

Exercise 8 page 264 in book

A skydiver of mass m in a vertical free fall experiences an aerodynamic drag force (Widerstand)

$F_D = C_D \cdot \dot{y}^2$ where y is measured downward from the start of the fall. The differential equation describing the fall is:

$$\ddot{y} = g - \frac{C_D}{m} \cdot \dot{y}^2 \quad \begin{array}{l} g = 9.80665 \text{ m/s}^2 \\ C_D = 0.2028 \text{ kg/m} \\ m = 80 \text{ kg} \end{array}$$

$(\dot{y} = \frac{dx}{dt}, \ddot{y} = \frac{d^2x}{dt^2})$

Determine the time of a 5000 m fall

Modify the code

Flexible RungeKutta4 such that you by studying the graph showing the position of the skydiver, determine how long time it takes!

Rewrite to a system of first order equations

$$y_0 = y, y_1 = \dot{y}$$

$$y_0' = y_1$$

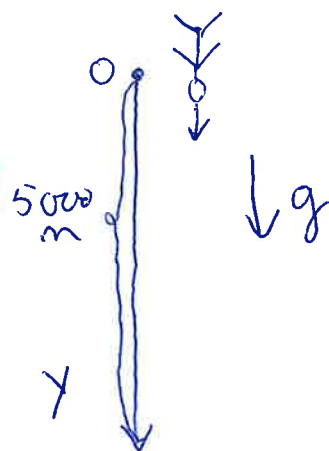
$$y_1' = \ddot{y} = g - \frac{C_D}{m} \cdot \dot{y}^2 = g - \frac{C_D}{m} \cdot y_1^2$$

$$\begin{bmatrix} y_0' \\ y_1' \end{bmatrix} = \begin{bmatrix} y_1 \\ g - \frac{C_D}{m} \cdot y_1^2 \end{bmatrix}$$

$$y_0(0) = y(0) = 0$$

$$y_1(0) = 0$$

No speed initially



Top position defined as zero

Tip: 1) Modify function $F(x, y)$

2) Modify initial condition

3) Play with xStop and appropriate h (h_1, h_2)

4) Modify what to plot

Answer, approx 85 seconds
seen from the graph.