

**VIBRATION ANALYSIS AND VIBROACOUSTICS**  
**MODULE 1: VIBRATION ANALYSIS (PROF. STEFANO ALFI)**  
**A.Y. 2022-2023**

**Assignment 3: Modal parameter identification**

The response of a structure to a virtual dynamometric hammer has been numerically simulated to represent an experimental test. The time histories of the impulsive force  $F$  at location  $x_1$  and the displacements  $x_i$  at 4 locations on the structure are collected in a matrix ("Data.mat") organized as follows:  $[t, F, x_1, x_2, x_3, x_4]$ .

Starting from the evaluation of the FRFs between displacements and force, it is requested to:

- 1) Plot the "experimental" FRF diagrams.
- 2) Estimate the natural frequencies, damping ratios and mode shapes of the resonating modes in the range  $0 - 5 \text{ Hz}$  employing simplified methods (e.g. half power point method, see slides 8,10,11 of 'Modal Parameters Identification.pdf'). Comment the obtained results.
- 3) Set up a modal parameter identification program, exploiting the residual minimization technique, for estimating natural frequencies, damping ratios and modes in the range  $0 - 5 \text{ Hz}$ . Compare the identified FRF with the "experimental" ones. Comment the obtained results.
- 4) Compare and comment the identified modal parameters with ones obtained with the above-mentioned methods.
- 5) Employing a modal approach, reconstruct the FRFs and compare with the "experimental" original ones.

**OPTIONAL**

- i. Evaluate the co-located FRF at the location corresponding to displacement  $x_2$ .
- ii. Evaluate the  $M, C, K$  matrices of the numerical model of the 4 d.o.f.  $(x_1, x_2, x_3, x_4)$  system.