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# Chapter 1

## Data Structure

### 1.1 Segment Tree

#### 1.1.1 Segment Tree & Lazy Propagation

```
1  class segtree
2  {
3      const static int N=100000;
4      int tr[4*N], lazy[4*N];
5  public:
6      segtree(){};
7      void clear()
8      {
9          memset(tr, 0, sizeof(tr));
10         memset(lazy, 0, sizeof(lazy));
11     }
12     void build(int no, int l, int r, vector<int>&data)
13     {
14         if(l==r)
15         {
16             tr[no]=data[l];
17             return;
18         }
19         int nxt=no*2;
20         int mid=(l+r)/2;
21         build(nxt, l, mid, data);
22         build(nxt+1, mid+1, r, data);
23         tr[no]=tr[nxt]+tr[nxt+1];
24     }
25     void propagate(int no, int l, int r)
26     {
27         if(!lazy[no])
28             return;
29
30         tr[no]+=(r-l+1)*lazy[no];
31         if(l!=r)
32         {
33             int nxt=no*2;
34             lazy[nxt]+=lazy[no];
35             lazy[nxt+1]+=lazy[no];
36         }
37         lazy[no]=0;
38     }
39     void update(int no, int l, int r, int i, int j, int x)
40     {
41         propagate(no, l, r);
42         if(l>j || r<i)
43             return;
44         if(l>=i && r<=j)
45         {
46             lazy[no]=x;
47             propagate(no, l, r);
48             return;
49         }
50         int nxt=no*2;
51         int mid=(l+r)/2;
52         update(nxt, l, mid, i, j, x);
```

```

53         update(nxt+1, mid+1, r, i, j, x);
54         tr[no]=tr[nxt]+tr[nxt+1];
55     }
56     int query(int no, int l, int r, int i, int j)
57     {
58         propagate(no, l, r);
59         if(l>j || r<i)
60             return 0;
61         if(l>=i && r<=j)
62             return tr[no];
63         int nxt=no*2;
64         int mid=(l+r)/2;
65         int ql=query(nxt, l, mid, i, j);
66         int qr=query(nxt+1, mid+1, r, i, j);
67         return (ql+qr);
68     }
69 };

```

### 1.1.2 Quadtree

```

1  class quadtree
2  {
3      //needs to be NxN
4      const static int N=100000;
5      int tr[16*N];
6  public:
7      quadtree(){};
8      void build(int node, int l1, int r1, int l2, int r2, vector< vector<int> >data)
9      {
10         if(l1==l2 && r1==r2)
11         {
12             tr[node]=data[l1][r1];
13             return;
14         }
15         int nxt=node*4;
16         int midl=(l1+l2)/2;
17         int midr=(r1+r2)/2;
18
19         build(nxt-2, l1, r1, midl, midr, data);
20         build(nxt-1, midl+1, r1, l2, midr, data);
21         build(nxt, l1, midr+1, midl, r2, data);
22         build(nxt+1, midl+1, midr+1, l2, r2, data);
23
24         tr[node]=tr[nxt-2]+tr[nxt-1]+tr[nxt]+tr[nxt+1];
25     }
26     void update(int node, int l1, int r1, int l2, int r2, int i, int j, int x)
27     {
28         if(l1>l2 || r1>r2)
29             return;
30         if(i>l2 || j>r2 || i<l1 || j<r1)
31             return;
32         if(i==l1 && i==l2 && j==r1 && j==r2)
33         {
34             tr[node]=x;
35             return;
36         }
37         int nxt=node*4;
38         int midl=(l1+l2)/2;
39         int midr=(r1+r2)/2;
40
41         update(nxt-2, l1, r1, midl, midr, i, j, x);
42         update(nxt-1, midl+1, r1, l2, midr, i, j, x);
43         update(nxt, l1, midr+1, midl, r2, i, j, x);
44         update(nxt+1, midl+1, midr+1, l2, r2, i, j, x);
45
46         tr[node]=tr[nxt-2]+tr[nxt-1]+tr[nxt]+tr[nxt+1];
47     }
48     int query(int node, int l1, int r1, int l2, int r2, int i1, int j1, int i2, int j2)
49     {
50         if(i1>l2 || j1>r2 || i2<l1 || j2<r1 || i1>i2 || j1>j2)
51             return 0;
52         if(i1<=l1 && j1<=r1 && l2<=i2 && r2<=j2)
53             return tr[node];
54         int nxt=node*4;
55         int midl=(l1+l2)/2;
56         int midr=(r1+r2)/2;
57
58         int q1=query(nxt-2, l1, r1, midl, midr, i1, j1, i2, j2);

```

```

59         int q2=query(nxt-1, midl+1, r1, l2, midr, i1, j1, i2, j2);
60         int q3=query(nxt, l1, midr+1, midl, r2, i1, j1, i2, j2);
61         int q4=query(nxt+1, midl+1, midr+1, l2, r2, i1, j2, i2, j2);
62     }
63 };

```

### 1.1.3 Mergesort Segtree

```

1  class mergesort_segtree
2  {
3      const static int N=100000;
4      vector<int>tr [4*N];
5  public:
6      mergesort_segtree() {};
7      void build(int no, int l, int r, vector<int>&data)
8      {
9          if(l==r)
10         {
11             tr[no].push_back(data[l]);
12             return;
13         }
14         int nxt=no*2;
15         int mid=(l+r)/2;
16         build(nxt, l, mid, data);
17         build(nxt+1, mid+1, r, data);
18         tr[no].resize(tr[nxt].size()+tr[nxt+1].size());
19         merge(tr[nxt].begin(), tr[nxt].end(), tr[nxt+1].begin(), tr[nxt+1].end(), tr[no].begin());
20     }
21     //how many numbers in (i, j) are greater or equal than k
22     int query(int no, int l, int r, int i, int j, int k)
23     {
24         if(r<i || l>j)
25             return 0;
26         if(l>=i && r<=j)
27             return (int)(tr[no].end()-upper_bound(tr[no].begin(), tr[no].end(), k));
28         int nxt=no*2;
29         int mid=(l+r)/2;
30         int ql=query(nxt, l, mid, i, j, k);
31         int qr=query(nxt+1, mid+1, r, i, j, k);
32         return ql+qr;
33     }
34 };

```

### 1.1.4 Persistent Segtree

```

1  class persistent_segtree
2  {
3      const static int N=100000;
4      int n;
5      int tr[N];
6      int root[N], L[N], R[N];
7      int cnt, id;
8  public:
9      persistent_segtree() {};
10     void set(int _n)
11     {
12         memset(tr, 0, sizeof(tr));
13         memset(root, 0, sizeof(root));
14         memset(L, 0, sizeof(L));
15         memset(R, 0, sizeof(R));
16         id=0;
17         cnt=1;
18         n=_n;
19     }
20     void build(int no, int l, int r, vector<int>&data)
21     {
22         if(l==r)
23         {
24             tr[no]=data[l];
25             return;
26         }
27         int mid=(l+r)/2;
28         L[no]=cnt++;
29         R[no]=cnt++;
30         build(L[no], l, mid, data);
31         build(R[no], mid+1, r, data);
32         tr[no]=tr[ L[no] ]+tr[ R[no] ];

```

```

33     }
34     int update(int no, int l, int r, int i, int x)
35     {
36         int newno=cnt++;
37         tr[newno]=tr[no];
38         L[newno]=L[no];
39         R[newno]=R[no];
40         if(l==r)
41         {
42             tr[newno]=x;
43             return newno;
44         }
45         int mid=(l+r)/2;
46         if(i<=mid)
47             L[newno]=update(L[newno], l, mid, i, x);
48         else
49             R[newno]=update(R[newno], mid+1, r, i, x);
50         tr[newno]=tr[ L[newno] ]+tr[ R[newno] ];
51         return newno;
52     }
53     int query(int no, int l, int r, int i, int j)
54     {
55         if(r<i || l>j)
56             return 0;
57         if(l>=i && r<=j)
58             return tr[no];
59         int mid=(l+r)/2;
60         int ql=query(L[no], l, mid, i, j);
61         int qr=query(R[no], mid+1, r, i, j);
62         return ql+qr;
63     }
64     //update the i-th value to x.
65     void update(int i, int x)
66     {
67         root[id+1]=update(root[id], 0, n-1, i, x);
68     }
69     //returns sum(l, r) after the k-th update.
70     int query(int l, int r, int k)
71     {
72         return query(root[k], 0, n-1, l, r);
73     }
74 };

```

## 1.2 Fenwick Tree

### 1.2.1 Fenwick Tree 1D

```

1  class fenwicktree
2  {
3      #define D(x) x&(-x)
4      const static int N=100000;
5      int tr[N], n;
6  public:
7      fenwicktree(){};
8      void build(int _n)
9      {
10         n=_n;
11         memset(tr, 0, sizeof(tr));
12     }
13     void update(int i, int x)
14     {
15         for(i++; i<=n; i+=D(i))
16             tr[i]+=x;
17     }
18     int query(int i)
19     {
20         int ret=0;
21         for(i++; i>0; i-=D(i))
22             ret+=tr[i];
23         return ret;
24     }
25     int rquery(int l, int r)
26     {
27         return query(r)-query(l-1);
28     }
29     void set(int i, int x)
30     {

```

```

31         update(i, -rquery(i, i)+x);
32     }
33     void rset(int l, int r, int x)
34     {
35         update(l, x);
36         update(r+1, -x);
37     }
38 };

```

## 1.2.2 Fenwick Tree 2D

```

1  class fenwicktree
2  {
3      #define D(x) x&(-x)
4      const static int N=1000;
5      int tr[N][N], n, m;
6  public:
7      fenwicktree(){};
8      void build(int _n, int _m)
9      {
10         n=_n, m=m;
11         memset(tr, 0, sizeof(tr));
12     }
13     void update(int r, int c, int x)
14     {
15         for(int i=r+1; i<=n; i+=D(i))
16             for(int j=c+1; j<=m; j+=D(j))
17                 tr[i][j]+=x;
18     }
19     int query(int r, int c)
20     {
21         int ret=0;
22         for(int i=r+1; i>0; i-=D(i))
23             for(int j=c+1; j>0; j-=D(j))
24                 ret+=tr[i][j];
25         return ret;
26     }
27     int rquery(int r1, int c1, int r2, int c2)
28     {
29         if((r1>r2 && c1>c2) || (r1==r2 && c1>c2) || (r1>r2 && c1==c2))
30         {
31             swap(r1, r2);
32             swap(c1, c2);
33         }
34         else if(r1<r2 && c1>c2)
35         {
36             swap(c1, c2);
37         }
38         else if(r1>r2 && c1<c2)
39         {
40             swap(r1, r2);
41         }
42         return query(r2, c2)-query(r1-1, c2)-query(r2, c1-1)+query(r1-1, c1-1);
43     }
44     void set(int r, int c, int x)
45     {
46         update(r, c, -rquery(r, c, r, c)+x);
47     }
48 };

```

## 1.3 Cartesian Tree

### 1.3.1 Cartesian Tree

```

1  //srand(time(NULL))
2  int vrand()
3  {
4      return abs(rand())<<(rand()%31);
5  }
6
7  struct node
8  {
9      //x=key, y=priority key, c=tree count
10     int x, y, c;
11     node *L, *R;
12     node(){};

```

```

13     node(int _x)
14     {
15         x=_x, y=vrand(), c=0;
16         L=R=NULL;
17     }
18 };
19
20 int cnt(node *root)
21 {
22     return root?root->c:0;
23 }
24
25 void upd_cnt(node *root)
26 {
27     if(root)
28         root->c=1+cnt(root->L)+cnt(root->R);
29 }
30
31 void split(node *root, int x, node *&L, node *&R)
32 {
33     if(!root)
34         L=R=NULL;
35     else if(x < root->x)
36         split(root->L, x, L, root->L), R=root;
37     else
38         split(root->R, x, root->R, R), L=root;
39     upd_cnt(root);
40 }
41
42 void insert(node *&root, node *it)
43 {
44     if(!root)
45         root=it;
46     else if(it->y > root->y)
47         split(root, it->x, it->L, it->R), root=it;
48     else
49         insert(it->x < root->x? root->L:root->R, it);
50     upd_cnt(root);
51 }
52
53 void merge(node *&root, node *L, node *R)
54 {
55     if(!L || !R)
56         root=L?L:R;
57     else if(L->y > R->y)
58         merge(L->R, L->R, R), root=L;
59     else
60         merge(R->L, L, R->L), root=R;
61     upd_cnt(root);
62 }
63
64 void erase(node *&root, int x)
65 {
66     if(root->x==x)
67         merge(root, root->L, root->R);
68     else
69         erase(x < root->x? root->L:root->R, x);
70     upd_cnt(root);
71 }
72
73 node *unite(node *L, node *R)
74 {
75     if(!L || !R)
76         return L?L:R;
77     if(L->y < R->y)
78         swap(L, R);
79     node *Lt, *Rt;
80     split(R, L->x, Lt, Rt);
81     L->L=unite(L->L, Lt);
82     L->R=unite(L->R, Rt);
83     return L;
84 }
85
86 int find(node *root, int x)
87 {
88     if(!root)
89         return 0;
90     if(root->x==x)
91         return 1;

```



```

92         if(x > root->x)
93             return find(root->R, x);
94         else
95             return find(root->L, x);
96     }
97
98     int findkth(node *root, int x)
99     {
100         if(!root)
101             return -1;
102         int Lc=cnt(root->L);
103         if(x-Lc-1==0)
104             return root->x;
105         if(x>Lc)
106             return findkth(root->R, x-Lc-1);
107         else
108             return findkth(root->L, x);
109     }

```

### 1.3.2 Implicit Cartesian Tree

```

1  //srand(time(NULL))
2  int vrand()
3  {
4      return abs(rand())<<(rand()%31);
5  }
6
7  struct node
8  {
9      //basic treap: x=key, y=priority key, c=tree count;
10     int x, y, c;
11     //treap operations: v=max(x), lazy=lazy value of propagation, rev=reversed
12     int v, lazy, rev;
13
14     node *L, *R;
15     node(){};
16     node(int _x)
17     {
18         x=_x, y=vrand();
19         L=R=NULL;
20         v=x;
21         lazy=0;
22         rev=0;
23     }
24 };
25
26 //updating functions
27 inline int get_cnt(node *root)
28 {
29     return root?root->c:0;
30 }
31
32 inline void upd_cnt(node *root)
33 {
34     if(root)
35         root->c=1+get_cnt(root->L)+get_cnt(root->R);
36 }
37
38 inline void push(node *&root)
39 {
40     if(root && root->rev)
41     {
42         root->rev=0;
43         swap(root->L, root->R);
44         if(root->L)
45             root->L->rev^=1;
46         if(root->R)
47             root->R->rev^=1;
48     }
49 }
50
51 inline void propagate(node *&root)
52 {
53     if(root)
54     {
55         if(!root->lazy)
56             return;
57         int lazy=root->lazy;

```

```

58         root->x+=lazy;
59
60         if (root->L)
61             root->L->lazy=lazy;
62         if (root->R)
63             root->R->lazy=lazy;
64         root->lazy=0;
65     }
66 }
67
68 inline int get_max(node *root)
69 {
70     return root?root->v:-INF;
71 }
72
73 inline void upd_max(node *root)
74 {
75     if (root)
76         root->v=max(root->x, max(get_max(root->L), get_max(root->R)));
77 }
78
79 inline void update(node *root)
80 {
81     propagate(root);
82     upd_cnt(root);
83     upd_max(root);
84 }
85
86 void merge(node *&root, node *L, node *R)
87 {
88     push(L);
89     push(R);
90     if (!L || !R)
91         root=L?L:R;
92     else if (L->y > R->y)
93         merge(L->R, L->R, R), root=L;
94     else
95         merge(R->L, L, R->L), root=R;
96     update(root);
97 }
98
99 void split(node *root, node *&L, node *&R, int x, int add=0)
100 {
101     if (!root)
102         return void(L=R=NULL);
103     push(root);
104     int ix=add+get_cnt(root->L); //implicit key
105     if (x<=ix)
106         split(root->L, L, root->L, x, add), R=root;
107     else
108         split(root->R, root->R, R, x, add+1+get_cnt(root->L)), L=root;
109     update(root);
110 }
111
112 //insert function
113 void insert(node *&root, int pos, int x)//(insert x at position pos)
114 {
115     node *R1, *R2;
116     split(root, R1, R2, pos);
117     merge(R1, R1, new node(x));
118     merge(root, R1, R2);
119 }
120
121 //erase value x
122 void erase_x(node *&root, int x)
123 {
124     if (!root)
125         return;
126     if (root->x==x)
127         merge(root, root->L, root->R);
128     else
129         erase_x(x < root->x? root->L:root->R, x);
130     update(root);
131 }
132
133 //erase kth value
134 void erase_kth(node *&root, int x)
135 {
136     if (!root)

```

```

137         return;
138         int Lc=get_cnt(root->L);
139         if(x-Lc-1==0)
140             merge(root, root->L, root->R);
141         else if(x>Lc)
142             erase_kth(root->R, x-Lc-1);
143         else
144             erase_kth(root->L, x);
145         update(root);
146     }
147
148     //add x to [l,r]
149     inline void paint(node *&root, int l, int r, int x)
150     {
151         node *R1, *R2, *R3;
152         split(root, R1, R2, l);
153         split(R2, R2, R3, r-l+1);
154         R2->lazy=x;
155         propagate(R2);
156
157         merge(root, R1, R2);
158         merge(root, root, R3);
159     }
160
161     //max range query [l,r]
162     inline int rquery(node *&root, int l, int r)
163     {
164         node *R1, *R2, *R3;
165         split(root, R1, R2, l);
166         split(R2, R2, R3, r-l+1);
167         int ret=R2->v;
168         merge(root, R1, R2);
169         merge(root, root, R3);
170         return ret;
171     }
172
173     inline void reverse(node *&root, int l, int r)//reverse elements [l, r]
174     {
175         node *R1, *R2, *R3;
176         split(root, R1, R2, l);
177         split(R2, R2, R3, r-l+1);
178         R2->rev^=1;
179         merge(root, R1, R2);
180         merge(root, root, R3);
181     }
182
183     //output functions
184     int poscnt=0;
185     void output_all(node *root)
186     {
187         if(!root)
188             return;
189         update(root);
190         push(root);
191         output_all(root->L);
192         printf("[%d]_%d\n", poscnt++, root->x);
193         output_all(root->R);
194     }
195
196     int output_kth(node *root, int x)
197     {
198         if(!root)
199             return -1;
200         update(root);
201         push(root);
202         int Lc=get_cnt(root->L);
203         if(x-Lc-1==0)
204             return root->x;
205         if(x>Lc)
206             return output_kth(root->R, x-Lc-1);
207         else
208             return output_kth(root->L, x);
209     }

```

## 1.4 Merge Sort & Swap Count

### 1.4.1 Merge Sort & Vector

```
1 #define INF 0x3F3F3F3F
2 int mergesort(vector<int>&data)
3 {
4     if(data.size()==1)
5         return 0;
6     vector<int>L, R;
7     int t=data.size();
8     for(int i=0; i<t/2; i++)
9         L.push_back(data[i]);
10    for(int i=t/2; i<t; i++)
11        R.push_back(data[i]);
12    int ret=mergesort(L)+mergesort(R);
13    for(int i=0, j=0, k=0; j<L.size() || k<R.size(); i++)
14    {
15        int x=j<L.size()?L[j]:INF;
16        int y=k<R.size()?R[k]:INF;
17        if(x<y)
18        {
19            data[i]=x;
20            j++;
21        }
22        else
23        {
24            data[i]=y;
25            k++;
26            ret+=(L.size()-j);
27        }
28    }
29    return ret;
30 }
```

### 1.4.2 Merge Sort

```
1 #define INF 0x3F3F3F3F
2 int temp[100000];
3 int mergesort(int data[], int l, int r)
4 {
5     if(abs(l-r)<=1)
6         return 0;
7     int mid=(l+r)/2;
8     int ret=mergesort(data, l, mid)+mergesort(data, mid, r);
9     for(int i=l; i<r; i++)
10        temp[i]=data[i];
11    for(int i=l, j=l, k=mid; j<mid || k<r; i++)
12    {
13        int x=j<mid?temp[j]:INF;
14        int y=k<r?temp[k]:INF;
15        if(x<y)//x<=y
16        {
17            data[i]=x;
18            j++;
19        }
20        else
21        {
22            data[i]=y;
23            k++;
24            ret+=(mid-j);
25        }
26    }
27    return ret;
28 }
```

## 1.5 Sparse Table

```
1 class sparsetable
2 {
3     #define lbit(x) 63-__builtin_clzll(x);
4     const static int N=100000, LN=20;
5     int data[N][LN], n, ln;
6 public:
7     sparsetable(){};
```

```

8         void clear()
9         {
10             memset(data, 0, sizeof(data));
11         }
12         void build(vector<int>&foo)
13         {
14             n=foo.size();
15             ln=lbit(n);
16             for(int i=0; i<n; i++)
17                 data[i][0]=foo[i];
18             for(int j=1; j<=ln; j++)
19                 for(int i=0; i<n-(1<<j)+1; i++)
20                     data[i][j]=max(data[i][j-1], data[i+(1<<(j-1))][j-1]);
21         }
22         int query(int l, int r)
23         {
24             int i=abs(l-r)+1;
25             int j=lbit(i);
26             return max(data[l][j], data[l-(1<<j)+1][j]);
27         }
28     };

```

## 1.6 SQRT Decomposition

### 1.6.1 Array

```

1  const int N=100000;
2  int SN=sqrt(N);
3
4  class mo
5  {
6  public:
7      int l, r, i;
8      mo(){};
9      mo(int _l, int _r, int _i)
10     {
11         l=_l, r=_r, i=_i;
12     }
13     bool operator <(const mo &foo) const
14     {
15         if((r/SN)!=(foo.r/SN))
16             return (r/SN)<(foo.r/SN);
17         if(l!=foo.l)
18             return l<foo.l;
19         return i<foo.i;
20     }
21 };
22
23 int data[N], freq[N], ans[N];
24 int cnt=0;
25 void update(int p, int s)
26 {
27     int x=data[p];
28     if(s==1)
29     {
30         if(freq[x]==0)
31             cnt++;
32     }
33     else
34     {
35         if(freq[x]==1)
36             cnt--;
37     }
38     freq[x]+=s;
39 }
40
41 int main()
42 {
43     int n;
44     scanf("%d", &n);
45     for(int i=1; i<=n; i++)
46         scanf("%d", &data[i]);
47
48     int q;
49     scanf("%d", &q);
50     vector<mo>querys;
51     for(int i=0; i<q; i++)

```

```

52     {
53         int l, r;
54         scanf("%d%d", &l, &r);
55         queries.push_back(mo(l, r, i));
56     }
57     sort(queries.begin(), queries.end());
58
59     int l=1, r=1;
60     cnt=0;
61     memset(freq, 0, sizeof(freq));
62     update(l, 1);
63     for(int i=0; i<q; i++)
64     {
65         int li=queries[i].l;
66         int ri=queries[i].r;
67         int ii=queries[i].i;
68         while(l>li)
69             update(--l, 1);
70         while(r<ri)
71             update(++r, 1);
72         while(l<li)
73             update(l++, -1);
74         while(r>ri)
75             update(r--, -1);
76         ans[ii]=cnt;
77     }
78     for(int i=0; i<queries.size(); i++)
79         printf("%d\n", ans[i]);
80     return 0;
81 }

```

## 1.6.2 Tree

```

1  #define pb push_back
2  #define ALL(x) x.begin(), x.end()
3
4  const int N=1e+5+35;
5  const int M=20;
6  const int SN=sqrt(2*N)+1;
7
8  class mo
9  {
10 public:
11     int l, r, i, lc;
12     mo() {};
13     mo(int _l, int _r, int _lc, int _i)
14     {
15         l=_l, r=_r, lc=_lc, i=_i;
16     }
17     bool operator <(const mo &foo) const
18     {
19         if((r/SN) != (foo.r/SN))
20             return (r/SN) < (foo.r/SN);
21         if(l != foo.l)
22             return l < foo.l;
23         return i < foo.i;
24     }
25 };
26
27 int n, q;
28 int h[N], lca[N][M];
29 vector<int> g[N];
30 int dl[N], dr[N], di[2*N], cur;
31
32 void dfs(int u, int p)
33 {
34     dl[u] = ++cur;
35     di[cur] = u;
36     lca[u][0] = p;
37     for(int i=1; i<M; i++)
38         lca[u][i] = lca[lca[u][i-1]][i-1];
39     for(int i=0; i<g[u].size(); i++)
40     {
41         int v = g[u][i];
42         if(v == p)
43             continue;
44         h[v] = h[u] + 1;
45         dfs(v, u);

```

```

46     }
47     dr[u]++;cur;
48     di[cur]=u;
49 }
50
51 inline int getLca(int u, int v)
52 {
53     if(h[u]>h[v])
54         swap(u, v);
55     for(int i=M-1; i>=0; i--)
56         if(h[v]-(1<<i)>=h[u])
57             v=lca[v][i];
58     if(u==v)
59         return u;
60     for(int i=M-1; i>=0; i--)
61     {
62         if(lca[u][i]!=lca[v][i])
63         {
64             u=lca[u][i];
65             v=lca[v][i];
66         }
67     }
68     return lca[u][0];
69 }
70
71 map<string,int>remap;
72 int data[N], ans[N], vis[N], freq[N], cnt;
73 inline void update(int u)
74 {
75     int x=data[u];
76     if(vis[u] && (---freq[ data[u] ]==0))
77         cnt--;
78     else if(!vis[u] && (freq[ data[u] ]++==0))
79         cnt++;
80     vis[u]^=1;
81 }
82
83 int main()
84 {
85     scanf("%d_%d", &n, &q);
86     for(int i=1; i<=n; i++)
87     {
88         char temp[25];
89         scanf("%s", temp);
90         string temp2=string(temp);
91         if(!remap.count(temp2))
92             remap[temp2]=remap.size();
93         data[i]=remap[temp2];
94     }
95     for(int i=1; i<n; i++)
96     {
97         int u, v;
98         scanf("%d_%d", &u, &v);
99         g[u].pb(v);
100        g[v].pb(u);
101    }
102    dfs(1, 0);
103
104    vector<mo>query;
105    for(int i=0; i<q; i++)
106    {
107        int u, v;
108        scanf("%d_%d", &u, &v);
109        int lc=getLca(u, v);
110        if(dl[u]>dl[v])
111            swap(u, v);
112        query.pb(mo(u==lc?dl[u]:dr[u], dl[v], lc, i));
113    }
114    sort(ALL(query));
115
116    int l=query[0].l, r=query[0].l-1;
117    cnt=0;
118    for(int i=0; i<q; i++)
119    {
120        int li=query[i].l;
121        int ri=query[i].r;
122        int lc=query[i].lc;
123        int ii=query[i].i;
124        while(l>li)

```

```
125         update(di[--l]);
126     while(r<ri)
127         update(di[++r]);
128     while(l<li)
129         update(di[l++]);
130     while(r>ri)
131         update(di[r--]);
132
133     int u=di[l], v=di[r];
134     if(lc!=u && lc!=v)
135         update(lc);
136     ans[ii]=cnt;
137     if(lc!=u && lc!=v)
138         update(lc);
139 }
140 for(int i=0; i<q; i++)
141     printf("%d\n", ans[i]);
142 return 0;
143 }
```



# Chapter 2

## Graph

### 2.1 Components

#### 2.1.1 Articulations, Bridges & Cycles

#### 2.1.2 Strongly Connected Components

#### 2.1.3 Semi-Strongly Connected Components

### 2.2 Single Source Shortest Path

#### 2.2.1 Dijkstra

#### 2.2.2 Bellmanford

### 2.3 All Pairs Shortest Path

#### 2.3.1 Floyd Warshall

### 2.4 Minimum Spannig Tree

#### 2.4.1 Kruskal

#### 2.4.2 Prim

### 2.5 Flow

#### 2.5.1 Maximum Bipartite Matching

```
1  const int MN=1e+3;
2  vector<int>g[MN];
3  int match[MN], rmatch[MN], vis[MN];
4  int findmatch(int u)
5  {
6      if(vis[u])
7          return 0;
8      vis[u]=true;
9      for(int v:g[u])
10     {
11         if(match[v]==-1 || findmatch(match[v]))
12             {
13                 match[v]=u;
14                 rmatch[u]=v;
15                 return 1;
16             }
```

```

16         }
17     }
18     return 0;
19 }
20
21 int maxMatch(int n)
22 {
23     int ret=0;
24     memset(match, -1, sizeof(match));
25     for(int i=0; i<n; i++)
26     {
27         memset(vis, false, sizeof(vis));
28         ret+=findmatch(i);
29     }
30     return ret;
31 }

```

## 2.5.2 Maximum Flow

### Dinic

```

1  class graph
2  {
3      const static int N=100000;
4  public:
5      vector< pair<int,int> >edge;
6      vector<int>adj[N];
7      int ptr[N];
8      int dist[N];
9
10     graph(){};
11     void clear()
12     {
13         for(int i=0; i<N; i++)
14             adj[i].clear();
15         edge.clear();
16     }
17     void add_edge(int u, int v, int c)
18     {
19         adj[u].push_back(edge.size());
20         edge.push_back(mp(v, c));
21         adj[v].push_back(edge.size());
22         edge.push_back(mp(u, 0)); //(u, c) if is non-directed
23     }
24     bool dinic_bfs(int s, int t)
25     {
26         memset(dist, -1, sizeof(dist));
27         dist[s]=0;
28
29         queue<int>bfs;
30         bfs.push(s);
31         while(!bfs.empty() && dist[t]==-1)
32         {
33             int u=bfs.front();
34             bfs.pop();
35             for(int i=0; i<adj[u].size(); i++)
36             {
37                 int idx=adj[u][i];
38                 int v=edge[idx].F;
39
40                 if(dist[v]==-1 && edge[idx].S>0)
41                 {
42                     dist[v]=dist[u]+1;
43                     bfs.push(v);
44                 }
45             }
46         }
47         return dist[t]!=-1;
48     }
49     int dinic_dfs(int u, int t, int flow)
50     {
51         if(u==t)
52             return flow;
53         for(int &i=ptr[u]; i<adj[u].size(); i++)
54         {
55             int idx=adj[u][i];
56             int v=edge[idx].F;
57             if(dist[v]==dist[u]+1 && edge[idx].S>0)

```

```

58         {
59             int cf=dinic_dfs(v, t, min(flow, edge[idx].S));
60             if(cf>0)
61             {
62                 edge[idx].S-=cf;
63                 edge[idx^1].S+=cf;
64                 return cf;
65             }
66         }
67     }
68     return 0;
69 }
70 int maxflow(int s, int t)
71 {
72     int ret=0;
73     while(dinic_bfs(s, t))
74     {
75         memset(ptr, 0, sizeof(ptr));
76         int cf=dinic_dfs(s, t, INF);
77         if(cf==0)
78             break;
79         ret+=cf;
80     }
81     return ret;
82 }
83 };

```

### 2.5.3 Minimum Cost Maximum Flow

#### Dijkstra

```

1  /*
2  undirected graph:
3  u->uu(flow, 0)
4  uu->vv(flow, cost)
5  vv->v(flow, 0)
6  v->xx(flow, 0)
7  vv->u(flow, 0)
8  */
9  typedef int FTYPE; //type of flow
10 typedef int CTYPE; //type of cost
11 typedef pair<FTYPE,CTYPE>pfc;
12 const CTYPE CINF=INF;
13 const FTYPE FINF=INF;
14
15 void operator+=(pfc &p1, pfc &p2)
16 {
17     p1.F+=p2.F;
18     p1.S+=p2.S;
19 }
20
21 class graph
22 {
23     const static int MN=1e+4;
24 public:
25     int n;
26     FTYPE flow[MN];
27     CTYPE dist[MN], pot[MN];
28     int prev[MN], eidx[MN];
29
30     struct Edge
31     {
32         int to;
33         FTYPE cap;
34         CTYPE cost;
35         Edge(){};
36         Edge(int _to, FTYPE _cap, CTYPE _cost)
37         {
38             to=_to;
39             cap=_cap;
40             cost=_cost;
41         }//
42     };
43     struct node
44     {
45         int u;
46         CTYPE d;
47         node(){};

```

```

48         node(int _u, CTYPE _d)
49     {
50         u=_u;
51         d=_d;
52     }
53     bool operator <(const node &foo) const
54     {
55         return d>foo.d;
56     }
57 };
58 graph(){};
59 vector<int>adj[MN];
60 vector<Edge>edge;
61 inline void set(int _n)
62 {
63     n=_n;
64 }
65 inline void reset()
66 {
67     for(int i=0; i<MN; i++)
68         adj[i].clear();
69     edge.clear();
70 }
71 inline void add_edge(int u, int v, FTYPE c, FTYPE cst)
72 {
73     adj[u].push_back(edge.size());
74     edge.push_back(Edge(v, c, cst));
75     adj[v].push_back(edge.size());
76     edge.push_back(Edge(u, 0, -cst));
77 }
78
79 pfc dijkstra(int s, int t)
80 {
81     for(register int i=0; i<n; i++)
82         dist[i]=CINF;
83     dist[s]=0;
84     flow[s]=FINF;
85     priority_queue<node>heap;
86     heap.push(node(s, 0));
87     while(!heap.empty())
88     {
89         int u=heap.top().u;
90         CTYPE d=heap.top().d;
91         heap.pop();
92         if(d>dist[u])
93             continue;
94         for(int i=0; i<adj[u].size(); i++)
95         {
96             int idx=adj[u][i];
97             int v=edge[idx].to;
98             CTYPE w=edge[idx].cost;
99             if(!edge[idx].cap || dist[v]<=d+w+pot[u]-pot[v])
100                 continue;
101             if(d+w<dist[v])
102             {
103                 dist[v]=d+w;
104                 prev[v]=u;
105                 eidv[idx]=idx;
106                 flow[v]=min(flow[u], edge[idx].cap);
107                 heap.push(node(v, d+w));
108             }
109         }
110     }
111     if(dist[t]==CINF)
112         return mp(FINF, CINF);
113     pfc ret=mp(flow[t], 0);
114     for(int u=t; u!=s; u=prev[u])
115     {
116         int idx=eidx[u];
117         edge[idx].cap-=flow[t];
118         edge[idx^1].cap+=flow[t];
119         ret.second+=flow[t]*edge[idx].cost;
120     }
121     return ret;
122 }
123
124 inline pfc mfmc(int s, int t)
125 {
126     pfc ret=mp(0, 0);

```

```

127         pfc got;
128         while((got=dijkstra(s, t)).first!=FINF)
129             ret+=got;
130         return ret;
131     }
132 };

```

## Bellmanford

### 2.5.4 Minimum Cut

## 2.6 Tree

### 2.6.1 Lowest Common Ancestor

### 2.6.2 Centroid Decomposition

```

1  const int N=1e+5;
2  const int M=log2(N)+1;
3
4  set<int>g[N]; //graph
5  int h[N]; //heigh of nodes
6  int trSz[N], sz; //tree subsize, size of current tree
7  int lca[N][M]; //lca sparse table
8  int cg[N]; //centroid graph
9
10 void dfs(int u, int l)
11 {
12     lca[u][0]=l;
13     for(int i=1; i<M; i++)
14         lca[u][i]=lca[lca[u][i-1]][i-1];
15     for(auto v:g[u])
16     {
17         if(v==l)
18             continue;
19         h[v]=h[u]+1;
20         dfs(v, u);
21     }
22 }
23
24 inline int getLca(int u, int v)
25 {
26     if(h[u]>h[v])
27         swap(u, v);
28     for(int i=M-1; i>=0; i--)
29         if(h[v]-(1<<i)>=h[u])
30             v=lca[v][i];
31     if(u==v)
32         return u;
33     for(int i=M-1; i>=0; i--)
34     {
35         if(lca[u][i]!=lca[v][i])
36         {
37             u=lca[u][i];
38             v=lca[v][i];
39         }
40     }
41     return lca[u][0];
42 }
43
44 inline int getDist(int u, int v)
45 {
46     return h[u]+h[v]-2*h[getLca(u, v)];
47 }
48
49 void centDfs(int u, int l)
50 {
51     trSz[u]=1;
52     sz++;
53     for(auto v:g[u])
54     {
55         if(v==l)
56             continue;
57         centDfs(v, u);

```

```

58         trSz[u]+=trSz[v];
59     }
60 }
61
62 int findCentroid(int u, int l)
63 {
64     for(auto v:g[u])
65     {
66         if(v==l)
67             continue;
68         if(trSz[v]*2>=sz)
69             return findCentroid(v, u);
70     }
71     return u;
72 }
73
74 inline void buildCentroid(int u, int l)
75 {
76     sz=0;
77     centDfs(u, u);
78     int c=findCentroid(u, u); //actual centroid
79     cg[c]=(u==l?c:l);
80     for(auto v:g[c])
81     {
82         g[v].erase(g[v].find(c));
83         buildCentroid(v, c);
84     }
85     g[c].clear();
86 }

```

### 2.6.3 Heavy Light Decomposition on Edges

```

1  class segtree
2  {
3      const static int N=1e+5;
4  public:
5      int tr[4*N];
6      segtree(){};
7      void reset()
8      {
9          memset(tr, 0, sizeof(tr));
10     }
11     void update(int no, int l, int r, int i, int val)
12     {
13         if(r<i || l>i)
14             return;
15         if(l>=i && r<=i)
16         {
17             tr[no]=val;
18             return;
19         }
20         int nxt=(no<<1);
21         int mid=(l+r)>>1;
22         update(nxt, l, mid, i, val);
23         update(nxt+1, mid+1, r, i, val);
24         tr[no]=tr[nxt]+tr[nxt+1];
25     }
26     int query(int no, int l, int r, int i, int j)
27     {
28         if(r<i || l>j)
29             return 0;
30         if(l>=i && r<=j)
31             return tr[no];
32         int nxt=(no<<1);
33         int mid=(l+r)>>1;
34         return query(nxt, l, mid, i, j)+query(nxt+1, mid+1, r, i, j);
35     }
36 };
37
38 const int N=1e+5;
39 const int M=log2(N)+1;
40 int n;
41 segtree tr;
42 vector<pair<int,int>> g[N];
43 int lca[N][M];
44 int h[N], trSz[N];
45
46 //in - use X[], Y[] in case

```

```

47 //of edge weights
48 int X[N], Y[N], W[N];
49
50 //hld
51 int chainInd[N], chainSize[N], chainHead[N], chainPos[N], chainNo, posInBase[N];
52 int ptr;
53
54 void dfs(int u, int l)
55 {
56     trSz[u]=1;
57     lca[u][0]=1;
58     for(int i=1; i<M; i++)
59         lca[u][i]=lca[ lca[u][i-1] ][i-1];
60     for(int i=0; i<g[u].size(); i++)
61     {
62         int v=g[u][i].first;
63         if(v==l)
64             continue;
65         h[v]=h[u]+1;
66         dfs(v, u);
67         trSz[u]+=trSz[v];
68     }
69 }
70
71 inline int getLca(int u, int v)
72 {
73     if(h[u]>h[v])
74         swap(u, v);
75     for(int i=M-1; i>=0; i--)
76         if(h[v]-(1<i)>=h[u])
77             v=lca[v][i];
78     if(u==v)
79         return u;
80     for(int i=M-1; i>=0; i--)
81     {
82         if(lca[u][i]!=lca[v][i])
83         {
84             u=lca[u][i];
85             v=lca[v][i];
86         }
87     }
88     return lca[u][0];
89 }
90
91 //dont use 'c' if the weight is on the vertex
92 //instead of the edge
93 inline void hld(int u, int l, int c)
94 {
95     if(chainHead[chainNo]==-1)
96         chainHead[chainNo]=u;
97     chainInd[u]=chainNo;
98     chainPos[u]=chainSize[chainNo]++;
99     tr.update(1, 0, n, ptr, c);
100     posInBase[u]=ptr++;
101
102     int msf, idx;
103     msf=idx=-1;
104     for(int i=0; i<g[u].size(); i++)
105     {
106         int v=g[u][i].first;
107         if(v==l)
108             continue;
109         if(trSz[v]>msf)
110         {
111             msf=trSz[v];
112             idx=i;
113         }
114     }
115     if(idx>=0)
116         hld(g[u][idx].first, u, g[u][idx].second);
117     for(int i=0; i<g[u].size(); i++)
118     {
119         if(i==idx)
120             continue;
121         int v=g[u][i].first;
122         int w=g[u][i].second;
123         if(v==l)
124             continue;
125         chainNo++;

```

```

126         hld(v, u, w);
127     }
128 }
129
130 inline int query_up(int u, int v)
131 {
132     int uchain=chainInd[u];
133     int vchain=chainInd[v];
134     int ret=0;
135     while(true)
136     {
137         uchain=chainInd[u];
138         if(uchain==vchain)
139         {
140             ret+=tr.query(1, 0, n, posInBase[v]+1, posInBase[u]);
141             break;
142         }
143         int head=chainHead[uchain];
144         ret+=tr.query(1, 0, n, posInBase[head], posInBase[u]);
145         u=head;
146         u=lca[u][0];
147     }
148     return ret;
149 }
150
151 //returns sum of all edges weights
152 //from 'u' to 'v'
153 inline int query(int u, int v)
154 {
155     if(u==v)
156         return 0;
157     int l=getLca(u, v);
158     return query_up(u, l)+query_up(v, l);
159 }
160
161 //set and edge to value 'val'
162 inline void update(int u, int val)
163 {
164     int x=X[u], y=Y[u];
165     if(lca[x][0]==y)
166         tr.update(1, 0, n, posInBase[x], val);
167     else
168         tr.update(1, 0, n, posInBase[y], val);
169 }
170
171 void clearHld()
172 {
173     //tr.reset();
174     for(int i=0; i<=n; i++)
175     {
176         g[i].clear();
177         chainHead[i]=-1;
178         chainSize[i]=0;
179     }
180     ptr=1;
181     chainNo=0;
182 }
183
184 int main()
185 {
186     scanf("%d", &n);
187     clearHld();
188     for(int i=1; i<n; i++)
189     {
190         scanf("%d_%d_%d", &X[i], &Y[i], &W[i]);
191         g[ X[i] ].push_back({Y[i], W[i]});
192         g[ Y[i] ].push_back({X[i], W[i]});
193     }
194     dfs(1, 0);
195     hld(1, 0, 0);
196     int q;
197     scanf("%d", &q);
198     while(q--)
199     {
200         int o, x, y;
201         scanf("%d_%d_%d", &o, &x, &y);
202         if(o==1)
203             printf("%d\n", query(x, y));
204         else

```



```
205         update(x, y);
206     }
207     return 0;
208 }
```

## **2.6.4 Heavy Light Decomposition on Vertex**

## **2.6.5 All-Pairs Distance Sum**

## **2.7 MISC**

### **2.7.1 2-SAT**

## Chapter 3

# Dynamic Programming

### 3.1 Optimizations

#### 3.1.1 Divide and Conquer

```
1  /// David Mateus Batista <david.batista3010@gmail.com>
2  /// Computer Science – Federal University of Itajuba – Brazil
3  /// Uri Online Judge – 2475
4  #include <bits/stdc++.h>
5
6  using namespace std;
7
8  typedef long long ll;
9  typedef unsigned long long ull;
10 typedef long double ld;
11 typedef pair<int,int> pii;
12 typedef pair<ll,ll> pll;
13
14 #define INF 0x3F3F3F3F
15 #define LINF 0x3F3F3F3F3F3F3F3F
16 #define DINF (double)1e+30
17 #define EPS (double)1e-9
18 #define PI (double)acos(-1.0)
19 #define RAD(x) (double)(x*PI)/180.0
20 #define PCT(x,y) (double)x*100.0/y
21 #define pb push_back
22 #define mp make_pair
23 #define pq priority_queue
24 #define F first
25 #define S second
26 #define D(x) x&(-x)
27 #define ALL(x) x.begin(),x.end()
28 #define SET(a,b) memset(a, b, sizeof(a))
29 #define DEBUG(x,y) cout << x << y << endl
30 #define gcd(x,y) __gcd(x, y)
31 #define lcm(x,y) (x/gcd(x,y))*y
32 #define bitcnt(x) __builtin_popcountll(x)
33 #define lbit(x) 63-__builtin_clzll(x)
34 #define zerosbitll(x) __builtin_ctzll(x)
35 #define zerosbit(x) __builtin_ctz(x)
36
37 enum {North, East, South, West};
38 //{0, 1, 2, 3}
39 //{Up, Right, Down, Left}
40
41 int mi[] = {-1, 0, 1, 0, -1, 1, 1, -1};
42 int mj[] = {0, 1, 0, -1, 1, 1, -1, -1};
43
44 const int MN=1e+4+35;
45 const int MN2=535;
46 int p, a;
47 ll data[MN];
48
49 inline ll getValue(int l, int r)
50 {
51     return (r-l+1)*(data[r]-data[l-1]);
52 }
```

```

53
54 ll dp[MN2][MN];
55 inline void solve(int k, int l, int r, int L, int R)
56 {
57     if(l>r)
58         return;
59     int m=(l+r)/2;
60     int s=L;
61     dp[k][m]=LINF;
62     for(int i=max(m, L); i<=R; i++)
63     {
64         if(dp[k][m]>dp[k-1][i+1]+getValue(m+1, i+1))
65         {
66             dp[k][m]=dp[k-1][i+1]+getValue(m+1, i+1);
67             s=i;
68         }
69     }
70     solve(k, l, m-1, L, s);
71     solve(k, m+1, r, s, R);
72 }
73
74 int main()
75 {
76     scanf("%d_%d", &p, &a);
77     for(int i=1; i<=p; i++)
78     {
79         ll x;
80         scanf("%lld", &x);
81         data[i]=data[i-1]+x;
82     }
83
84     for(int i=0; i<=p; i++)
85         dp[0][i]=LINF;
86     for(int i=0; i<=a; i++)
87         dp[i][p]=0;
88     for(int i=1; i<=a; i++)
89         solve(i, 0, p-1, 0, p-1);
90     printf("%lld\n", dp[a][0]);
91     return 0;
92 }

```

### 3.1.2 Convex Hull I

#### Linear

```

1  //Original recurrence:
2  //      dp[i]=min(dp[j]+b[j]*a[i]) for j<i
3  //Condition:
4  //      b[j]>=b[j+1]
5  //      a[i]<=a[i+1]
6  // Solution:
7  //  Hull cht=Hull();
8  //  cht.insertLine(b[0], dp[0])
9  //  for(int i=1; i<n; i++)
10 // {
11 //      dp[i]=cht.query(a[i]);
12 //      cht.insertLine(b[i], dp[i])
13 // }
14 // answer is dp[n-1]
15
16 class Hull
17 {
18     const static int CN=1e+5+35;
19 public:
20     long long a[CN], b[CN];
21     double x[CN];
22     int head, tail;
23     Hull():head(1), tail(0){};
24
25     long long query(long long xx)
26     {
27         if(head>tail)
28             return 0;
29         while(head<tail && x[head+1]<=xx)
30             head++;
31         x[head]=xx;
32         return a[head]*xx+b[head];
33     }

```

```

34
35 void insertLine(long long aa, long long bb)
36 {
37     double xx=-1e18;
38     while(head<=tail)
39     {
40         if(aa==a[tail])
41             return;
42         xx=1.0*(b[tail]-bb)/(aa-a[tail]);
43         if(head==tail || xx>=x[tail])
44             break;
45         tail--;
46     }
47     a[++tail]=aa;
48     b[tail]=bb;
49     x[tail]=xx;
50 }
51 };

```

## Dynamic

```

1 //Original recurrence:
2 // dp[i]=min(dp[j]+b[j]*a[i]) for j<i
3 //Condition:
4 // b[j]>=b[j+1]
5 // a[i]<=a[i+1]
6 // Solution:
7 // HullDynamic cht;
8 // cht.insertLine(b[0], dp[0])
9 // for(int i=1; i<n; i++)
10 // {
11 //     dp[i]=cht.query(a[i]);
12 //     cht.insertLine(b[i], dp[i])
13 // }
14 // answer is dp[n-1]
15
16 const long long is_query=-(1LL<<62);
17 class Line
18 {
19 public:
20     long long m, b;
21     mutable function<const Line*()>succ;
22     bool operator < (const Line &rhs) const
23     {
24         if(rhs.b!=is_query)
25             return m<rhs.m;
26         const Line *s=succ();
27         if(!s)
28             return 0;
29         long long x=rhs.m;
30         return (b-s->b)<((s->m-m)*x);
31     }
32 };
33
34 class HullDynamic: public multiset<Line>
35 {
36 public:
37     void clear()
38     {
39         clear();
40     }
41     bool bad(iterator y)
42     {
43         auto z=next(y);
44         if(y==begin())
45         {
46             if(z==end())
47                 return 0;
48             return (y->m==z->m && y->b<=z->b);
49         }
50         auto x=prev(y);
51         if(z==end())
52             return (y->m == x->m && y->b<=x->b);
53         return ((x->b - y->b)*(z->m - y->m) >= (y->b - z->b)*(y->m - x->m));
54     }
55     void insertLine(ll m, ll b)
56     {
57         auto y=insert({m, b});
58         y->succ=[=]

```

```

59         {
60             return next(y)==end()?0:*next(y);
61         };
62         if(bad(y))
63         {
64             erase(y);
65             return;
66         }
67         while(next(y)!=end() && bad(next(y)))
68             erase(next(y));
69         while(y!=begin() && bad(prev(y)))
70             erase(prev(y));
71     }
72     long long query(long long x)
73     {
74         auto ret=*lower_bound((Line){x, is_query});
75         return ret.m*x+ret.b;
76     }
77 };

```

### 3.1.3 Convex Hull II

### 3.1.4 Knuth Optimization

## 3.2 Digits

## 3.3 Grundy Numbers

## Chapter 4

# String

4.1 Hash

4.2 KMP

4.3 Aho Corasick

4.4 Manacher

4.5 Z-Algorithm

4.6 Suffix Array & LCP

4.7 Suffix Tree

# Chapter 5

## Mathematic

### 5.1 Prime Numbers

#### 5.1.1 Erastotenes Sieve

#### 5.1.2 Linear Sieve

#### 5.1.3 Miller Rabin

#### 5.1.4 BPSW

#### 5.1.5 Primality Test

### 5.2 Chinese Remainder Theorem

### 5.3 Fast Fourier Transformation

```
1 #define PI (double)acos(-1.0)
2 typedef complex<double> base;
3 void fft(vector<base>&data, bool invert)
4 {
5     int n=data.size();
6     for(int i=1, j=0; i<n; i++)
7     {
8         int bit=n>>1;
9         for(; j>=bit; bit>>=1)
10             j-=bit;
11         j+=bit;
12         if(i<j)
13             swap(data[i], data[j]);
14     }
15     for(int len=2; len<=n; len<=1)
16     {
17         double ang=2*PI/len*(invert?-1:1);
18         base wlen(cos(ang), sin(ang));
19         for(int i=0; i<n; i+=len)
20         {
21             base w(1);
22             for(int j=0; j<len/2; j++)
23             {
24                 base u=data[i+j], v=data[i+j+len/2]*w;
25                 data[i+j]=u+v;
26                 data[i+j+len/2]=u-v;
27                 w*=wlen;
28             }
29         }
30     }
31     if(invert)
32         for(int i=0; i<n; i++)
33             data[i]/=n;
```

```

35 }
36
37 vector<int>fft_multiply(vector<int>&a, vector<int>&b)
38 {
39     vector<base>fa(a.begin(), a.end());
40     vector<base>fb(b.begin(), b.end());
41     int n=1;
42     while(n<max(a.size(), b.size()))
43         n<<=1;
44     n<<=1;
45     fa.resize(n);
46     fb.resize(n);
47     fft(fa, false);
48     fft(fb, false);
49     for(int i=0; i<n; i++)
50         fa[i]*=fb[i];
51     fft(fa, true);
52
53     vector<int>ret(n);
54     for(int i=0; i<n; i++)
55         ret[i]=(int)(fa[i].real()+0.5);
56
57     int carry=0;
58     for(int i=0; i<n; i++)
59     {
60         ret[i]+=carry;
61         carry=ret[i]/10;
62         ret[i]%=10;
63     }
64     return ret;
65 }
66
67 int main()
68 {
69     int n, m;
70     scanf("%d_%d", &n, &m);
71     vector<int>a,b;
72
73     for(int i=0; i<n; i++)
74     {
75         int x;
76         scanf("%d", &x);
77         a.pb(x);
78     }
79
80     for(int i=0; i<m; i++)
81     {
82         int x;
83         scanf("%d", &x);
84         b.pb(x);
85     }
86     reverse(a.begin(), a.end());
87     reverse(b.begin(), b.end());
88
89     vector<int>ans=fft_multiply(a, b);
90     reverse(ans.begin(), ans.end());
91     bool flag=false;
92     for(int i=0; i<ans.size(); i++)
93     {
94         if(ans[i])
95             flag=true;
96         if(flag)
97             printf("%d", ans[i]);
98     }
99     printf("\n");
100     return 0;
101 }

```



## **5.4 Modular Math**

### **5.4.1 Multiplicative Inverse**

### **5.4.2 Linear All Multiplicative Inverse**

## **5.5 Gaussian Elimination**

## **5.6 Combinatorics**

# Chapter 6

## Geometry

### 6.1 2d Template

### 6.2 3d Template

### 6.3 Polygon Template

### 6.4 Convex Hull

#### 6.4.1 Graham Scan

#### 6.4.2 Monotone Chain

### 6.5 Rotating Calipers

### 6.6 KD Tree

### 6.7 Range Tree

### 6.8 Circle Sweep