ECE 351-51

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Lab 4

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1 Introduction

The purpose of this lab was to convolve three functions using the user-defined convolution function from Lab 3 and then comparing it to hand calculations of the functions.

2 Equations

The following signal equations were used to create functions in Python:

$$h1(t) = e^{-2t} * [u(t) - u(t-3)]$$

$$h2(t) = u(t-2) - u(t-6)$$

$$h3(t) = cos(w_0 * t) * u(t) for f_0 = 0.25 Hz$$

The convolutions of the transfer functions and the step function were calculated and the results are given below:

$$y1(t) = 0.5 * [(1 - e^{-2t}) * u(t) - (1 - e^{-2(t-3)}) * u(t-3)]$$

$$y2(t) = r(t-2) * u(t-2) - r(t-6) * u(t-6)$$

$$y3(t) = (1/w) * sin(wt)u(t)$$

3 Methodology

The first part involved plotting the three signals given above from -10 to 10. Listing 1 provides the necessary code for the user-defined functions as well as the ramp and step functions used previously. The plots are seen in the Results section.

```
import numpy as np
import matplotlib.pyplot as plt
import math

def u(t):
    if t < 0:
        return 0
    if t >= 0:
        return 1

def r(t):
    if t < 0:
        return 0
if t >= 0:
        return 1
```

```
return t
16
17 def h1(t):
      y = np.zeros((len(t), 1))
18
      for i in range(len(t)):
19
           y[i] = np.exp(-2*t[i])*(u(t[i])-u(t[i]-3))
20
      return y
21
22
  def h2(t):
23
      y = np.zeros((len(t), 1))
24
      for i in range(len(t)):
25
           y[i] = u(t[i]-2) - u(t[i]-6)
26
      return y
27
28
29 def h3(t):
      f = 0.25
30
      w = f*2*np.pi
31
      y = np.zeros((len(t), 1))
32
      for i in range(len(t)):
33
           y[i] = math.cos(w*t[i]) * u(t[i])
34
      return y
35
37 \text{ steps} = .01
t = np.arange(-10, 10 + steps, steps)
40 y1 = h1(t)
y2 = h2(t)
42 y3 = h3(t)
```

Listing 1: Defining the functions to plot the three signals from -10 < t < 10

The user-defined convolution function is given below in Listing 2. This was used to convolve the transer functions with the step function. Another function was defined to create a step function array.

```
def my_conv(f1, f2):
      Nf1 = len(f1)
                              #variable with the length of f1
      Nf2 = len(f2)
                              #variable with the length of f2
3
      f1Ex = np.append(f1, np.zeros((1, Nf2-1))) #creates an array
     that is the same size as f1 and f2
6
      f2Ex = np.append(f2, np.zeros((1, Nf1-1)))
                                      #creates a zero-filled array
     result = np.zeros(f1Ex.shape)
     the same size as both functions
     for i in range((Nf2+Nf1-2)):
                                      #goes through the length of f1
     and f2
11
         result[i] = 0
```

```
for j in range(Nf1):
                                         #goes through the length of f1
12
               if (i-j+1 > 0):
                                         #makes sure the loop doesn't go
13
      past 0 entries
14
                   try:
                        result[i] = result[i] + f1Ex[j]*f2Ex[i-j+1]
15
      #combines the previous results with the product of the new
     entries
16
                   except:
                        print(i,j)
17
      return result
18
19
20 #step function array
  def u_array(t):
21
      y = np.zeros((len(t), 1))
22
      for i in range(len(t)):
23
          y[i] = u(t[i])
24
      return y
26
t = np.arange(-10, 10 + steps, steps)
128 \text{ time} = 1en(t);
_{29} tEx = np.arange(-20, (2*t[time-1]) + steps, steps)
31 a = my_conv(y1, step)*steps
32 b = my_conv(y2, step)*steps
c = my_conv(y3, step)*steps
```

Listing 2: Convolution and step array functions

```
def c1(t):
      y = np.zeros((len(t),1))
      for i in range(len(t)):
3
          y[i] = 0.5*((1-np.exp(-2*t[i]))*u(t[i]) - ((1-np.exp(-2*t[i]))*u(t[i])
     i]-3)))*u(t[i]-3)))
      return y
  def c2(t):
      y = np.zeros((len(t),1))
      for i in range(len(t)):
9
          y[i] = r(t[i]-2)*u(t[i]-2) - r(t[i]-6)*u(t[i]-6)
11
      return y
12
  def c3(t):
13
      f = 0.25
14
      w = 2*f*np.pi
      y = np.zeros((len(t),1))
      for i in range(len(t)):
17
          y[i] = (1/w)*math.sin(w*t[i])*u(t[i])
18
```

Listing 3: Defining functions for plotting the hand calculations

4 Results

The hand calculations foe the convolutions are shown below:

$$y1(t) = \int_0^t h1(T)u(t-T)dT$$
$$= \int_0^t e^{-2T} * [u(T) - u(T-3)]u(t-T)dT$$
$$= 0.5[(1 - e^{-2t})u(t) - (1 - e^{-2(t-3)})u(t-3)]$$

$$y2(t) = \int_0^t h2(T)u(t-T)dT$$

= $\int_0^t [u(T-2) - u(T-6)]u(t-T)dT$
= $r(t-2)u(t-2) - r(t-6)u(t-6)$

$$y3(t) = \int_0^t h3(T)u(t-T)dT$$
$$= \int_0^t \cos(w_0 * T)u(T)u(t-T)dT$$
$$= (1/w_0)\sin(w_0 * t)u(t)$$

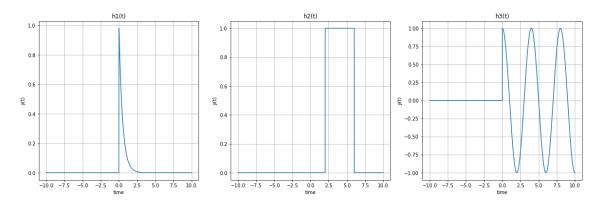


Figure 1: Plots of the three initial given signals

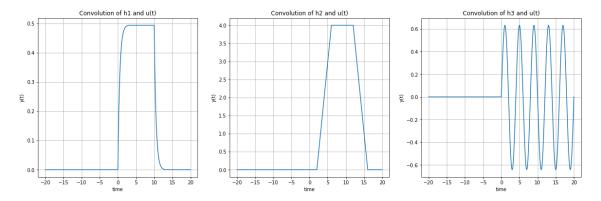


Figure 2: User-defined convolutions of the three signals

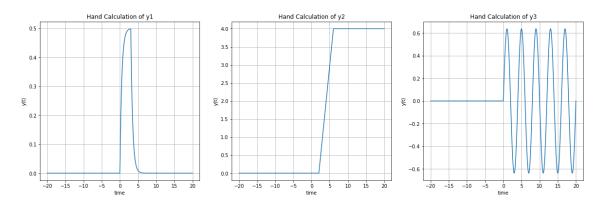


Figure 3: Convolutions using the scipy.signal library

5 Error Analysis

My hand calculation convolution for the first transfer function doesn't look like the user-defined convolution. I tried reworking my equation, but I don't know if my equation itself is wrong, or if there is an error in the Python.

6 Questions

1. Leave any feedback on the clarity of lab tasks, expectations, and deliverables.

Everything was clear on what needed to be done and turned in.

7 Conclusion

A comparison between hand calculated and Python convolution was explored. There was some error on the hand calculation side since the first convolution decreases at a sooner point than the user-defined convolution. There is also some scaling issues with the second hand convolution since compared to the user-defined one. The Python and LATEX code are seen in https://github.com/Eniac618/ECE351_Code and https://github.com/Eniac618/ECE351_Reports respectively.