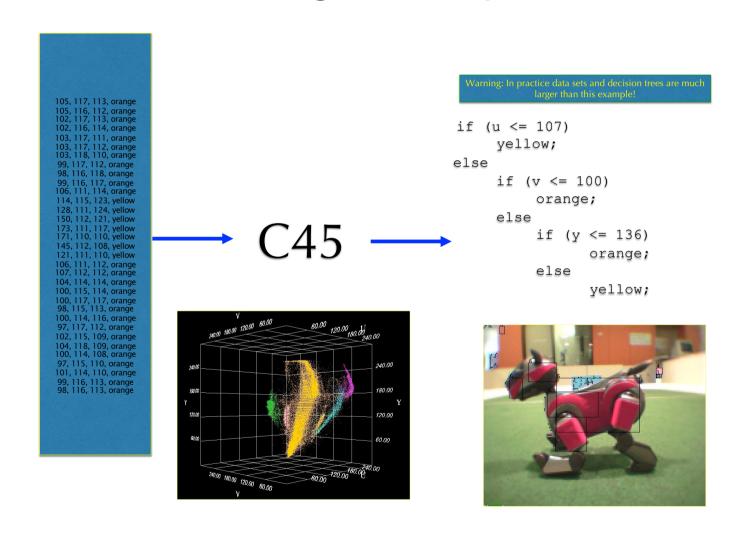
INDUCTIVE LOGIC PROGRAMMING

COMP3411/9814 Artificial Intelligence

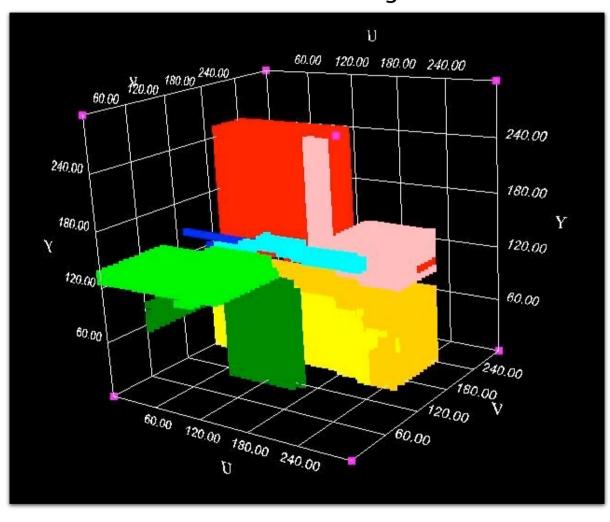
Shape of Discriminator

- Machine Learning algorithms can be characterised by the way the divide up the attribute space.
- What is the shape of the surface that separates classes?

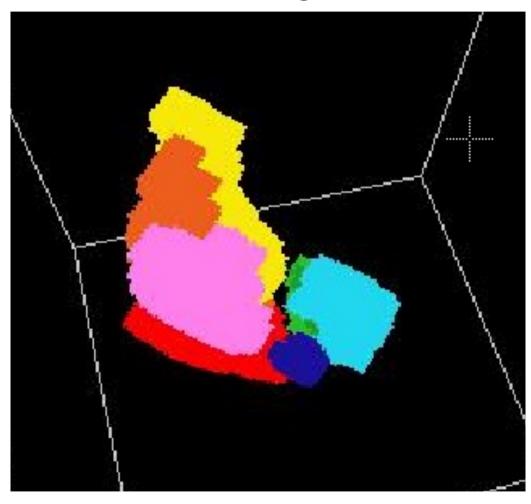
Learning in Perception



Colour Classes using C4.5



Nearest Neighbour



Description Language

- A concept can also be represented by sentences in a description language.
- May be if-then-else, or rules, like Horn clauses (Prolog):

The colour decision tree can be written as:

```
yellow :- u =< 107.

yellow :- u > 107, v =< 100, y > 136.

orange :- u > 107, v =< 100, y =< 136.
```

Generalisation Ordering

- If we can define a generalisation ordering on a language, learning can be done by syntactic transformations.
- E.g

$$class \leftarrow size = large \tag{1}$$

is a generalisation of

$$class \leftarrow size = large \land colour = red$$
 (2)

because (2) describes a more constrained set

Subsumption

A clause C_1 subsumes, or is more general than, another clause C_2 if

there is a substitution σ such that $C_2 \supseteq C_1 \sigma$.

$$class \leftarrow size = large$$

 $class \leftarrow size = large \land colour = red$

The least general generalisation of

$$p(g(a), a) \tag{3}$$

and
$$p(g(b), b)$$
 (4)

is
$$p(g(X), X). (5)$$

Under the substitution $\{a \mid X\}$ (5) is equivalent to (3).

Under the substitution {b / X} (5) is equivalent to (4).

Inverse Substitution

The least general generalisation of

p(g(a), a)

and p(g(b), b)

is p(g(X), X).

and results in the inverse substitution {X / {a, b}}

Least General Generalisation

E.g.

The result of heating this bit of iron to 419°C was that it melted.

The result of heating that bit of iron to 419°C was that it melted.

The result of heating any bit of iron to 419°C was that it melted.

We can formalise this as:

```
melted(bit1):- bit_of_iron(bit1), heated(bit1, 419).

melted(bit2):- bit_of_iron(bit2), heated(bit2, 419).

melted(X):- bit_of_iron(X), heated(X, 419).
```

Least General Generalisation

• Find a substitution so that there is no other clause that is more general

LGG of Clauses

q(g(a)) := p(g(a), h(b)), r(h(b), c), r(h(b), e).

$$q(x) := p(x, y), r(y, z), r(h(w), z), s(a, b)$$

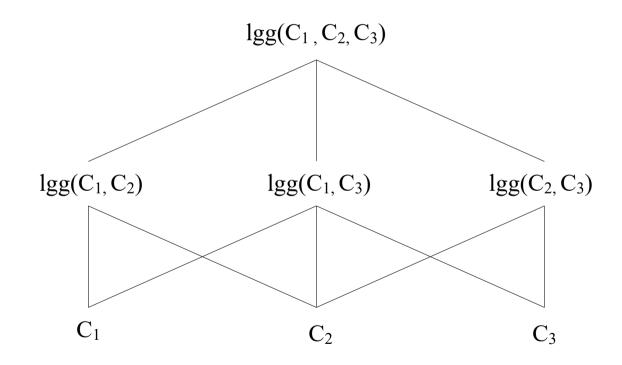
results in an LGG:

$$q(X) := p(X, Y), r(Y, Z), r(h(U), Z), r(Y, V), r(h(U), V)$$

with inverse substitutions:

 $\{X/(g(a), x), Y/(h(b), y), Z/(c, z), U/(b, w), V/(e, z)\}$

LGG of sets of clauses



Background Knowledge

- Background knowledge can assist learning
- It must be possible to interpret a concept description as a recognition procedure.
- If the description of chair has been learned, then it should be possible to refer to chair in other concept descriptions.
- E.g. the chair "program" will recognise the chairs in an office scene.

Saturation

Given a set of clauses, the body of one of which is completely contained in the bodies of the others, such as:

$$X \leftarrow A \land B \land C \land D \land E$$

$$Y \leftarrow A \wedge B \wedge C$$

we can *saturate* the first clause:

$$X \leftarrow A \land B \land C \land D \land E \land Y$$

Saturation Example

Suppose we are given two instances of a concept cuddly_pet,

$$cuddly_pet(X) \leftarrow fluffy(X) \land dog(X)$$

$$cuddly_pet(X) \leftarrow fluffy(X) \land cat(X)$$

and:

$$pet(X) \leftarrow dog(X)$$

$$pet(X) \leftarrow cat(X)$$

Saturated clauses are:

$$cuddly_pet(X) \leftarrow fluffy(X) \land dog(X) \land pet(X)$$

$$cuddly_pet(X) \leftarrow fluffy(X) \land cat(X) \land pet(X)$$

LGG is

$$cuddly_pet(X) \leftarrow fluffy(X) \land pet(X)$$

Relative Least General Generalisation (RLGG)

- Apply background knowledge to saturate example clauses.
- Find LGG of saturated clauses

```
heavier(A, B): - denser(A, B), larger(A, B).
```

fall_together(hammer, feather) :same_height(hammer, feather), denser(hammer, feather), larger(hammer, feather).

```
fall_together(hammer, feather):-
same_height(hammer, feather),
denser(hammer, feather),
larger(hammer, feather),
heavier(hammer, feather).
```

GOLEM

- LGG is very inefficient for large numbers of examples
- GOLEM uses a *hill-climbing* as an approximation
 - Randomly select pairs of examples
 - Find LGG's and pick the one that covers most positive examples and excludes all negative examples, call it *S*.
 - Randomly select another set of examples
 - Find all LGG's with S
 - Pick best one
 - Repeat as long as cover of positive examples increases.

Inverting Resolution

- Resolution provides an efficient means of deriving a solution to a problem, giving a set of axioms which define the task environment.
- Resolution takes two terms and resolves them into a most general unifier.
- Anti-unification finds the least general generalisation of two terms.

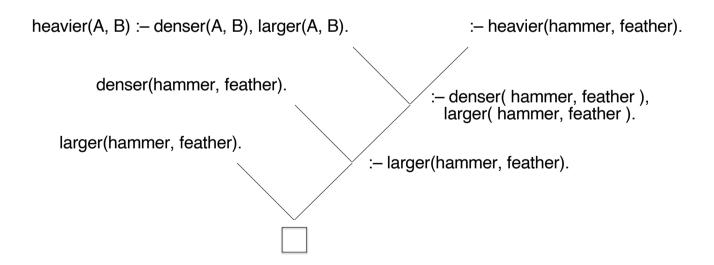
Resolution Proofs

```
larger(hammer, feather).

denser(hammer, feather).

heavier(A, B) :- denser(A, B), larger(A, B).

:- heavier(hammer, feather).
```



Absorption

Given a set of clauses, the body of one of which is completely contained in the bodies of the others, such as:

$$X \leftarrow A \land B \land C \land D \land E$$

$$Y \leftarrow A \wedge B \wedge C$$

we can hypothesise:

$$X \leftarrow Y \land D \land E$$

$$Y \leftarrow A \wedge B \wedge C$$

Intra-construction

This is the distributive law of Boolean equations. Intra-construction takes a group of rules all having the same head, such as:

$$X \leftarrow B \land C \land D \land E$$

$$X \leftarrow A \land B \land D \land F$$

and replaces them with:

$$X \leftarrow B \land D \land Z$$

$$Z \leftarrow C \wedge E$$

$$Z \leftarrow A \wedge F$$

Intra-construction automatically creates a new term in its attempt to simplify descriptions.

Automatic Programming

```
member(blue, [blue]).
member(eye, [eye, nose, throat]).

Is member(A, [A|B]) always true? y

Is member(A, [B|C]) always true? n

member(2,[1,2,3,4,5,6]).

Is member(A,[B,A|C]) always true? y

Is member(A,[B|C]) :- member(A,C) always true? y

Generalisation:
    member(A, [A|B]).
    member(A, [B|C]) :- member(A, C).
```

Problems with Incremental Learning

- Experiments can never validate a world model.
- Experiments usually involve noisy data, they can cause damage to the environment, they may cause misleading side-effects.
- A robot may have an incomplete theory and incorrect model.
- Need to be able to handle exceptions.
- Need to be able to repair knowledge base.
- If concepts are represented by Horn clauses, we can use a program debugger (declarative diagnosis).

Summary

- If a concept can be represented by sentences in a description language, concepts can be learned by generalising sentences in language
- Machine Learning as search through the space of possible sentences for the most compact that best covers +ve examples and excludes -ve examples
 - Least general generalisation
 - Inverse resolution
 - Automatic Programming