

ACM ICPC - Code Notebook

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Chapter 1

Data Structure

1.1 Segment Tree

1.1.1 Segment Tree & Lazy Propagation

```
1  class segtree
2  {
3      const static int N=100000;
4      int tr[4*N], lazy[4*N];
5  public:
6      segtree(){};
7      void clear()
8      {
9          memset(tr, 0, sizeof(tr));
10         memset(lazy, 0, sizeof(lazy));
11     }
12     void build(int no, int l, int r, vector<int>&data)
13     {
14         if(l==r)
15         {
16             tr[no]=data[l];
17             return;
18         }
19         int nxt=no*2;
20         int mid=(l+r)/2;
21         build(nxt, l, mid, data);
22         build(nxt+1, mid+1, r, data);
23         tr[no]=tr[nxt]+tr[nxt+1];
24     }
25     void propagate(int no, int l, int r)
26     {
27         if(!lazy[no])
28             return;
29
30         tr[no]+=(r-l+1)*lazy[no];
31         if(l!=r)
32         {
33             int nxt=no*2;
34             lazy[nxt]+=lazy[no];
35             lazy[nxt+1]+=lazy[no];
36         }
37         lazy[no]=0;
38     }
39     void update(int no, int l, int r, int i, int j, int x)
40     {
41         propagate(no, l, r);
42         if(l>j || r<i)
43             return;
44         if(l>=i && r<=j)
45         {
46             lazy[no]=x;
47             propagate(no, l, r);
48             return;
49         }
50         int nxt=no*2;
```

```

51     int mid=(l+r)/2;
52     update(nxt, l, mid, i, j, x);
53     update(nxt+1, mid+1, r, i, j, x);
54     tr [no]=tr [nxt]+tr [nxt+1];
55 }
56 int query(int no, int l, int r, int i, int j)
57 {
58     propagate(no, l, r);
59     if(l>j || r<i)
60         return 0;
61     if(l>=i && r<=j)
62         return tr [no];
63     int nxt=no*2;
64     int mid=(l+r)/2;
65     int ql=query(nxt, l, mid, i, j);
66     int qr=query(nxt+1, mid+1, r, i, j);
67     return (ql+qr);
68 }
69 };

```

1.1.2 Segment Tree & Hash

```
1  const int NC=1e+5;
2  ull aux[NC];
3  void precalc(ull k)//prime k
4  {
5      aux[0]=1LL;
6      for(int i=1; i<NC; i++)
7          aux[i]=aux[i-1]*k;
8  }
9
10 class node
11 {
12 public:
13     ull v;
14     int s;
15     node(){};
16     node(ull _v, int _s)
17     {
18         v=_v; s=_s;
19     }//
20     node operator +(const node &foo) const
21     {
22         return node(v+(foo.v*aux[s]), s+foo.s);
23     }
24 };
25
26 class segtree
27 {
28     const static int N=1e+5+35;
29     node tr[4*N];
30 public:
31     segtree(){};
32     void update(int no, int l, int r, int i, int j, node x)
33     {
34         if(l>j || r<i)
35             return;
36         if(l>=i && r<=j)
37         {
38             tr[no]=x;
39             return;
40         }
41         int mid=(l+r)>>1;
42         int nxt=no<<1;
43         update(nxt, l, mid, i, j, x);
44         update(nxt+1, mid+1, r, i, j, x);
45         tr[no]=tr[nxt]+tr[nxt+1];
46     }
47     node query(int no, int l, int r, int i, int j)
48     {
49         if(l>j || r<i)
50             return node(0LL, 0);
51         if(l>=i && r<=j)
52             return tr[no];
53         int mid=(l+r)>>1;
54         int nxt=no<<1;
55         node ql=query(nxt, l, mid, i, j);
56         node qr=query(nxt+1, mid+1, r, i, j);
57         return ql+qr;
58     }
59 };
```

1.1.3 Quadtree

```
1  class quadtree
2  {
3      //needs to be NxN
4      const static int N=100000;
5      int tr[16*N];
6  public:
7      quadtree(){};
8      void build(int node, int l1, int r1, int l2, int r2, vector< vector<int> >data)
9      {
10         if(l1==l2 && r1==r2)
11         {
12             tr[node]=data[l1][r1];
13             return;
14         }
15         int nxt=node*4;
16         int midl=(l1+l2)/2;
17         int midr=(r1+r2)/2;
18
19         build(nxt-2, l1, r1, midl, midr, data);
20         build(nxt-1, midl+1, r1, l2, midr, data);
21         build(nxt, l1, midr+1, midl, r2, data);
22         build(nxt+1, midl+1, midr+1, l2, r2, data);
23
24         tr[node]=tr[nxt-2]+tr[nxt-1]+tr[nxt]+tr[nxt+1];
25     }
26     void update(int node, int l1, int r1, int l2, int r2, int i, int j, int x)
27     {
28         if(l1>l2 || r1>r2)
29             return;
30         if(i>l2 || j>r2 || i<l1 || j<r1)
31             return;
32         if(i==l1 && i==l2 && j==r1 && j==r2)
33         {
34             tr[node]=x;
35             return;
36         }
37         int nxt=node*4;
38         int midl=(l1+l2)/2;
39         int midr=(r1+r2)/2;
40
41         update(nxt-2, l1, r1, midl, midr, i, j, x);
42         update(nxt-1, midl+1, r1, l2, midr, i, j, x);
43         update(nxt, l1, midr+1, midl, r2, i, j, x);
44         update(nxt+1, midl+1, midr+1, l2, r2, i, j, x);
45
46         tr[node]=tr[nxt-2]+tr[nxt-1]+tr[nxt]+tr[nxt+1];
47     }
48     int query(int node, int l1, int r1, int l2, int r2, int i1, int j1, int i2, int j2)
49     {
50         if(i1>l2 || j1>r2 || i2<l1 || j2<r1 || i1>i2 || j1>j2)
51             return 0;
52         if(i1<=l1 && j1<=r1 && l2<=i2 && r2<=j2)
53             return tr[node];
54         int nxt=node*4;
55         int midl=(l1+l2)/2;
56         int midr=(r1+r2)/2;
57
58         int q1=query(nxt-2, l1, r1, midl, midr, i1, j1, i2, j2);
59         int q2=query(nxt-1, midl+1, r1, l2, midr, i1, j1, i2, j2);
60         int q3=query(nxt, l1, midr+1, midl, r2, i1, j1, i2, j2);
61         int q4=query(nxt+1, midl+1, midr+1, l2, r2, i1, j2, i2, j2);
62     }
63 };
```

1.1.4 Mergesort Segtree

```
1  class mergesort_segtree
2  {
3      const static int N=100000;
4      vector<int>tr[4*N];
5  public:
6      mergesort_segtree(){};
7      void build(int no, int l, int r, vector<int>&data)
8      {
9          if(l==r)
10         {
11             tr[no].push_back(data[l]);
12             return;
13         }
14         int nxt=no*2;
15         int mid=(l+r)/2;
16         build(nxt, l, mid, data);
17         build(nxt+1, mid+1, r, data);
18         tr[no].resize(tr[nxt].size()+tr[nxt+1].size());
19         merge(tr[nxt].begin(), tr[nxt].end(), tr[nxt+1].begin(), tr[nxt+1].end(), tr[no].begin());
20     }
21     //how many numbers in (i, j) are greater or equal than k
22     int query(int no, int l, int r, int i, int j, int k)
23     {
24         if(r<i || l>j)
25             return 0;
26         if(l>=i && r<=j)
27             return (int)(tr[no].end()-upper_bound(tr[no].begin(), tr[no].end(), k));
28         int nxt=no*2;
29         int mid=(l+r)/2;
30         int ql=query(nxt, l, mid, i, j, k);
31         int qr=query(nxt+1, mid+1, r, i, j, k);
32         return ql+qr;
33     }
34 };
```


1.1.5 Persistent Segtree

```
1  class persistent_segtree
2  {
3      const static int N=100000;
4      int n, cnt, id;
5      int tr[N];
6      int root[N], L[N], R[N];
7  public:
8      persistent_segtree(){};
9      void set(int _n)
10     {
11         memset(tr, 0, sizeof(tr));
12         memset(root, 0, sizeof(root));
13         memset(L, 0, sizeof(L));
14         memset(R, 0, sizeof(R));
15         id=0;
16         cnt=1;
17         n=_n;
18     }
19     void build(int no, int l, int r, vector<int>&data)
20     {
21         if(l==r)
22         {
23             tr[no]=data[l];
24             return;
25         }
26         int mid=(l+r)/2;
27         L[no]=cnt++;
28         R[no]=cnt++;
29         build(L[no], l, mid, data);
30         build(R[no], mid+1, r, data);
31         tr[no]=tr[ L[no] ]+tr[ R[no] ];
32     }
33     int update(int no, int l, int r, int i, int x)
34     {
35         int newno=cnt++;
36         tr[newno]=tr[no];
37         L[newno]=L[no];
38         R[newno]=R[no];
39         if(l==r)
40         {
41             tr[newno]=x;
42             return newno;
43         }
44         int mid=(l+r)/2;
45         if(i<=mid)
46             L[newno]=update(L[newno], l, mid, i, x);
47         else
48             R[newno]=update(R[newno], mid+1, r, i, x);
49         tr[newno]=tr[ L[newno] ]+tr[ R[newno] ];
50         return newno;
51     }
52     int query(int no, int l, int r, int i, int j)
53     {
54         if(r<i || l>j)
55             return 0;
56         if(l>=i && r<=j)
57             return tr[no];
58         int mid=(l+r)/2;
59         int ql=query(L[no], l, mid, i, j);
60         int qr=query(R[no], mid+1, r, i, j);
61         return ql+qr;
62     }
63     //update the i-th value to x.
64     void update(int i, int x)
65     {
66         root[id+1]=update(root[id], 0, n-1, i, x);
67         id++;
68     }
69     //returns sum(l, r) after the k-th update.
70     int query(int l, int r, int k)
71     {
72         return query(root[k], 0, n-1, l, r);
73     }
74 };
```

1.2 Fenwick Tree

1.2.1 Fenwick Tree 1D

```
1  class fenwicktree
2  {
3      #define D(x) x&(-x)
4      const static int N=100000;
5      int tr[N], n;
6  public:
7      fenwicktree(){};
8      void build(int _n)
9      {
10         n=_n;
11         memset(tr, 0, sizeof(tr));
12     }
13     void update(int i, int x)
14     {
15         for(i++; i<=n; i+=D(i))
16             tr[i]+=x;
17     }
18     int query(int i)
19     {
20         int ret=0;
21         for(i++; i>0; i-=D(i))
22             ret+=tr[i];
23         return ret;
24     }
25     int rquery(int l, int r)
26     {
27         return query(r)-query(l-1);
28     }
29     void set(int i, int x)
30     {
31         update(i, -rquery(i, i)+x);
32     }
33     void rset(int l, int r, int x)
34     {
35         update(l, x);
36         update(r+1, -x);
37     }
38 };;
```

1.2.2 Fenwick Tree 2D

```
1  class fenwicktree
2  {
3      #define D(x) x&(-x)
4      const static int N=1000;
5      int tr[N][N], n, m;
6  public:
7      fenwicktree(){};
8      void build(int _n, int _m)
9      {
10         n=_n, m=_m;
11         memset(tr, 0, sizeof(tr));
12     }
13     void update(int r, int c, int x)
14     {
15         for(int i=r+1; i<=n; i+=D(i))
16             for(int j=c+1; j<=m; j+=D(j))
17                 tr[i][j]+=x;
18     }
19     int query(int r, int c)
20     {
21         int ret=0;
22         for(int i=r+1; i>0; i-=D(i))
23             for(int j=c+1; j>0; j-=D(j))
24                 ret+=tr[i][j];
25         return ret;
26     }
27     int rquery(int r1, int c1, int r2, int c2)
28     {
29         if((r1>r2 && c1>c2) || (r1==r2 && c1>c2) || (r1>r2 && c1==c2))
30         {
31             swap(r1, r2);
32             swap(c1, c2);
33         }
34         else if(r1<r2 && c1>c2)
35         {
36             swap(c1, c2);
37         }
38         else if(r1>r2 && c1<c2)
39         {
40             swap(r1, r2);
41         }
42         return query(r2, c2)-query(r1-1, c2)-query(r2, c1-1)+query(r1-1, c1-1);
43     }
44     void set(int r, int c, int x)
45     {
46         update(r, c, -rquery(r, c, r, c)+x);
47     }
48 };
```

1.3 Cartesian Tree

1.3.1 Cartesian Tree

```
1 //srand(time(NULL))
2 int vrand()
3 {
4     return abs(rand()<<(rand()%31));
5 }
6
7 struct node
8 {
9     //x=key, y=priority key, c=tree count
10    int x, y, c;
11    node *L, *R;
12    node(){};
13    node(int _x)
14    {
15        x=_x, y=vrand(), c=0;
16        L=R=NULL;
17    }
18 };
19
20 int cnt(node *root)
21 {
22     return root?root->c:0;
23 }
24
25 void upd_cnt(node *root)
26 {
27     if(root)
28         root->c=1+cnt(root->L)+cnt(root->R);
29 }
30
31 void split(node *root, int x, node *&L, node *&R)
32 {
33     if(!root)
34         L=R=NULL;
35     else if(x < root->x)
36         split(root->L, x, L, root->L), R=root;
37     else
38         split(root->R, x, root->R, R), L=root;
39     upd_cnt(root);
40 }
41
42 void insert(node *&root, node *it)
43 {
44     if(!root)
45         root=it;
46     else if(it->y > root->y)
47         split(root, it->x, it->L, it->R), root=it;
48     else
49         insert(it->x < root->x? root->L:root->R, it);
50     upd_cnt(root);
51 }
52
53 void merge(node *&root, node *L, node *R)
54 {
55     if(!L || !R)
56         root=L?L:R;
57     else if(L->y > R->y)
58         merge(L->R, L->R, R), root=L;
59     else
60         merge(R->L, L, R->L), root=R;
61     upd_cnt(root);
62 }
63
64 void erase(node *&root, int x)
65 {
66     if(root->x==x)
67         merge(root, root->L, root->R);
68     else
69         erase(x < root->x? root->L:root->R, x);
70     upd_cnt(root);
71 }
```

```

72 node *unite(node *L, node *R)
73 {
74     if (!L || !R)
75         return L?L:R;
76     if (L->y < R->y)
77         swap(L, R);
78     node *Lt, *Rt;
79     split(R, L->x, Lt, Rt);
80     L->L=unite(L->L, Lt);
81     L->R=unite(L->R, Rt);
82     return L;
83 }
84
85
86 int find(node *root, int x)
87 {
88     if (!root)
89         return 0;
90     if (root->x==x)
91         return 1;
92     if (x > root->x)
93         return find(root->R, x);
94     else
95         return find(root->L, x);
96 }
97
98 int findkth(node *root, int x)
99 {
100     if (!root)
101         return -1;
102     int Lc=cnt(root->L);
103     if (x-Lc-1==0)
104         return root->x;
105     if (x>Lc)
106         return findkth(root->R, x-Lc-1);
107     else
108         return findkth(root->L, x);
109 }

```

1.3.2 Implicit Cartesian Tree

```
1 //srand(time(NULL))
2 int vrand()
3 {
4     return abs(rand() << (rand() % 31));
5 }
6
7 struct node
8 {
9     //basic treap: x=key, y=priority key, c=tree count;
10    int x, y, c;
11    //treap operations: v=max(x), lazy=lazy value of propagation, rev=reversed
12    int v, lazy, rev;
13
14    node *L, *R;
15    node() {}
16    node(int _x)
17    {
18        x=_x, y=vrand();
19        L=R=NULL;
20        v=x;
21        lazy=0;
22        rev=0;
23    }
24 };
25
26 //updating functions
27 inline int get_cnt(node *root)
28 {
29     return root?root->c:0;
30 }
31
32 inline void upd_cnt(node *root)
33 {
34     if(root)
35         root->c=1+get_cnt(root->L)+get_cnt(root->R);
36 }
37
38 inline void push(node *&root)
39 {
40     if(root && root->rev)
41     {
42         root->rev=0;
43         swap(root->L, root->R);
44         if(root->L)
45             root->L->rev^=1;
46         if(root->R)
47             root->R->rev^=1;
48     }
49 }
50
51 inline void propagate(node *&root)
52 {
53     if(root)
54     {
55         if(!root->lazy)
56             return;
57         int lazy=root->lazy;
58         root->x+=lazy;
59
60         if(root->L)
61             root->L->lazy=lazy;
62         if(root->R)
63             root->R->lazy=lazy;
64         root->lazy=0;
65     }
66 }
67
68 inline int get_max(node *root)
69 {
70     return root?root->v:-INF;
71 }
72
73 inline void upd_max(node *root)
74 {
```

```

75     if (root)
76         root->v=max(root->x, max(get_max(root->L), get_max(root->R)));
77     }
78
79     inline void update(node *root)
80     {
81         propagate(root);
82         upd_cnt(root);
83         upd_max(root);
84     }
85
86     void merge(node *&root, node *L, node *R)
87     {
88         push(L);
89         push(R);
90         if (!L || !R)
91             root=L?L:R;
92         else if (L->y > R->y)
93             merge(L->R, L->R, R), root=L;
94         else
95             merge(R->L, L, R->L), root=R;
96         update(root);
97     }
98
99     void split(node *root, node *&L, node *&R, int x, int add=0)
100    {
101        if (!root)
102            return void(L=R=NULL);
103        push(root);
104        int ix=add+get_cnt(root->L); //implicit key
105        if (x<=ix)
106            split(root->L, L, root->L, x, add), R=root;
107        else
108            split(root->R, root->R, R, x, add+1+get_cnt(root->L)), L=root;
109        update(root);
110    }
111
112    //insert function
113    void insert(node *&root, int pos, int x)//(insert x at position pos)
114    {
115        node *R1, *R2;
116        split(root, R1, R2, pos);
117        merge(R1, R1, new node(x));
118        merge(root, R1, R2);
119    }
120
121    //erase value x
122    void erase_x(node *&root, int x)
123    {
124        if (!root)
125            return;
126        if (root->x==x)
127            merge(root, root->L, root->R);
128        else
129            erase_x(x < root->x? root->L:root->R, x);
130        update(root);
131    }
132
133    //erase kth value
134    void erase_kth(node *&root, int x)
135    {
136        if (!root)
137            return;
138        int Lc=get_cnt(root->L);
139        if (x-Lc-1==0)
140            merge(root, root->L, root->R);
141        else if (x>Lc)
142            erase_kth(root->R, x-Lc-1);
143        else
144            erase_kth(root->L, x);
145        update(root);
146    }
147
148    //add x to [l,r]
149    inline void paint(node *&root, int l, int r, int x)
150    {
151        node *R1, *R2, *R3;

```

```

152     split(root, R1, R2, l);
153     split(R2, R2, R3, r-l+1);
154     R2->lazy=x;
155     propagate(R2);
156
157     merge(root, R1, R2);
158     merge(root, root, R3);
159 }
160
161 //max range query [l,r]
162 inline int rquery(node *&root, int l, int r)
163 {
164     node *R1, *R2, *R3;
165     split(root, R1, R2, l);
166     split(R2, R2, R3, r-l+1);
167     int ret=R2->v;
168     merge(root, R1, R2);
169     merge(root, root, R3);
170     return ret;
171 }
172
173 inline void reverse(node *&root, int l, int r)//reverse elements [l, r]
174 {
175     node *R1, *R2, *R3;
176     split(root, R1, R2, l);
177     split(R2, R2, R3, r-l+1);
178     R2->rev^=1;
179     merge(root, R1, R2);
180     merge(root, root, R3);
181 }
182
183 //output functions
184 int poscnt=0;
185 void output_all(node *root)
186 {
187     if(!root)
188         return;
189     update(root);
190     push(root);
191     output_all(root->L);
192     printf("[%d]_%d\n", poscnt++, root->x);
193     output_all(root->R);
194 }
195
196 int output_kth(node *root, int x)
197 {
198     if(!root)
199         return -1;
200     update(root);
201     push(root);
202     int Lc=get_cnt(root->L);
203     if(x-Lc-1==0)
204         return root->x;
205     if(x>Lc)
206         return output_kth(root->R, x-Lc-1);
207     else
208         return output_kth(root->L, x);
209 }

```


1.3.3 Implicit Cartesian Tree & Hash

```
1  const int NC=1e+5;
2  ull aux[NC];
3  void precalc(ull k)//prime k
4  {
5      aux[0]=1LL;
6      for(int i=1; i<NC; i++)
7          aux[i]=aux[i-1]*k;
8  }
9  class hnode
10 {
11 public:
12     ull v;
13     int s;
14     hnode(){};
15     hnode(ull _v, int _s)
16     {
17         v=_v; s=_s;
18     }
19     hnode operator +(const hnode &foo) const
20     {
21         return hnode(v+(foo.v*aux[s]), s+foo.s);
22     }
23 };
24
25 //srand(time(NULL))
26 int vrand()
27 {
28     return abs(rand()<<(rand()%31));
29 }
30 struct node
31 {
32     int x, y, c;
33     int lazy, rev;
34     hnode v;
35     node *L, *R;
36     node(){};
37     node(int _x)
38     {
39         x=_x, y=vrand();
40         L=R=NULL;
41         v=hnode((ull)_x, 1);
42         lazy=0;
43         rev=0;
44     }
45 };
46
47 //updating functions
48 inline int get_cnt(node *root)
49 {
50     return root?root->c:0;
51 }
52
53 inline void upd_cnt(node *root)
54 {
55     if(root)
56     {
57         root->c=1+get_cnt(root->L)+get_cnt(root->R);
58     }
59 }
60
61 inline void push(node *&root)
62 {
63     if(root && root->rev)
64     {
65         root->rev=0;
66         swap(root->L, root->R);
67         if(root->L)
68             root->L->rev^=1;
69         if(root->R)
70             root->R->rev^=1;
71     }
72 }
73
74 inline void propagate(node *&root)
```

```

75 {
76     if(root)
77     {
78         if(!root->lazy)
79             return;
80         int lazy=root->lazy;
81         root->x=lazy;
82         root->v=hnode(lazy, root->v.s);
83         if(root->L)
84             root->L->lazy=lazy;
85         if(root->R)
86             root->R->lazy=lazy;
87         root->lazy=0;
88     }
89 }
90
91 inline hnode getHash(node *root)
92 {
93     if(root)
94     {
95         propagate(root);
96         return root->v;
97     }
98     return hnode(0, 0);
99 }
100
101 inline void updHash(node *root)
102 {
103     if(root)
104         root->v=(hnode(root->x, 1)+getHash(root->L))+getHash(root->R);
105 }
106
107 inline void update(node *root)
108 {
109     propagate(root);
110     upd_cnt(root);
111     updHash(root);
112 }
113
114 void merge(node *&root, node *L, node *R)
115 {
116     push(L);
117     push(R);
118     if(!L || !R)
119         root=L?L:R;
120     else if(L->y > R->y)
121         merge(L->R, L->R, R), root=L;
122     else
123         merge(R->L, L, R->L), root=R;
124     update(root);
125 }
126
127 void split(node *root, node *&L, node *&R, int x, int add=0)
128 {
129     if(!root)
130         return void(L=R=NULL);
131     push(root);
132     int ix=add+get_cnt(root->L); //implicit key
133     if(x<=ix)
134         split(root->L, L, root->L, x, add), R=root;
135     else
136         split(root->R, root->R, R, x, add+1+get_cnt(root->L)), L=root;
137     update(root);
138 }
139
140 //insert function
141 void insert(node *&root, int pos, int x)//(insert x at position pos)
142 {
143     node *R1, *R2;
144     split(root, R1, R2, pos);
145     merge(R1, R1, new node(x));
146     merge(root, R1, R2);
147 }
148
149 //erase value x
150 void erase_x(node *&root, int x)
151 {

```

```

152     if (!root)
153         return;
154     if (root->x==x)
155         merge(root, root->L, root->R);
156     else
157         erase_x(x < root->x? root->L:root->R, x);
158     update(root);
159 }
160
161 //1-indexed: erase kth value
162 void erase_kth(node *&root, int x)
163 {
164     if (!root)
165         return;
166     int Lc=get_cnt(root->L);
167     if (x-Lc-1==0)
168         merge(root, root->L, root->R);
169     else if (x>Lc)
170         erase_kth(root->R, x-Lc-1);
171     else
172         erase_kth(root->L, x);
173     update(root);
174 }
175
176 //change [l, r] to x: l==r only
177 inline void paint(node *&root, int l, int r, int x)
178 {
179     node *R1, *R2, *R3;
180     split(root, R1, R2, l);
181     split(R2, R2, R3, r-l+1);
182     R2->lazy=x;
183     propagate(R2);
184
185     merge(root, R1, R2);
186     merge(root, root, R3);
187 }
188
189 //hash from [l, r]
190 inline hnode rquery(node *&root, int l, int r)
191 {
192     node *R1, *R2, *R3;
193     split(root, R1, R2, l);
194     split(R2, R2, R3, r-l+1);
195     hnode ret=R2->v;
196     merge(root, R1, R2);
197     merge(root, root, R3);
198     return ret;
199 }
200
201 //reverse elements [l, r]
202 inline void reverse(node *&root, int l, int r)
203 {
204     node *R1, *R2, *R3;
205     split(root, R1, R2, l);
206     split(R2, R2, R3, r-l+1);
207     R2->rev^=1;
208     merge(root, R1, R2);
209     merge(root, root, R3);
210 }
211
212 //output functions
213 int poscnt=0;
214 void output_all(node *root)
215 {
216     if (!root)
217         return;
218     update(root);
219     push(root);
220     output_all(root->L);
221     printf("[%d]_%d\n", poscnt++, root->x);
222     output_all(root->R);
223 }
224
225 //1-indexed
226 int output_kth(node *root, int x)
227 {
228     if (!root)

```

```
229     return -1;
230     update(root);
231     push(root);
232     int Lc=get_cnt(root->L);
233     if(x-Lc-1==0)
234         return root->x;
235     if(x>Lc)
236         return output_kth(root->R, x-Lc-1);
237     else
238         return output_kth(root->L, x);
239 }
```

1.4 Merge Sort & Swap Count

1.4.1 Merge Sort & Vector

```
1  #define INF 0x3F3F3F3F
2  int mergesort(vector<int>&data)
3  {
4      if(data.size()==1)
5          return 0;
6      vector<int>L, R;
7      int t=data.size();
8      for(int i=0; i<t/2; i++)
9          L.push_back(data[i]);
10     for(int i=t/2; i<t; i++)
11         R.push_back(data[i]);
12     int ret=mergesort(L)+mergesort(R);
13     for(int i=0, j=0, k=0; j<L.size() || k<R.size(); i++)
14     {
15         int x=j<L.size()?L[j]:INF;
16         int y=k<R.size()?R[k]:INF;
17         if(x<y)
18         {
19             data[i]=x;
20             j++;
21         }
22         else
23         {
24             data[i]=y;
25             k++;
26             ret+=(L.size()-j);
27         }
28     }
29     return ret;
30 }
```

1.4.2 Merge Sort & Array

```
1 #define INF 0x3F3F3F3F
2 int temp[100000];
3 int mergesort(int data[], int l, int r)
4 {
5     if(abs(l-r)<=1)
6         return 0;
7     int mid=(l+r)/2;
8     int ret=mergesort(data, l, mid)+mergesort(data, mid, r);
9     for(int i=l; i<r; i++)
10         temp[i]=data[i];
11     for(int i=l, j=l, k=mid; j<mid || k<r; i++)
12     {
13         int x=j<mid?temp[j]:INF;
14         int y=k<r?temp[k]:INF;
15         if(x<y)//x<=y
16         {
17             data[i]=x;
18             j++;
19         }
20         else
21         {
22             data[i]=y;
23             k++;
24             ret+=(mid-j);
25         }
26     }
27     return ret;
28 }
```

1.5 Sparse Table

```
1  class sparsetable
2  {
3      #define lbit(x) 63-__builtin_clzll(x);
4      const static int N=100000, LN=20;
5      int data[N][LN], n, ln;
6  public:
7      sparsetable(){};
8      void clear()
9      {
10         memset(data, 0, sizeof(data));
11     }
12     void build(vector<int>&foo)
13     {
14         n=foo.size();
15         ln=lbit(n);
16         for(int i=0; i<n; i++)
17             data[i][0]=foo[i];
18         for(int j=1; j<=ln; j++)
19             for(int i=0; i<n-(1<<j)+1; i++)
20                 data[i][j]=max(data[i][j-1], data[i+(1<<(j-1))][j-1]);
21     }
22     int query(int l, int r)
23     {
24         int i=abs(l-r)+1;
25         int j=lbit(i);
26         return max(data[l][j], data[l-(1<<j)+1][j]);
27     }
28 };
```

1.6 Sqrt Decomposition

1.6.1 Array

```
1  const int N=100000;
2  int SN=sqrt(N);
3
4  class mo
5  {
6  public:
7      int l, r, i;
8      mo(){};
9      mo(int _l, int _r, int _i)
10     {
11         l=_l, r=_r, i=_i;
12     }
13     bool operator <(const mo &foo) const
14     {
15         if((r/SN)!=(foo.r/SN))
16             return (r/SN)<(foo.r/SN);
17         if(l!=foo.l)
18             return l<foo.l;
19         return i<foo.i;
20     }
21 };
22
23 int data[N], freq[N], ans[N];
24 int cnt=0;
25 void update(int p, int s)
26 {
27     int x=data[p];
28     if(s==1)
29     {
30         if(freq[x]==0)
31             cnt++;
32     }
33     else
34     {
35         if(freq[x]==1)
36             cnt--;
37     }
38     freq[x]+=s;
39 }
40
41 int main()
42 {
43     int n;
44     scanf("%d", &n);
45     for(int i=1; i<=n; i++)
46         scanf("%d", &data[i]);
47
48     int q;
49     scanf("%d", &q);
50     vector<mo>qurys;
51     for(int i=0; i<q; i++)
52     {
53         int l, r;
54         scanf("%d_%d", &l, &r);
55         qurys.push_back(mo(l, r, i));
56     }
57     sort(qurys.begin(), qurys.end());
58
59     int l=1, r=1;
60     cnt=0;
61     memset(freq, 0, sizeof(freq));
62     update(l, 1);
63     for(int i=0; i<q; i++)
64     {
65         int li=qurys[i].l;
66         int ri=qurys[i].r;
67         int ii=qurys[i].i;
68         while(l>li)
69             update(--l, 1);
70         while(r<ri)
71             update(++r, 1);
```



```
72     while(l<li)
73         update(l++, -1);
74     while(r>ri)
75         update(r--, -1);
76     ans[ii]=cnt;
77 }
78 for(int i=0; i<querys.size(); i++)
79     printf("%d\n", ans[i]);
80 return 0;
81 }
```

1.6.2 Tree

```
1 #define pb push_back
2 #define ALL(x) x.begin(), x.end()
3
4 const int N=1e+5+35;
5 const int M=20;
6 const int SN=sqrt(2*N)+1;
7
8 class mo
9 {
10 public:
11     int l, r, i, lc;
12     mo(){};
13     mo(int _l, int _r, int _lc, int _i)
14     {
15         l=_l, r=_r, lc=_lc, i=_i;
16     }
17     bool operator <(const mo &foo) const
18     {
19         if((r/SN)!=(foo.r/SN))
20             return (r/SN)<(foo.r/SN);
21         if(l!=foo.l)
22             return l<foo.l;
23         return i<foo.i;
24     }
25 };
26
27 int n, q;
28 int h[N], lca[N][M];
29 vector<int>g[N];
30 int dl[N], dr[N], di[2*N], cur;
31
32 void dfs(int u, int p)
33 {
34     dl[u]=++cur;
35     di[cur]=u;
36     lca[u][0]=p;
37     for(int i=1; i<M; i++)
38         lca[u][i]=lca[lca[u][i-1]][i-1];
39     for(int i=0; i<g[u].size(); i++)
40     {
41         int v=g[u][i];
42         if(v==p)
43             continue;
44         h[v]=h[u]+1;
45         dfs(v, u);
46     }
47     dr[u]=++cur;
48     di[cur]=u;
49 }
50
51 inline int getLca(int u, int v)
52 {
53     if(h[u]>h[v])
54         swap(u, v);
55     for(int i=M-1; i>=0; i--)
56         if(h[v]-(1<<i)>=h[u])
57             v=lca[v][i];
58     if(u==v)
59         return u;
60     for(int i=M-1; i>=0; i--)
61     {
62         if(lca[u][i]!=lca[v][i])
63         {
64             u=lca[u][i];
65             v=lca[v][i];
66         }
67     }
68     return lca[u][0];
69 }
70
71 map<string, int>remap;
72 int data[N], ans[N], vis[N], freq[N], cnt;
73 inline void update(int u)
74 {
```

```

75     int x=data[u];
76     if(vis[u] && (--freq[ data[u] ]==0))
77         cnt--;
78     else if(!vis[u] && (freq[ data[u] ]++==0))
79         cnt++;
80     vis[u]^=1;
81 }
82
83 int main()
84 {
85     scanf("%d_%d", &n, &q);
86     for(int i=1; i<=n; i++)
87     {
88         char temp[25];
89         scanf("%s", temp);
90         string temp2=string(temp);
91         if(!remap.count(temp2))
92             remap[temp2]=remap.size();
93         data[i]=remap[temp2];
94     }
95     for(int i=1; i<n; i++)
96     {
97         int u, v;
98         scanf("%d_%d", &u, &v);
99         g[u].pb(v);
100        g[v].pb(u);
101    }
102    dfs(1, 0);
103
104    vector<mo>query;
105    for(int i=0; i<q; i++)
106    {
107        int u, v;
108        scanf("%d_%d", &u, &v);
109        int lc=getLca(u, v);
110        if(dl[u]>dl[v])
111            swap(u, v);
112        query.pb(mo(u==lc?dl[u]:dr[u], dl[v], lc, i));
113    }
114    sort(ALL(query));
115
116    int l=query[0].l, r=query[0].l-1;
117    cnt=0;
118    for(int i=0; i<q; i++)
119    {
120        int li=query[i].l;
121        int ri=query[i].r;
122        int lc=query[i].lc;
123        int ii=query[i].i;
124        while(l>li)
125            update(di[--l]);
126        while(r<ri)
127            update(di[++r]);
128        while(l<li)
129            update(di[l++]);
130        while(r>ri)
131            update(di[r--]);
132
133        int u=di[l], v=di[r];
134        if(lc!=u && lc!=v)
135            update(lc);
136        ans[ii]=cnt;
137        if(lc!=u && lc!=v)
138            update(lc);
139    }
140    for(int i=0; i<q; i++)
141        printf("%d\n", ans[i]);
142    return 0;
143 }

```

Chapter 2

Graph

2.1 Components

2.1.1 Articulations, Bridges & Cycles

2.1.2 Strongly Connected Components

Tarjan

```
1  class graph
2  {
3      const static int MN=1e+5;
4  public:
5      vector<int>data[MN], aux;
6      bool vis[MN];
7      int grp[MN];
8      int dfs_num[MN], dfs_low[MN];
9      int dfs_cnt, numSCC;
10
11     graph(){};
12     void clear()
13     {
14         for(int i=0; i<MN; i++)
15         {
16             data[i].clear();
17             dfs_num[i]=-1;
18             dfs_low[i]=0;
19             vis[i]=false;
20         }
21         aux.clear();
22         dfs_cnt=numSCC=0;
23     }
24     void add_edge(int u, int v)
25     {
26         data[u].push_back(v);
27     }
28     void tarjanSCC(int u)
29     {
30         dfs_num[u]=dfs_low[u]=dfs_cnt++;
31         aux.push_back(u);
32         vis[u]=true;
33
34         for(int i=0; i<data[u].size(); i++)
35         {
36             int v=data[u][i];
37             if(dfs_num[v]==-1)
38                 tarjanSCC(v);
39             if(vis[v])
40                 dfs_low[v]=min(dfs_low[v], dfs_low[u]);
41         }
42
43         if(dfs_num[u]==dfs_low[u])
44         {
45             while(1)
46             {
47                 int v=aux.back();
48                 aux.pop_back();
49                 vis[v]=false;
50                 grp[v]=numSCC;
51                 if(u==v)
52                     break;
53             }
54             numSCC++;
55         }
56     }
57 };
```

2.1.3 Semi-Strongly Connected Components

2.2 Single Source Shortest Path

2.2.1 Dijkstra

2.2.2 Bellmanford

```
1  class node
2  {
3  public:
4      int x, y, d;
5      node(){};
6      node(int _x, int _y, int _d)
7      {
8          x=_x, y=_y, d=_d;
9      }
10 };
11
12 int n, v;
13 vector<node>graph;
14 int dist[1035];
15 bool bellmanford(int s)
16 {
17     memset(dist, INF, sizeof(dist));
18     dist[s]=0;
19     for(int i=0; i<n-1; i++)
20     {
21         for(int j=0; j<graph.size(); j++)
22         {
23             int x=graph[j].x;
24             int y=graph[j].y;
25             int d=graph[j].d;
26             if(dist[y]>dist[x]+d)
27                 dist[y]=dist[x]+d;
28         }
29     }
30
31     for(int i=0; i<graph.size(); i++)
32     {
33         int x=graph[i].x;
34         int y=graph[i].y;
35         int d=graph[i].d;
36         if(dist[x]<INF && dist[y]>dist[x]+d)
37             return true;
38     }
39     return false;
40 }
```

2.3 All Pairs Shortest Path

2.3.1 Floyd Warshall

2.4 Minimum Spannig Tree

2.4.1 Kruskal

2.4.2 Prim

2.5 Flow

2.5.1 Maximum Bipartite Matching

```
1  const int MN=1e+3;
2  vector<int>g[MN];
3  int match[MN], rmatch[MN], vis[MN];
4  int findmatch(int u)
5  {
6      if(vis[u])
7          return 0;
8      vis[u]=true;
9      for(int v:g[u])
10     {
11         if(match[v]==-1 || findmatch(match[v]))
12         {
13             match[v]=u;
14             rmatch[u]=v;
15             return 1;
16         }
17     }
18     return 0;
19 }
20
21 int maxMatch(int n)
22 {
23     int ret=0;
24     memset(match, -1, sizeof(match));
25     for(int i=0; i<n; i++)
26     {
27         memset(vis, false, sizeof(vis));
28         ret+=findmatch(i);
29     }
30     return ret;
31 }
```

2.5.2 Maximum Flow

Dinic

```
1  class graph
2  {
3      const static int N=100000;
4  public:
5      vector< pair<int ,int> >edge;
6      vector<int>adj[N];
7      int ptr[N];
8      int dist[N];
9
10     graph(){};
11     void clear()
12     {
13         for(int i=0; i<N; i++)
14             adj[i].clear();
15         edge.clear();
16     }
17     void add_edge(int u, int v, int c)
18     {
19         adj[u].push_back(edge.size());
20         edge.push_back(mp(v, c));
21         adj[v].push_back(edge.size());
22         edge.push_back(mp(u, 0)); //(u, c) if is non-directed
23     }
24     bool dinic_bfs(int s, int t)
25     {
26         memset(dist, -1, sizeof(dist));
27         dist[s]=0;
28
29         queue<int>bfs;
30         bfs.push(s);
31         while(!bfs.empty() && dist[t]==-1)
32         {
33             int u=bfs.front();
34             bfs.pop();
35             for(int i=0; i<adj[u].size(); i++)
36             {
37                 int idx=adj[u][i];
38                 int v=edge[idx].F;
39
40                 if(dist[v]==-1 && edge[idx].S>0)
41                 {
42                     dist[v]=dist[u]+1;
43                     bfs.push(v);
44                 }
45             }
46         }
47         return dist[t]!=-1;
48     }
49     int dinic_dfs(int u, int t, int flow)
50     {
51         if(u==t)
52             return flow;
53         for(int &i=ptr[u]; i<adj[u].size(); i++)
54         {
55             int idx=adj[u][i];
56             int v=edge[idx].F;
57             if(dist[v]==dist[u]+1 && edge[idx].S>0)
58             {
59                 int cf=dinic_dfs(v, t, min(flow, edge[idx].S));
60                 if(cf>0)
61                 {
62                     edge[idx].S-=cf;
63                     edge[idx^1].S+=cf;
64                     return cf;
65                 }
66             }
67         }
68         return 0;
69     }
70     int maxflow(int s, int t)
71     {
72         int ret=0;
```



```
73     while(dinic_bfs(s, t))
74     {
75         memset(ptr, 0, sizeof(ptr));
76         int cf=dinic_dfs(s, t, INF);
77         if(cf==0)
78             break;
79         ret+=cf;
80     }
81     return ret;
82 }
83 };
```

2.5.3 Minimum Cost Maximum Flow

Undirected graph:

$u \rightarrow uu(flow, 0)$
 $uu \rightarrow vv(flow, cost)$
 $vv \rightarrow v(flow, 0)$
 $v \rightarrow uu(flow, 0)$
 $vv \rightarrow u(flow, 0)$

Dijkstra

```
1  typedef int FTYPE; //type of flow
2  typedef int CTYPE; //type of cost
3  typedef pair<FTYPE, CTYPE> pfc;
4  const CTYPE CINF=INF;
5  const FTYPE FINF=INF;
6
7  void operator+=(pfc &p1, pfc &p2)
8  {
9      p1.F+=p2.F;
10     p1.S+=p2.S;
11 }
12
13 class graph
14 {
15     const static int MN=1e+4;
16 public:
17     int n;
18     FTYPE flow[MN];
19     CTYPE dist[MN], pot[MN];
20     int prev[MN], eid[MN];
21
22     struct Edge
23     {
24         int to;
25         FTYPE cap;
26         CTYPE cost;
27         Edge() {};
28         Edge(int _to, FTYPE _cap, CTYPE _cost)
29         {
30             to=_to;
31             cap=_cap;
32             cost=_cost;
33         } //
34     };
35     struct node
36     {
37         int u;
38         CTYPE d;
39         node() {};
40         node(int _u, CTYPE _d)
41         {
42             u=_u;
43             d=_d;
44         }
45         bool operator <(const node &foo) const
46         {
47             return d>foo.d;
48         }
49     };
50     graph() {};
51     vector<int> adj[MN];
52     vector<Edge> edge;
53     inline void set(int _n)
54     {
55         n=_n;
56     }
57     inline void reset()
58     {
59         for(int i=0; i<MN; i++)
60             adj[i].clear();
61         edge.clear();
62     }
```

```

63 inline void add_edge(int u, int v, FTYPE c, FTYPE cst)
64 {
65     adj[u].push_back(edge.size());
66     edge.push_back(Edge(v, c, cst));
67     adj[v].push_back(edge.size());
68     edge.push_back(Edge(u, 0, -cst));
69 }
70
71 pfc dijkstra(int s, int t)
72 {
73     for(register int i=0; i<n; i++)
74         dist[i]=CINF;
75     dist[s]=0;
76     flow[s]=FINF;
77     priority_queue<node>heap;
78     heap.push(node(s, 0));
79     while(!heap.empty())
80     {
81         int u=heap.top().u;
82         CTYPE d=heap.top().d;
83         heap.pop();
84         if(d>dist[u])
85             continue;
86         for(int i=0; i<adj[u].size(); i++)
87         {
88             int idx=adj[u][i];
89             int v=edge[idx].to;
90             CTYPE w=edge[idx].cost;
91             if(!edge[idx].cap || dist[v]<=d+w+pot[u]-pot[v])
92                 continue;
93             if(d+w<dist[v])
94             {
95                 dist[v]=d+w;
96                 prev[v]=u;
97                 eidv[v]=idx;
98                 flow[v]=min(flow[u], edge[idx].cap);
99                 heap.push(node(v, d+w));
100             }
101         }
102     }
103     if(dist[t]==CINF)
104         return mp(FINF, CINF);
105     pfc ret=mp(flow[t], 0);
106     for(int u=t; u!=s; u=prev[u])
107     {
108         int idx=eidx[u];
109         edge[idx].cap-=flow[t];
110         edge[idx^1].cap+=flow[t];
111         ret.second+=flow[t]*edge[idx].cost;
112     }
113     return ret;
114 }
115
116 inline pfc mfmc(int s, int t)
117 {
118     pfc ret=mp(0, 0);
119     pfc got;
120     while((got=dijkstra(s, t)).first!=FINF)
121         ret+=got;
122     return ret;
123 }
124 };

```

Bellmanford

2.5.4 Minimum Cut

Stoer Wagner

```
1  int stoer_wagner(int n)
2  {
3      int ret=INF;
4      for(int i=0; i<n; i++)
5          v[i]=i;
6
7      while(n>1)
8      {
9          a[ v[0] ]=true;
10         for(int i=1; i<n; i++)
11         {
12             a[ v[i] ]=false;
13             na[i-1]=i;
14             w[i]=graph[ v[0] ][ v[i] ];
15         }
16
17         int prev=v[0];
18         for(int i=1; i<n; i++)
19         {
20             int zj=-1;
21             for(int j=1; j<n; j++)
22             {
23                 if(!a[ v[j] ] && (zj<0 || w[j]>w[zj]))
24                     zj=j;
25             }
26
27             a[ v[zj] ]=true;
28
29             if(i==n-1)
30             {
31                 ret=min(ret , w[zj] );
32
33                 for(int j=0; j<n; j++)
34                     graph[ v[j] ][prev]=graph[prev][ v[j] ]+=graph[ v[zj] ][ v[j] ];
35                 v[zj]=v[--n];
36                 break;
37             }
38             prev=v[zj];
39
40             for(int j=1; j<n; j++)
41                 if(!a[ v[j] ])
42                     w[j]+=graph[ v[zj] ][ v[j] ];
43         }
44     }
45     return ret;
46 }
```

2.6 Tree

2.6.1 Lowest Common Ancestor

```
1  const int MN=1e+5+35;
2  const int LMN=1+log2(MN);
3  vector<int>graph[MN];
4  int LVL[MN];
5  int T[MN];
6  int dp[MN][LMN];
7  bool vis[MN];
8
9  void dfs(int u, int f, int d)
10 {
11     vis[u]=true;
12     LVL[u]=d;
13     dp[u][0]=f;
14     for(int i=1; i<LMN; i++)
15         dp[u][i]=dp[ dp[u][i-1] ][i-1];
16
17     vis[x]=true;
18     for(int i=0; i<graph[x].size(); i++)
19     {
20         int v=graph[x][u];
21         if(!vis[v])
22             dfs(v, x, d+1);
23     }
24 }
25
26 inline int lca(int u, int v)
27 {
28     if(LVL[u]>LVL[v])
29         swap(u, v);
30     for(int i=LMN-1; i>=0; i--)
31         if(LVL[v]-(1<<i)>=LVL[u])
32             v=dp[v][i];
33     if(u==v)
34         return u;
35     for(int i=LMN-1; i>=0; i--)
36     {
37         if(dp[u][i]!=dp[v][i])
38         {
39             u=dp[u][i];
40             v=dp[v][i];
41         }
42     }
43     return dp[u][0];
44 }
```

2.6.2 Centroid Decomposition

```
1  class graph
2  {
3      const static int N=1e+5;
4      const static int LN=log2(N)+1;
5  public:
6      vector<int>g[N];
7      int h[N], lca[N][LN];
8
9      int sz[N];
10     int cg[N], gsz, dlt[N];
11     graph(){};
12     inline void addEdge(int u, int v)
13     {
14         g[u].pb(v);
15         g[v].pb(u);
16     }
17     void buildLca(int u, int f)
18     {
19         lca[u][0]=f;
20         for(int i=1; i<LN; i++)
21             lca[u][i]=lca[lca[u][i-1]][i-1];
22         for(int v:g[u])
23         {
24             if(v==f)
25                 continue;
26             h[v]=h[u]+1;
27             buildLca(v, u);
28         }
29     }
30     inline int getLca(int u, int v)
31     {
32         if(h[u]>h[v])
33             swap(u, v);
34         for(int i=LN-1; i>=0; i--)
35             if(h[v]-(1<<i)>=h[u])
36                 v=lca[v][i];
37         if(u==v)
38             return u;
39         for(int i=LN-1; i>=0; i--)
40         {
41             if(lca[u][i]!=lca[v][i])
42             {
43                 u=lca[u][i];
44                 v=lca[v][i];
45             }
46         }
47         return lca[u][0];
48     }
49     inline int getDist(int u, int v)
50     {
51         return h[u]+h[v]-2*h[getLca(u, v)];
52     }
53     void buildSz(int u, int f)
54     {
55         gsz++;
56         sz[u]=1;
57         for(int v:g[u])
58         {
59             if(v==f || dlt[v])
60                 continue;
61             buildSz(v, u);
62             sz[u]+=sz[v];
63         }
64     }
65     int findCentroid(int u, int f)
66     {
67         for(int v:g[u])
68         {
69             if(v==f || dlt[v])
70                 continue;
71             if(sz[v]*2>=gsz)
72                 return findCentroid(v, u);
73         }
74         return u;
```

```

75     }
76     inline void buildCentroid(int u, int f)
77     {
78         gsz=0;
79         buildSz(u, u);
80         int c=findCentroid(u, u);
81         cg[c]=(u==f)?c:f;
82         dlt[c]=1;
83         for(int v:g[c])
84         {
85             if(v==c || dlt[v])
86                 continue;
87             buildCentroid(v, c);
88         }
89     }
90 };

```

2.6.3 Heavy Light Decomposition on Edges

```
1  class segtree
2  {
3      const static int N=1e+5;
4  public:
5      int tr[4*N];
6      segtree(){};
7      void reset()
8      {
9          memset(tr, 0, sizeof(tr));
10     }
11     void update(int no, int l, int r, int i, int val)
12     {
13         if(r<i || l>i)
14             return;
15         if(l>=i && r<=i)
16         {
17             tr[no]=val;
18             return;
19         }
20         int nxt=(no<<1);
21         int mid=(l+r)>>1;
22         update(nxt, l, mid, i, val);
23         update(nxt+1, mid+1, r, i, val);
24         tr[no]=tr[nxt]+tr[nxt+1];
25     }
26     int query(int no, int l, int r, int i, int j)
27     {
28         if(r<i || l>j)
29             return 0;
30         if(l>=i && r<=j)
31             return tr[no];
32         int nxt=(no<<1);
33         int mid=(l+r)>>1;
34         return query(nxt, l, mid, i, j)+query(nxt+1, mid+1, r, i, j);
35     }
36 };
37
38 const int N=1e+5;
39 const int M=log2(N)+1;
40 int n;
41 segtree tr;
42 vector< pair<int,int> >g[N];
43 int lca[N][M];
44 int h[N], trSz[N];
45
46 //in - use X[], Y[] in case
47 //of edge weights
48 int X[N], Y[N], W[N];
49
50 //hld
51 int chainInd[N], chainSize[N], chainHead[N], chainPos[N], chainNo, posInBase[N];
52 int ptr;
53
54 void dfs(int u, int l)
55 {
56     trSz[u]=1;
57     lca[u][0]=l;
58     for(int i=1; i<M; i++)
59         lca[u][i]=lca[lca[u][i-1]][i-1];
60     for(int i=0; i<g[u].size(); i++)
61     {
62         int v=g[u][i].first;
63         if(v==l)
64             continue;
65         h[v]=h[u]+1;
66         dfs(v, u);
67         trSz[u]+=trSz[v];
68     }
69 }
70
71 inline int getLca(int u, int v)
72 {
73     if(h[u]>h[v])
74         swap(u, v);
```



```

75     for(int i=M-1; i>=0; i--)
76         if(h[v]-(1<<i)>=h[u])
77             v=lca[v][i];
78     if(u==v)
79         return u;
80     for(int i=M-1; i>=0; i--)
81     {
82         if(lca[u][i]!=lca[v][i])
83         {
84             u=lca[u][i];
85             v=lca[v][i];
86         }
87     }
88     return lca[u][0];
89 }
90
91 //dont use 'c' if the weight is on the vertex
92 //instead of the edge
93 inline void hld(int u, int l, int c)
94 {
95     if(chainHead[chainNo]==-1)
96         chainHead[chainNo]=u;
97     chainInd[u]=chainNo;
98     chainPos[u]=chainSize[chainNo]++;
99     tr.update(1, 0, n, ptr, c);
100     posInBase[u]=ptr++;
101
102     int msf, idx;
103     msf=idx=-1;
104     for(int i=0; i<g[u].size(); i++)
105     {
106         int v=g[u][i].first;
107         if(v==l)
108             continue;
109         if(trSz[v]>msf)
110         {
111             msf=trSz[v];
112             idx=i;
113         }
114     }
115     if(idx>=0)
116         hld(g[u][idx].first, u, g[u][idx].second);
117     for(int i=0; i<g[u].size(); i++)
118     {
119         if(i==idx)
120             continue;
121         int v=g[u][i].first;
122         int w=g[u][i].second;
123         if(v==l)
124             continue;
125         chainNo++;
126         hld(v, u, w);
127     }
128 }
129
130 inline int query_up(int u, int v)
131 {
132     int uchain=chainInd[u];
133     int vchain=chainInd[v];
134     int ret=0;
135     while(true)
136     {
137         uchain=chainInd[u];
138         if(uchain==vchain)
139         {
140             ret+=tr.query(1, 0, n, posInBase[v]+1, posInBase[u]);
141             break;
142         }
143         int head=chainHead[uchain];
144         ret+=tr.query(1, 0, n, posInBase[head], posInBase[u]);
145         u=head;
146         u=lca[u][0];
147     }
148     return ret;
149 }
150
151 //returns sum of all edges weights

```

```

152 //from 'u' to 'v'
153 inline int query(int u, int v)
154 {
155     if(u==v)
156         return 0;
157     int l=getLca(u, v);
158     return query_up(u, l)+query_up(v, l);
159 }
160
161 //set and edge to value 'val'
162 inline void update(int u, int val)
163 {
164     int x=X[u], y=Y[u];
165     if(lca[x][0]==y)
166         tr.update(1, 0, n, posInBase[x], val);
167     else
168         tr.update(1, 0, n, posInBase[y], val);
169 }
170
171 void clearHld()
172 {
173     //tr.reset();
174     for(int i=0; i<=n; i++)
175     {
176         g[i].clear();
177         chainHead[i]=-1;
178         chainSize[i]=0;
179     }
180     ptr=1;
181     chainNo=0;
182 }
183
184 int main()
185 {
186     scanf("%d", &n);
187     clearHld();
188     for(int i=1; i<n; i++)
189     {
190         scanf("%d_%d_%d", &X[i], &Y[i], &W[i]);
191         g[ X[i] ].push_back({Y[i], W[i]});
192         g[ Y[i] ].push_back({X[i], W[i]});
193     }
194     dfs(1, 0);
195     hld(1, 0, 0);
196     int q;
197     scanf("%d", &q);
198     while(q--)
199     {
200         int o, x, y;
201         scanf("%d_%d_%d", &o, &x, &y);
202         if(o==1)
203             printf("%d\n", query(x, y));
204         else
205             update(x, y);
206     }
207     return 0;
208 }

```

2.6.4 Heavy Light Decomposition on Vertex

2.6.5 All-Pairs Distance & Centroid Decomposition

2.6.6 All-Pairs Distance & FFT

2.7 MISC

2.7.1 2-SAT

Chapter 3

Dynamic Programming

3.1 Optimizations

3.1.1 Divide and Conquer - Exemple 1

Memory can be optimized by using $dp[2][N]$ & $dp[k\%2][m] + dp[(k-1)\%2][m]$

```
1  typedef long long ll;
2  const int MN=1e+4+35;
3  const int MN2=535;
4  int p, a;
5  ll data[MN];
6  inline ll getValue(int l, int r)
7  {
8      return (r-l+1)*(data[r]-data[l-1]);
9  }
10 ll dp[MN2][MN];
11 inline void solve(int k, int l, int r, int L, int R)
12 {
13     if(l>r)
14         return;
15     int m=(l+r)/2;
16     int s=L;
17     dp[k][m]=LINF;
18     for(int i=max(m, L); i<=R; i++)
19     {
20         if(dp[k][m]>dp[k-1][i+1]+getValue(m+1, i+1))
21         {
22             dp[k][m]=dp[k-1][i+1]+getValue(m+1, i+1);
23             s=i;
24         }
25     }
26     solve(k, l, m-1, L, s);
27     solve(k, m+1, r, s, R);
28 }
29 int main()
30 {
31     scanf("%d_%d", &p, &a);
32     for(int i=1; i<=p; i++)
33     {
34         ll x;
35         scanf("%lld", &x);
36         data[i]=data[i-1]+x;
37     }
38     for(int i=0; i<=p; i++)
39         dp[0][i]=LINF;
40     for(int i=0; i<=a; i++)
41         dp[i][p]=0;
42     for(int i=1; i<=a; i++)
43         solve(i, 0, p-1, 0, p-1);
44     printf("%lld\n", dp[a][0]);
45 }
```

3.1.2 Divide and Counquer - Exemple 2

```
1  typedef long long ll;
2  const int MN=6005;
3  ll v[MN];
4  ll dp[MN][MN];
5  ll c[MN][MN];
6
7  ll sum[MN];
8  ll multisum[MN];
9
10 void solve(int k, int l, int r, int L, int R)
11 {
12     if(l>r)
13         return;
14     int m=(l+r)/2;
15     int s=-1;
16     dp[k][m]=LINF;
17     for(int i=max(m, L); i<=R; i++)
18     {
19         if(dp[k][m]>dp[k-1][i+1]+c[m][i])
20         {
21             dp[k][m]=dp[k-1][i+1]+c[m][i];
22             s=i;
23         }
24     }
25     solve(k, l, m-1, L, s);
26     solve(k, m+1, r, s, R);
27 }
28
29 ll dist(int l, int r, int mid)
30 {
31     ll s1=sum[mid]-sum[l];
32     ll p1=multisum[mid]-multisum[l];
33     ll s2=sum[r+1]-sum[mid+1];
34     ll p2=multisum[r+1]-multisum[mid+1];
35     return (s1*mid-p1)+(p2-s2*mid);
36 }
37
38 int main()
39 {
40     int n;
41     ll b, k;
42     scanf("%d_%lld_%lld", &n, &b, &k);
43     for(int i=0; i<n; i++)
44     {
45         scanf("%lld", &v[i]);
46         sum[i+1]=sum[i]+v[i];
47         multisum[i+1]=multisum[i]+v[i]*1LL*i;
48     }
49
50     for(int i=0; i<n; i++)
51     {
52         int mid=i;
53         ll tot=0;
54         ll smid=v[i];
55         for(int j=i; j<n; j++)
56         {
57             tot+=v[j];
58             while(smid+smid<tot)
59                 smid+=v[++mid];
60             c[i][j]=k*dist(i, j, mid);
61         }
62     }
63     for(int i=0; i<=n; i++)
64         dp[0][i]=LINF;
65     for(int i=0; i<=k; i++)
66         dp[i][n]=0;
67
68     for(int i=1; i<=n; i++)
69     {
70         solve(i, 0, n-1, 0, n-1);
71         i>1?printf("_"):NULL;
72         printf("%lld", i*b+dp[i][0]);
73     }
74     printf("\n");
```

75
76
77

```
return 0;
```

```
}
```

3.1.3 Convex Hull I

Original recurrence:

$$dp[i] = \min(dp[j] + b[j] * a[i]) \text{ for } j < i$$

Conditions:

$$b[j] \geq b[j + 1]$$

$$a[i] \leq a[i + 1]$$

Solution:

Hull cht=Hull() or DynamicHull cht;

cht.insertLine(b[0], dp[0])

for(int i=1; i<n; i++)

```
{
    dp[i]=cht.query(a[i]);
    cht.insertLine(b[i], dp[i]);
}
```

answer is dp[n-1];

Linear

```
1  class Hull
2  {
3      const static int CN=1e+5+35;
4      public:
5          long long a[CN], b[CN];
6          double x[CN];
7          int head, tail;
8          Hull():head(1), tail(0){};
9
10         long long query(long long xx)
11         {
12             if(head>tail)
13                 return 0;
14             while(head<tail && x[head+1]<=xx)
15                 head++;
16             x[head]=xx;
17             return a[head]*xx+b[head];
18         }
19
20         void insertLine(long long aa, long long bb)
21         {
22             double xx=-1e18;
23             while(head<=tail)
24             {
25                 if(aa==a[tail])
26                     return;
27                 xx=1.0*(b[tail]-bb)/(aa-a[tail]);
28                 if(head==tail || xx>=x[tail])
29                     break;
30                 tail--;
31             }
32             a[++tail]=aa;
33             b[tail]=bb;
34             x[tail]=xx;
35         }
36     };
```

Dynamic

```
1  const long long is_query=-(1LL<<62);
2  class Line
3  {
4  public:
5      long long m, b;
6      mutable function<const Line*>succ;
7      bool operator < (const Line &rhs) const
8      {
9          if (rhs.b!=is_query)
10             return m<rhs.m;
11             const Line *s=succ();
12             if (!s)
13                 return 0;
14             long long x=rhs.m;
15             return (b-s->b)<((s->m-m)*x);
16         }
17 };
18
19 class HullDynamic: public multiset<Line>
20 {
21 public:
22     void clear()
23     {
24         clear();
25     }
26     bool bad(iterator y)
27     {
28         auto z=next(y);
29         if (y==begin())
30         {
31             if (z==end())
32                 return 0;
33             return (y->m==z->m && y->b<=z->b);
34         }
35         auto x=prev(y);
36         if (z==end())
37             return (y->m == x->m && y->b<=x->b);
38         return ((x->b - y->b)*(z->m - y->m) >= (y->b - z->b)*(y->m - x->m));
39     }
40     void insertLine(ll m, ll b)
41     {
42         auto y=insert({m, b});
43         y->succ=[=]
44         {
45             return next(y)==end()?0:&*next(y);
46         };
47         if (bad(y))
48         {
49             erase(y);
50             return;
51         }
52         while (next(y)!=end() && bad(next(y)))
53             erase(next(y));
54         while (y!=begin() && bad(prev(y)))
55             erase(prev(y));
56     }
57     long long query(long long x)
58     {
59         auto ret=*lower_bound((Line){x, is_query});
60         return ret.m*x+ret.b;
61     }
62 };;
```

3.1.4 Convex Hull II

3.1.5 Knuth Optimization

3.2 Matrix Exponentiation

```
1  typedef long long ll;
2  typedef vector<vector<ll>> matrix;
3  const ll MOD=303700049;
4  int n, t;
5  ll k;
6  ll val[101];
7
8  ll modmul(ll a, ll b)
9  {
10     return ((a%MOD)*(b%MOD))%MOD;
11 }
12
13 ll modsum(ll a, ll b)
14 {
15     return ((a%MOD)+(b%MOD))%MOD;
16 }
17
18 matrix basem;
19 matrix mat_mul(matrix A, matrix B)
20 {
21     int t=A.size();
22     matrix ret=basem;
23     for(int i=0; i<t; i++)
24     {
25         for(int j=0; j<t; j++)
26         {
27             for(int k=0; k<t; k++)
28             {
29                 ret[i][j]=(ret[i][j]+A[i][k]*B[k][j]);
30             }
31             ret[i][j]%=MOD;
32         }
33     }
34     return ret;
35 }
36
37 matrix mat_pow(matrix &A, ll k)
38 {
39     if(k==1)
40         return A;
41     if(k&1)
42         return mat_mul(A, mat_pow(A,k-1));
43     matrix ret=mat_pow(A, k>>1);
44     return mat_mul(ret, ret);
45 }
46
47 //o build pode variar, sendo ele a base do fibonacci
48 matrix build()
49 {
50     matrix ret(t, vector<ll>(t));
51     for(int i=0; i<n; i++)
52         ret[0][i]=i+1;
53     for(int i=1; i<n; i++)
54         for(int j=0; j<n; j++)
55             ret[i][j]=(j+1==i);
56     for(int i=0; i<n; i++)
57         ret[t-1][i]=i+1;
58     ret[t-1][t-1]=1;
59     return ret;
60 }
61
62 pair<ll,ll>calc(ll k)
63 {
64     if(n>=k)
65         return mp(val[k-1], 0);
66     matrix base=build();
67     matrix fib=mat_pow(base, k-n);
68
69     ll ret=0;
70     reverse(val, val+n);
71     for(int i=0; i<n; i++)
72         ret=modsum(ret, modmul(fib[0][i], val[i]));
73
74     ll sum=0;
```



```

75     for(int i=0; i<n; i++)
76         sum=modsum(sum, modmul(fib[n][i], val[i]));
77     return mp(ret, sum);
78 }
79
80 void solve()
81 {
82     //First = f(n-x), Second = somatoria de f(0) ate f(n-x)
83     pair<ll, ll>ans=calc(k);
84     if(k>n)
85     {
86         for(int i=0; i<n; i++)
87         {
88             ans.S=ans.S+val[i];
89             if(ans.S>MOD)
90                 ans.S%=MOD;
91         }
92     }
93     else
94     {
95         for(int i=0; i<k; i++)
96         {
97             ans.S=ans.S+val[i];
98             if(ans.S>MOD)
99                 ans.S%=MOD;
100         }
101     }
102     printf("%lld_%lld\n", ans.F, ans.S);
103 }
104
105 int main()
106 {
107     while(scanf("%d_%lld", &n, &k)!=EOF)
108     {
109         t=n+1;
110         basem.clear();
111         basem.resize(t, vector<ll>(t));
112         //val[i] = valores iniciais conhecidos da recorrência
113         for(int i=0; i<n; i++)
114         {
115             scanf("%lld", &val[i]);
116         }
117         solve();
118     }
119     return 0;
120 }

```

3.3 Digits

```
1 char str[100];
2 int dp[100][300][2];
3 bool memo[100][300][2];
4 int n, k;
5
6 //numeros de 0 a x, tal que a soma dos digitos eh igual a k
7 int solve(int i, int s, int t)
8 {
9     if(i==n)
10     {
11         if(!t && s==k)
12             return 1;
13         return 0;
14     }
15     if(s>k)
16         return 0;
17     if(memo[i][s][t])
18         return dp[i][s][t];
19     int &ret=dp[i][s][t]=0;
20     if(t)
21     {
22         for(int j=0; j<=str[i]-'0'; j++)
23         {
24             if(j==str[i]-'0')
25                 ret+=solve(i+1, s+j, 1);
26             else
27                 ret+=solve(i+1, s+j, 0);
28         }
29     }
30     else
31     {
32         for(int j=0; j<10; j++)
33         {
34             ret+=solve(i+1, s+j, 0);
35         }
36     }
37     memo[i][s][t]=true;
38     return ret;
39 }
40
41 //quantos bits ativos existem entre 0 e x
42 string str2;
43 int n2;
44 int dp2[100][300][2];
45 bool memo2[100][300][2];
46 int solve2(int i, int s, int t)
47 {
48     if(i==n2)
49         return s;
50     if(memo2[i][s][t])
51         return dp2[i][s][t];
52     int &ret=dp2[i][s][t]=0;
53     if(t)
54     {
55         for(int j=0; j<=str2[i]-'0'; j++)
56         {
57             if(j==str2[i]-'0')
58                 ret+=solve2(i+1, s+(j==1), 1);
59             else
60                 ret+=solve2(i+1, s+(j==1), 0);
61         }
62     }
63     else
64     {
65         for(int j=0; j<2; j++)
66         {
67             ret+=solve2(i+1, s+(j==1), 0);
68         }
69     }
70     memo2[i][s][t]=true;
71     return ret;
72 }
73
74 //numeros de 1 a x, tal que a soma dos digitos eh multiplo de k
```

```

75 char str3[100];
76 int n3;
77 int dp3[100][300][2];
78 bool memo3[100][300][2];
79 int solve3(int i, int s, int t)
80 {
81     if(i==n3)
82         return !s;
83     if(memo3[i][s][t])
84         return dp3[i][s][t];
85     int &ret=dp3[i][s][t]=0;
86     if(t)
87     {
88         for(int j=0; j<=str3[i]-'0'; j++)
89         {
90             if(j==str3[i]-'0')
91                 ret+=solve3(i+1, (s+j)%k, 1);
92             else
93                 ret+=solve3(i+1, (s+j)%k, 0);
94         }
95     }
96     else
97     {
98         for(int j=0; j<10; j++)
99         {
100             ret+=solve3(i+1, (s+j)%k, 0);
101         }
102     }
103     memo3[i][s][t]=true;
104     return ret;
105 }
106
107 //numeros de 1 a x, tal que o xor dos digitos eh igual a k
108 char str4[100];
109 int n4;
110 int dp4[100][300][2];
111 bool memo4[100][300][2];
112 int solve4(int i, int s, int t)
113 {
114     if(i==n4)
115         return s==k;
116     if(memo4[i][s][t])
117         return dp4[i][s][t];
118     int &ret=dp4[i][s][t]=0;
119     if(t)
120     {
121         for(int j=0; j<=str4[i]-'0'; j++)
122         {
123             if(j==str4[i]-'0')
124                 ret+=solve4(i+1, (s^j), 1);
125             else
126                 ret+=solve4(i+1, (s^j), 0);
127         }
128     }
129     else
130     {
131         for(int j=0; j<10; j++)
132         {
133             ret+=solve4(i+1, (s^j), 0);
134         }
135     }
136     memo4[i][s][t]=true;
137     return ret;
138 }

```

3.4 Grundy Numbers

Positions have the following properties:

- All terminal positions are losing.
- If a player is able to move to a losing position then he is in a winning position.
- If a player is able to move only to the winning positions then he is in a losing position.

```
1  const int MN=1e+5;
2  bool memo[MN];
3  int dp[MN];
4  int grundy(int x)
5  {
6      if(x==0)
7          return 0;
8      if(memo[x])
9          return dp[x];
10     set<int>mex;
11     for(;;) //moves
12         mex.insert(grundy(x-(moves)));
13     int &ret=dp[x]=0;
14     while(mex.count(ret))
15         ret++;
16     memo[x]=true;
17     return ret;
18 }
```

Chapter 4

String

4.1 Hash

```
1 typedef unsigned long long ull;
2 class hashc
3 {
4 public:
5     vector<ull>prefix;
6     vector<ull>power;
7     int k=37;
8     int t;
9     hashc(){};
10    hashc(vector<int>&data)
11    {
12        t=data.size();
13        prefix.resize(t+1, 0);
14        power.resize(t+1, 0);
15        prefix[0]=0;
16        power[0]=1;
17        for(int i=0; i<t; i++)
18        {
19            prefix[i+1]=prefix[i]*k+data[i];
20            power[i+1]=power[i]*k;
21        }
22    }
23
24    hashc build(string &str)
25    {
26        vector<int>data(str.size());
27        for(int i=0; i<str.size(); i++)
28            data[i]=(str[i]-'a'+1);
29        return hashc(data);
30    }
31
32    ull get()
33    {
34        return prefix[t];
35    }
36    ull calc(int l, int r)
37    {
38        return prefix[r]-(prefix[l-1]*power[r-l+1]);
39    }
40    bool same(int xl, int xr, int yl, int yr)
41    {
42        return this->calc(xl, xr)==this->calc(yl, yr);
43    }
44    int find(hashc &pattern)
45    {
46        int pt=pattern.t;
47        ull val=pattern.calc(1, pt);
48        for(int i=1; i<=t-pt+1; i++)
49        {
50            if(this->calc(i, i+pt-1)==val)
51                return i-1;
52        }
53        return -1;
```

```
54     }  
55 };
```

4.2 KMP

```
1  int lps[1000000];
2  void lps_calc(string &str)
3  {
4      lps[0]=0;
5      for(int i=1, j=0, f=0; i<str.size(); i+=f, f=0)
6      {
7          if(str[i]==str[j])
8          {
9              lps[i]=j;
10             j++;
11             f=1;
12         }
13         else
14         {
15             if(j>0)
16             {
17                 j=lps[j-1];
18             }
19             else
20             {
21                 lps[i]=0;
22                 f=1;
23             }
24         }
25     }
26 }
27
28 //finding str in pat
29 void kmp(string &str, string &pat)
30 {
31     lps_calc(pat);
32     int i=0, j=0;
33     while(i<str.size())
34     {
35         if(str[i]==pat[j])
36         {
37             i++;
38             j++;
39         }
40         if(j==pat.size())
41         {
42             printf("Padrao_encontrado_em:_%d,_%d", i-j, (i-j)+pat.size()-1);
43             j=lps[j-1];
44         }
45         else if(i<str.size() && str[i]!=pat[j])
46         {
47             if(j!=0)
48                 j=lps[j-1];
49             else
50                 i++;
51         }
52     }
53 }
```

4.3 Aho Corasick

```
1  class aho_corasick
2  {
3  private:
4      static const int MNT=1e+6;
5      static const int MNC=26;
6  public:
7      int trie[MNT][MNC];
8      int term[MNT];
9      int link[MNT];
10     int sum[MNT];
11     int cnt=1;
12     aho_corasick(){};
13     void clear()
14     {
15         RESET(trie, 0);
16         RESET(term, 0);
17         RESET(link, 0);
18         RESET(sum, 0);
19         cnt=1;
20     }
21     int node(int x, int j)
22     {
23         return trie[x][j];
24     }
25     int end(int x, int j)
26     {
27         return term[ node(x,j) ];
28     }
29     void insert(char *str)
30     {
31         int sz=strlen(str);
32         int no=0;
33         for(int i=0; i<sz; i++)
34         {
35             int x=str[i]-'a';
36             if(!trie[no][x])
37                 trie[no][x]=cnt++;
38             sum[ trie[no][x] ]++;
39             no=trie[no][x];
40         }
41         term[no]++;
42     }
43     bool find(char *str)
44     {
45         int sz=strlen(str);
46         int no=0;
47         for(int i=0; i<sz; i++)
48         {
49             int x=str[i]-'a';
50             if(!sum[ trie[no][x] ])
51                 return false;
52             no=trie[no][x];
53         }
54         return true;
55     }
56     void erase(char *str)
57     {
58         int sz=strlen(str);
59         int no=0;
60         for(int i=0; i<sz; i++)
61         {
62             int x=str[i]-'a';
63             sum[ trie[no][x] ]--;
64             no=trie[no][x];
65         }
66         term[no]--;
67     }
68     void update_link()
69     {
70         queue<int> aho;
71         aho.push(0);
72         while(!aho.empty())
73         {
74             int x=aho.front();
```



```

75     aho.pop();
76     term[x]=term[ link[x] ];
77     for(int i=0; i<MNC; i++)
78     {
79         if(trie[x][i])
80         {
81             int y=trie[x][i];
82             aho.push(y);
83             link[y]=x? trie[ link[x] ][i]:0;
84         }
85         else
86         {
87             trie[x][i]=trie[ link[x] ][i];
88         }
89     }
90 }
91 }
92 };

```

4.4 Manacher

4.5 Z-Algorithm

4.6 Suffix Array & LCP

```
1  const int MN=1e+6+35;
2  int data[MN], sa[MN], lcp[MN], lcp_rank[MN];
3
4  // lexicographic order for pairs
5  inline bool leq(int a1, int a2, int b1, int b2)
6  {
7      return(a1 < b1 || a1 == b1 && a2 <= b2);
8  }
9
10 // and triples
11 inline bool leq(int a1, int a2, int a3, int b1, int b2, int b3)
12 {
13     return(a1 < b1 || a1 == b1 && leq(a2,a3, b2,b3));
14 } // and triples
15
16 // stably sort a[0..n-1] to b[0..n-1] with keys in 0..K from r
17 static void radixPass(int* a, int* b, int* r, int n, int K)
18 { // count occurrences
19     int* c = new int[K + 1]; // counter array
20     for (int i = 0; i <= K; i++)
21         c[i] = 0; // reset counters
22     for (int i = 0; i < n; i++)
23         c[r[a[i]]]++; // count occurrences
24     for (int i = 0, sum = 0; i <= K; i++) // exclusive prefix sums
25     {
26         int t = c[i];
27         c[i] = sum;
28         sum += t;
29     }
30     for (int i = 0; i < n; i++)
31         b[c[r[a[i]]]++] = a[i]; // sort
32 }
33
34 // find the suffix array SA of s[0..n-1] in {1..K}^n
35 // require s[n]=s[n+1]=s[n+2]=0, n>=2
36 void suffixArray(int* s, int* SA, int n, int K)
37 {
38     int n0 = (n+2)/3, n1 = (n+1)/3, n2 = n/3, n02 = n0+n2;
39     int* s12 = new int[n02+3]; s12[n02] = s12[n02+1] = s12[n02+2] = 0;
40     int* SA12 = new int[n02+3]; SA12[n02] = SA12[n02+1] = SA12[n02+2] = 0;
41     int* s0 = new int[n0];
42     int* SA0 = new int[n0];
43     // generate positions of mod 1 and mod 2 suffixes
44     // the "+(n0-n1)" adds a dummy mod 1 suffix if n%3 == 1
45     for (int i=0, j=0; i < n + (n0-n1); i++)
46         if (i%3 != 0) s12[j++] = i;
47     // lsb radix sort the mod 1 and mod 2 triples
48     radixPass(s12, SA12, s+2, n02, K);
49     radixPass(SA12, s12, s+1, n02, K);
50     radixPass(s12, SA12, s, n02, K);
51     // find lexicographic names of triples
52     int name = 0, c0 = -1, c1 = -1, c2 = -1;
53     for (int i = 0; i < n02; i++)
54     {
55         if (s[SA12[i]] != c0 || s[SA12[i]+1] != c1 || s[SA12[i]+2] != c2)
56         {
57             name++;
58             c0 = s[SA12[i]];
59             c1 = s[SA12[i]+1];
60             c2 = s[SA12[i]+2];
61         }
62         if (SA12[i]%3 == 1) s12[SA12[i]/3] = name; // left half
63         else s12[SA12[i]/3 + n0] = name; // right half
64     }
65     // recurse if names are not yet unique
66     if (name < n02)
67     {
68         suffixArray(s12, SA12, n02, name);
69         // store unique names in s12 using the suffix array
70         for(int i=0; i<n02; i++)
71             s12[SA12[i]] = i + 1;
72     }
73     else // generate the suffix array of s12 directly
```

```

74     {
75         for(int i = 0; i < n02; i++)
76             SA12[s12[i] - 1] = i;
77     }
78     // stably sort the mod 0 suffixes from SA12 by their first character
79     for (int i=0, j=0; i<n02; i++)
80         if (SA12[i] < n0) s0[j++] = 3*SA12[i];
81     radixPass(s0, SA0, s, n0, K);
82     // merge sorted SA0 suffixes and sorted SA12 suffixes
83     for (int p = 0, t = n0-n1, k = 0; k < n; k++)
84     {
85         #define GetI() (SA12[t] < n0 ? SA12[t] * 3 + 1 : (SA12[t] - n0) * 3 + 2)
86         int i = GetI(); // pos of current offset 12 suffix
87         int j = SA0[p]; // pos of current offset 0 suffix
88         if (SA12[t] < n0 ? // different compares for mod 1 and mod 2 suffixes
89             leq(s[i], s12[SA12[t] + n0], s[j], s12[j/3]) :
90             leq(s[i], s[i+1], s12[SA12[t]-n0+1], s[j], s[j+1], s12[j/3+n0]))
91             { // suffix from SA12 is smaller
92                 SA[k] = i; t++;
93                 if (t == n02) // done — only SA0 suffixes left
94                     for (k++; p < n0; p++, k++) SA[k] = SA0[p];
95             }
96             else
97             { // suffix from SA0 is smaller
98                 SA[k] = j; p++;
99                 if (p == n0) // done — only SA12 suffixes left
100                     for (k++; t < n02; t++, k++) SA[k] = GetI();
101             }
102     }
103 }
104
105 void buildlcp(int n)
106 {
107     int k=0;
108     for(int i=0; i<n; i++)
109         lcp_rank[ sa[i] ]=i;
110     for(int i=0; i<n; i++, k?k--:0)
111     {
112         if(lcp_rank[i]==n-1)
113         {
114             k=0;
115             continue;
116         }
117         int j=sa[ lcp_rank[i]+1 ];
118         while(i+k<n && j+k<n && data[i+k]==data[k+j])
119             k++;
120         lcp[ lcp_rank[i] ]=k;
121     }
122 }
123
124 int main()
125 {
126     int n;
127     scanf("%d", &n);
128     for(int i=0; i<n; i++)
129     {
130         char x;
131         scanf("%c", &x);
132         data[i]=(int)x;
133     }
134     //data[i]>=1
135     data[n]=data[n+1]=data[n+2]=data[n+3]=0;
136     n++;
137     //suffixArray(string, ponteiro para suffix array, numero de elementos da string, number of
        elementos do alfabeto);
138     suffixArray(data, sa, n, 256);
139     for(int i=0; i<n; i++)
140         printf("%d_", sa[i]);
141     printf("\n\n");
142
143     //buildlcp(numero de elementos da string)
144     buildlcp(n);
145     for(int i=0; i<n; i++)
146         printf("%d\n", lcp[i]);
147     return 0;
148 }

```

4.7 Suffix Tree

Chapter 5

Mathematic

5.1 Prime Numbers

5.1.1 Erastotenes Sieve

5.1.2 Linear Sieve

```
1 //prime(x):(lp[x]==x)
2 const int MN=1e+6;
3 long long lp[MN+1];
4 vector<long long>pr;
5
6 void sieve()
7 {
8     for(long long i=2; i<=MN; i++)
9     {
10         if(lp[i]==0)
11         {
12             lp[i]=i;
13             pr.push_back(i);
14         }
15         for(long long j=0; j<pr.size() && pr[j]<=lp[i] && i*pr[j]<=MN; j++)
16             lp[i*pr[j]]=pr[j];
17     }
18 }
```

5.1.3 Miller Rabin

```
1 //millerRabin(n) returns if n is prime
2 //not accurate for all n
3 #define gcd(x, y) __gcd(x, y)
4 ll powmod(ll a, ll b, ll m)
5 {
6     ll ret=1;
7     while(b)
8     {
9         if(b&1)
10             ret=(ret*a)%m, —b;
11         else
12             a=(a*a)%m, b>>=1;
13     }
14     return ret;
15 }
16
17 bool millerRabin(ll n)
18 {
19     ll b=2;
20     for(ll g; (g=gcd(n, b))!=1; b++)
21         if(n>g)
22             return false;
23     ll p=0, q=n-1;
24     while((q&1)==0)
25         p++, q>>=1;
26     ll rem=powmod(b, q, n);
27     if(rem==1 || rem==n-1)
28         return true;
29     for(ll i=1; i<p; i++)
30     {
31         rem=(rem*rem)%n;
32         if(rem==n-1)
33             return true;
34     }
35     return false;
36 }
```

5.1.4 BPSW

```
1 //bpsw(n) returns if n is prime
2 #define gcd(x, y) __gcd(x, y)
3 ll jacobi(ll a, ll b)
4 {
5     if(a==0 || a==1)
6         return a;
7     if(a<0)
8     {
9         if((b&2)==0)
10             return jacobi(-a, b);
11         return -jacobi(-a, b);
12     }
13     ll a1=a, e=0;
14     while((a1&1)==0)
15         a1>>=1, e++;
16     ll s;
17     if((e&1)==0 || (b&7)==1 || (b&7)==7)
18         s=1;
19     else
20         s=-1;
21     if((b&3)==3 && (a1&3)==3)
22         s=-s;
23     if(a1==1)
24         return s;
25     return s*jacobi(b%a1, a1);
26 }
27
28 bool bpsw(ll n)
29 {
30     if((ll)sqrt(n+0.0)*(ll)sqrt(n+0.0)==n)
31         return false;
32     ll dd=5;
33     while(1)
34     {
35         ll g=gcd(n, abs(dd));
36         if(1<g && g<n)
37             return false;
38         if(jacobi(dd, n)==-1)
39             break;
40         dd=dd<0?-dd+2:-dd-2;
41     }
42     ll p=1, q=(p*p-dd)/4;
43     ll d=n+1, s=0;
44     while((d&1)==0)
45         s++, d>>=1;
46     ll u=1, v=p, u2m=1, v2m=p, qm=q, qm2=q*2, qkd=q;
47     for(ll mask=2; mask<=d; mask<<=1)
48     {
49         u2m=(u2m*v2m)%n;
50         v2m=(v2m*v2m)%n;
51         while(v2m<qm2)
52             v2m+=n;
53         v2m-=qm2;
54         qm=(qm*qm)%n;
55         qm2=qm*2;
56         if(d&mask)
57         {
58             ll t1=(u2m*v)%n, t2=(v2m*u)%n;
59             ll t3=(v2m*v)%n, t4=((u2m*u)%n)*dd%n;
60             u=t1+t2;
61             if(u&1)
62                 u+=n;
63             u=(u>>1)%n;
64             v=(t3+t4);
65             if(v&1)
66                 v+=n;
67             v=(v>>1)%n;
68             qkd=(qkd*qm)%n;
69         }
70     }
71     if(u==0 || v==0)
72         return true;
73     ll qkd2=qkd*2;
74     for(ll r=1; r<s; r++)
```



```

75     {
76         v=(v*v)%n-qkd2;
77         v+=v<0?n:0;
78         v+=v<0?n:0;
79         v-=v>=n?n:0;
80         v-=v>=n?n:0;
81         if (v==0)
82             return true;
83         if (r<s-1)
84             {
85                 qkd=(qkd*1LL*qkd)%n;
86                 qkd2=qkd*2;
87             }
88     }
89     return false;
90 }

```

5.1.5 Primality Test

```
1 //call sieve() before isPrime(x)
2 //define k=50 as trivial limit
3 bool isPrime(ll x)
4 {
5     if(x==1)
6         return false;
7     if(x==2)
8         return true;
9     if(x%2==0)
10        return false;
11    for(int i=0; i<k && x>pr[i]; i++)
12        if(x%pr[i]==0)
13            return false;
14    if(pr[k-1]*pr[k-1]>=x)
15        return true;
16    //return only millerRabin(x) for fast process
17    //not accurate for all x
18    return millerRabin(x)?bpsw(x):false;
19 }
```

5.1.6 Java Pollard Rho Decomposition

```
1 public static Random rand = new Random();
2 public static long v, ans=1, fact;
3 public static long gcd(long x, long y)
4 {
5     if(y==0)
6         return x;
7     return gcd(y, x%y);
8 }
9 public static long rho(long x)
10 {
11     long a, b, cnt=2;
12     a=b=rand.nextLong()%x;
13     for(long i=1; ;i++)
14     {
15         BigInteger Ba=BigInteger.valueOf(a);
16         BigInteger Bx=BigInteger.valueOf(x);
17         BigInteger aux=Ba.multiply(Ba).add(BigInteger.valueOf(2)).mod(Bx);
18         a=aux.longValue();
19         if(a==b)
20             return 0;
21         long g=gcd(Math.abs(a-b), x);
22         if(g!=1)
23             return g;
24         if(i==cnt)
25         {
26             b=a;
27             cnt*=2;
28         }
29     }
30 }
31 public static void solve(long x)
32 {
33     BigInteger Bx=BigInteger.valueOf(x);
34     if(Bx.isProbablePrime(20))
35     {
36         long cnt=0;
37         while(v%x==0)
38         {
39             v/=x;
40             cnt++;
41         }
42         ans*=(cnt+1);
43         if(v!=1)
44             solve(v);
45     }
46     else
47     {
48         for(fact=rho(x); fact==0; fact=rho(x)){}
49         solve(fact);
50     }
51 }
52 public static void main(String[] args) throws Exception
53 {
54     ans=1;
55     v=sc.nextLong();
56     if(v!=1)
57         solve(v);
58     System.out.println(ans);
59 }
```

5.2 Chinese Remainder Theorem

5.3 Fast Fourier Transformation

```
1  #define PI (double)acos(-1.0)
2  typedef complex<double> base;
3  void fft(vector<base>&data, bool invert)
4  {
5      int n=data.size();
6      for(int i=1, j=0; i<n; i++)
7      {
8          int bit=n>>1;
9          for(; j>=bit; bit>>=1)
10             j-=bit;
11             j+=bit;
12             if(i<j)
13                 swap(data[i], data[j]);
14     }
15
16     for(int len=2; len<=n; len<<=1)
17     {
18         double ang=2*PI/len*(invert?-1:1);
19         base wlen(cos(ang), sin(ang));
20         for(int i=0; i<n; i+=len)
21         {
22             base w(1);
23             for(int j=0; j<len/2; j++)
24             {
25                 base u=data[i+j], v=data[i+j+len/2]*w;
26                 data[i+j]=u+v;
27                 data[i+j+len/2]=u-v;
28                 w*=wlen;
29             }
30         }
31     }
32     if(invert)
33         for(int i=0; i<n; i++)
34             data[i]/=n;
35 }
36
37 vector<int>fft_multiply(vector<int>&a, vector<int>&b)
38 {
39     vector<base>fa(a.begin(), a.end());
40     vector<base>fb(b.begin(), b.end());
41     int n=1;
42     while(n<max(a.size(), b.size()))
43         n<<=1;
44     n<<=1;
45     fa.resize(n);
46     fb.resize(n);
47     fft(fa, false);
48     fft(fb, false);
49     for(int i=0; i<n; i++)
50         fa[i]*=fb[i];
51     fft(fa, true);
52
53     vector<int>ret(n);
54     for(int i=0; i<n; i++)
55         ret[i]=(int)(fa[i].real()+0.5);
56
57     int carry=0;
58     for(int i=0; i<n; i++)
59     {
60         ret[i]+=carry;
61         carry=ret[i]/10;
62         ret[i]%=10;
63     }
64     return ret;
65 }
66
67 int main()
68 {
69     int n, m;
70     scanf("%d_%d", &n, &m);
71     vector<int>a,b;
72
73     for(int i=0; i<n; i++)
74     {
```

```

75     int x;
76     scanf("%d", &x);
77     a.pb(x);
78 }
79
80 for(int i=0; i<n; i++)
81 {
82     int x;
83     scanf("%d", &x);
84     b.pb(x);
85 }
86 reverse(a.begin(), a.end());
87 reverse(b.begin(), b.end());
88
89 vector<int>ans=fft_multiply(a, b);
90 reverse(ans.begin(), ans.end());
91 bool flag=false;
92 for(int i=0; i<ans.size(); i++)
93 {
94     if(ans[i])
95         flag=true;
96     if(flag)
97         printf("%d", ans[i]);
98 }
99 printf("\n");
100 return 0;
101 }

```

5.4 Modular Math

5.4.1 Multiplicative Inverse

5.4.2 Linear All Multiplicative Inverse

5.5 Gaussian Elimination

5.6 Combinatorics

Chapter 6

Geometry

6.1 2d Template

6.2 3d Template

6.3 Polygon Template

6.4 Convex Hull

6.4.1 Graham Scan

6.4.2 Monotone Chain

6.5 Rotating Calipers

6.6 KD Tree

6.7 Range Tree

6.8 Circle Sweep

Chapter 7

Templates

7.1 C++

```
1  /// David Mateus Batista <david.batista3010@gmail.com>
2  /// Computer Science – Federal University of Itajuba – Brazil
3
4  #include <bits/stdc++.h>
5
6  using namespace std;
7
8  typedef long long ll;
9  typedef unsigned long long ull;
10 typedef long double ld;
11 typedef pair<int,int> pii;
12 typedef pair<ll,ll> pll;
13
14 #define INF 0x3F3F3F3F
15 #define LINF 0x3F3F3F3F3F3F3F3FLL
16 #define DINF (double)1e+30
17 #define EPS (double)1e-9
18 #define PI (double)acos(-1.0)
19 #define RAD(x) (double)(x*PI)/180.0
20 #define PCT(x,y) (double)x*100.0/y
21
22 #define pb push_back
23 #define mp make_pair
24 #define pq priority_queue
25 #define F first
26 #define S second
27
28 #define D(x) x&(-x)
29 #define SZ(x) (int)x.size()
30 #define ALL(x) x.begin(),x.end()
31 #define SET(a,b) memset(a, b, sizeof(a))
32
33 #define gcd(x,y) __gcd(x, y)
34 #define lcm(x,y) (x/gcd(x,y))*y
35
36 #define bitcnt(x) __builtin_popcountll(x)
37 #define lbit(x) 63-__builtin_clzll(x)
38 #define zerosbitll(x) __builtin_ctzll(x)
39 #define zerosbit(x) __builtin_ctz(x)
40
41 enum {North, East, South, West};
42 //{0, 1, 2, 3}
43 //{Up, Right, Down, Left}
44
45 int mi[] = {-1, 0, 1, 0, -1, 1, 1, -1};
46 int mj[] = {0, 1, 0, -1, 1, 1, -1, -1};
47
48 inline void solve()
49 {
50
51 }
52
53 template<class num>inline void rd(num &x)
```

```

54 {
55     char c;
56     while(isspace(c = getchar()));
57     bool neg = false;
58     if(!isdigit(c))
59         neg=(c=='-'), x=0;
60     else
61         x=c-'0';
62     while(isdigit(c=getchar()))
63         x=(x<3)+(x<1)+c-'0';
64     if(neg)
65         x=-x;
66 }
67
68 int main()
69 {
70     #ifdef LOCAL_PROJECT
71     freopen("in.txt", "r", stdin);
72     freopen("out.txt", "w", stdout);
73     #else
74     #endif
75
76     solve();
77     return 0;
78 }

```

7.2 Java

7.3 Time Check

```
1 using namespace std::chrono;
2 class timecheck
3 {
4 public:
5     high_resolution_clock::time_point t1, t2;
6     void start()
7     {
8         t1 = high_resolution_clock::now();
9     }
10    void end()
11    {
12        t2= high_resolution_clock::now();
13        duration<double> time_span = duration_cast<duration<double>>(t2 - t1);
14        cout << "Time:_" << time_span.count() << "s" << endl;
15    }
16 };
```

Chapter 8

Formulas

8.1 Areas

8.2 Volumes

8.3 Series

8.4 Combinatorics

8.5 Integral