

Microeconomics 1 Lecture Notes

Enrico Mattia Salonia

September 27, 2025

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Introduction

Before starting, you might want to read Kreps (1988, ch. 1), Debreu (1959, p. ix-xi), (Myerson, 1997, p. 1-7).

You will see smaller text like this in some places. These are remarks which are not essential to understand the main text, but which you might find interesting. You can skip them if you want.

At the end of each lecture there are exercises.

Choice under uncertainty.

- Kreps (1988).
- Fishburn (1970).
- Mas-Colell et al. (1995), Chapter 6.
- Savage (1972).
- Gilboa (2009).
- Kreps (2013), Chapter 7.

General equilibrium theory.

- Mas-Colell et al. (1995), Chapters 15-17.
- Kreps (2013), Chapters 10-11.
- Debreu (1959).
- McKenzie (2005).
- Fleurbaey & Maniquet (2011), for the part related to no-envy.

References

Debreu, G. (1959). *Theory of value: An axiomatic analysis of economic equilibrium* (Vol. 17). Yale University Press. 1

Fishburn, P. C. (1970). *Utility theory for decision making*. New York: Wiley. 1

- Fleurbaey, M., & Maniquet, F. (2011). *A theory of fairness and social welfare* (Vol. 48). Cambridge University Press. 1
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- Kreps, D. M. (1988). *Notes on the theory of choice*. Westview Press. 1
- Kreps, D. M. (2013). *Microeconomic foundations* (Vol. 1). Princeton university press. 1
- Mas-Colell, A., Whinston, M. D., & Green, J. R. (1995). *Microeconomic theory*. Oxford university press New York. 1
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Lecture 1

Introduction to Expected Utility

1.1 How to model uncertainty

Let's start by thinking about how we represent uncertainty. Say that you made a bet with a friend: if a fair coin toss results in heads, you get 10 euros; otherwise you pay 10 euros to your friend. There are two outcomes, 10 and -10 , and since the coin is fair, each occurs with probability $1/2$. To describe this simple example, we started from a set of outcomes, monetary transfers, and specified the probability of each outcome occurring. I refer to such an object as a *lottery*. Denote the set of outcomes by X . Generic elements of X will be denoted x, y, z . For now, we assume that X is finite. Outcomes alone are not enough to describe a lottery: we need probability distributions over outcomes, as in the $1/2-1/2$ distribution of the fair coin above. The set of lotteries over X is denoted by $\Delta(X)$.¹ Each element of $\Delta(X)$ is a function $p : X \rightarrow [0, 1]$ such that $\sum_{x \in X} p(x) = 1$, it maps each outcome x to a number $p(x)$ in $[0, 1]$, representing the probability that x occurs.²

Example 1.1. In the example above, the set of outcomes is $\{10, -10\}$ and the lottery induced by the fair coin toss satisfies $p(10) = p(-10) = 1/2$.

Remark 1.1. Notice that, in this setup, we are missing something: whether the coin lands on heads or tails is irrelevant; only the probabilities of outcomes matter, not the events that induced them. This is a limitation of this model, which we will address when we introduce a state-space representation of uncertainty.

We now need to make statements such as “an individual prefers lottery p to lottery q .” To do so, we introduce a binary relation \succsim over $\Delta(X)$, so that $p \succsim q$ means that the individual weakly prefers lottery p to lottery q . Compared to choice under certainty, we are now comparing lotteries—i.e., probability distributions over outcomes—rather than outcomes themselves. The set we are ranking, the set of lotteries, has *structure*, whereas the set of outcomes does not. For example, we can consider a lottery r that yields p with probability α and q with probability $1 - \alpha$, where $\alpha \in [0, 1]$. This is called a *compound lottery*, and it is an element of $\Delta(X)$ as well, we can write $r = \alpha p + (1 - \alpha)q$. For instance, if $p(10) = 1$ and $q(-10) = 1$, then $r(10) = \alpha$ and $r(-10) = 1 - \alpha$. This *mixing* operation is generally not possible with an unstructured set of outcomes. As an illustration, suppose the set of outcomes comprises fruits. We can have an apple or a banana, but there is

¹Wonder why this notation? You will realise soon.

²Why do we write the sum $\sum_{x \in X} p(x) = 1$ instead of an integral?

no fruit that is a mixture of an apple and a banana. Imposing structure on the set of elements to be ranked is a key move of microeconomic theory. In fact, we will later assume that the set of outcomes is \mathbb{R} , the set of real numbers representing monetary outcomes, allowing us to say more than what we can say with a generic set of outcomes.

Technically, \lesssim is a subset of $\Delta(X) \times \Delta(X)$, i.e., a set of ordered pairs of lotteries. For example, if $p, q, r \in \Delta(X)$, the individual prefers p to q , and is indifferent between q and r , then \lesssim contains at least the pairs $(p, q), (q, r), (p, r), (p, p), (q, q), (r, r)$.

In what follows, we consider what assumptions preferences over lotteries might satisfy, and what these assumptions imply.

1.2 Things to read

Check Kreps (1988, p. 31-33) for an introduction of the lottery model in this chapter.

1.3 Exercises

Some exercises here.

Exercise 1.1. Nice exercise.

References

Kreps, D. M. (1988). *Notes on the theory of choice*. Westview Press. 4