conclusion:

Implemented All Pairs Shortest Path Problem using Floyd Warshall Algorithm.