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Máster Universitario en Estructuras  
Curso 2020-2021

# Tema I: Análisis modal dentro del marco del mantenimiento de la salud estructural

Módulo: MÓDULO FUNDAMENTAL: CALIDAD Y DAÑO

Materia: Análisis Modal y Detección de Defectos

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**Departamento de Mecánica de Estructuras e  
Ingeniería Hidráulica**

# Desarrollo del curso

		FECHA		HORA	PROFESOR	TEMA	
Clase 1	Lunes	1	febrero	9:30-11:30	EGM	1	Introducción: Análisis modal dentro del marco del mantenimiento de la salud estructural.
Clase 2	Lunes	8	febrero	9:30-11:30	EGM	2	Fuentes de deterioro, patologías estructurales, y tecnologías de monitorización.
Clase 3	Lunes	15	febrero	9:30-11:30	EGM	3	Taller: procesamiento de señales.
Clase 4	Lunes	22	febrero	9:30-11:30	EGM	4	Análisis modal experimental.
Clase 5	Lunes	15	marzo	9:30-11:30	EGM	5	Análisis modal operacional.
Clase 6	Lunes	12	abril	9:30-11:30	EGM	6	Análisis modal operacional automatizado. Práctica de laboratorio I.
Clase 7	Lunes	19	abril	9:30-11:30	EGM	7	Taller: Identificación del daño estructural.
Clase 8	Lunes	26	abril	9:30-11:30	RCT	8	Técnicas de identificación dinámica basadas en análisis modal operacional.
Clase 9	Lunes	26	abril	12:00-14:00	RCT	9	Práctica de laboratorio II: Test de vibración ambiental.
Clase 10	Martes	27	abril	9:30-11:30	RCT	10	Casos de estudio.
Clase 11	Martes	27	abril	12:00-14:00	RCT		Presentación de trabajos.

ENTREGA DE TRABAJOS Y EVALUACIÓN

Del 3 al 28 de mayo



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# ÍNDICE

- Introducción al paradigma del mantenimiento de la salud estructural.
- Historia del SHM.
- Motivaciones y retos del SHM.
- Análisis modal como técnica revolucionaria dentro del SHM.





# Introducción al paradigma del mantenimiento de la salud estructural.

## Structural Health Monitoring (SHM)

*The process of implementing a **damage identification** strategy for aerospace, civil and mechanical engineering infrastructure is referred to as Structural Health Monitoring (SHM) [1].*

*SHM is the integration of sensing and possibly also actuation devices to allow the loading and damaging conditions of a structure to be **recorded**, **analyzed**, **localized**, and **predicted** in a way that **nondestructive testing** (NDT) becomes an *integral part of the structure and a material* [2].*

[1] Farrar, C. R., & Worden, K. (2006). An introduction to structural health monitoring. *Philosophical Transactions of the Royal Society A: Mathematical, Physical and Engineering Sciences*, 365(1851), 303-315.

[2] Boller, C., Chang, F. K., & Fujino, Y. (Eds.). (2009). *Encyclopedia of structural health monitoring*. Wiley.

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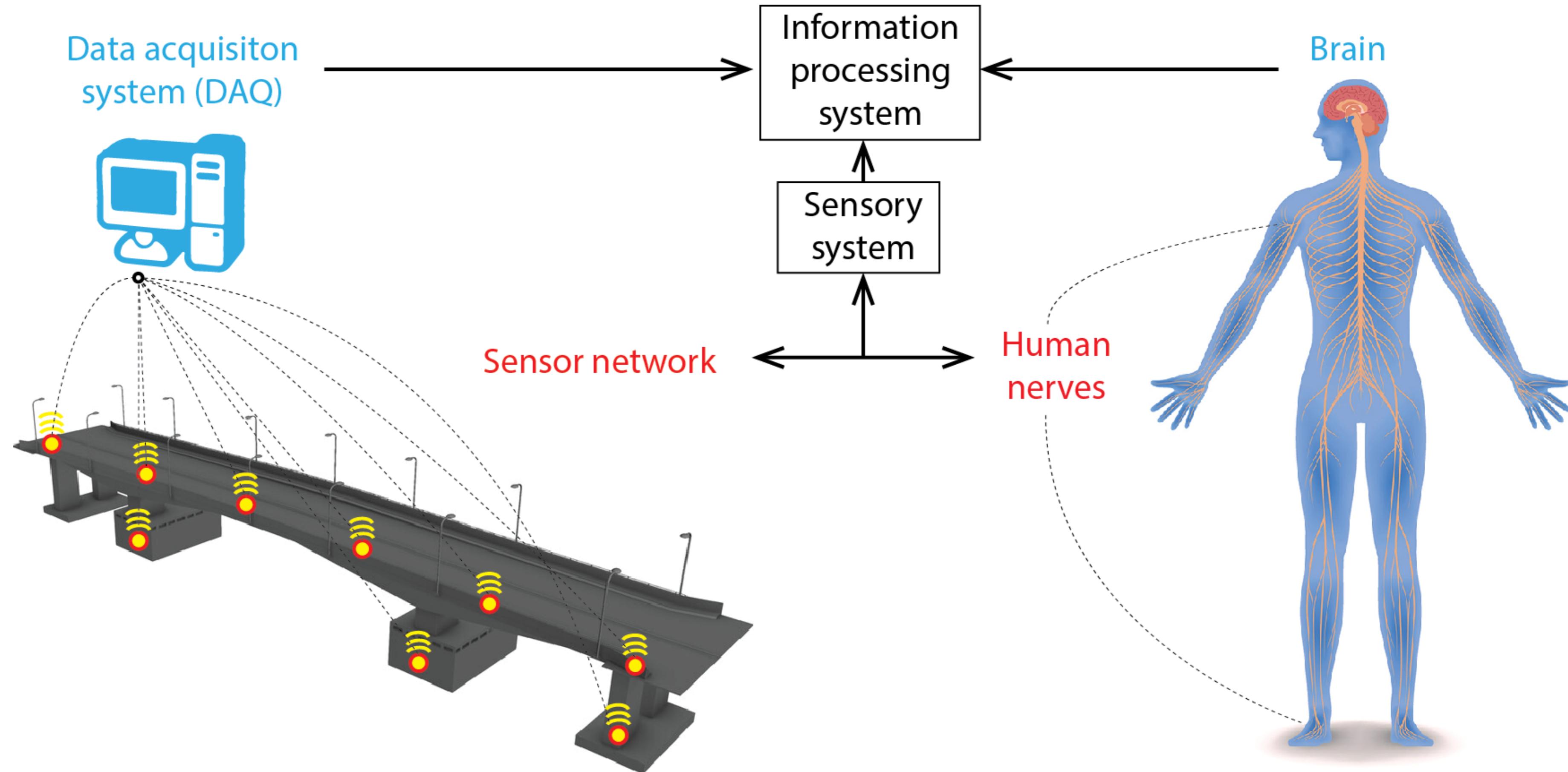
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*An **automated** process to conduct **non-destructive** damage **diagnosis**, **localization**, and **prognosis** of **structures**.*

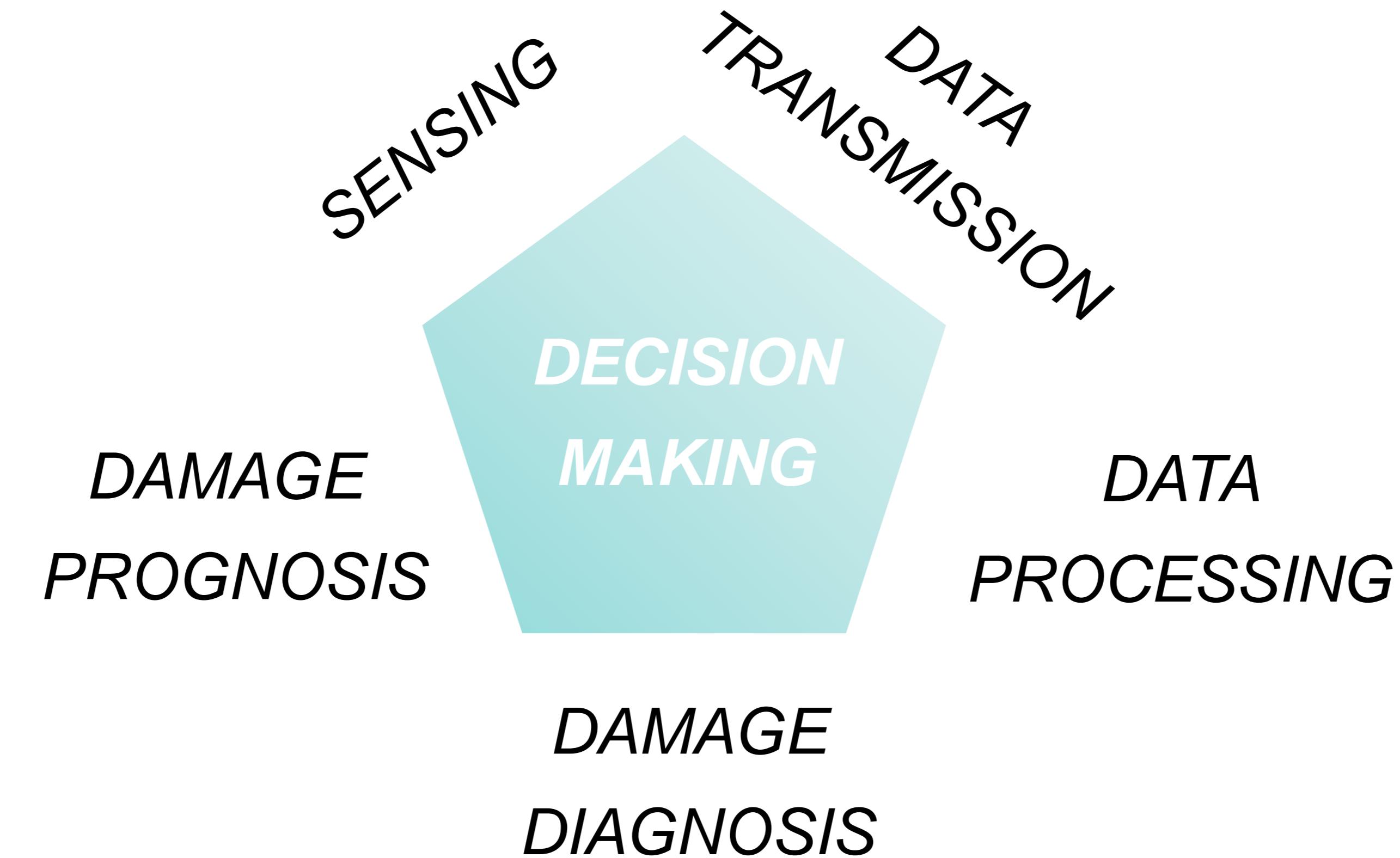
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# Introducción al paradigma del mantenimiento de la salud estructural

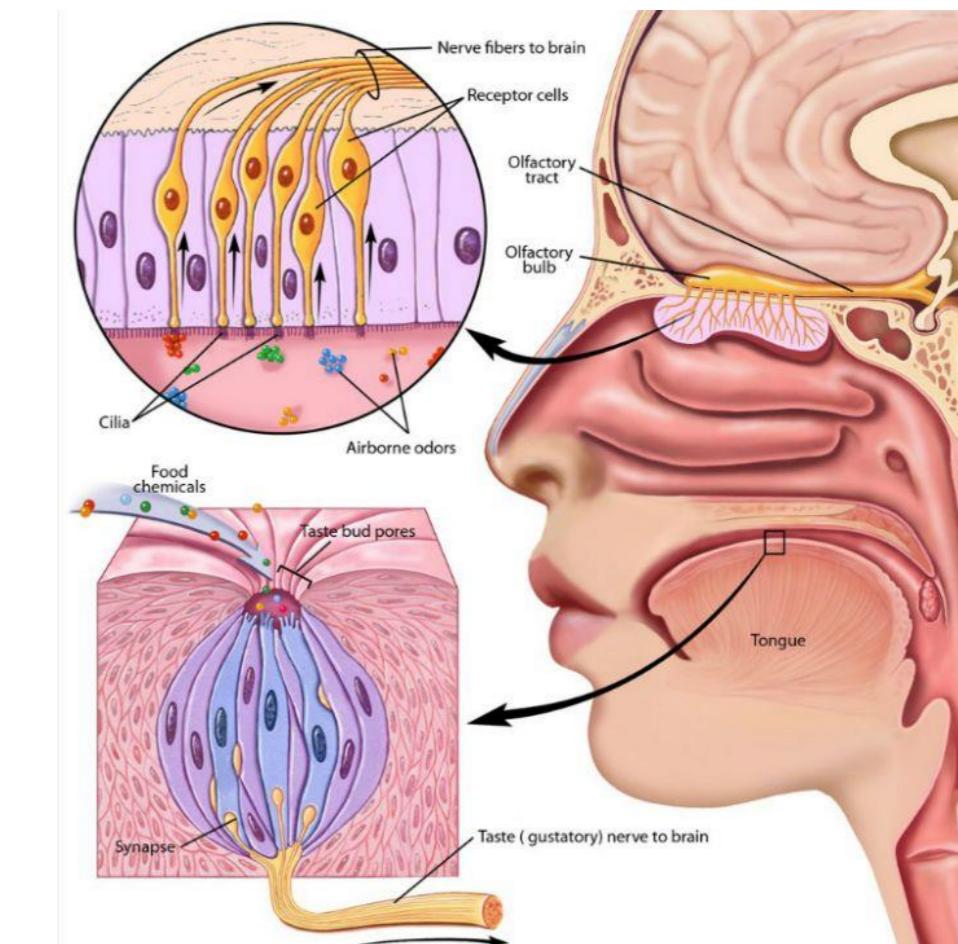
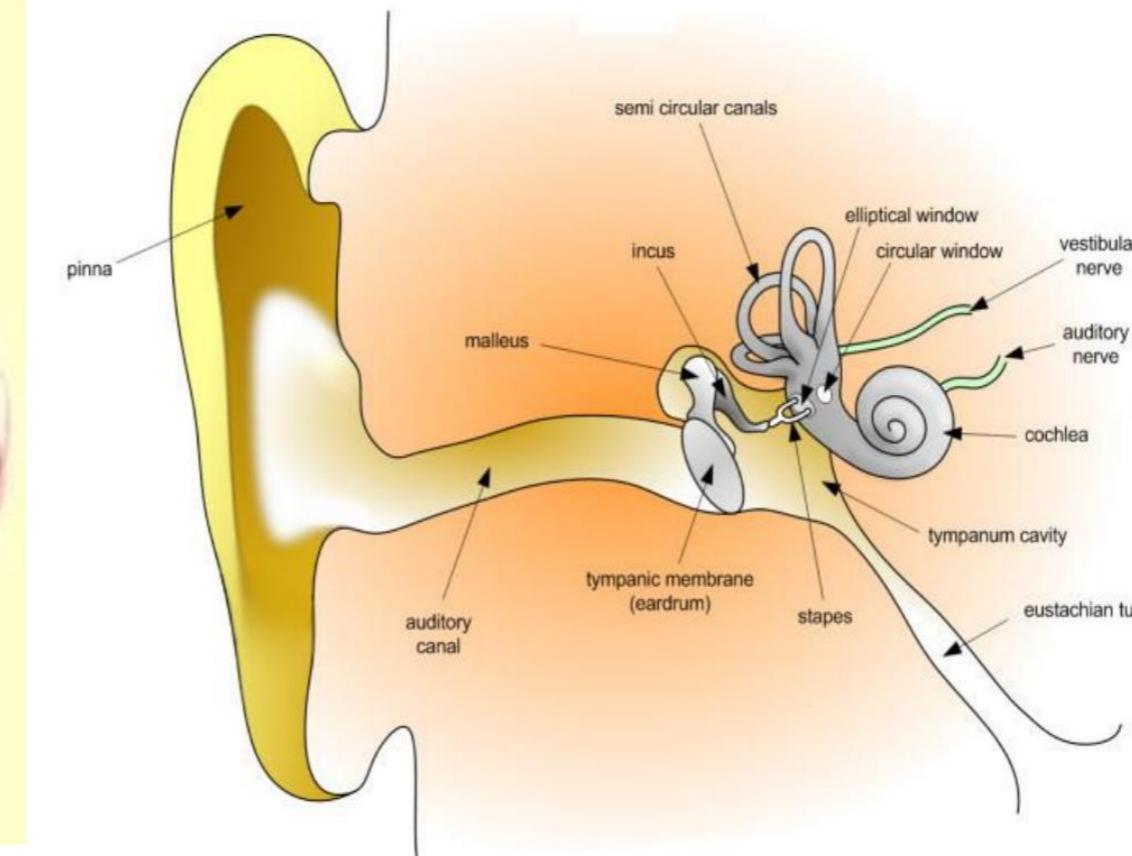
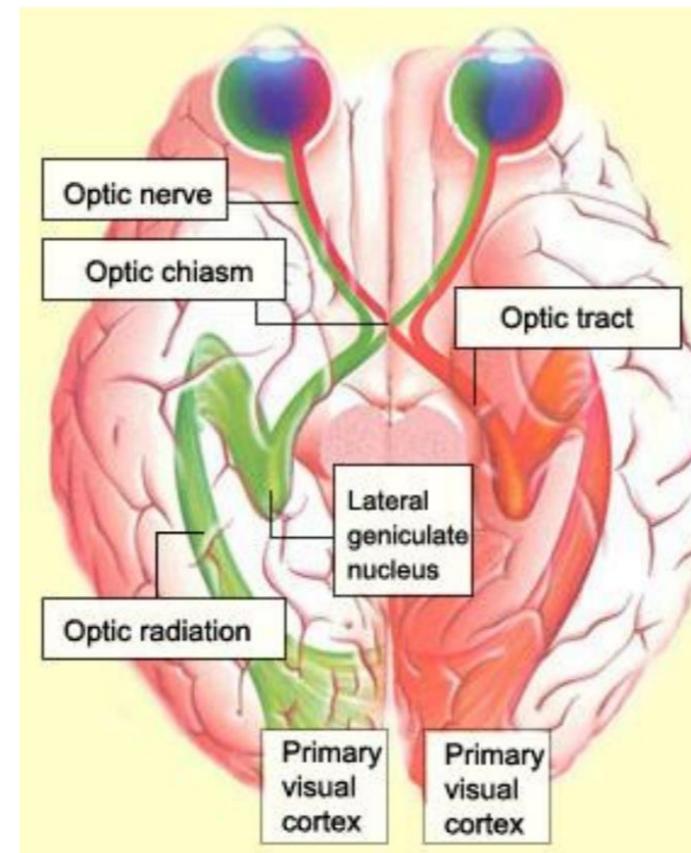
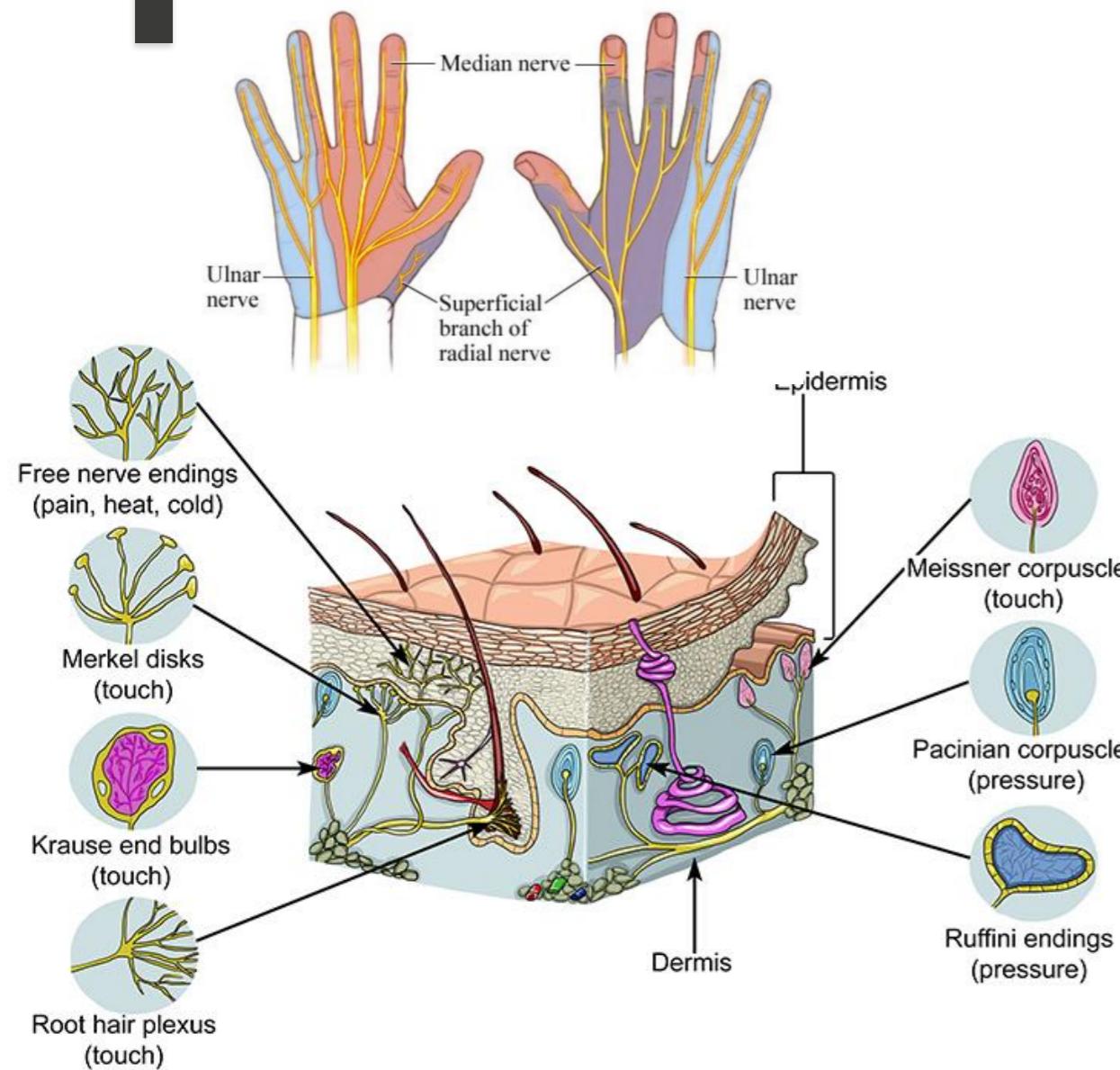


# Introducción al paradigma del mantenimiento de la salud estructural



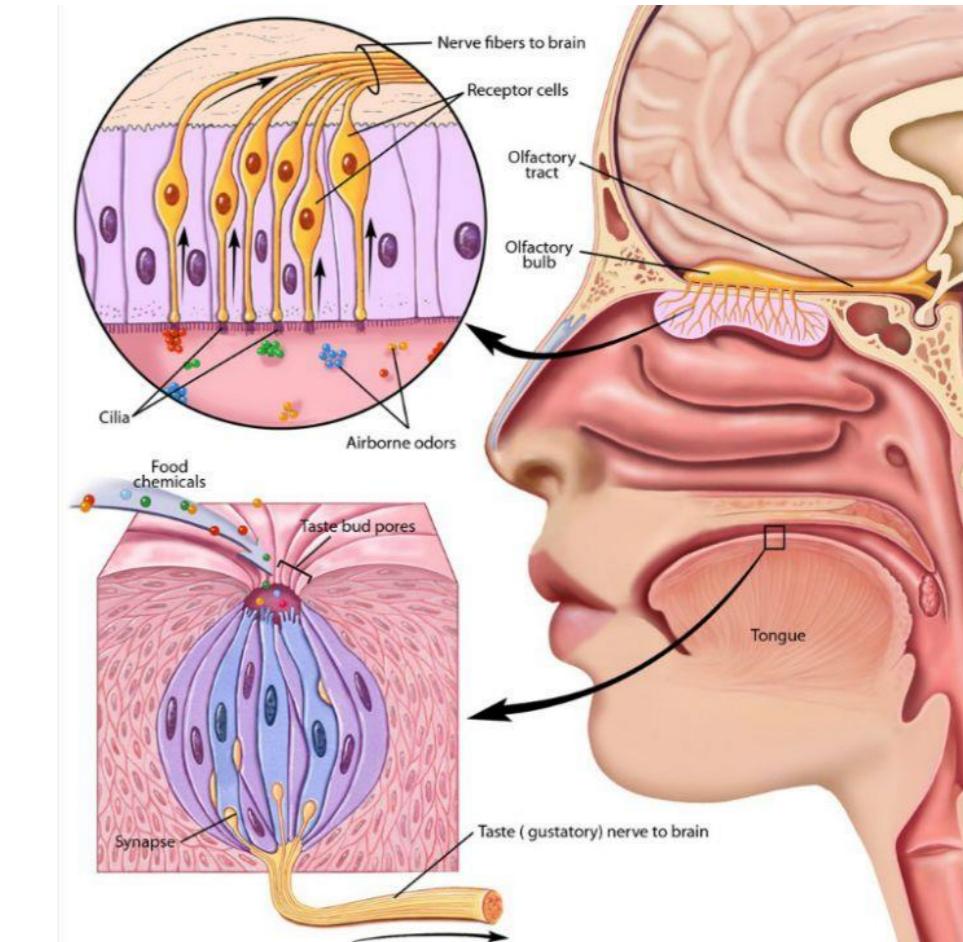
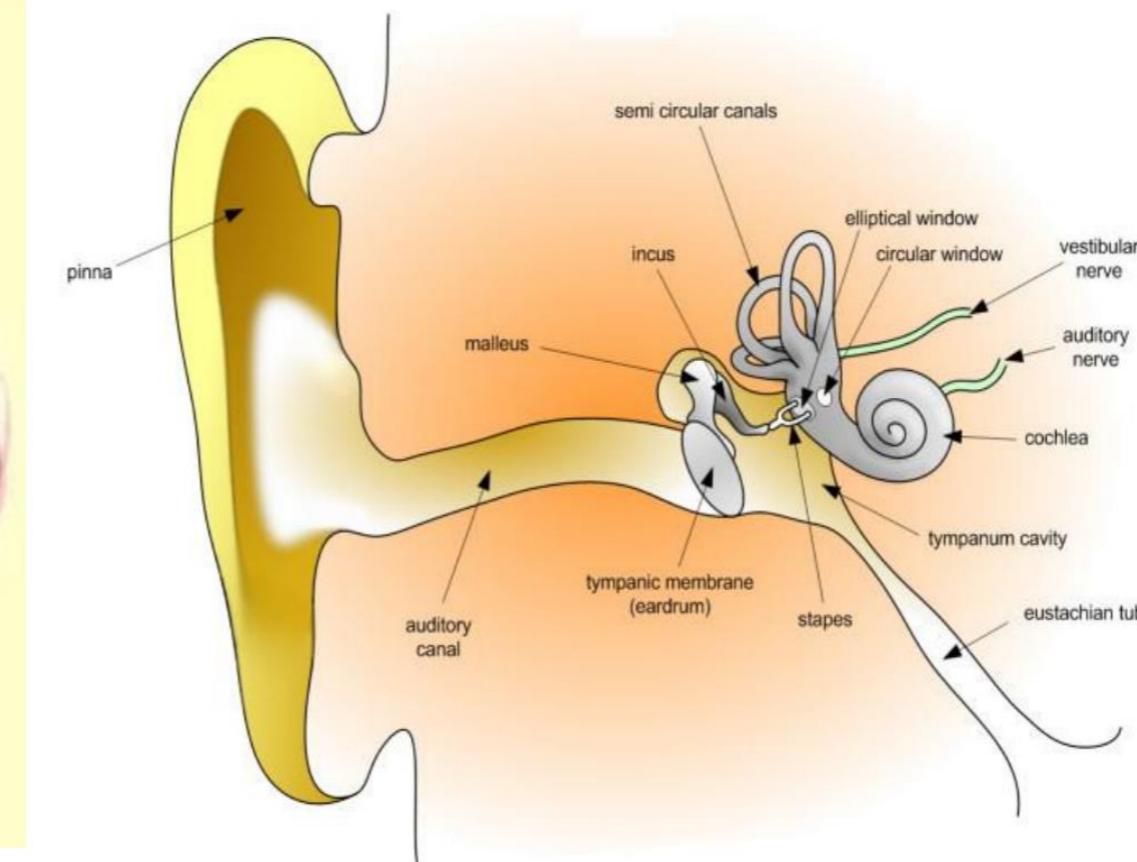
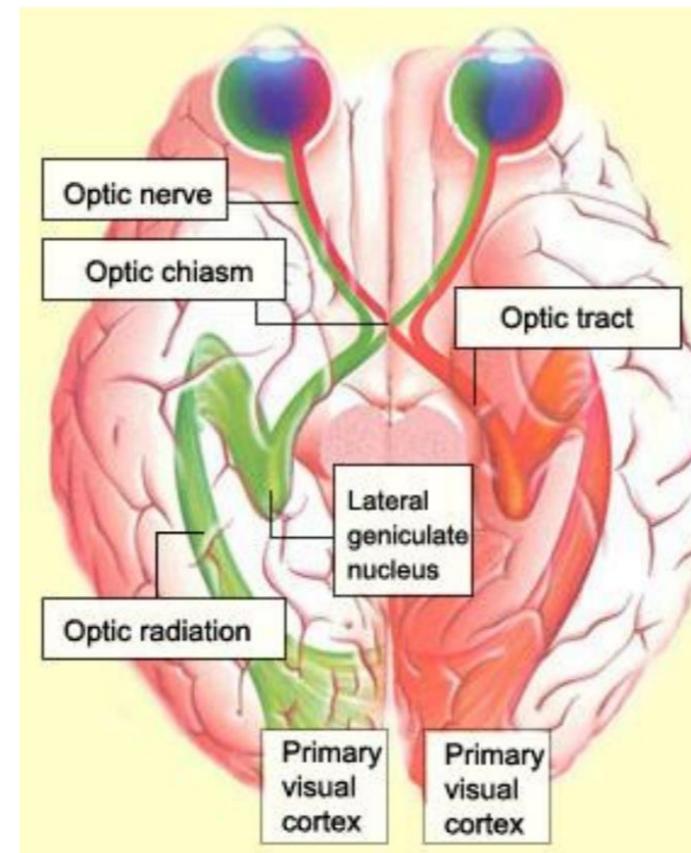
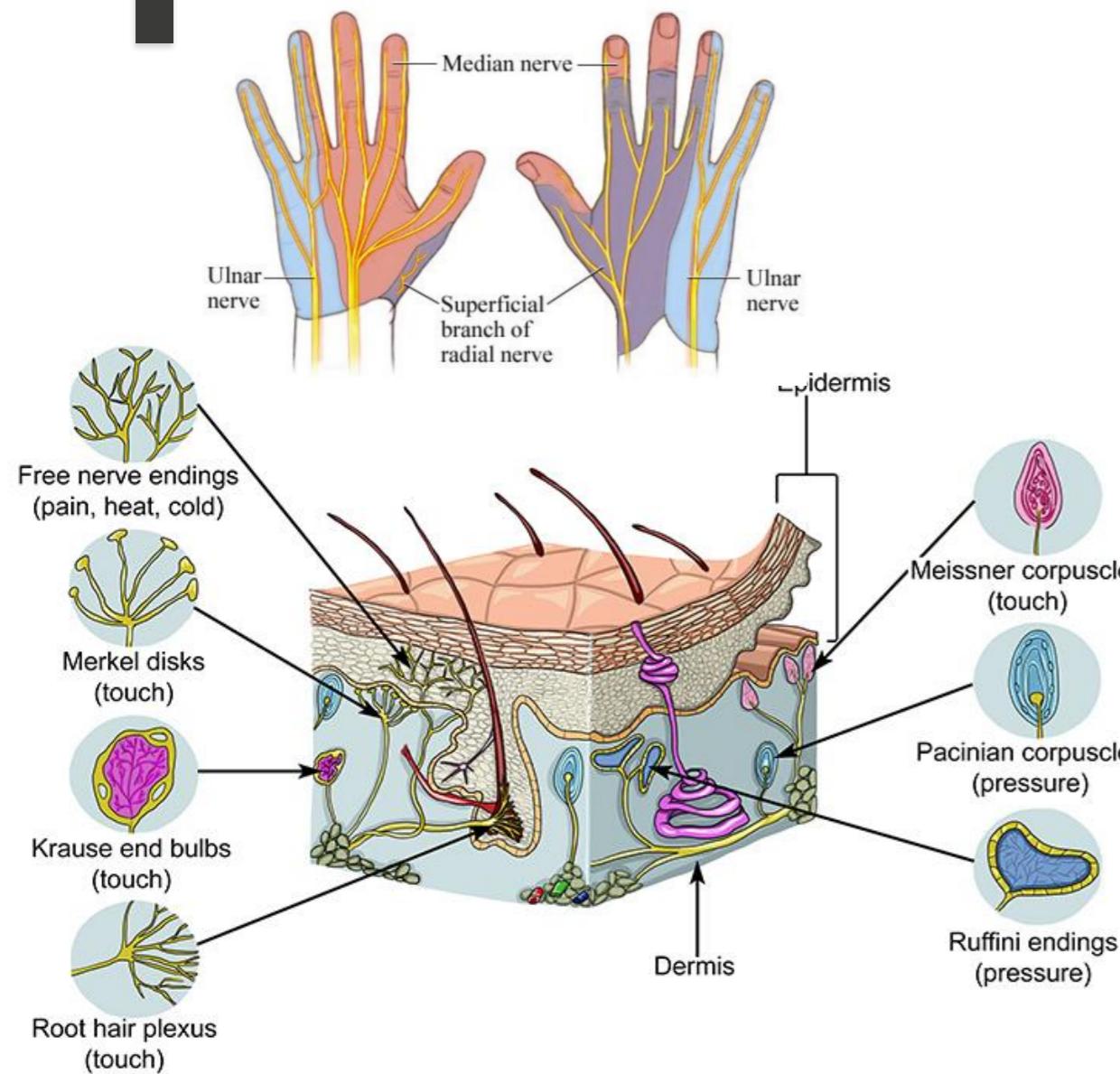
# Introducción al paradigma del mantenimiento de la salud estructural

## SENSING



# Introducción al paradigma del mantenimiento de la salud estructural

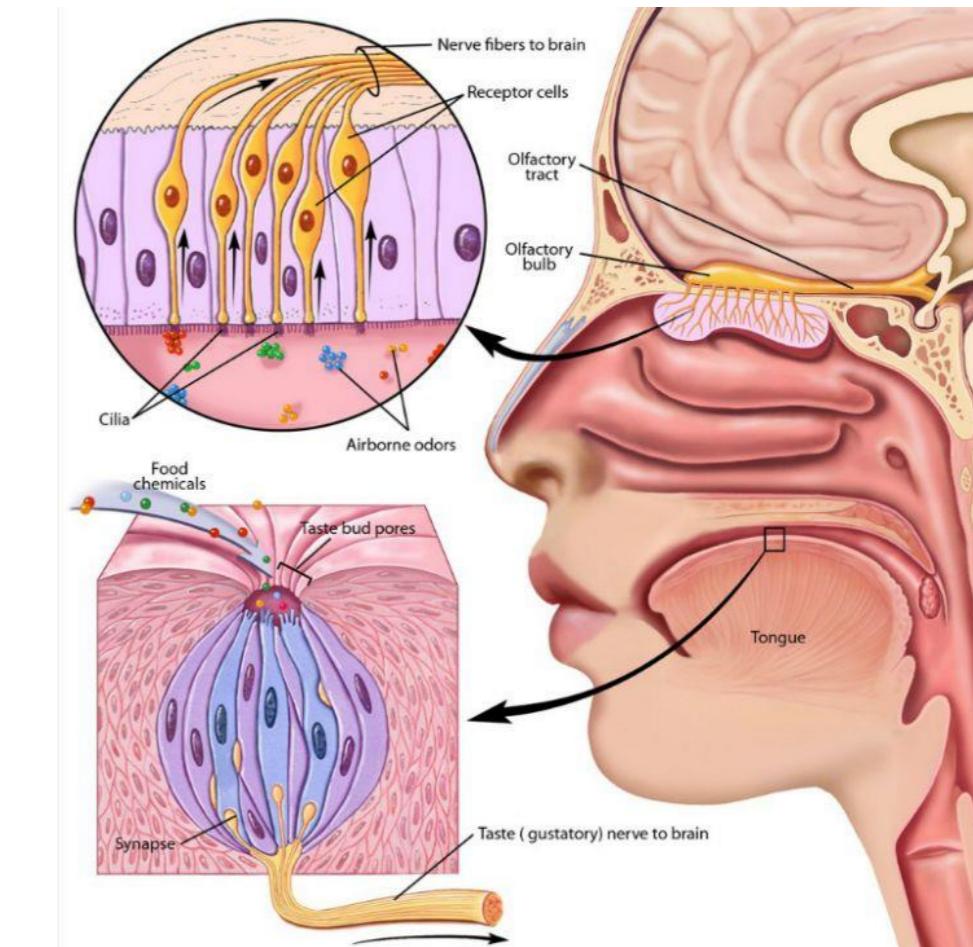
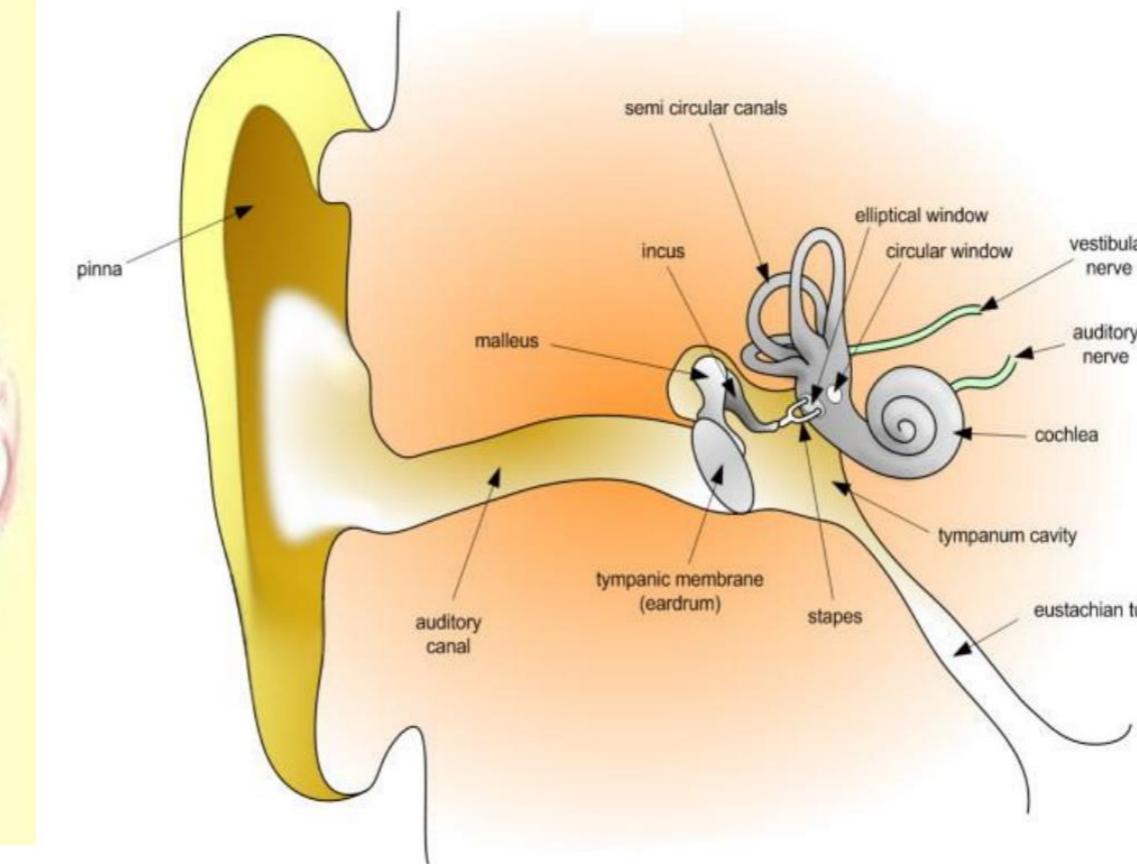
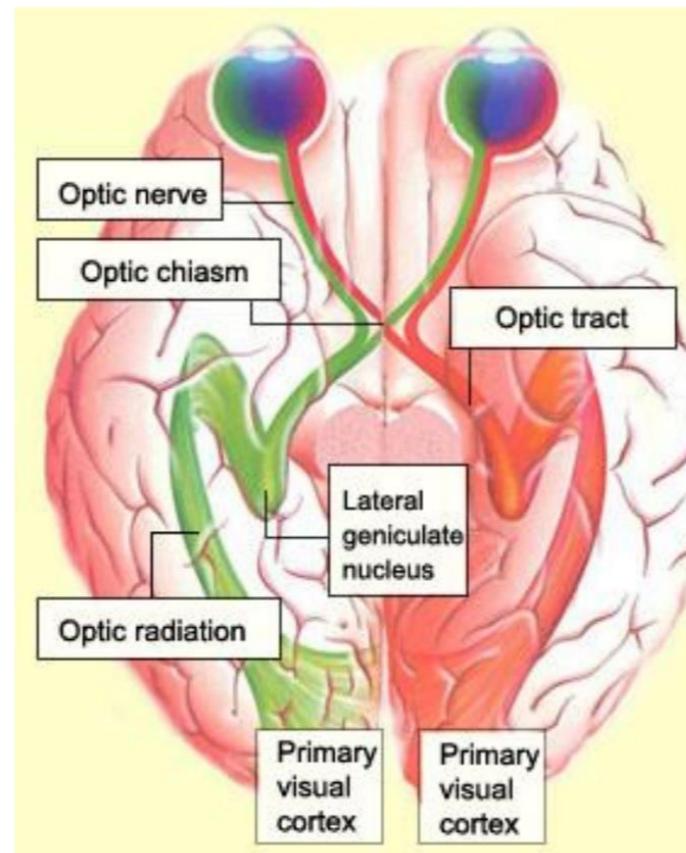
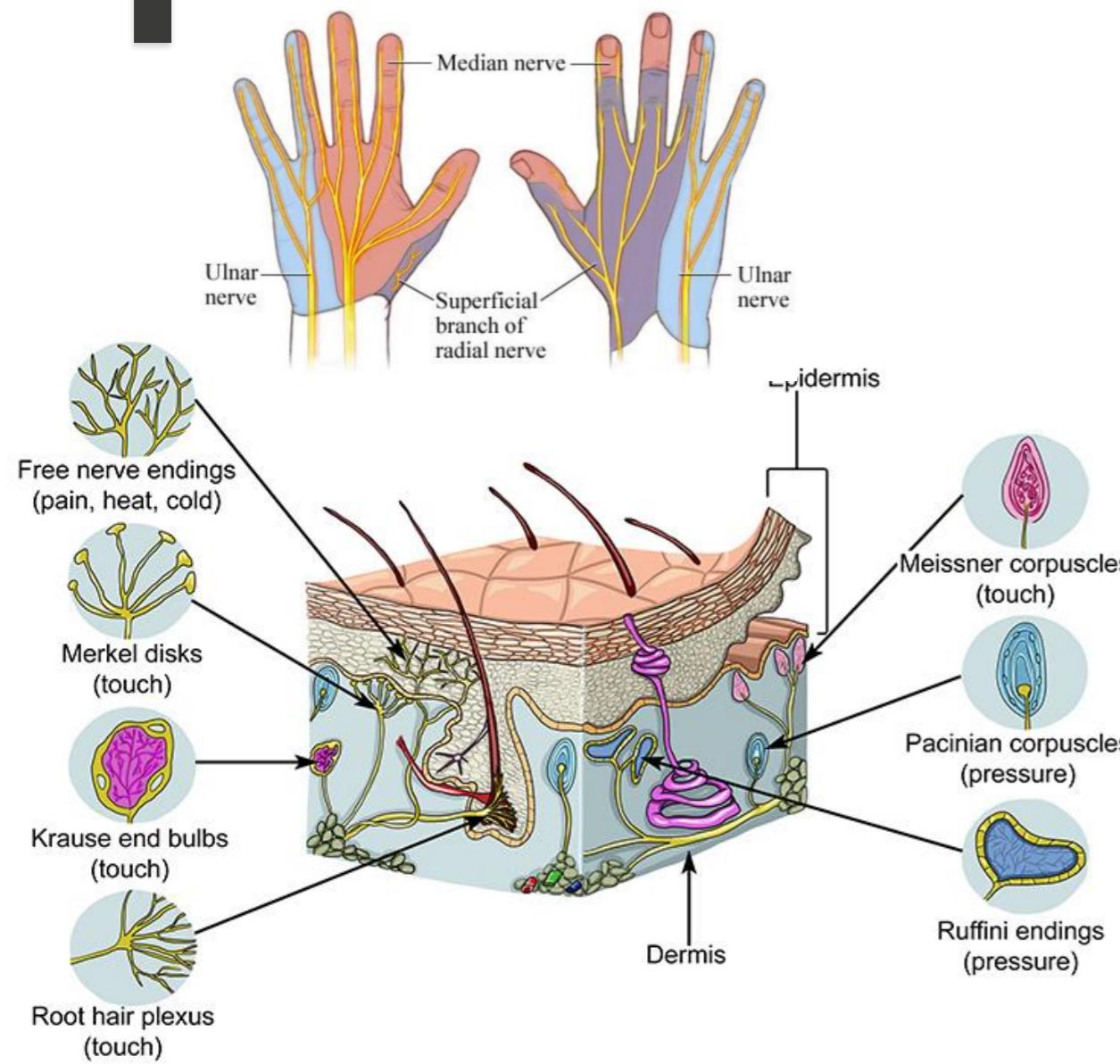
## SENSING



- ❖ Long-term/permanent
- ❖ Automated
- ❖ Aggregated (it combines heterogeneous sensing solutions)

# Introducción al paradigma del mantenimiento de la salud estructural

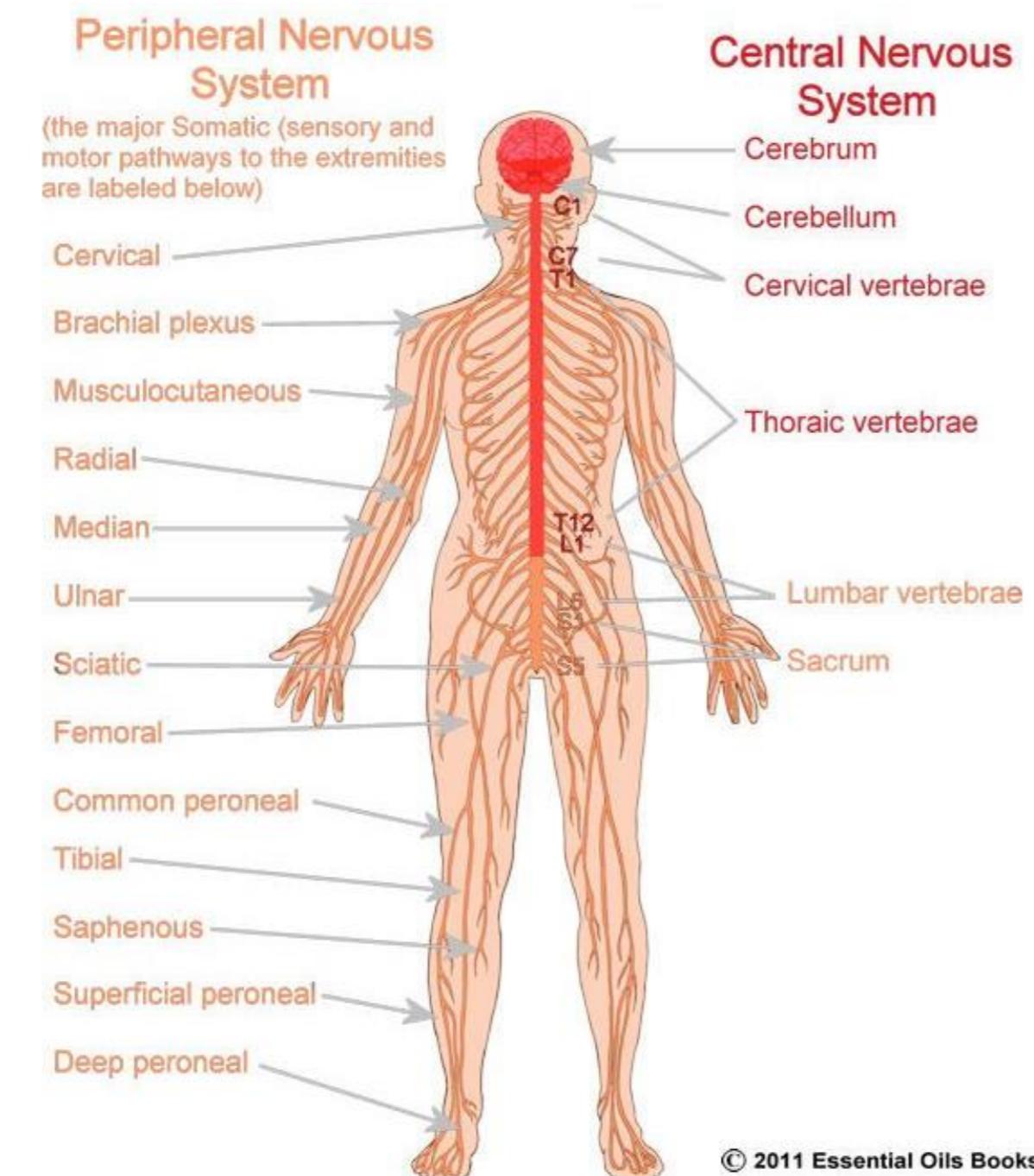
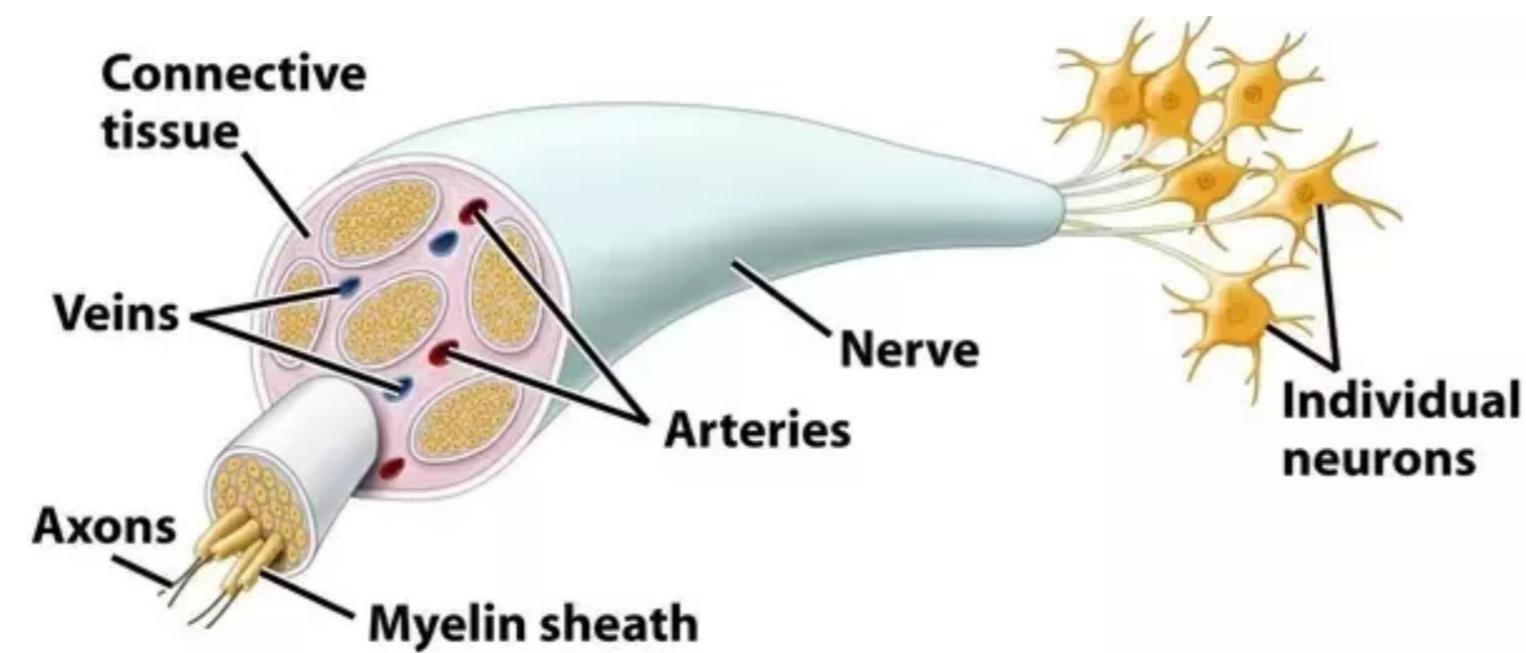
SENSING



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# Introducción al paradigma del mantenimiento de la salud estructural

DATA TRANSMISSION



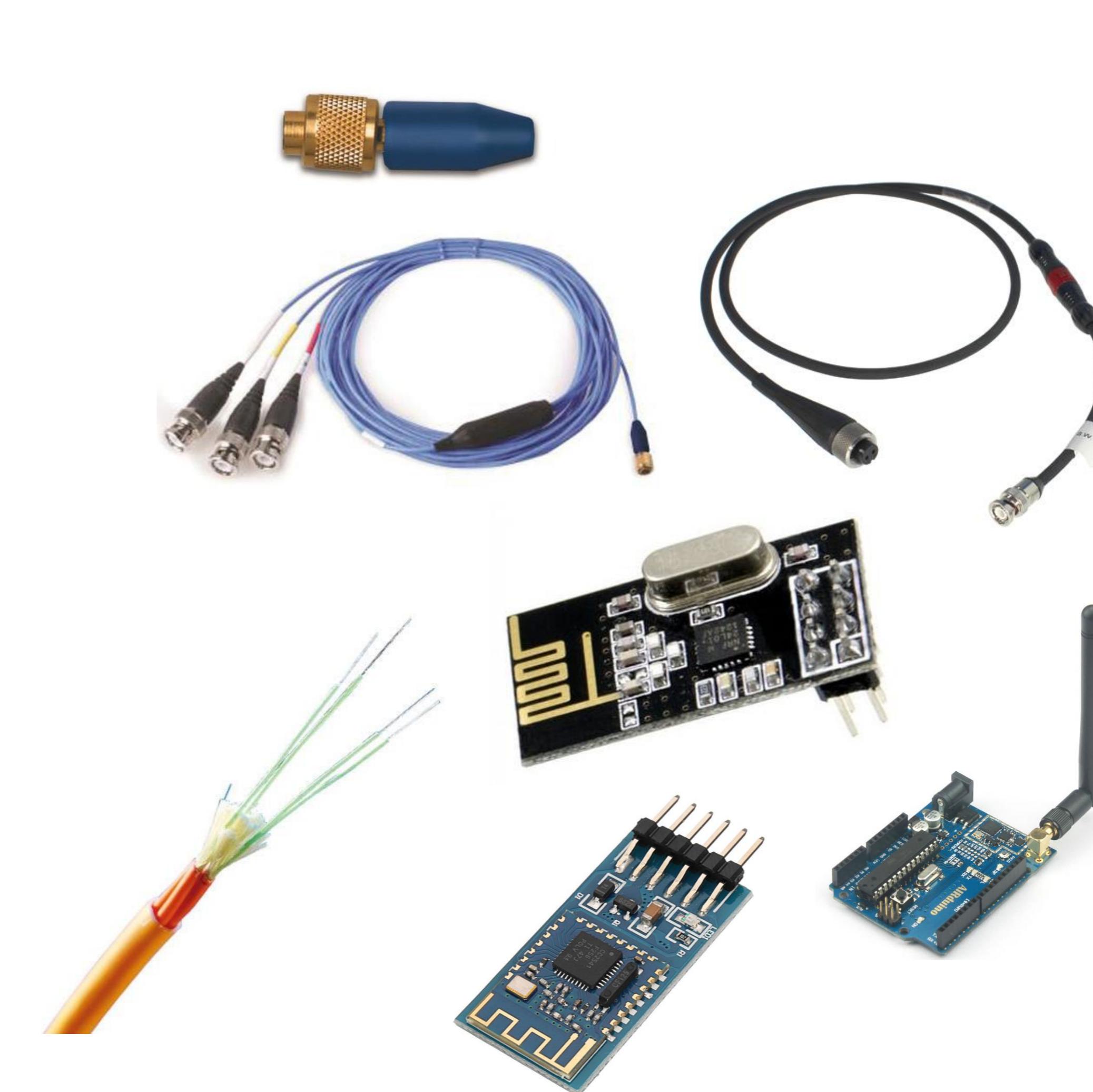
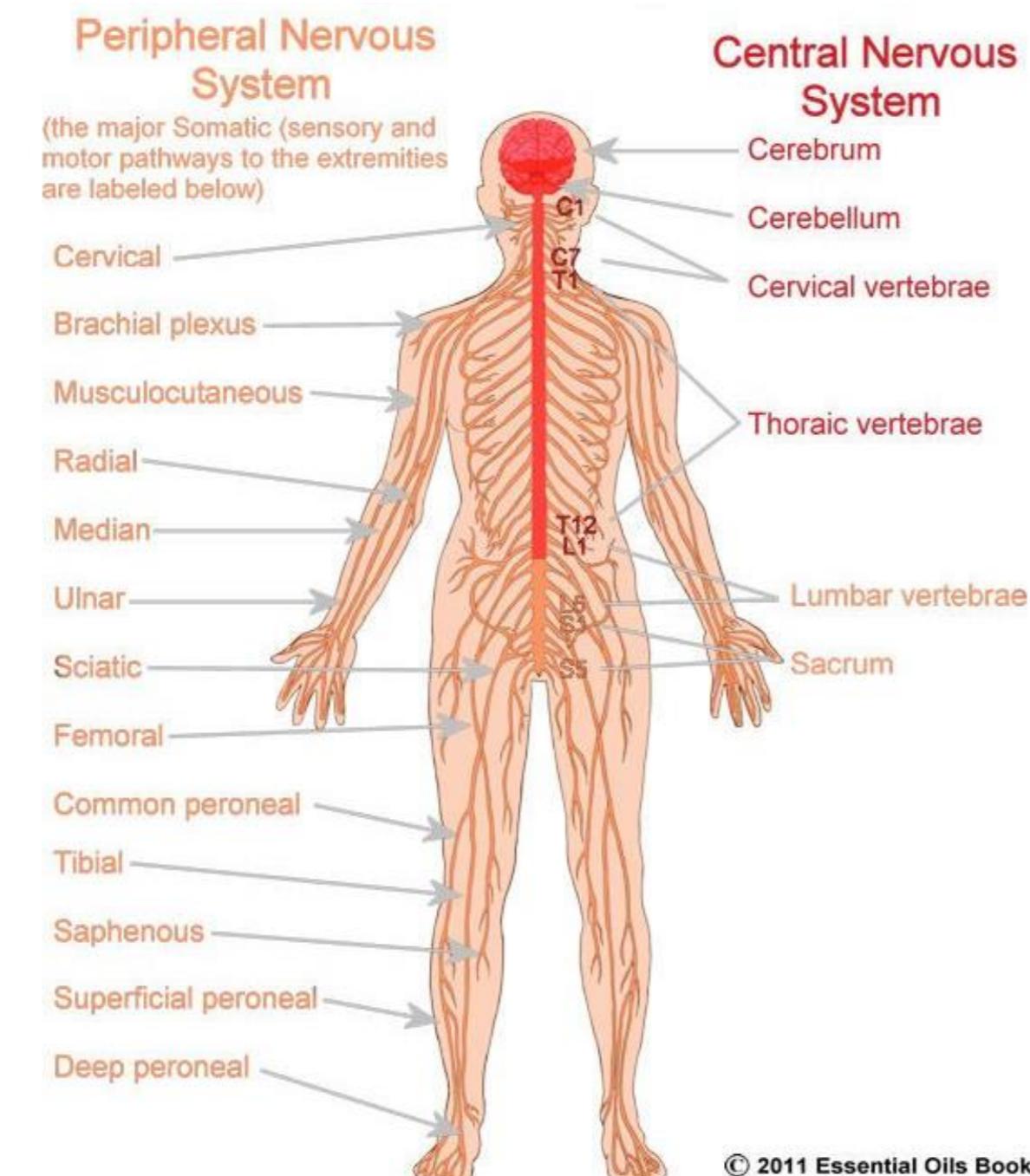
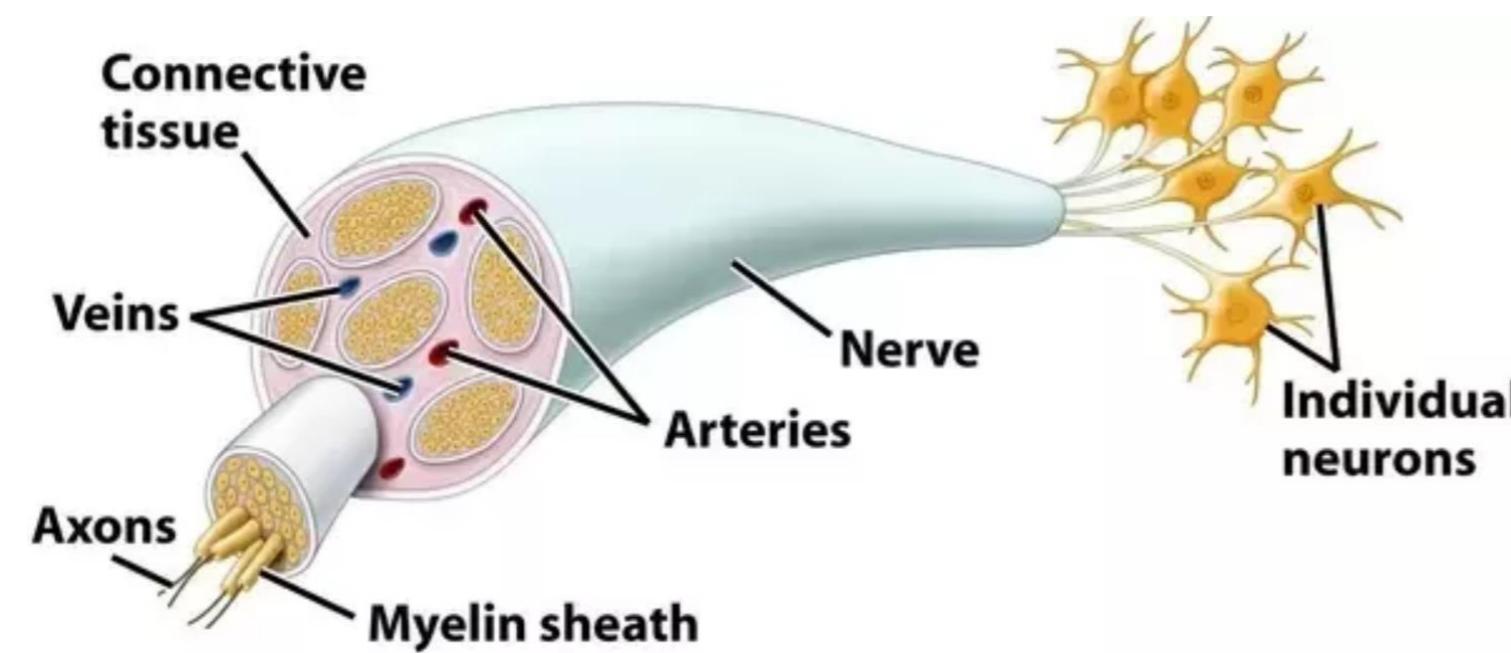
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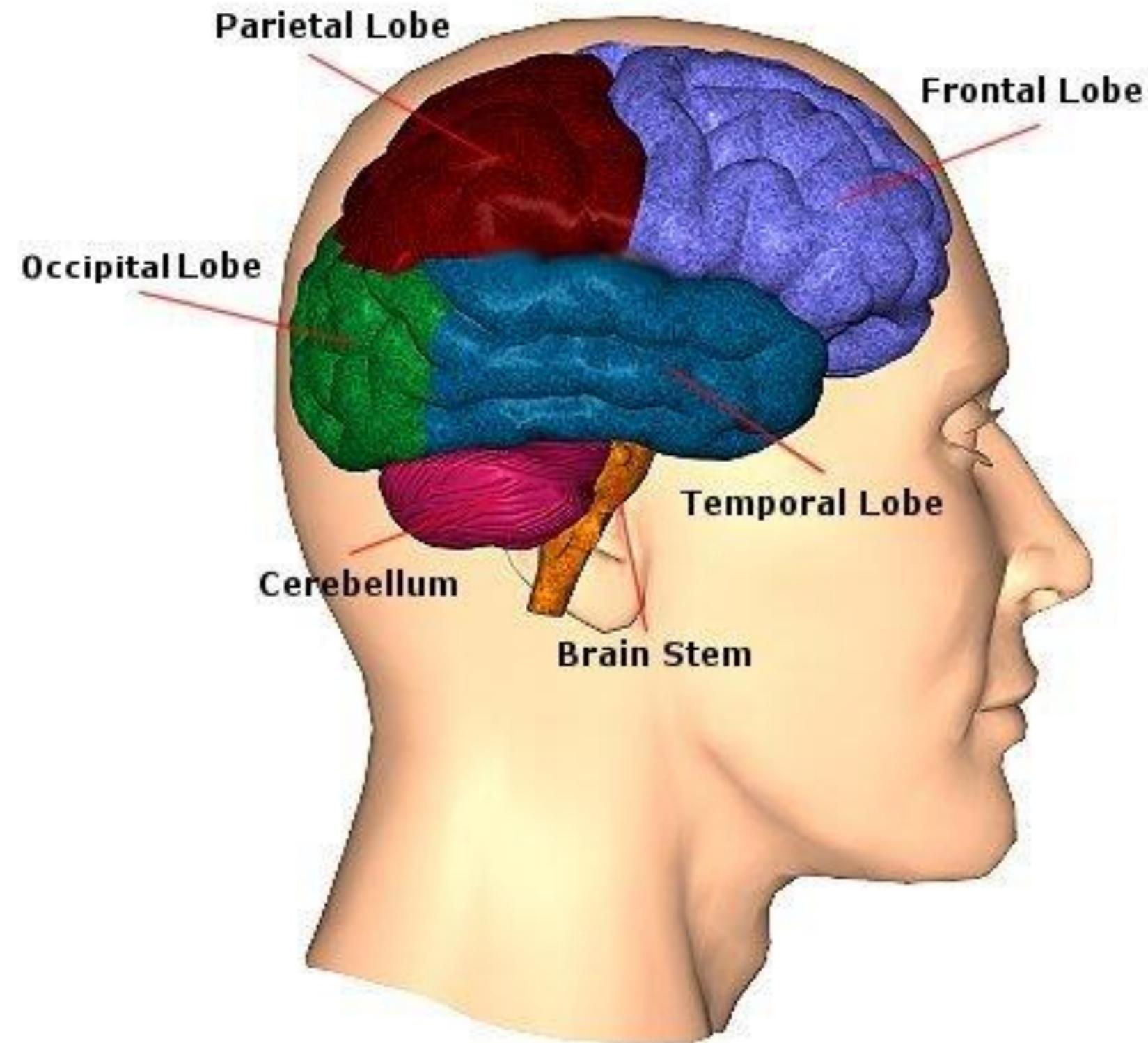
# Introducción al paradigma del mantenimiento de la salud estructural

## DATA TRANSMISSION



# Introducción al paradigma del mantenimiento de la salud estructural

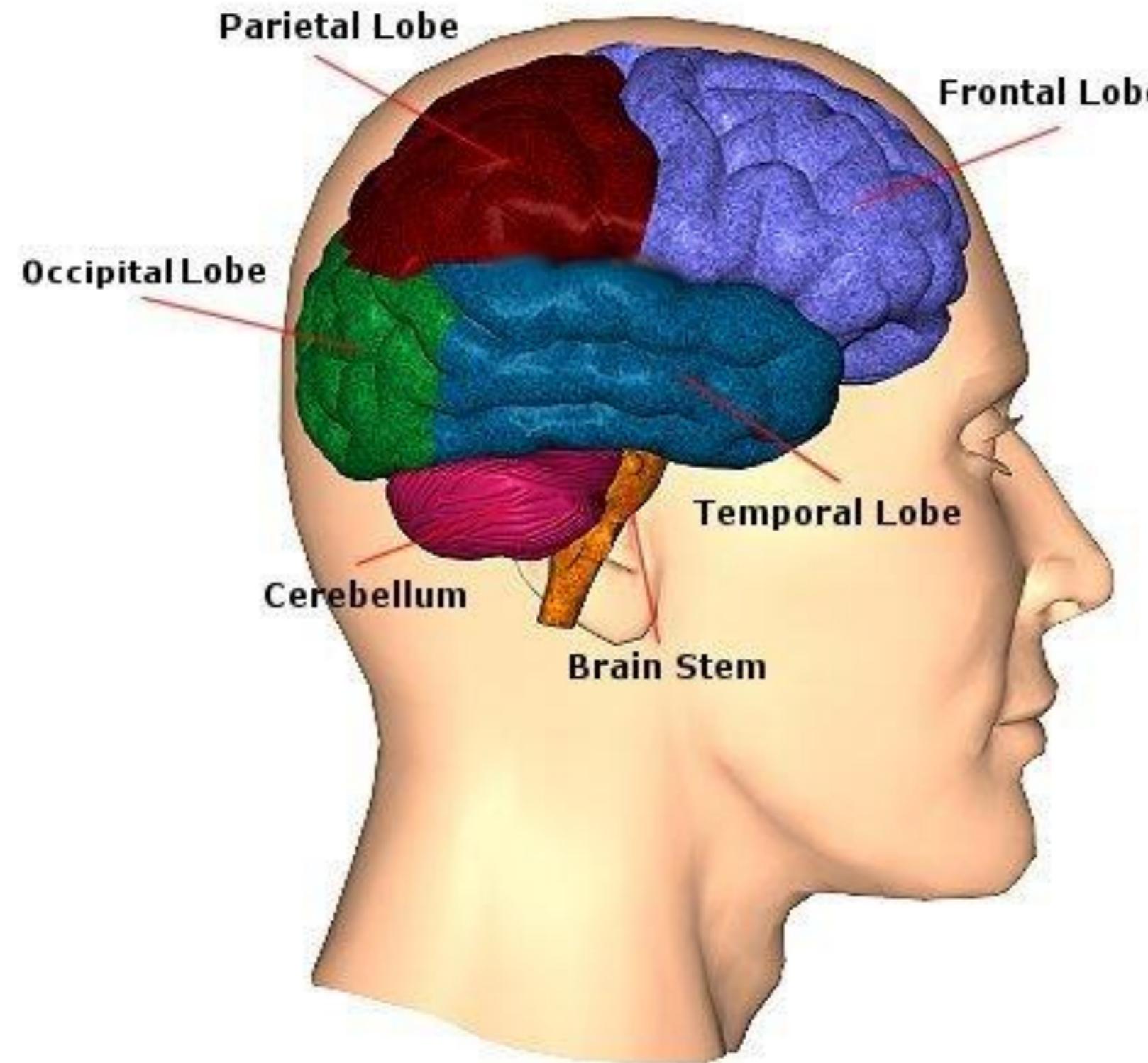
**DATA ACQUISITION  
(DAQs)**



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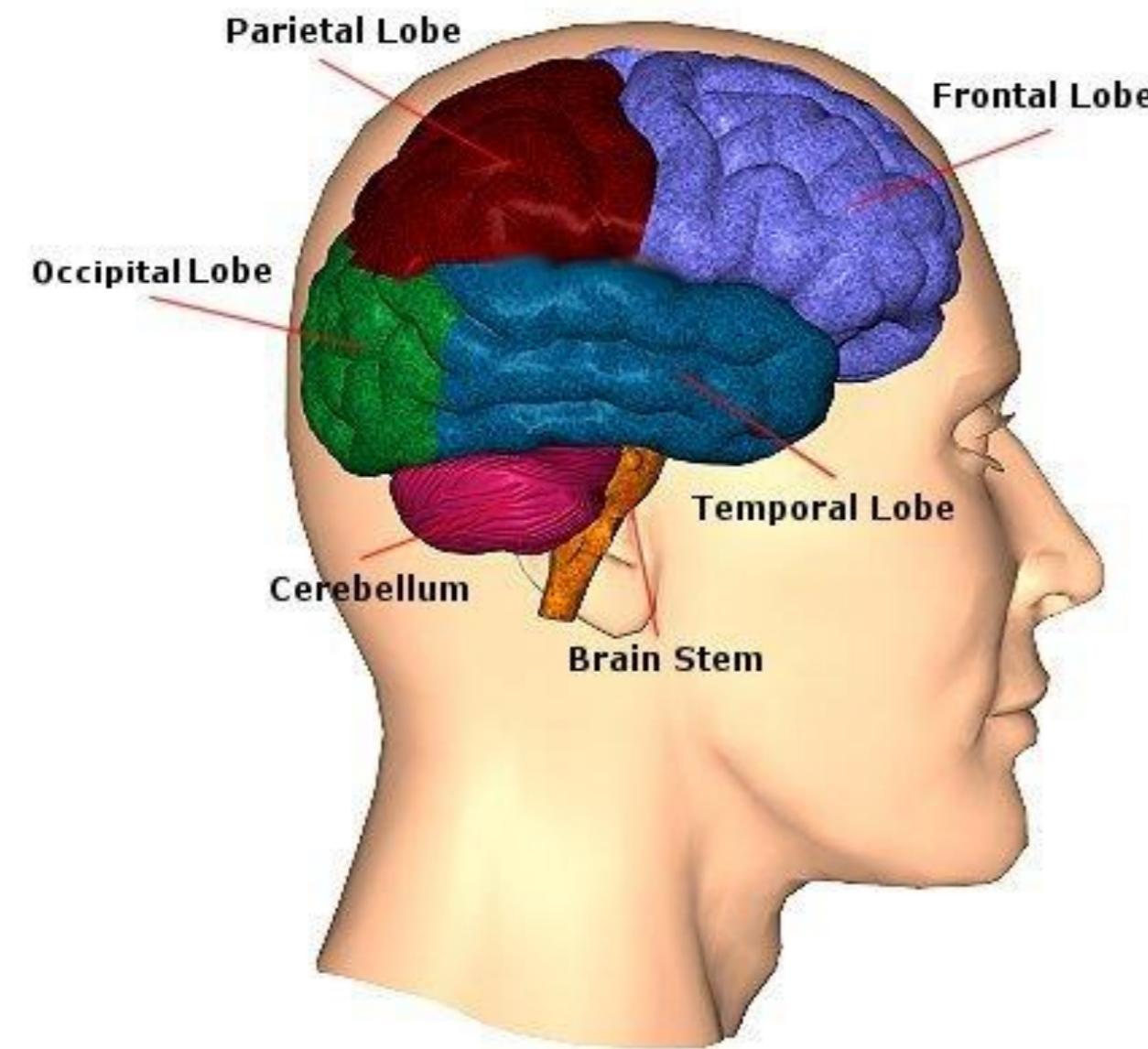
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**DATA ACQUISITION  
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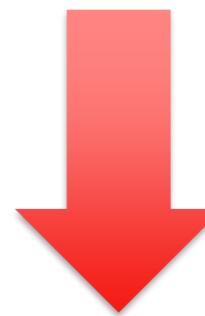


# Introducción al paradigma del mantenimiento de la salud estructural

**DIAGNOSIS, PROGNOSIS,  
DECISION-MAKING**



- ❖ *Diagnosis*
- ❖ *Prognosis*
- ❖ *Decision-making*

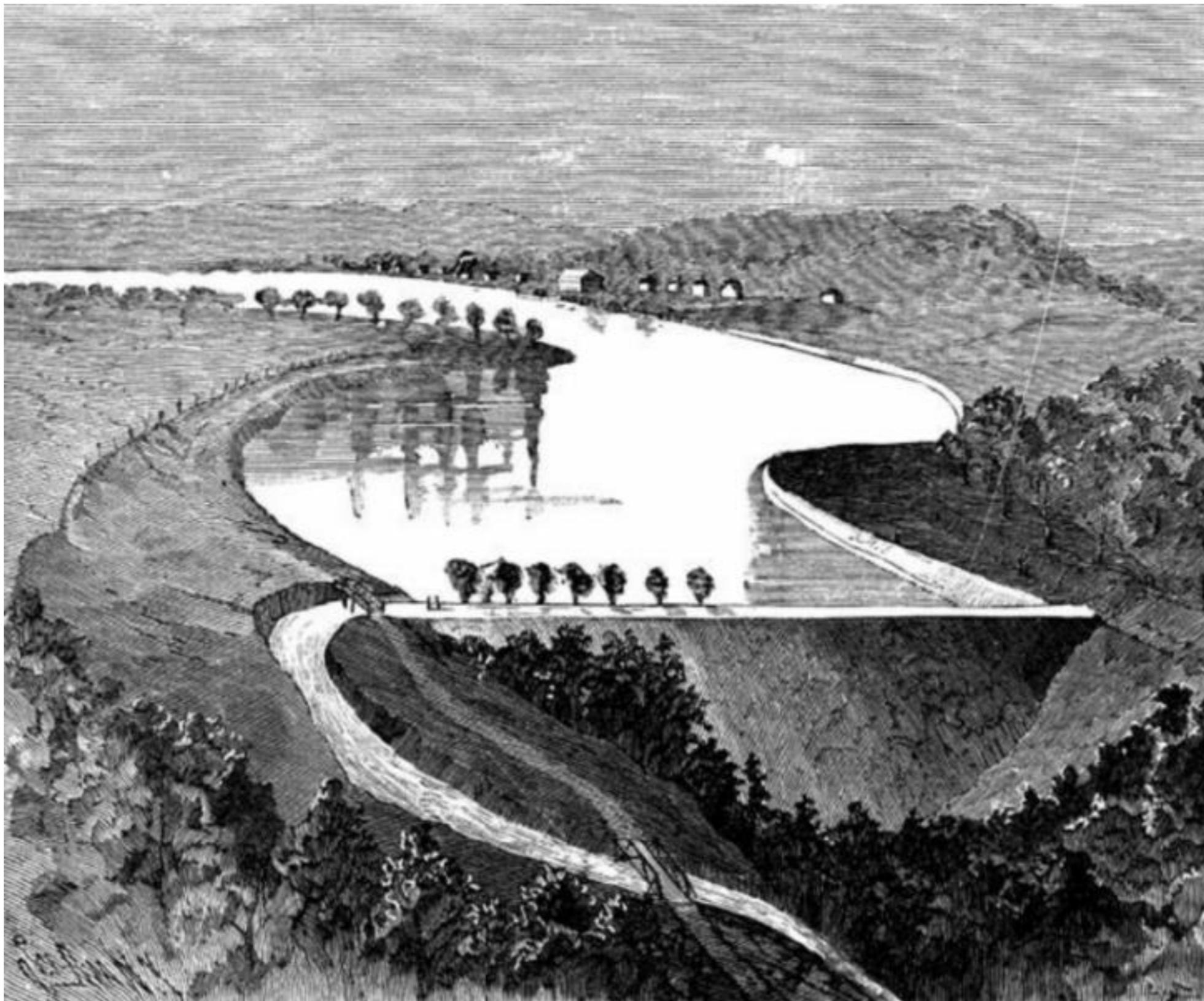




# Historia del SHM.

# Historia del SHM

South Fork Dam - The Johnstown Flood (1889)



# Historia del SHM

Tacoma Narrows, WA (1940)



<https://www.youtube.com/watch?v=3mclp9QmCGs>



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# Historia del SHM

Clifton Bridge (2015)



<https://www.youtube.com/watch?v=4we-3tplppw>

Nürnberg stadium (2016)



<https://www.youtube.com/watch?v=X50qwgBuXpY>



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# Historia del SHM

Kobe (1995)



# Historia del SHM

L'Aquila (2009)



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# Historia del SHM

Morandi Bridge collapse (2018)



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The header of the France 24 news website. It features the 'FRANCE 24' logo with a blue globe icon. To the right is a circular 'LIVE' button with a play icon. Below the logo is a navigation bar with links: '#IRAN', '#IMPEACHMENT', 'FRANCE', 'AFRICA', 'CULTURE', 'TV SHOWS', and 'FIGHT THE FAKE'. A small house icon and the word 'Europe' are also present. The background of the header is light blue.

## Genoa bridge collapse sounds the alarm on aging infrastructure in Europe



Issued on: 17/08/2018 - 19:24 Modified: 18/08/2018 - 16:55



Piero Cruciatti, AFP | This general view taken on August 15, 2018, shows abandoned vehicles on the Morandi motorway bridge after a section collapsed in the northwestern Italian city of Genoa.



## Motivaciones y retos del SHM.

¿Cuáles son las motivaciones para  
implementar un sistema SHM?



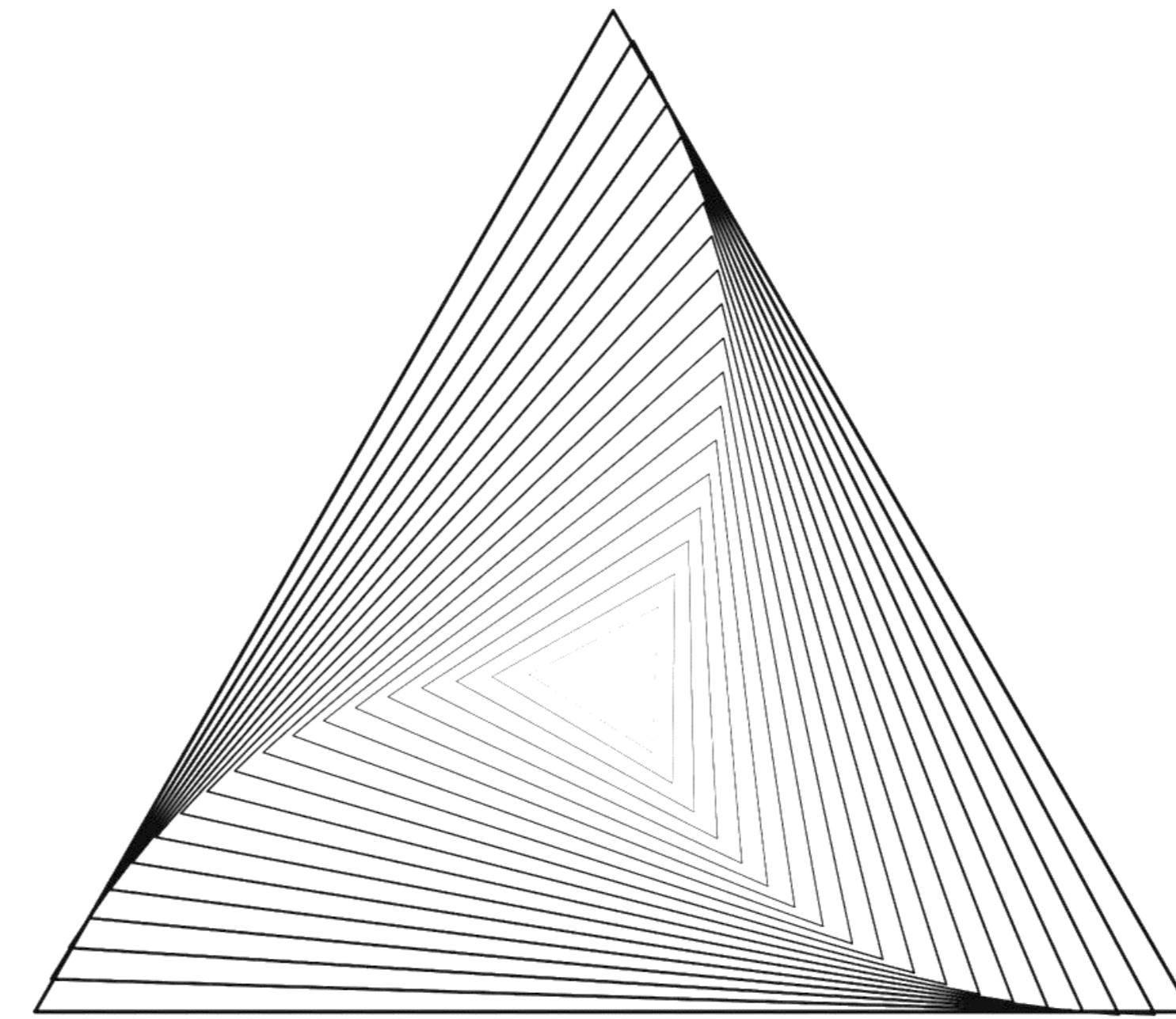
## Motivaciones y retos del SHM

- ❖ Performance based design can be undertaken by recording site-specific environmental conditions such as wind, load demands or temperature.
- ❖ Design assumptions and parameters can be validated with the potential benefit of improving design specifications and guidelines for future similar structures.
- ❖ Inspections can be scheduled on an “as needed” basis informed by structure-specific data when indicated by monitoring data.
- ❖ Performance thresholds can be established to provide warning when prescribed limits are violated, such as for anomalies in loading and response.
- ❖ Real-time safety assessment can be carried out during normal operations or immediately after disasters and extreme events.
- ❖ Accuracy of in-situ inspections can be improved by analysing recorded structural response data.
- ❖ More accurate information can be used for optimally scheduling maintenance and repair activities, leading to cost savings.

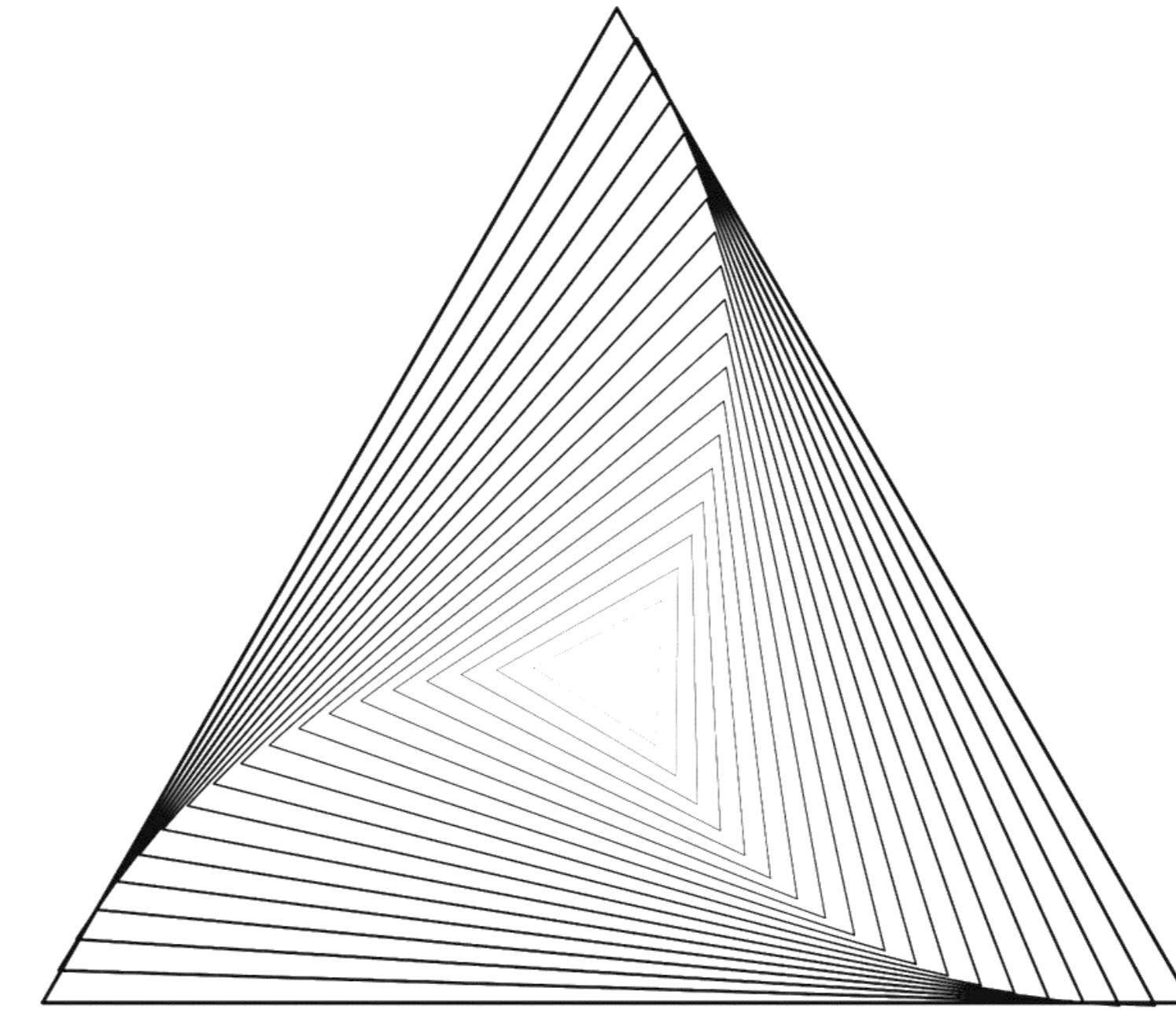


# Motivaciones y retos del SHM

- ❖ Improving safety.
- ❖ Automating inspections.
- ❖ Data for improving designs.



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# Motivaciones y retos del SHM

**Improving safety:** optimal use of structures, a minimized downtime, and the avoidance of catastrophic failures.

Aloha Airlines Flight 243 (Boeing 737) (1988)



I-95's Mianus River Bridge collapse, Greenwich, Connecticut (1983)



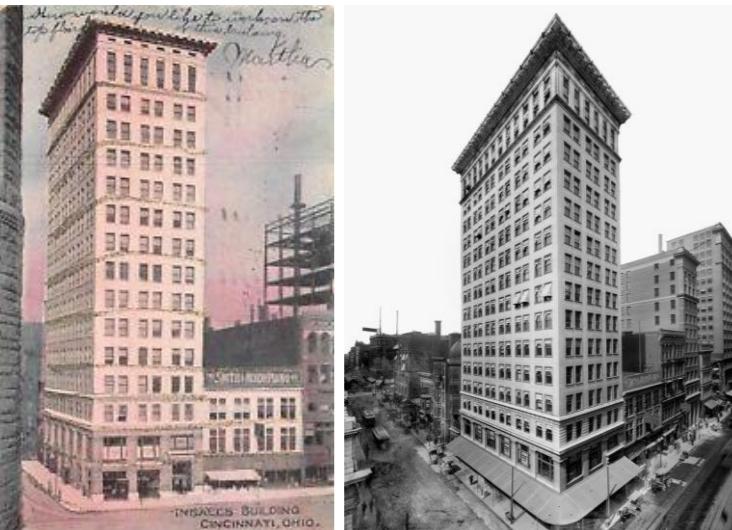
# Motivaciones y retos del SHM



- 1853 – The French industrialist François Coignet built the first reinforced concrete structure, a four-story house in Paris.



- 1875 – Joseph Monier built the first reinforced concrete bridge, the Chazalet Bridge (14 meters long span).



- 1903 – Ingalls Building. The world's first reinforced concrete skyscraper (16-story building, 54 meters tall, USA).

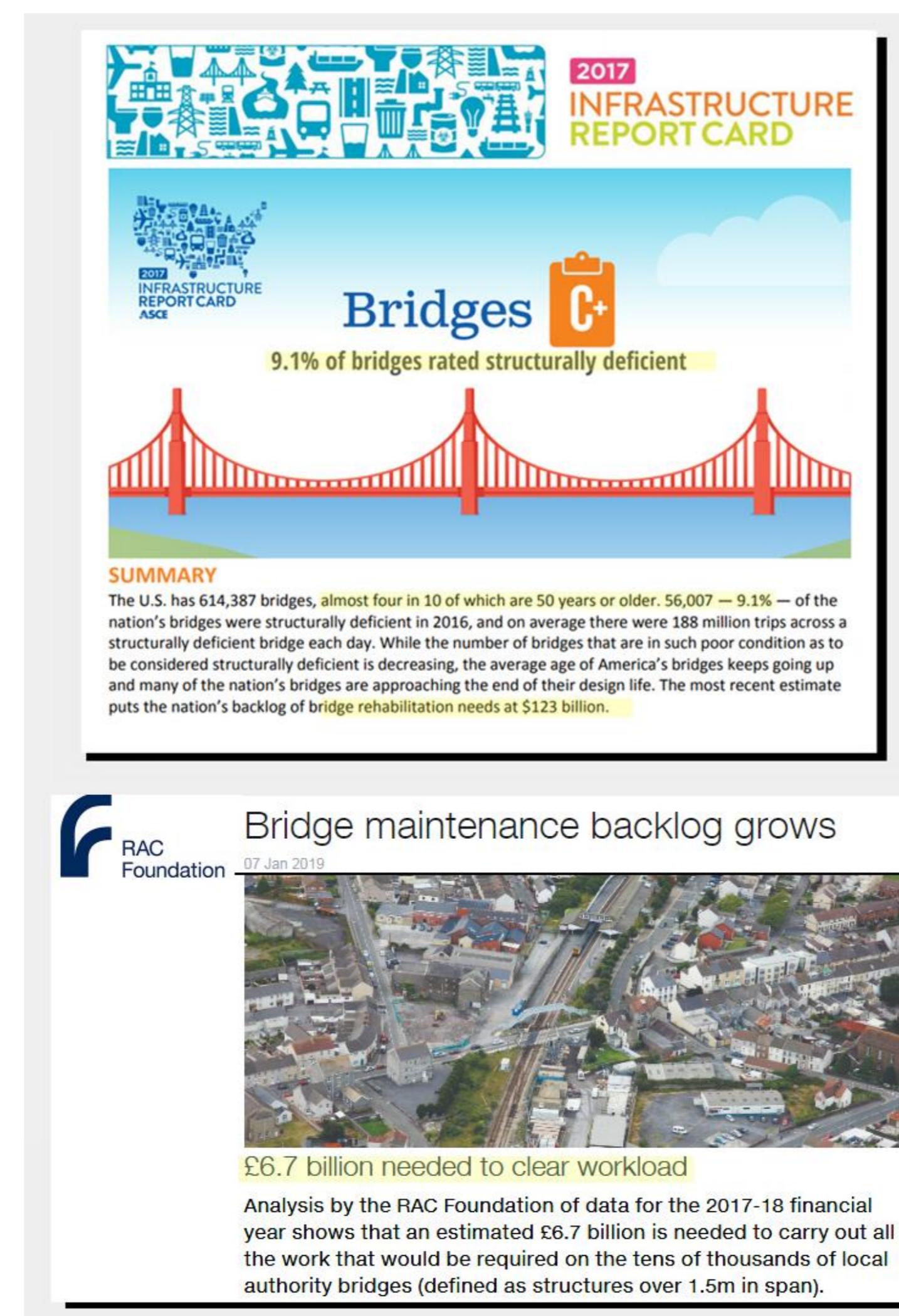


- 1936 – Franz Dischinger designed the first post-tensioned concrete bridge (Aue/Saxony).



- 1938 - Eugène Freyssinet built the first pre-stressed concrete bridge (Algeria)
- 1940 - Oelde Bridge (Germany)

# Motivaciones y retos del SHM



## Corrosion Costs by Industry Sector



way bridges, gas and liquid transmission pipelines, waterways and ports, hazardous materials storage, airports, and railroads. The annual direct cost in this category was estimated to be \$22.6 billion (Figure 2).

**HIGHWAY BRIDGES**  
There are approximately 583,000 bridges in the U.S.



are constructed of concrete, and the other construction materials. Approximately 15% of these bridges are structurally deficient because of corroded steel and steel reinforcement. Annual direct cost estimates total \$8.3 billion, including \$3.8 billion to replace deficient bridges over the next 10 years, \$2 billion for main-

tenance and capital costs for concrete bridge decks and \$2 billion for their concrete substructures, and \$0.5 billion for maintenance painting of steel bridges. Indirect costs to the user, such as traffic delays and lost productivity, were estimated to be as high as 10 times that of direct corrosion costs.

### GAS AND LIQUID TRANSMISSION PIPELINES

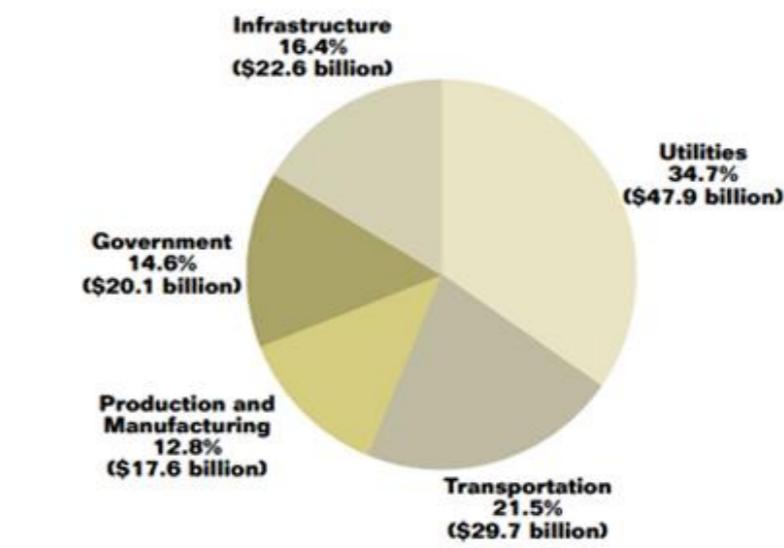
Corrosion is the primary factor affecting the longevity and reliability of pipelines that transport crucial energy sources throughout the nation. There are more than 528,000 km (328,000 miles) of natural gas transmission and gathering pipelines, 119,000 km (74,000 miles) of crude transmission and gathering pipelines, and 132,000 km (82,000 miles) of hazardous liquid transmission pipelines. The average annual corrosion-related cost is esti-

The U.S. economy was divided into five major sector categories for analysis in the corrosion cost study, and these were further broken down into 26 sectors. The categories were infrastructure, production and manufacturing, government, transportation, and utilities. When added together, the total cost of all five sectors was \$137.9 billion. This total was extrapolated to the total U.S. economy to an annual cost of corrosion of \$22.6 billion.

### Infrastructure

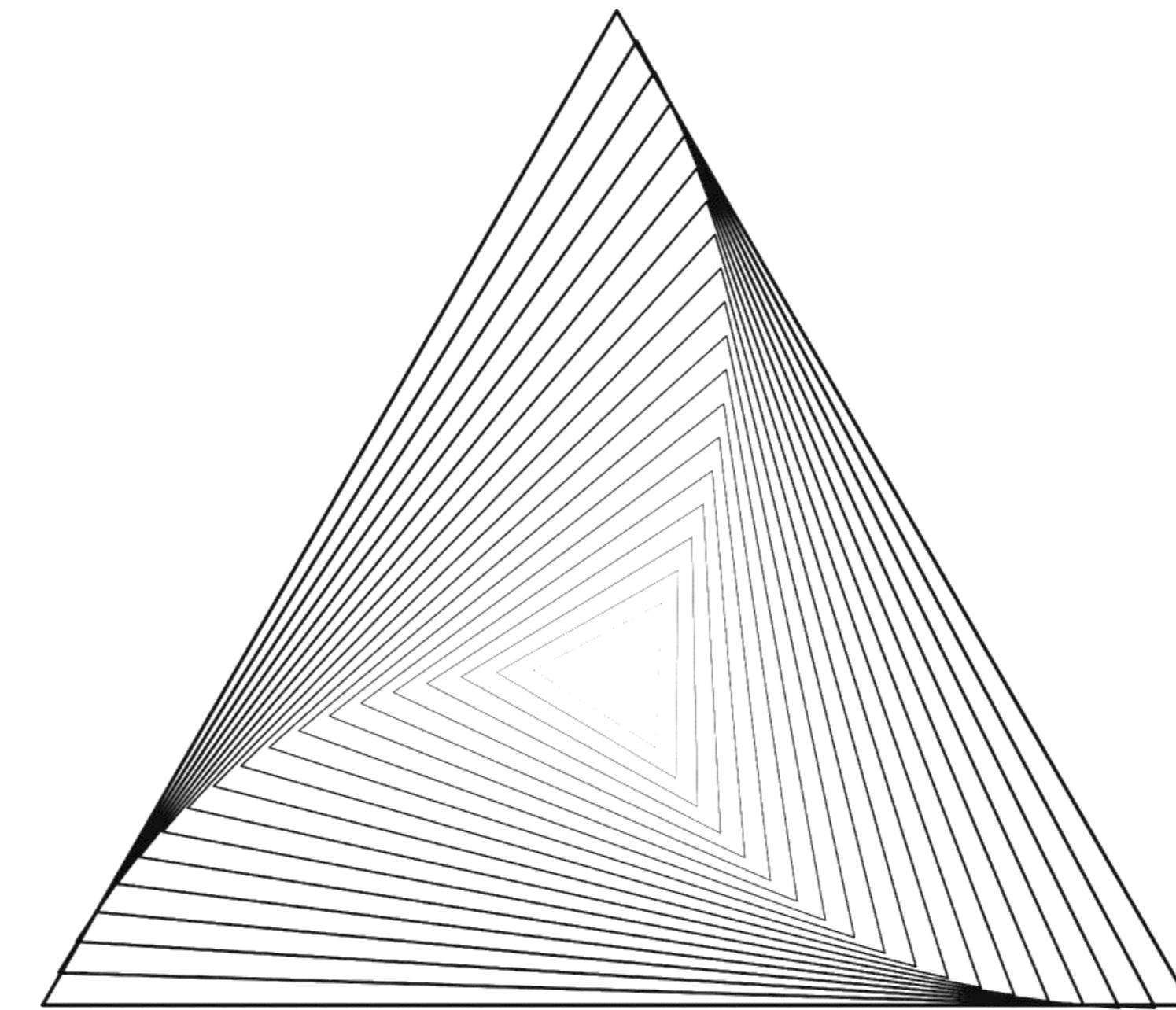
The aging infrastructure is the most serious problem facing society today. In past decades, corrosion professionals focused primarily on new construction—specifying materials and designing corrosion prevention and control systems for buildings,

**FIGURE 1**  
**COST OF CORROSION IN INDUSTRY CATEGORIES (\$137.9 BILLION)**



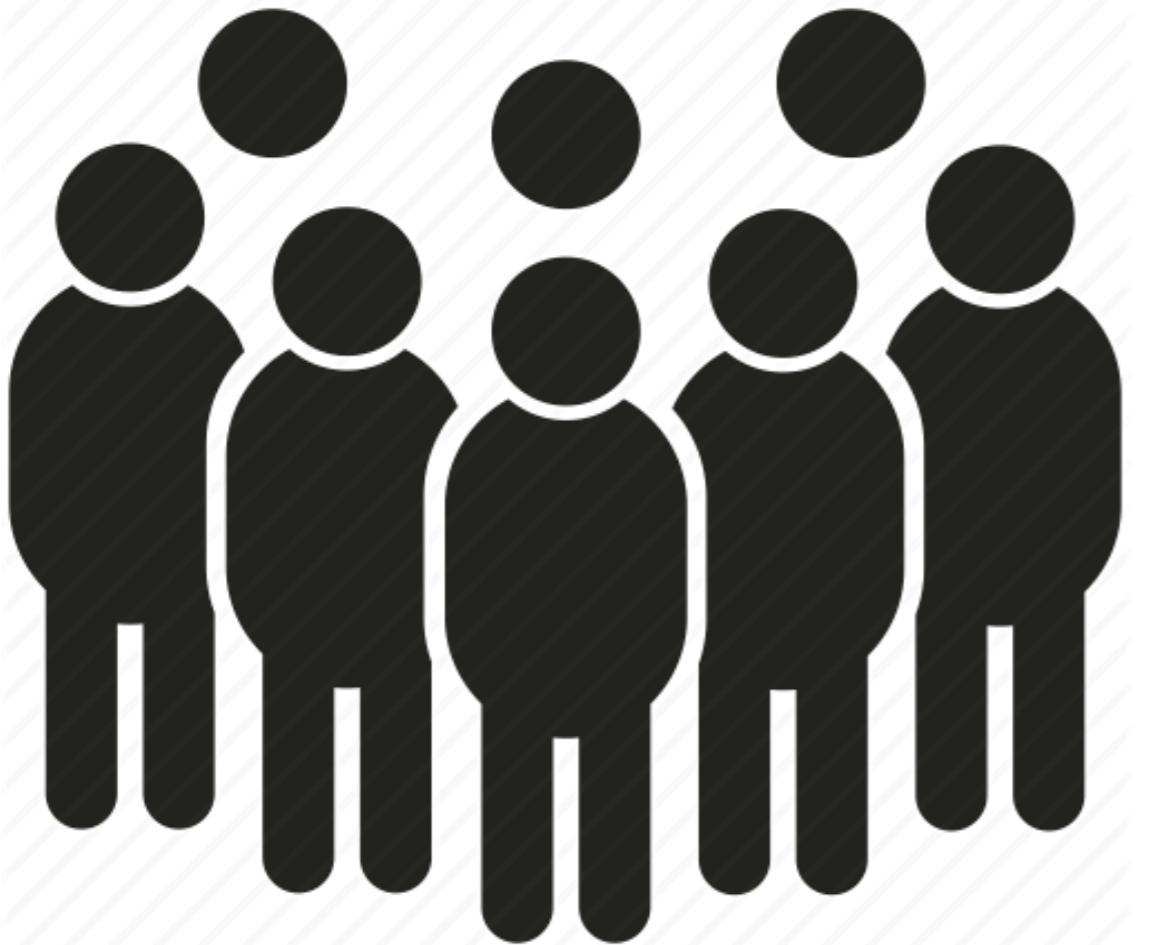
# Motivaciones y retos del SHM

- ❖ Improving safety.
- ❖ Automating inspections.
- ❖ Data for improving designs.



# Motivaciones y retos del SHM

## MAINTENANCE STRATEGIES



Ageing degradation

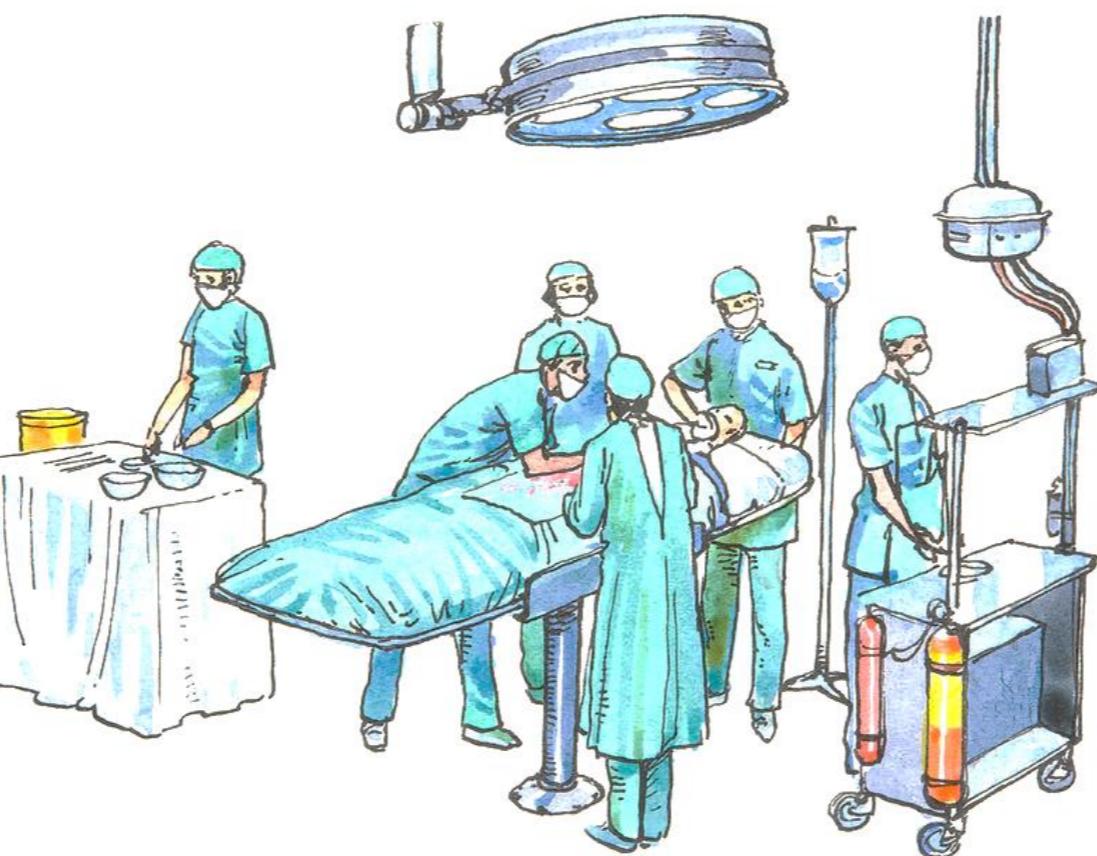
# Motivaciones y retos del SHM

## MAINTENANCE STRATEGIES



Ageing degradation

Corrective maintenance



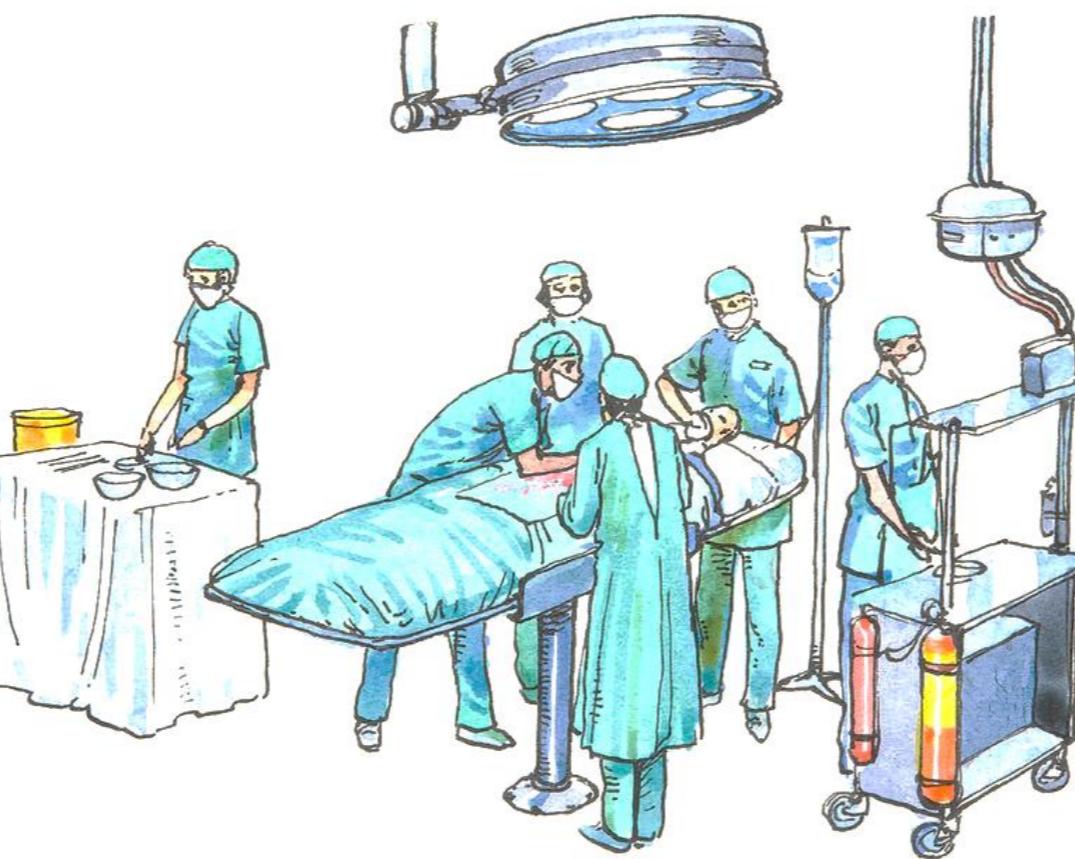
# Motivaciones y retos del SHM

## MAINTENANCE STRATEGIES



Ageing degradation

Corrective maintenance



Preventive maintenance



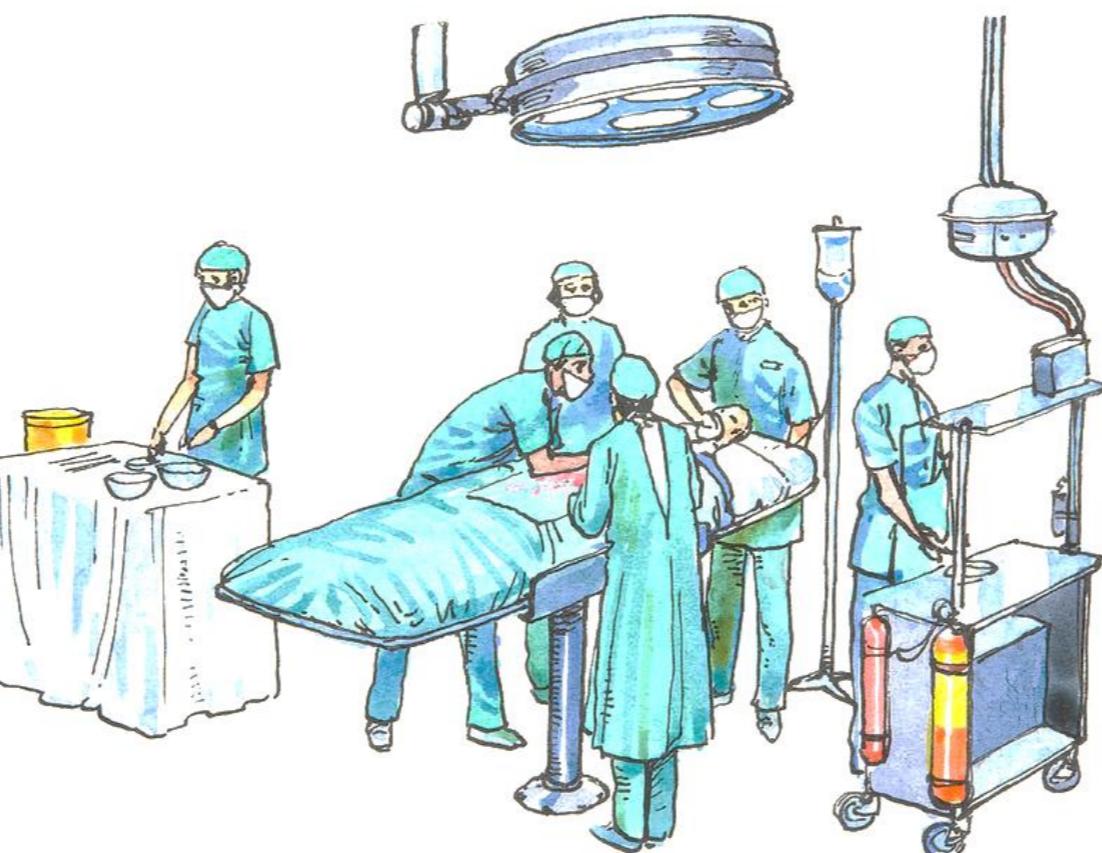
# Motivaciones y retos del SHM

## MAINTENANCE STRATEGIES

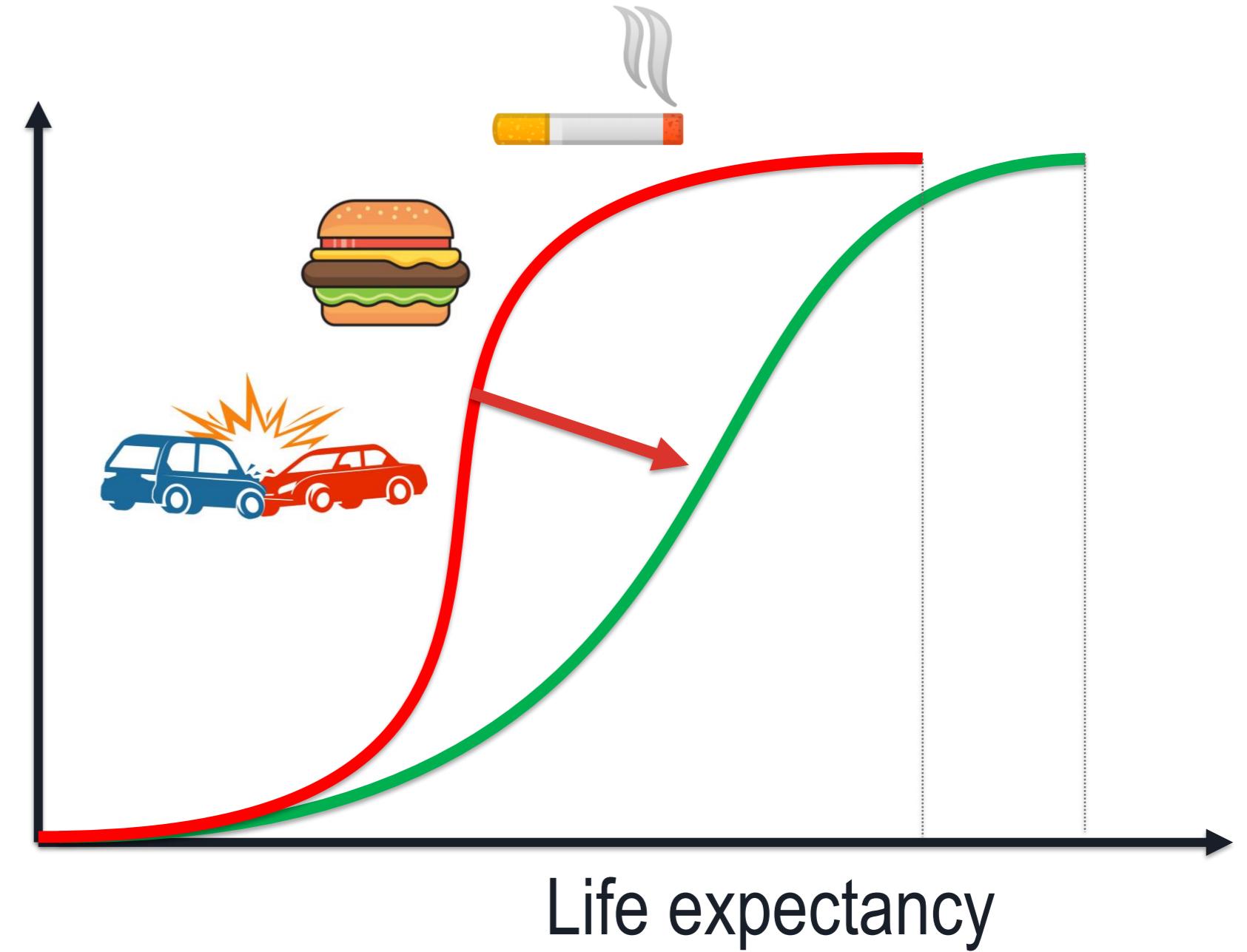


Ageing degradation

Corrective maintenance



Probability of failure



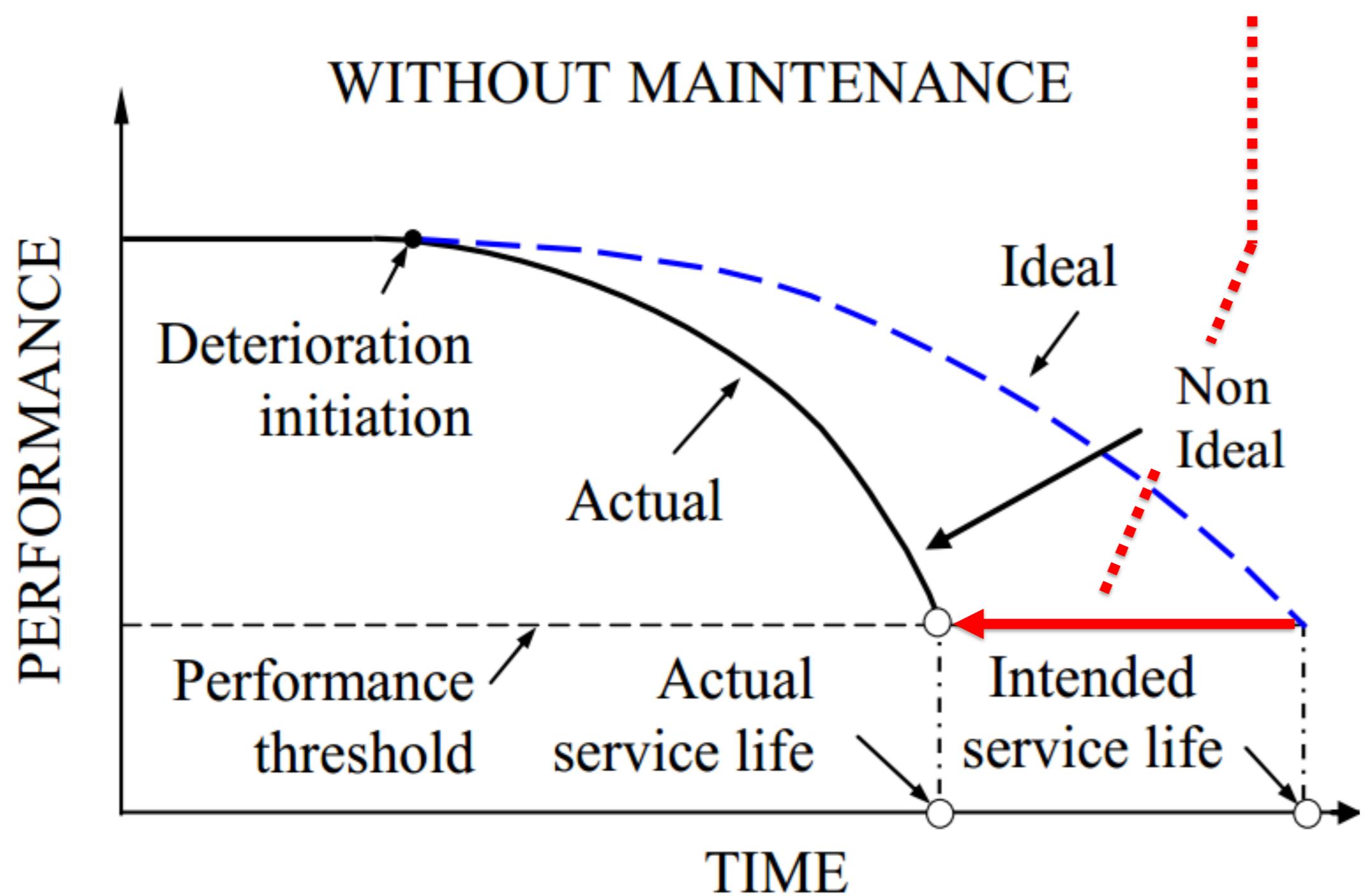
Life expectancy

Preventive maintenance



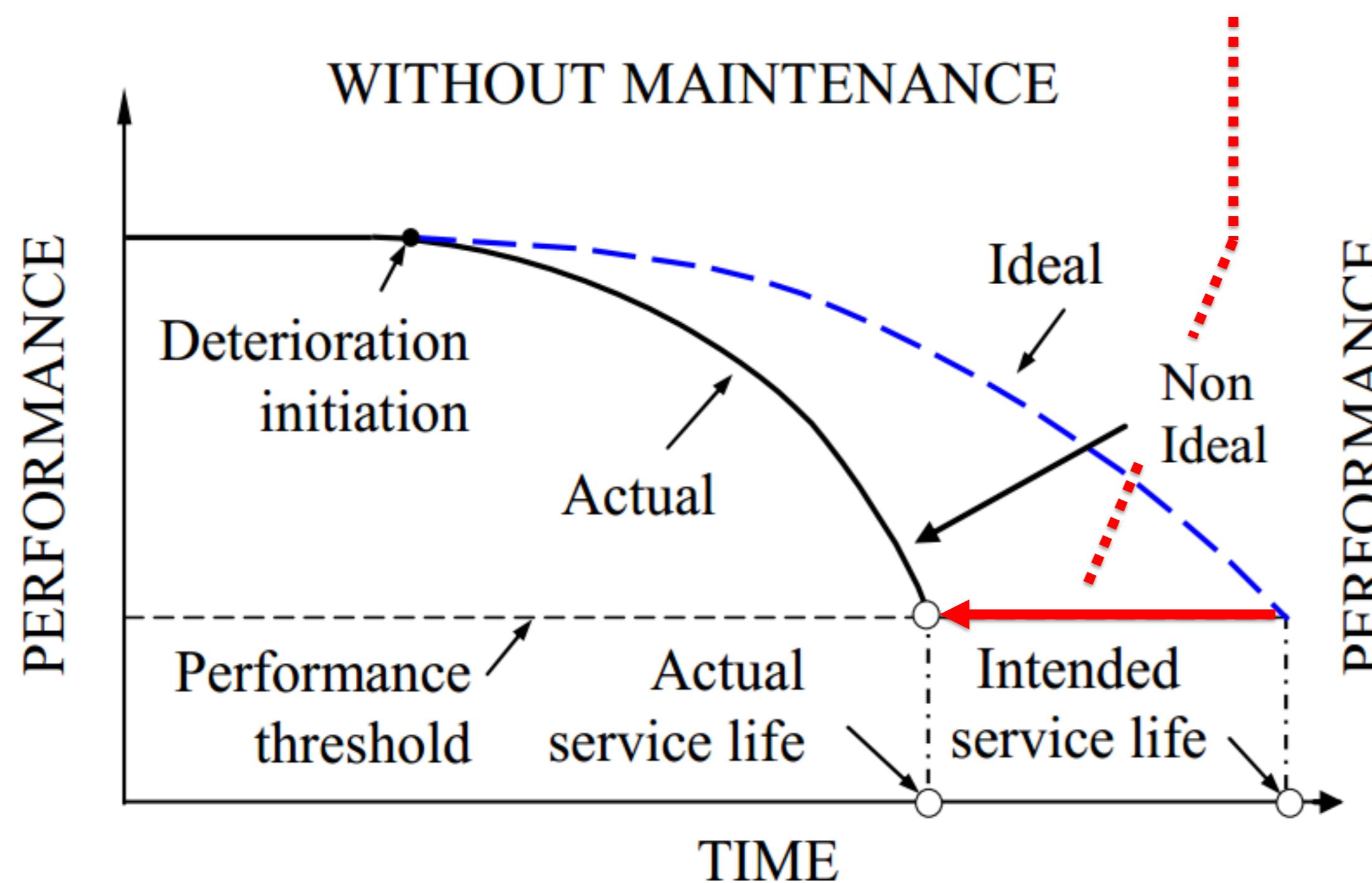
## Motivaciones y retos del SHM

- Natural hazards
- Man-made disasters
- Accelerated aging

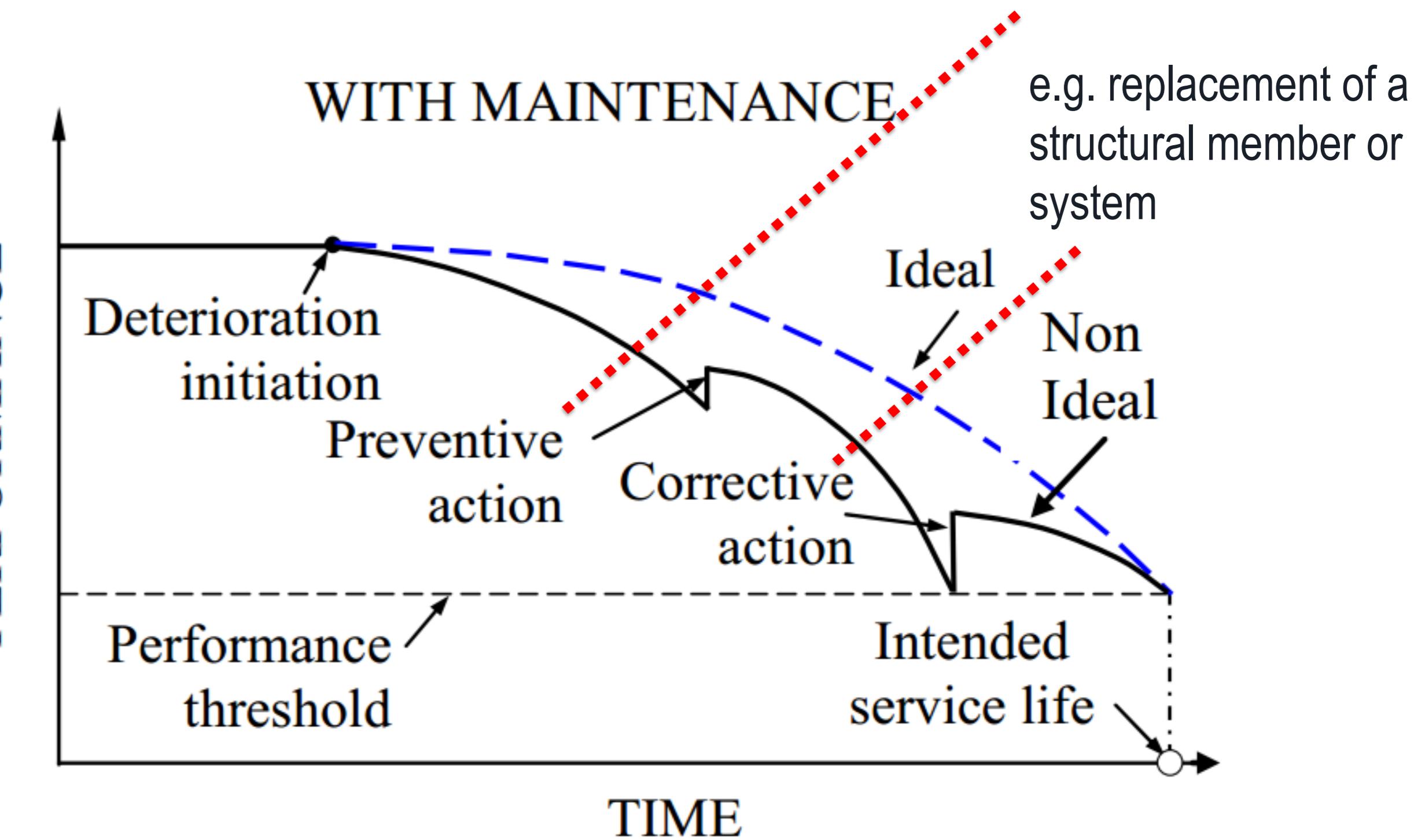


# Motivaciones y retos del SHM

- Natural hazards
- Man-made disasters
- Accelerated aging

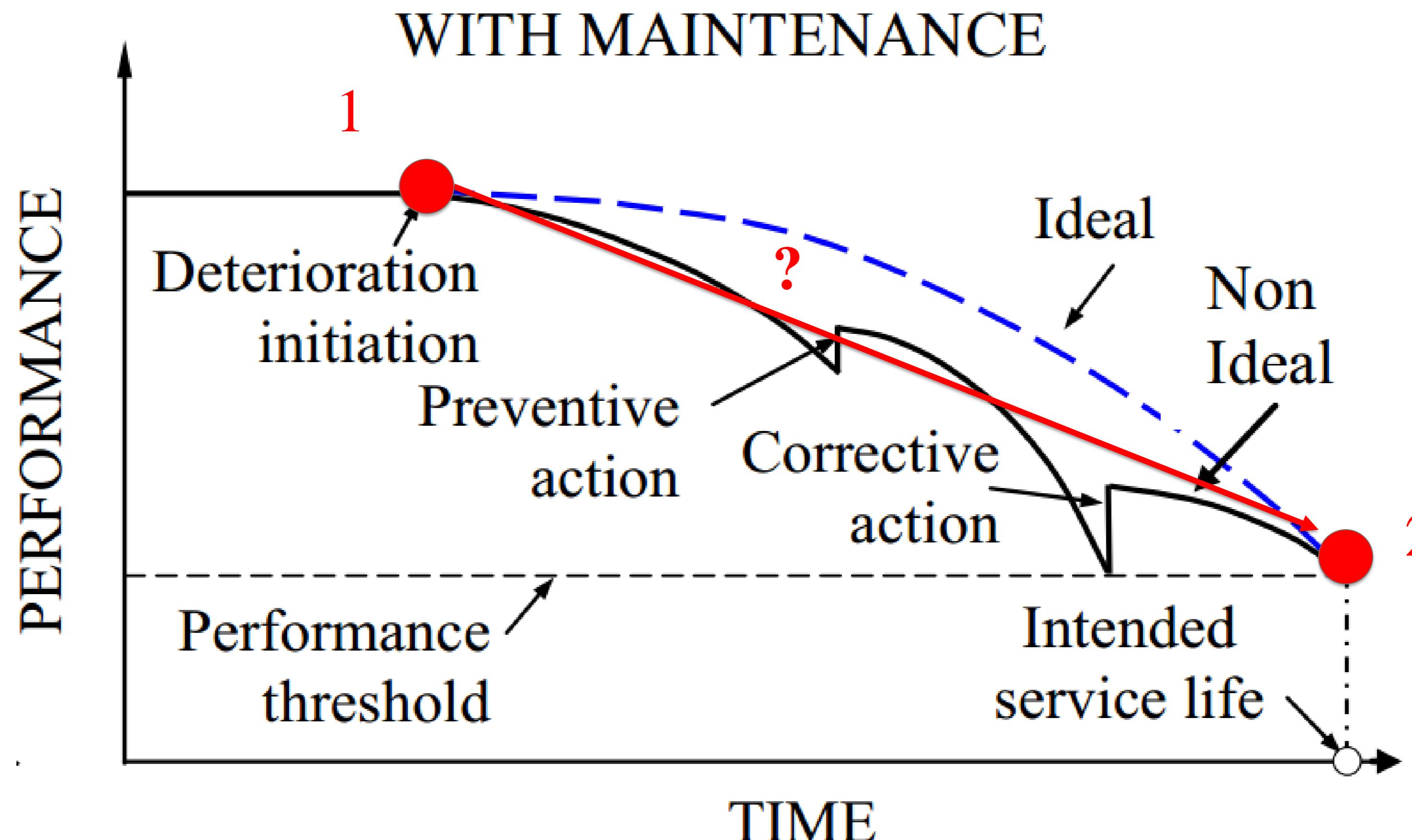


e.g. application of sealer on a bridge deck

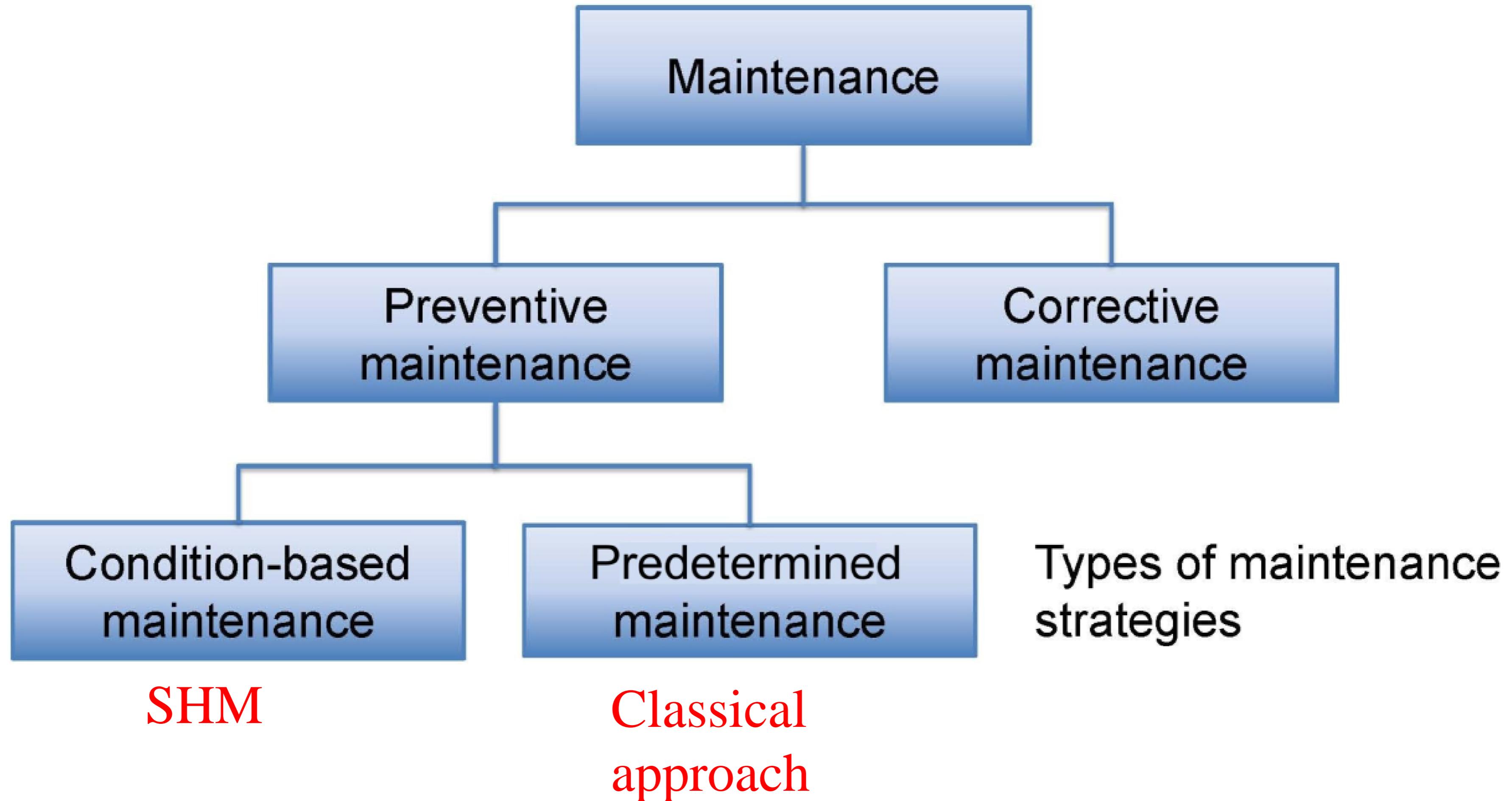


e.g. replacement of a structural member or system

## Motivaciones y retos del SHM



# Motivaciones y retos del SHM



# Motivaciones y retos del SHM

## Optimal intervals for time-based inspections?

Maintenance needs often are greater than available funds, decisions and scenarios for maintaining infrastructural systems must be based on a **life-cycle cost (LCC)** analysis.

- (a) Reliable modeling of loadings (extreme loads, deterioration..etc)
- (b) Prediction of structural safety and performance evolution.
- (c) Estimation of costs of interventions.

Optimization problem

$$C_{ET} = C_T + C_{PM} + C_{INS} + C_{REP} + C_F$$

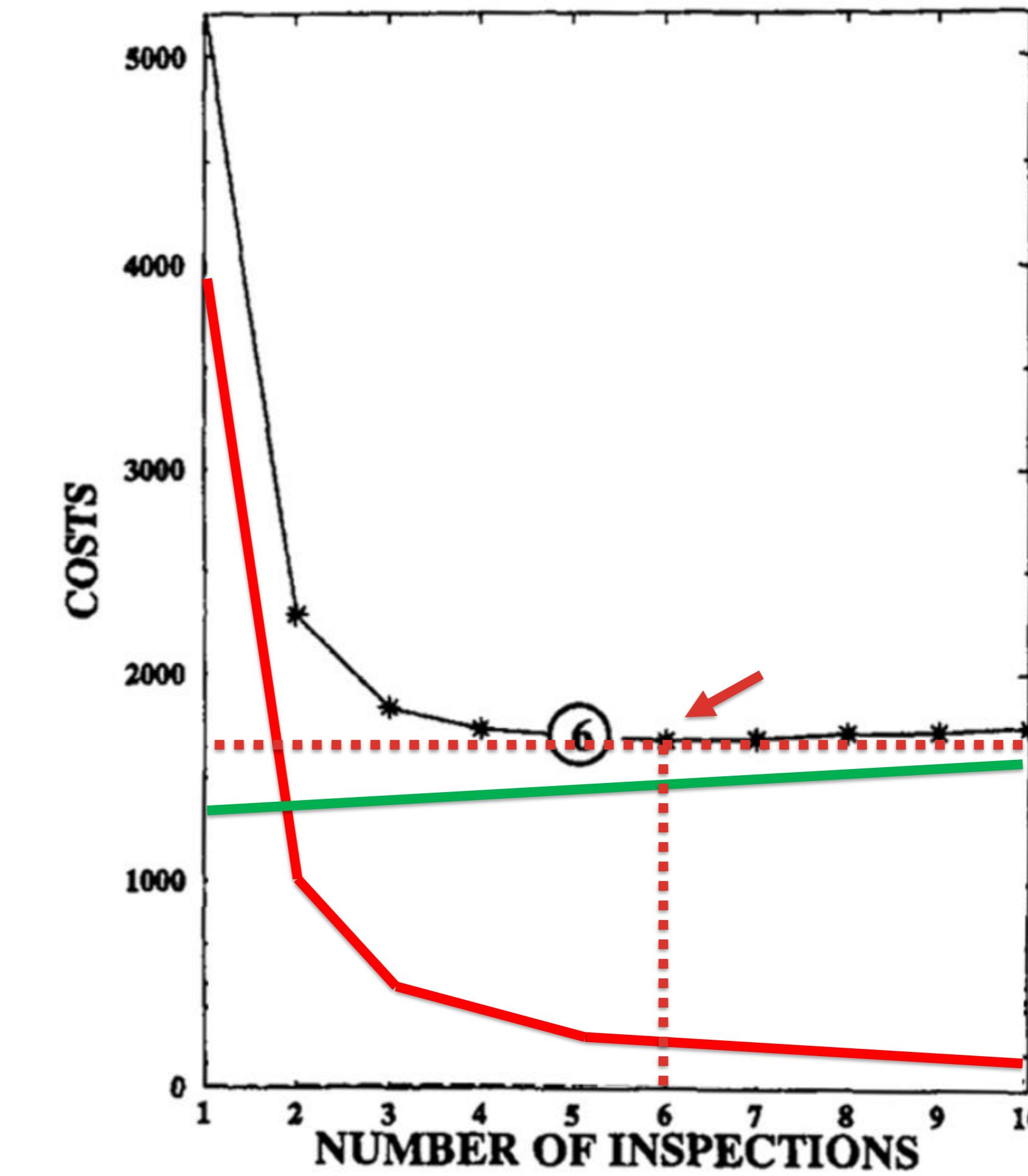
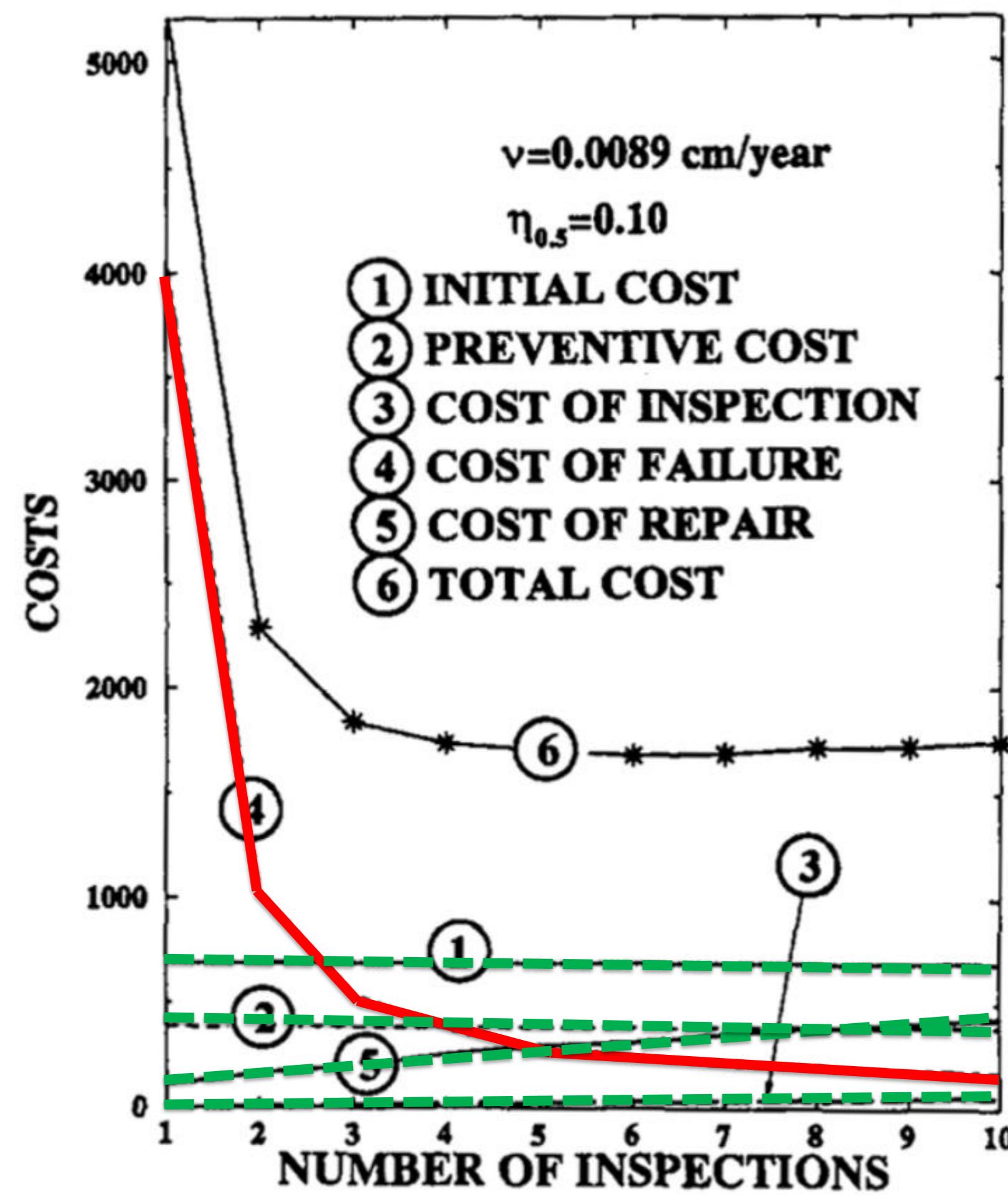
$C_{ET}$	Expected total cost
$C_T$	Initial design/construction cost
$C_{PM}$	Expected cost of routine maintenance
$C_{INS}$	Expected cost of performing inspections
$C_{REP}$	Expected cost of repairs
$C_F$	Expected cost of failure

Frangopol, D. M., Lin, K. Y., & Estes, A. C. (1997). Life-cycle cost design of deteriorating structures. *Journal of structural engineering*, 123(10), 1390-1401.

Frangopol, D. M., Dong, Y., & Sabatino, S. (2017). Bridge life-cycle performance and cost: analysis, prediction, optimisation and decision-making. *Structure and Infrastructure Engineering*, 13(10), 1239-1257.



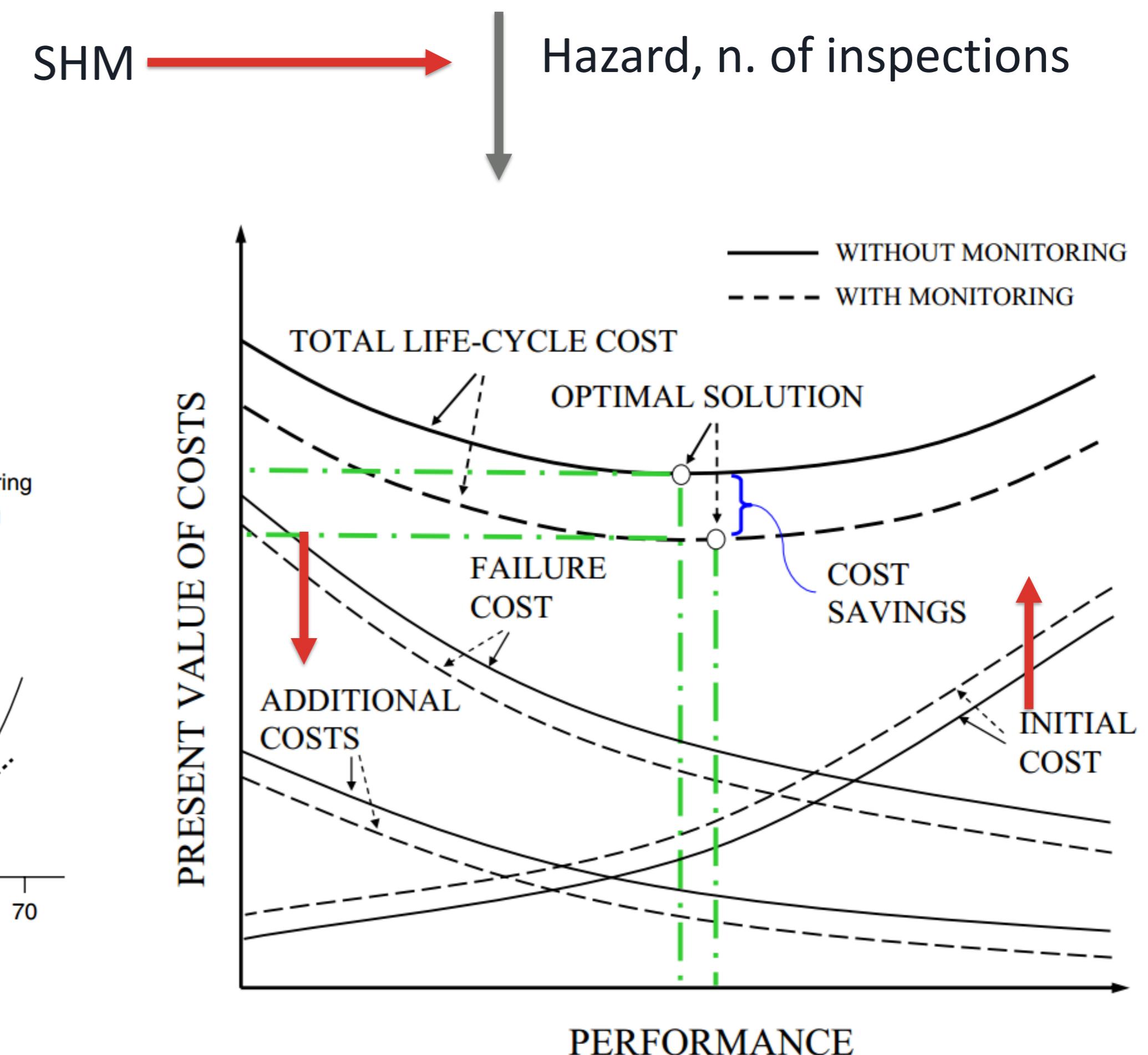
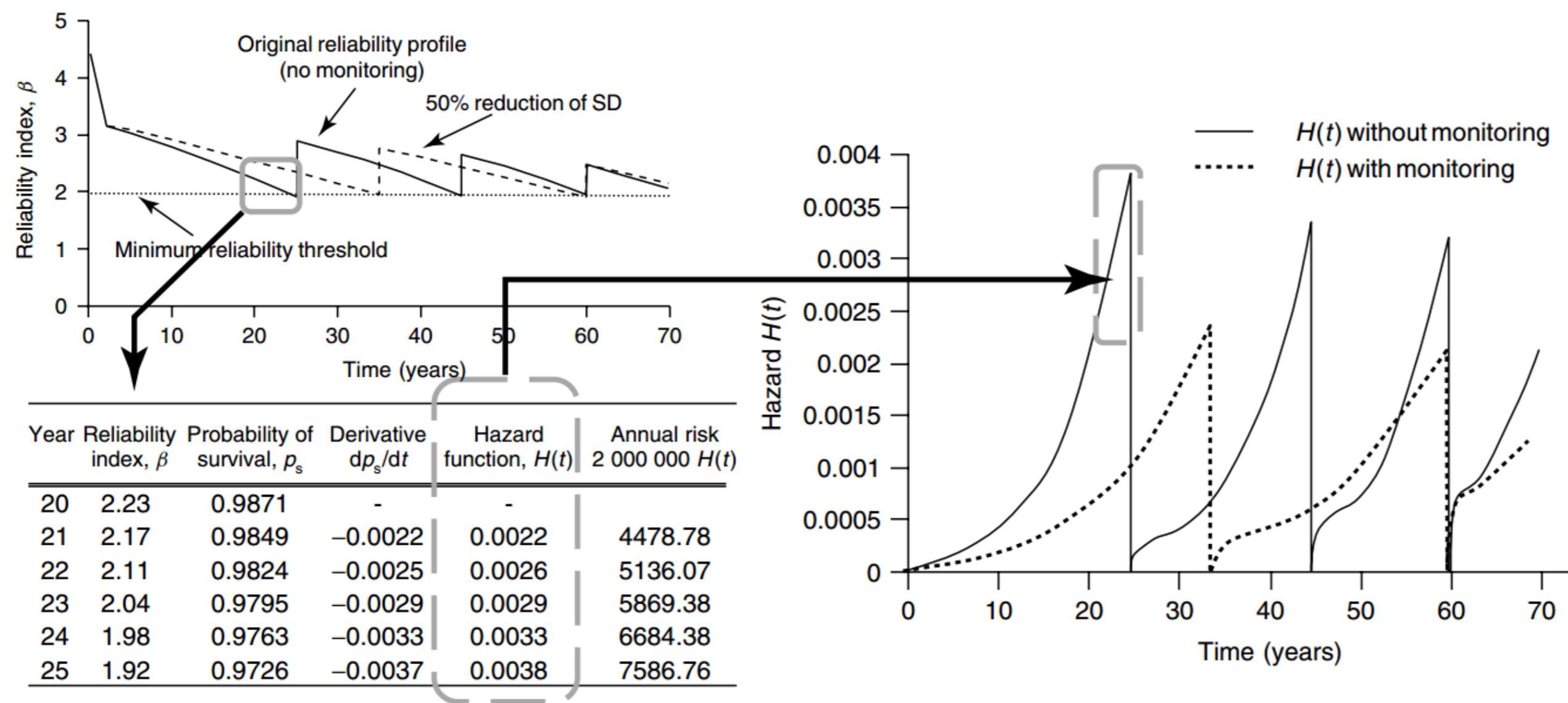
## Motivaciones y retos del SHM



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# Motivaciones y retos del SHM

## Automating inspections: economic improvements for end-users



Frangopol, D. M., & Messervey, T. B. (2009). Maintenance principles for civil structures. Encyclopedia of structural health monitoring.

Faulstich, S., Hahn, B., Jung, H., Rafik, K., & und Prozessmodellierung, I. Z. (2009, January). Suitable failure statistics as a key for improving availability. In *Proceedings of the European Wind Energy Conference, EWEC*.

# Motivaciones y retos del SHM



Saint Brieuc offshore wind farm



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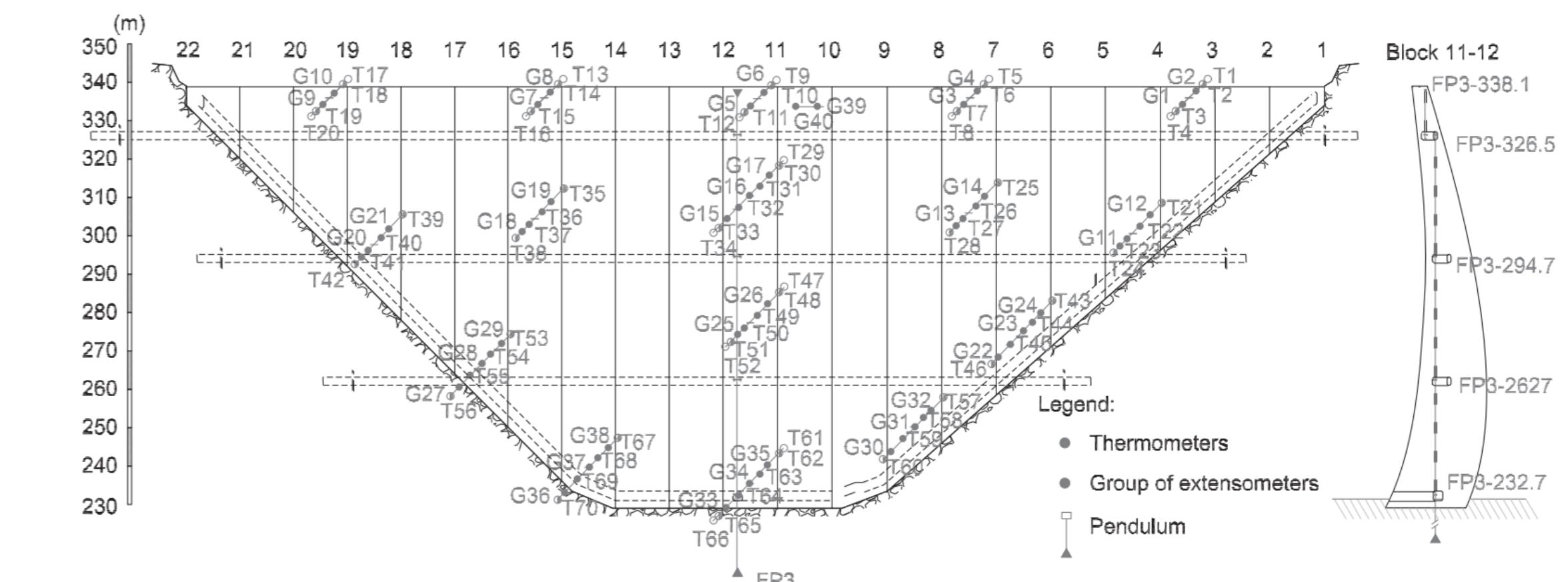
# Motivaciones y retos del SHM



Alto Lindoso dam, Portugal



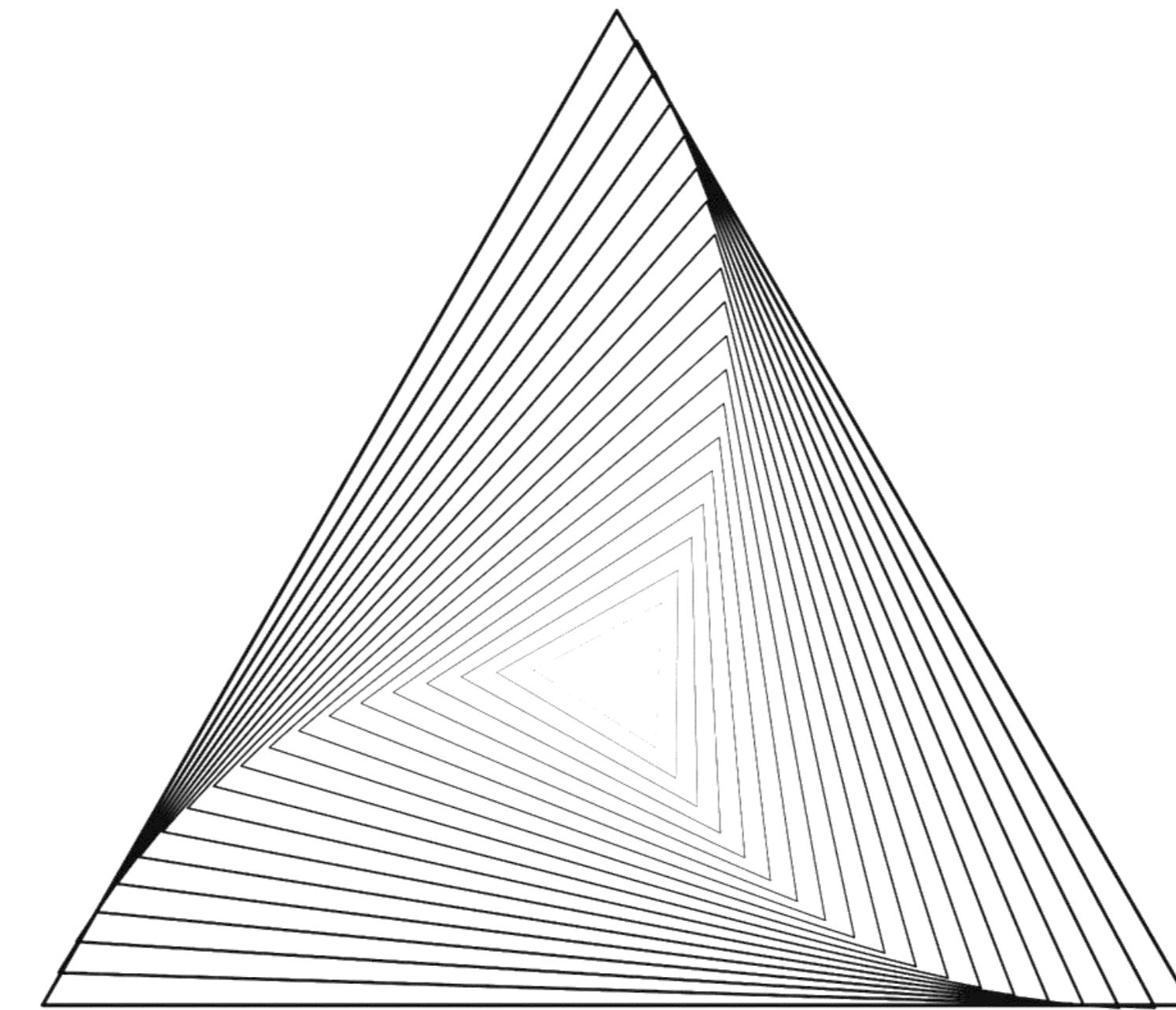
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Mata, J., Tavares de Castro, A., & Sá da Costa, J. (2014). Constructing statistical models for arch dam deformation. *Structural Control and Health Monitoring*, 21(3), 423-437.

# Motivaciones y retos del SHM

- ❖ Improving safety.
- ❖ Automating inspections.
- ❖ Data for improving designs.



❖ Improving safety.

❖ Automating inspections.

❖ Data for improving designs.

- Los datos de monitorización se pueden usar para confirmar o mejorar los coeficientes de seguridad de las acciones existentes, de resistencia y de las combinaciones de carga para eventos extremos usados en los códigos de diseño.
- La monitorización se puede utilizar para mejorar el diseño proporcionando al ingeniero la información estadística necesaria para emplear un diseño probabilístico basado en confiabilidad/desempeño/riesgo.



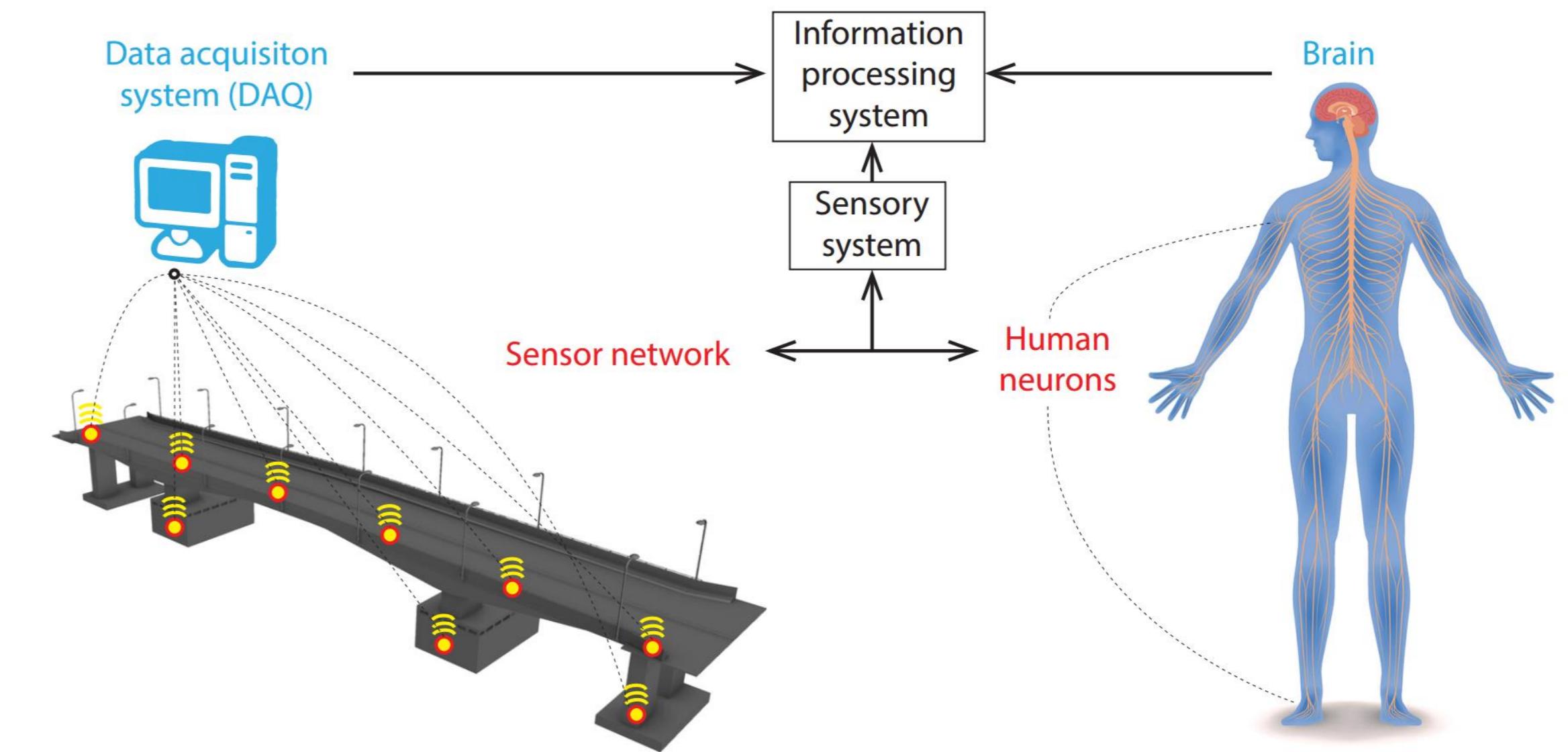
## ❖ Retos del SHM



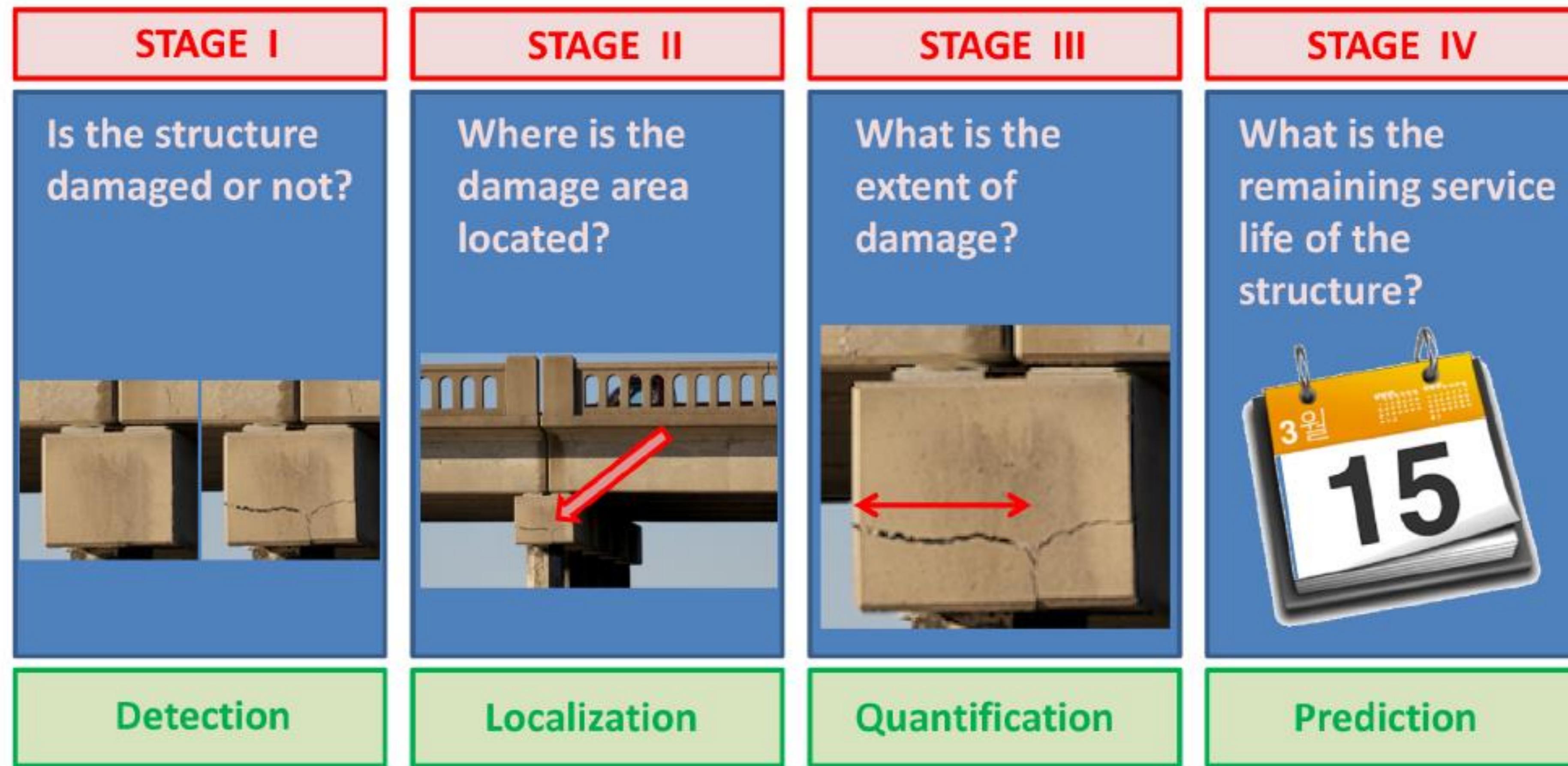
# Motivaciones y retos del SHM

Structural Health Monitoring is highly Multidisciplinary!

- Sensors
- Data acquisition/transmission
- Sensor installation/application
- Data processing
- Structural/Material modelling
- Machine Learning
- Decision making
- .....



# Motivaciones y retos del SHM



A. Rytter. Vibrational based inspection of civil engineering structures. PhD thesis, Aalborg University, 1993.



## Motivaciones y retos del SHM

Ser capaz de diseñar soluciones SHM para sistemas a gran escala.

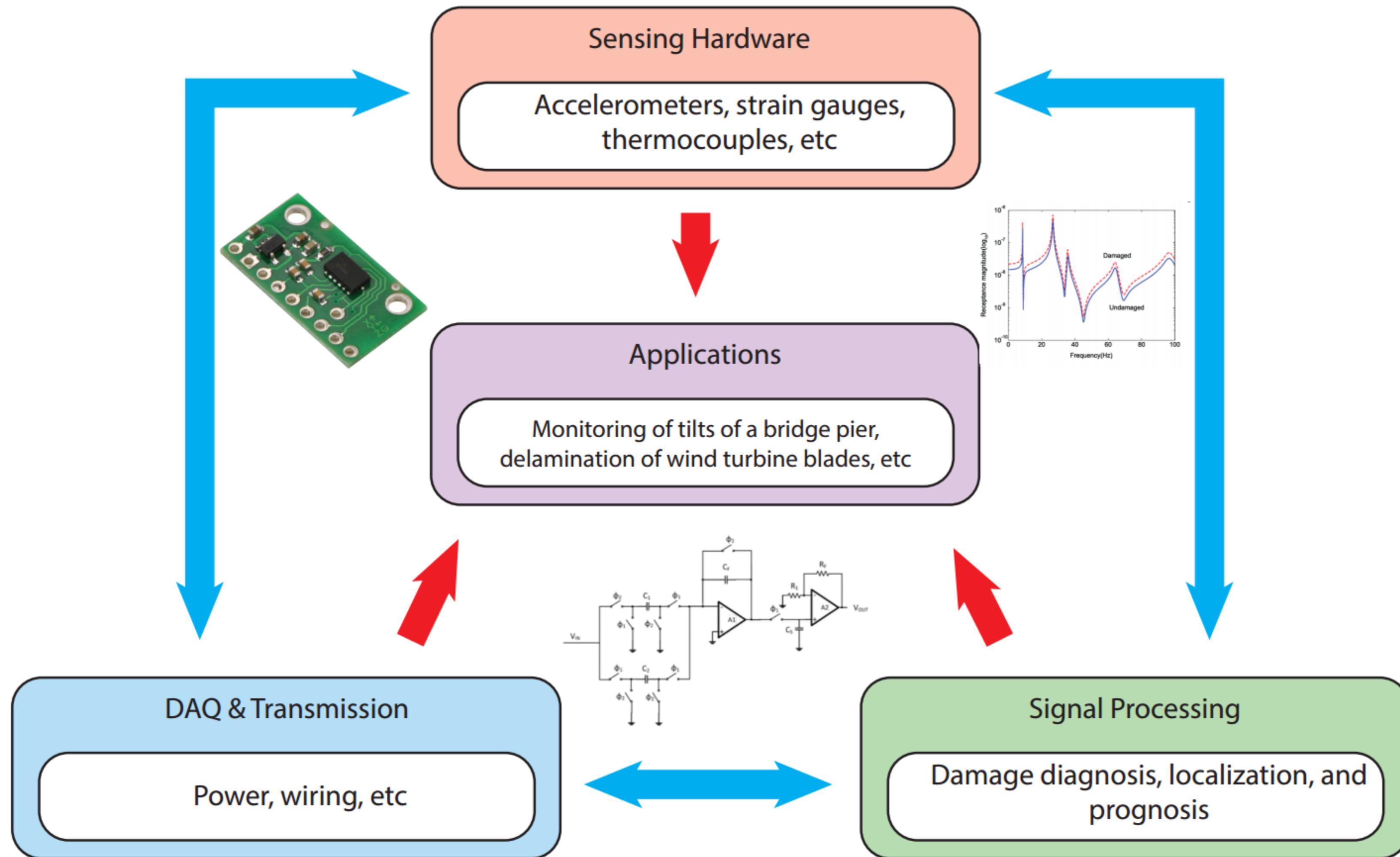
Especificamente, es necesario ampliar la comprensión de:

- Desafíos SHM para sistemas a gran escala (economía, aplicaciones, etc.).
- Transductores, adquisición de datos y técnicas de procesamiento de señales.
- Sistemas de decisión basados en mediciones.
- Aplicaciones en campo.

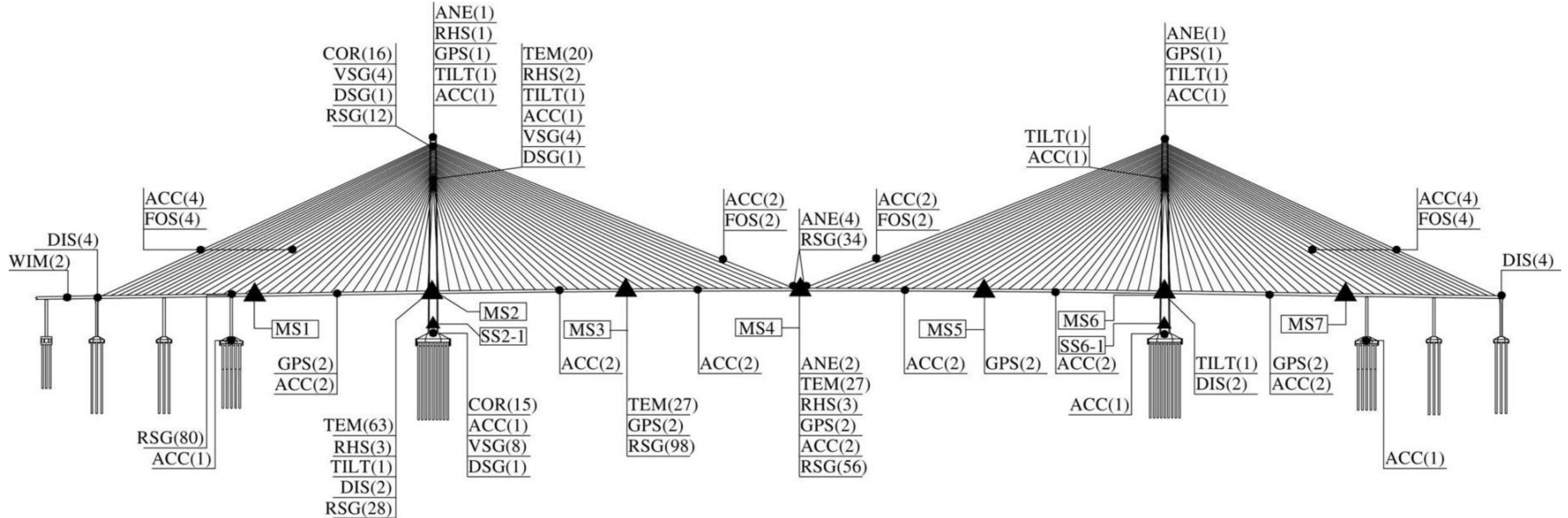


# Motivaciones y retos del SHM

## Sensor-based SHM



# Motivaciones y retos del SHM



ANE: anemometer

TEM: temperature sensor

RHS: air temperature and relative humidity sensor

WIM: weigh-in-motion system

COR: corrosion sensor

GPS: global positioning system

TILT: tiltmeter

DIS: displacement transducer

ACC: accelerometer

RSG: foiled resistance strain gauge

VSG: vibrating-wire strain gauge

DSG: dummy strain gauge

FOS: fiber optic sensor

MS: main station

SS: sub-station

Mao, J. X., Wang, H., & Li, J. (2018). Fatigue reliability assessment of a long-span cable-stayed bridge based on one-year monitoring strain data. *Journal of Bridge Engineering*, 24(1), 05018015.

### SHM Design

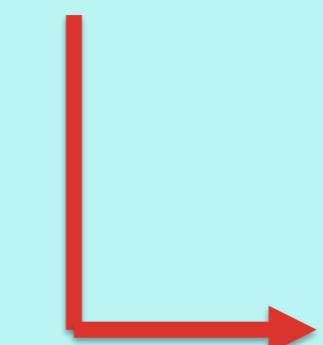
- ¿Qué quiero monitorizar?
- ¿Es útil la monitorización?
- ¿Cuánto retorno de la inversión obtendría?
- Identificar los estados que se deben monitorizar para una SHM exitosa

### Structural Design

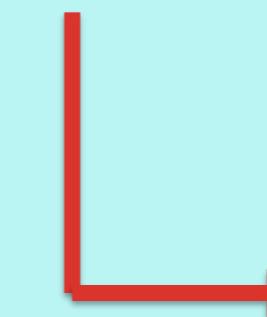
- ¿Qué quiero construir?
- ¿Es útil la estructura?
- ¿Cuánto retorno de la inversión obtendría?



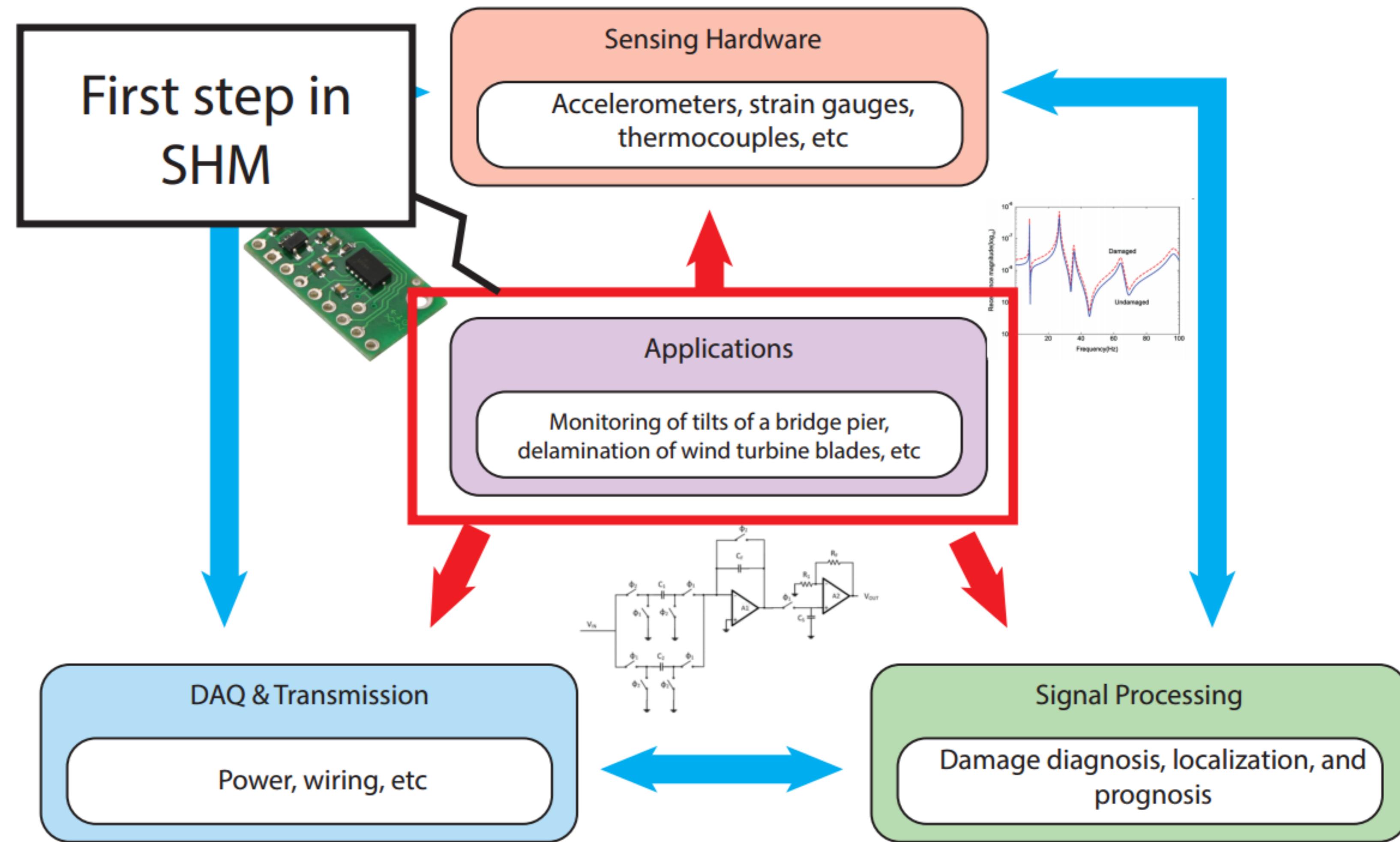
- Diseño de hardware de detección
- Electrónica de diseño
- Diseñar algoritmos de procesamiento de señales



- Monitoriza la estructura



- Diseña la estructura
- Construye la estructura



Análisis modal como técnica revolucionaria  
dentro del SHM.



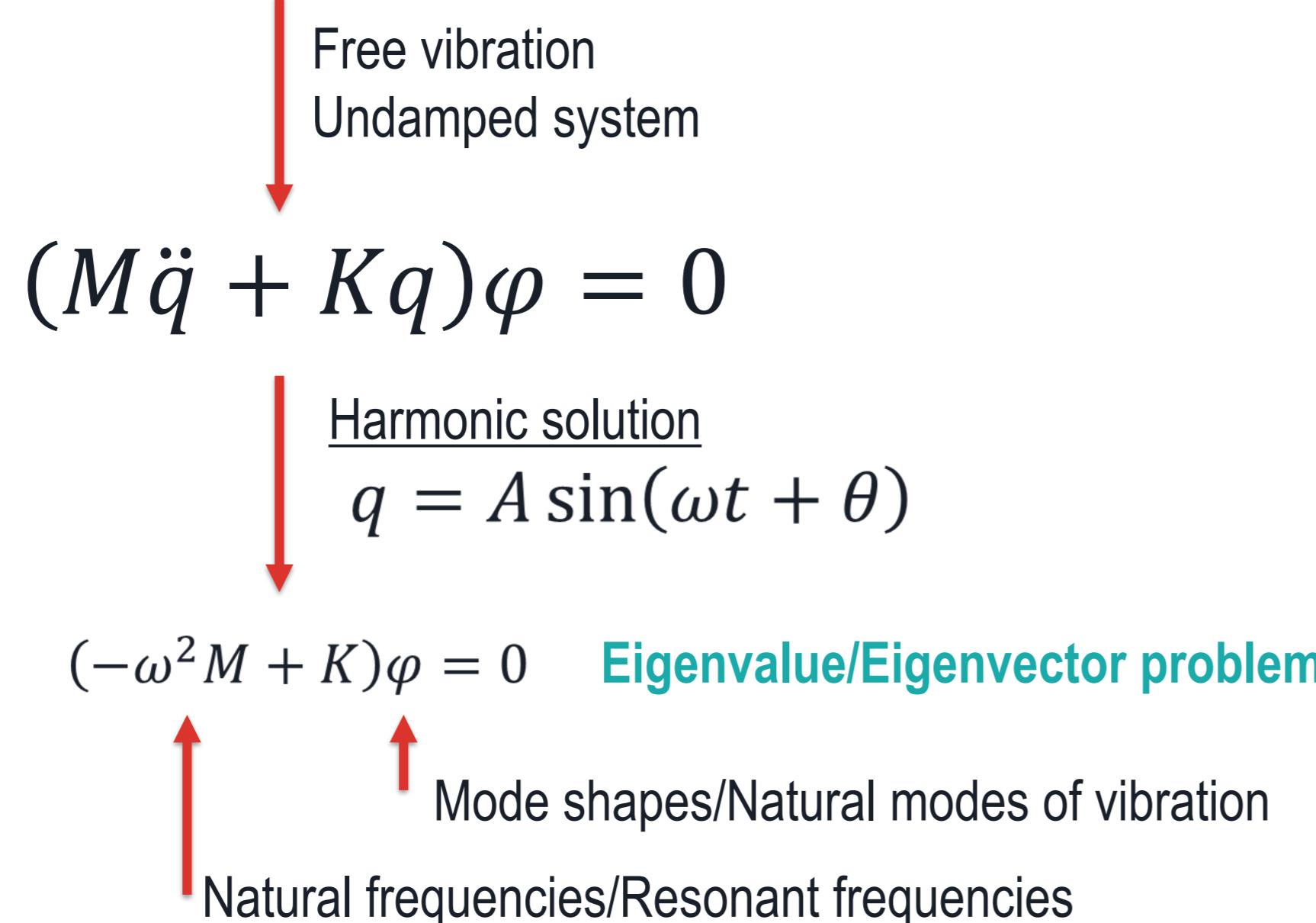
## Análisis Modal como técnica revolucionaria dentro del SHM

**El análisis modal es una técnica más dentro del marco general del SHM!**



# Análisis modal como técnica revolucionaria dentro del SHM

$$M\ddot{u} + C\dot{u} + Ku = f$$
$$u(x, t) = q(t)\varphi(x)$$



El SHM basado en vibraciones, o pruebas dinámicas, se basa en la identificación de variaciones inducidas por daños en las propiedades modales de las estructuras (es decir, **frecuencias resonantes, formas modales y propiedades de amortiguamiento**).

## - Identificación global de daños.

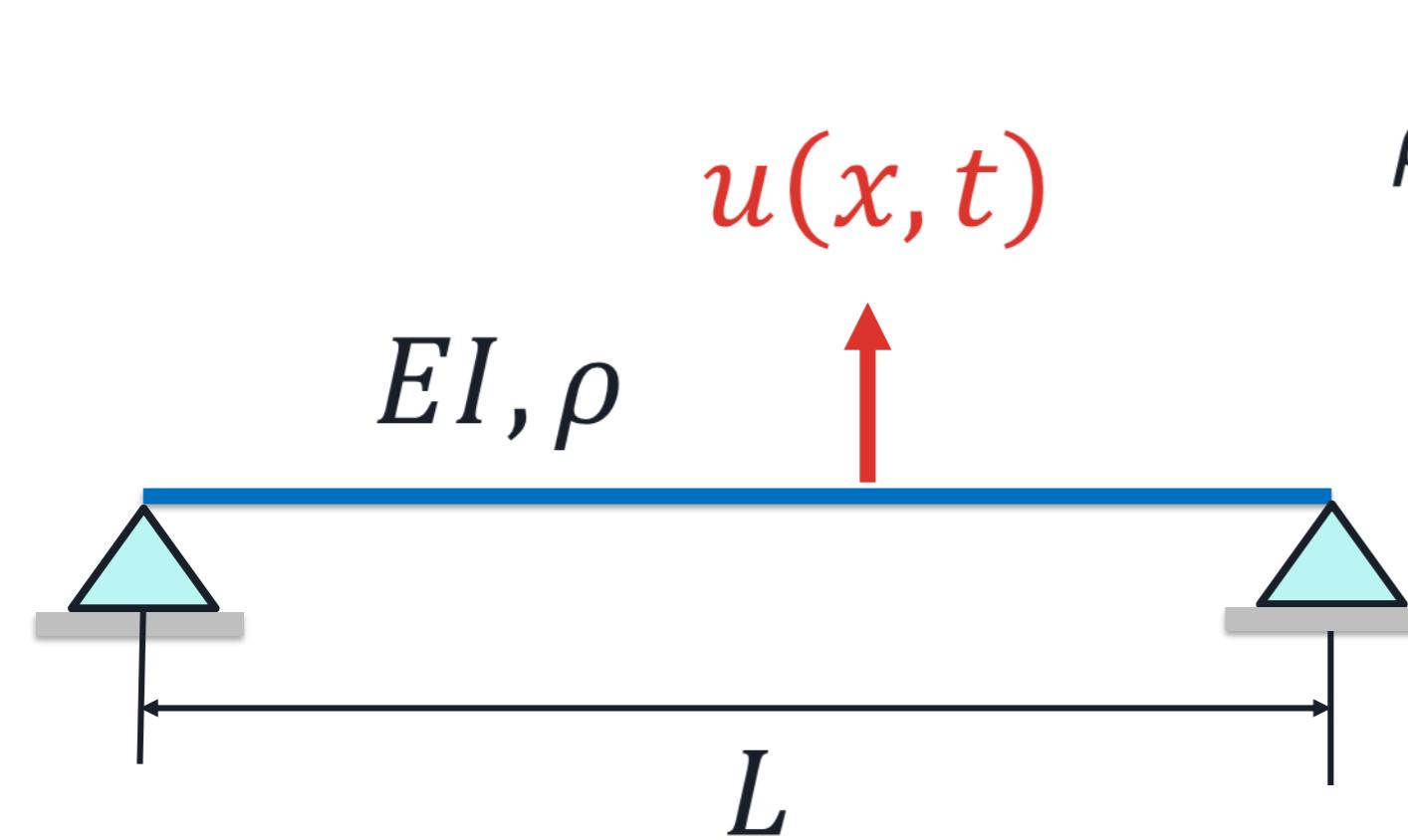
- Las patologías estructurales locales con efecto limitado sobre la rigidez general de las estructuras pueden pasar desapercibidas.
- El amortiguamiento (mecanismos de disipación de energía) es muy sensible al daño, sin embargo, su identificación depende en gran medida del nivel de excitación modal y generalmente está sujeto a altos niveles de incertidumbre.
- **La capacidad de un sistema SHM para detectar defectos localizados está directamente relacionada con su capacidad para identificar modos de vibración de alta frecuencia.**

- Hay dos tipologías principales de pruebas dinámicas:

- Utilización de excitaciones artificiales - **Análisis modal experimental (EMA)**.
- Uso de vibraciones ambientales - **Análisis modal operacional (OMA)**.



# Análisis modal como técnica revolucionaria dentro del SHM



$$\rho(x) \frac{\partial^2 u(x, t)}{\partial t^2} + \frac{\partial^2}{\partial x^2} \left[ EI \frac{\partial^2 u(x, t)}{\partial x^2} \right] = 0$$

Variable separation

$$u(x, t) = \varphi(x)y(t)$$

└ Modal displacements  
Mode shapes

+ BCs

$$\varphi(x, n) = \sin\left(\frac{n\pi x}{L}\right) \quad \text{Mode shapes}$$

$$\omega_n = n^2\pi^2 \sqrt{\frac{EI}{\rho L^4}} \quad \text{Natural angular frequency}$$

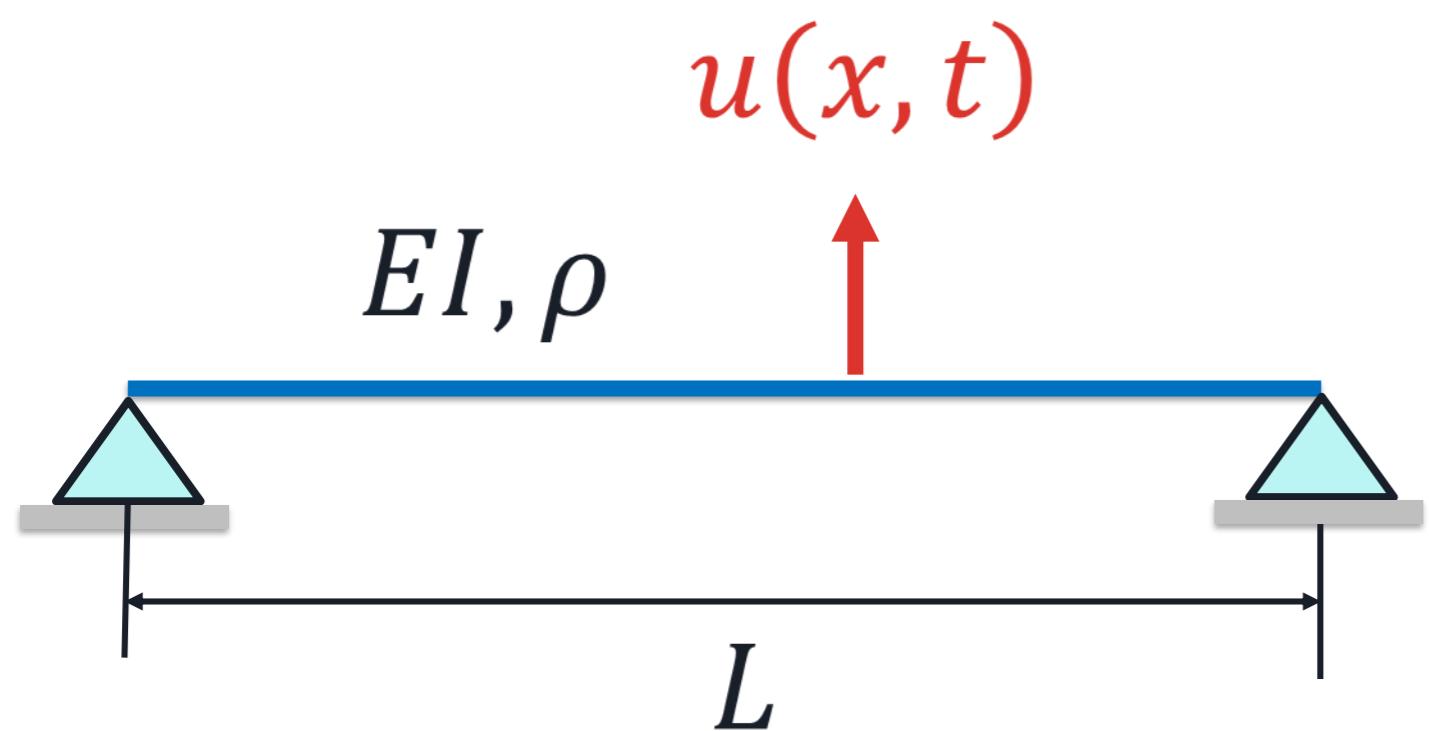
$$f_n = \frac{\omega_n}{2\pi}$$

Orthogonality Property

$$\int_0^L \varphi(x)\varphi(x)dx = 0 \quad (i \neq j), 1 \quad (i = j)$$

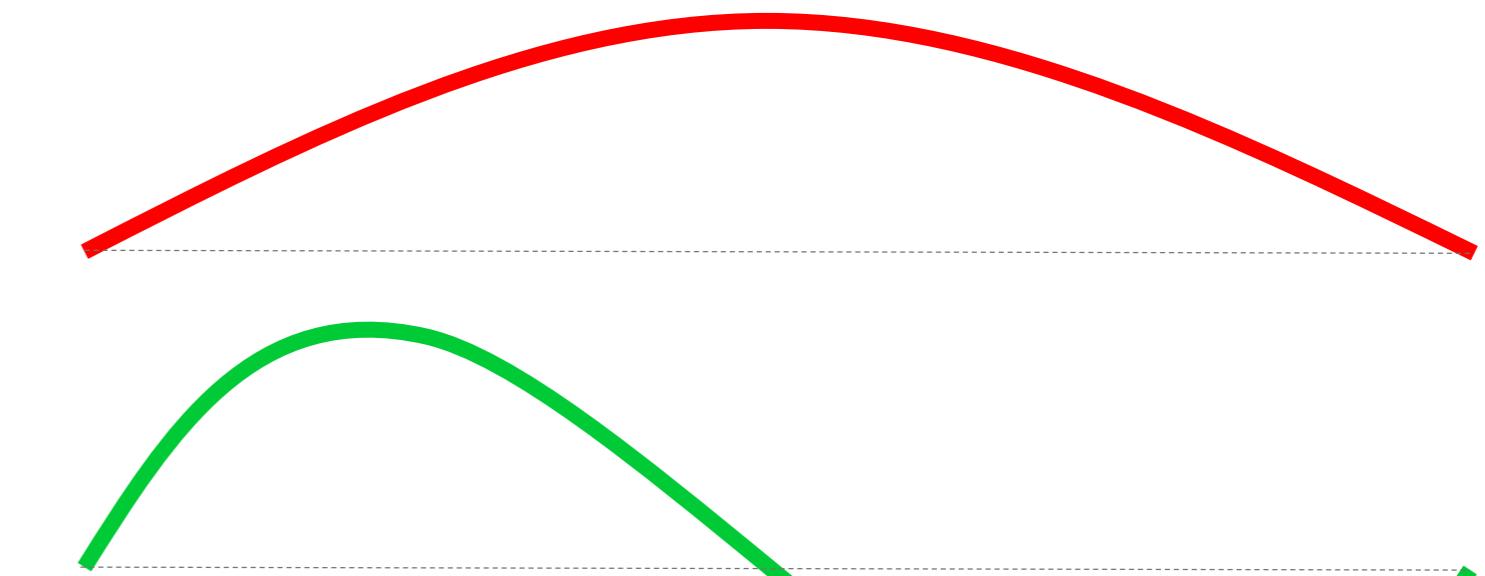
# Análisis modal como técnica revolucionaria dentro del SHM

Ejemplo:  $EI=7694081.0 \text{ kNm}^2$ ,  $L = 15 \text{ m}$ ,  $\rho = 15000 \text{ kg/m}^2$

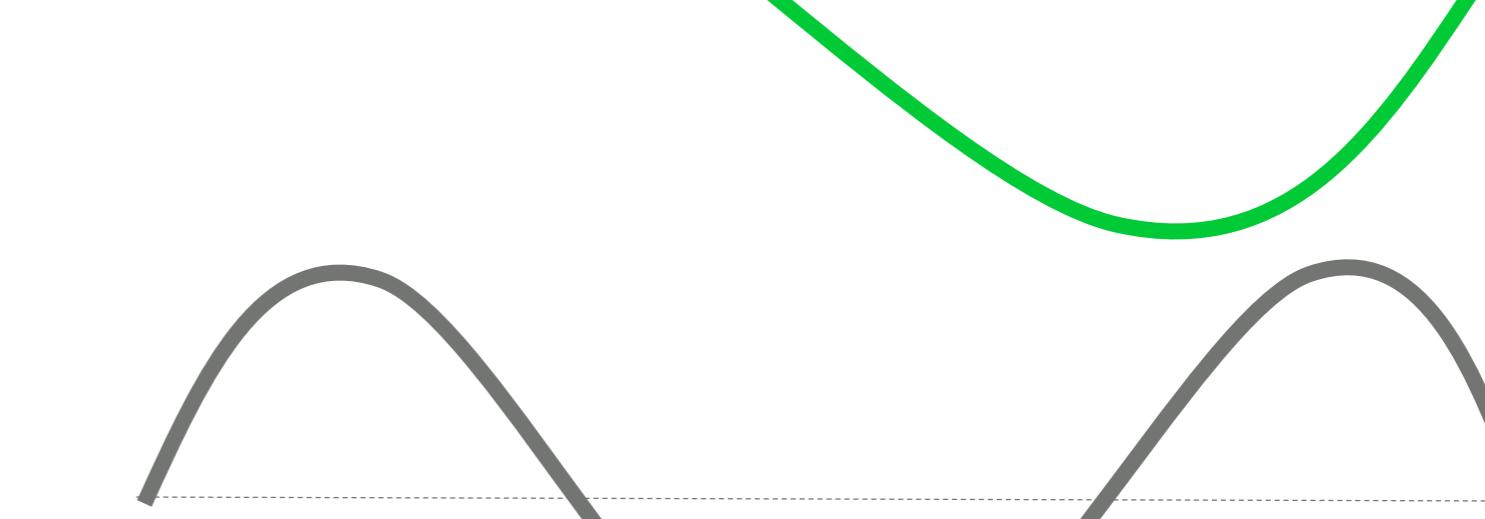


$$\varphi(x, n) = \sin\left(\frac{n\pi x}{L}\right)$$
$$f_n = \frac{\omega_n}{2\pi}$$
$$\omega_n = n^2\pi^2 \sqrt{\frac{EI}{\rho L^4}}$$

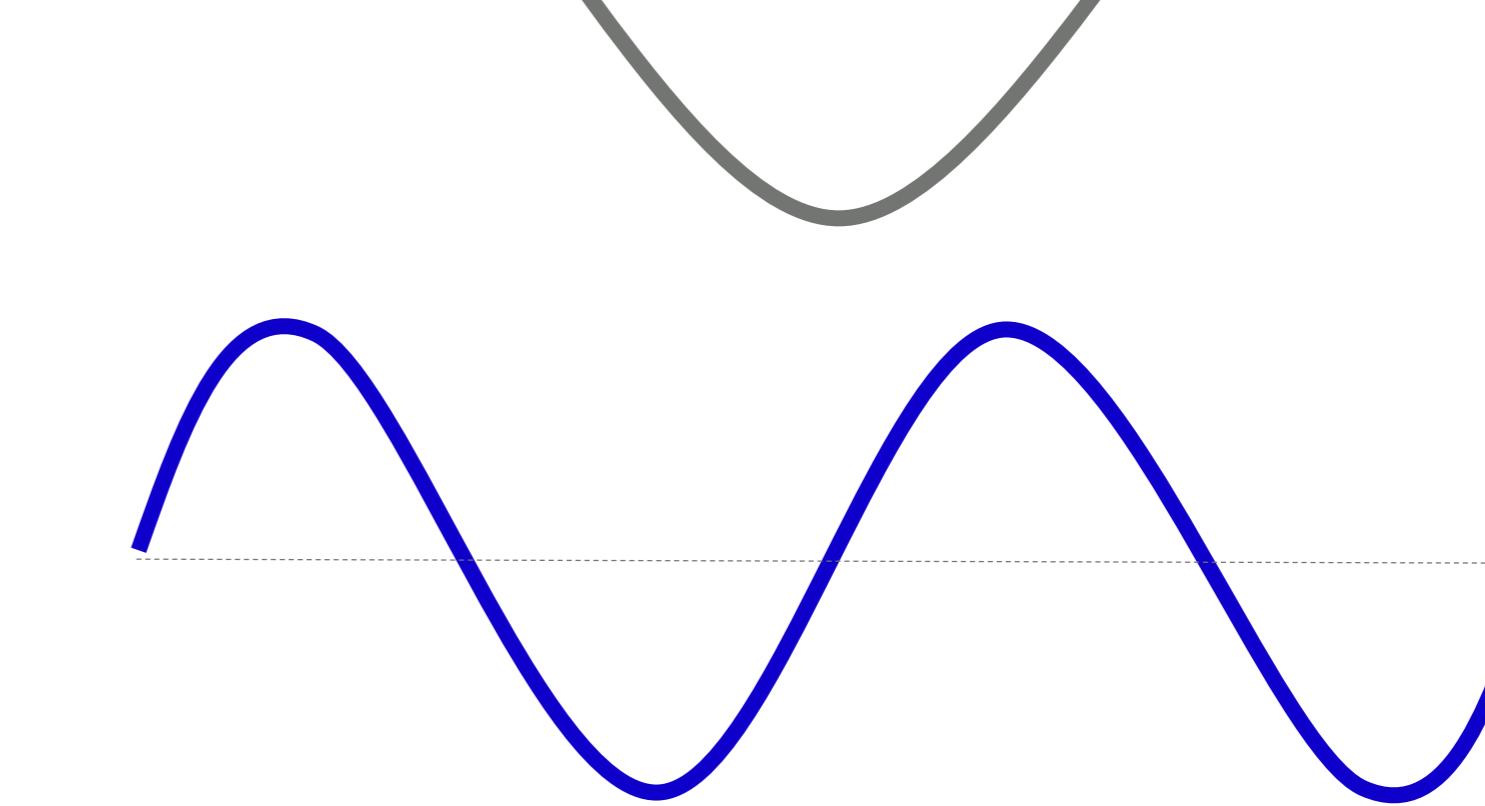
Mode 1 ->  $f=5 \text{ Hz}$



Mode 2 ->  $f=20 \text{ Hz}$

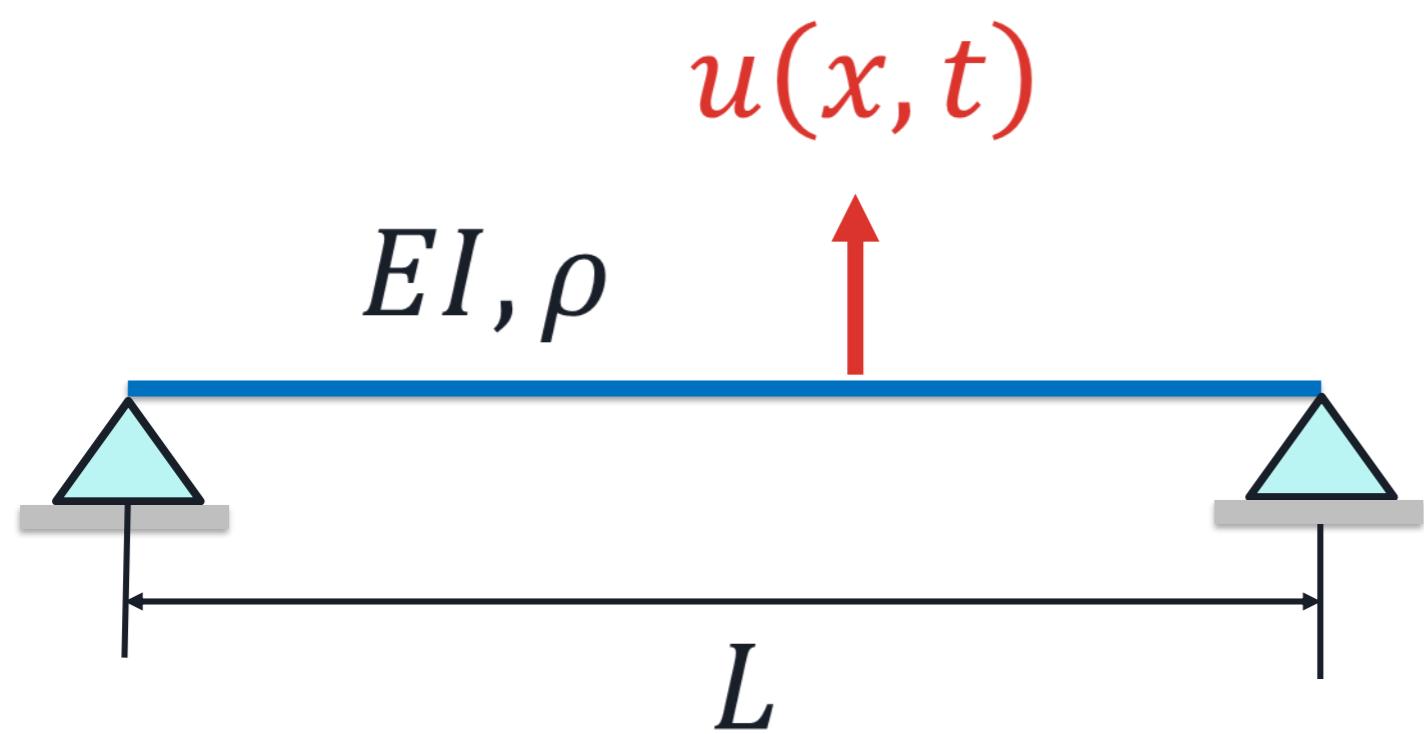


Mode 3 ->  $f=45 \text{ Hz}$



# Análisis modal como técnica revolucionaria dentro del SHM

Ejemplo:  $EI=7694081.0 \text{ kNm}^2$ ,  $L = 15 \text{ m}$ ,  $\rho = 15000 \text{ kg/m}^2$



$$\varphi(x, n) = \sin\left(\frac{n\pi x}{L}\right)$$

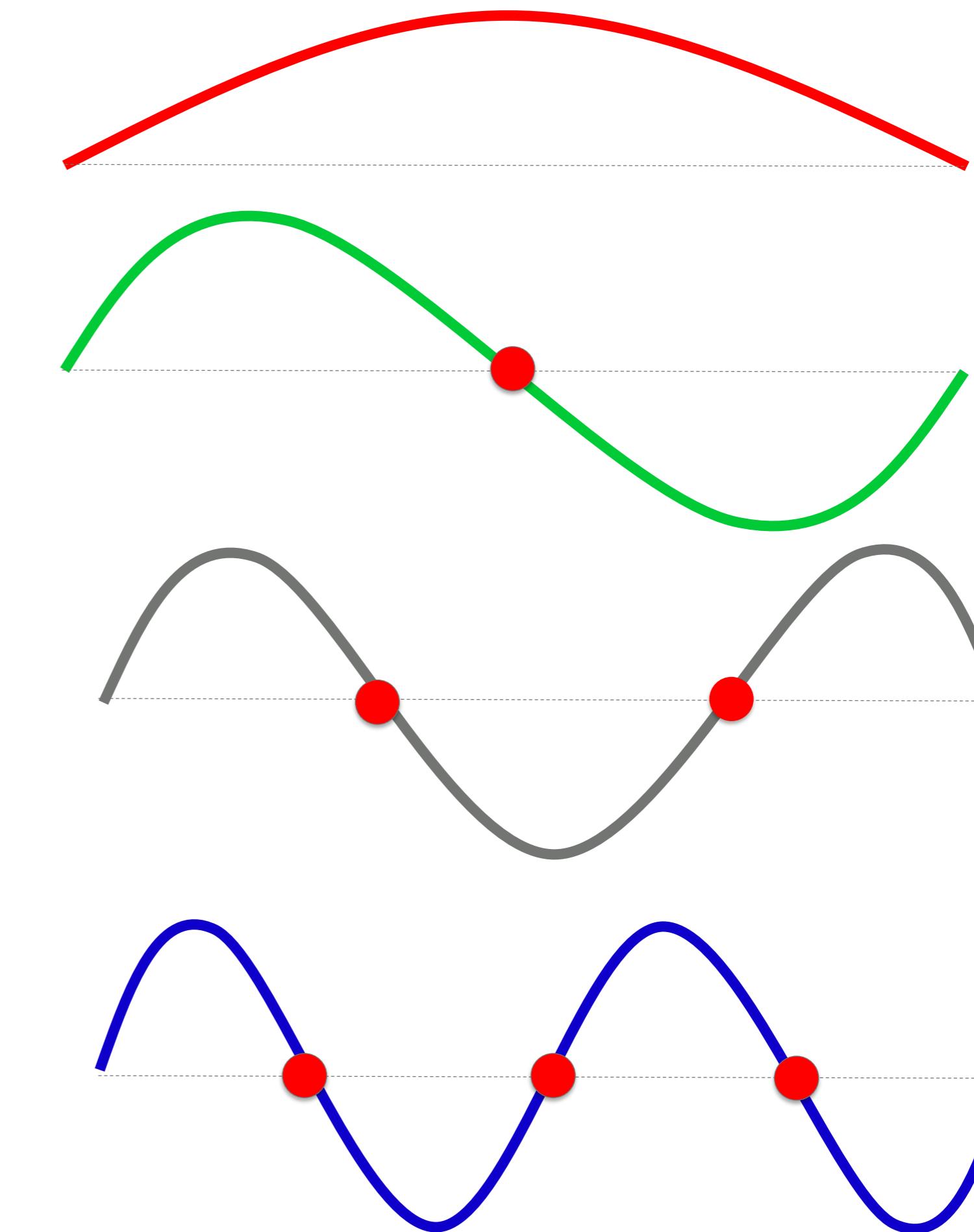
$$\omega_n = n^2\pi^2 \sqrt{\frac{EI}{\rho L^4}}$$

$$f_n = \frac{\omega_n}{2\pi}$$

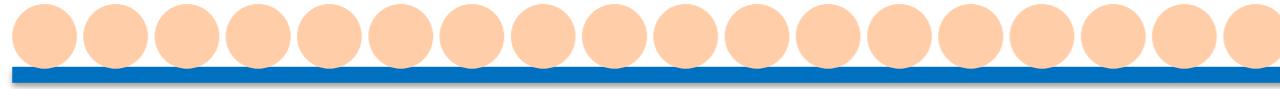
Mode 1 ->  $f=5 \text{ Hz}$

Mode 2 ->  $f=20 \text{ Hz}$

Mode 3 ->  $f=45 \text{ Hz}$

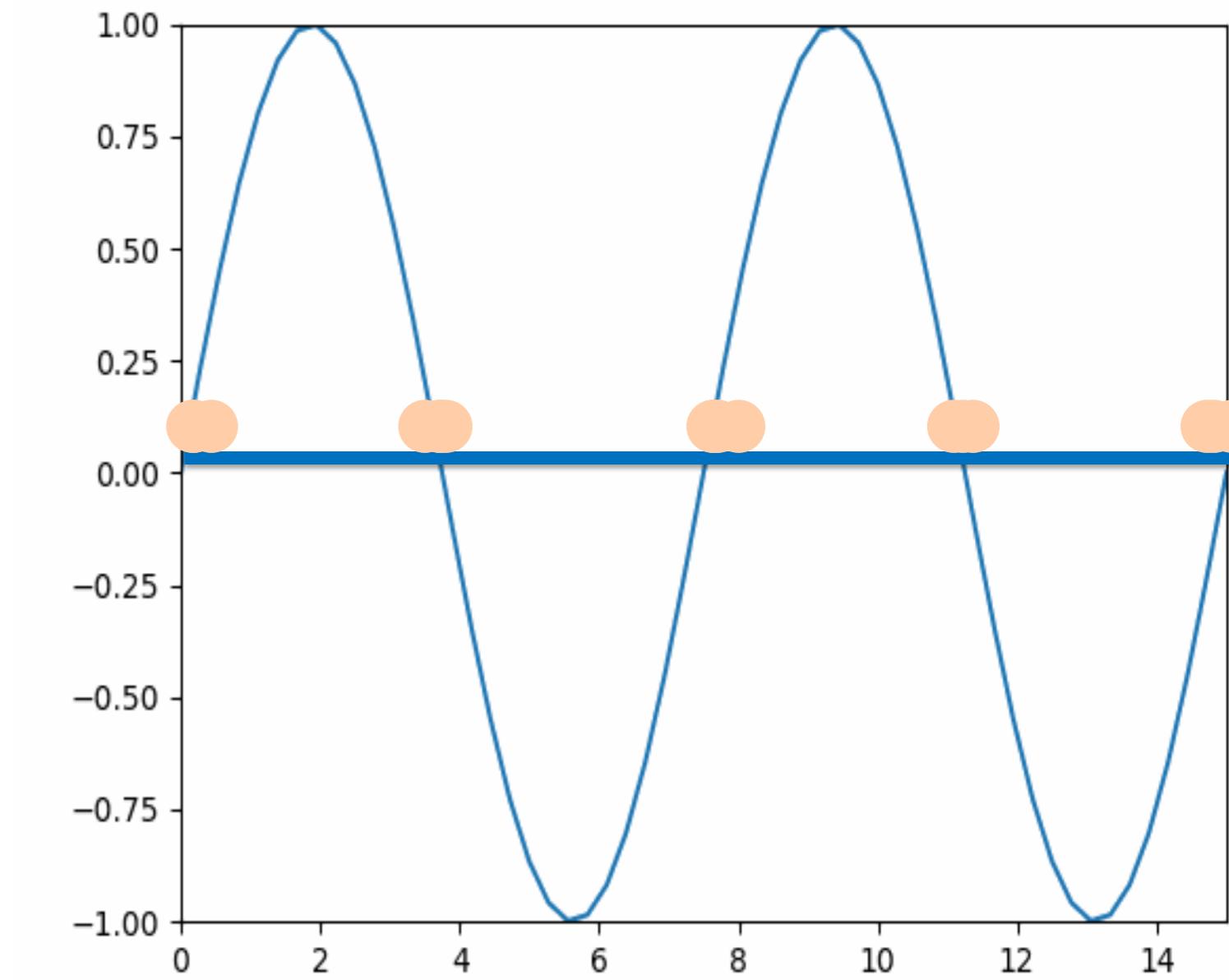
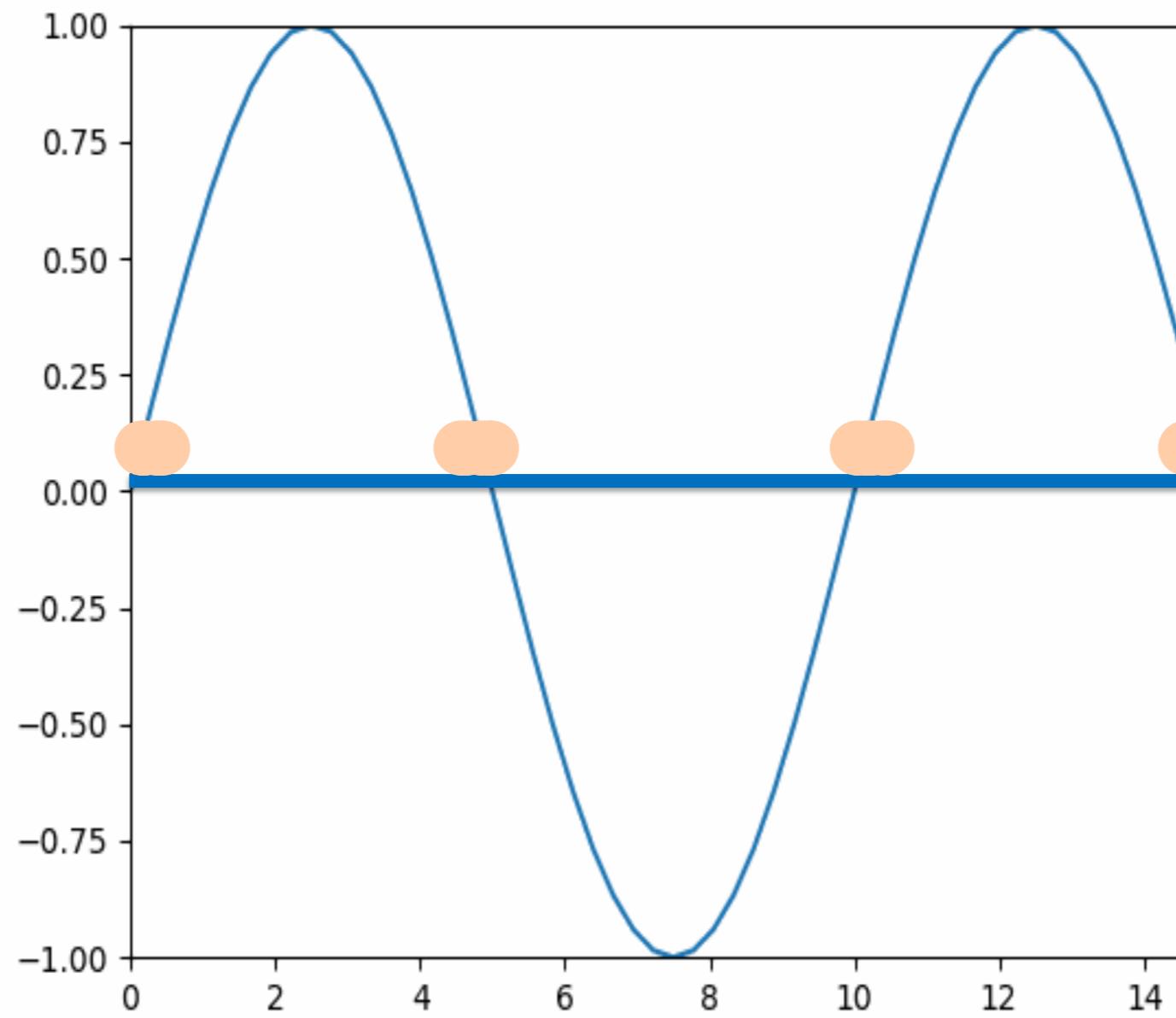
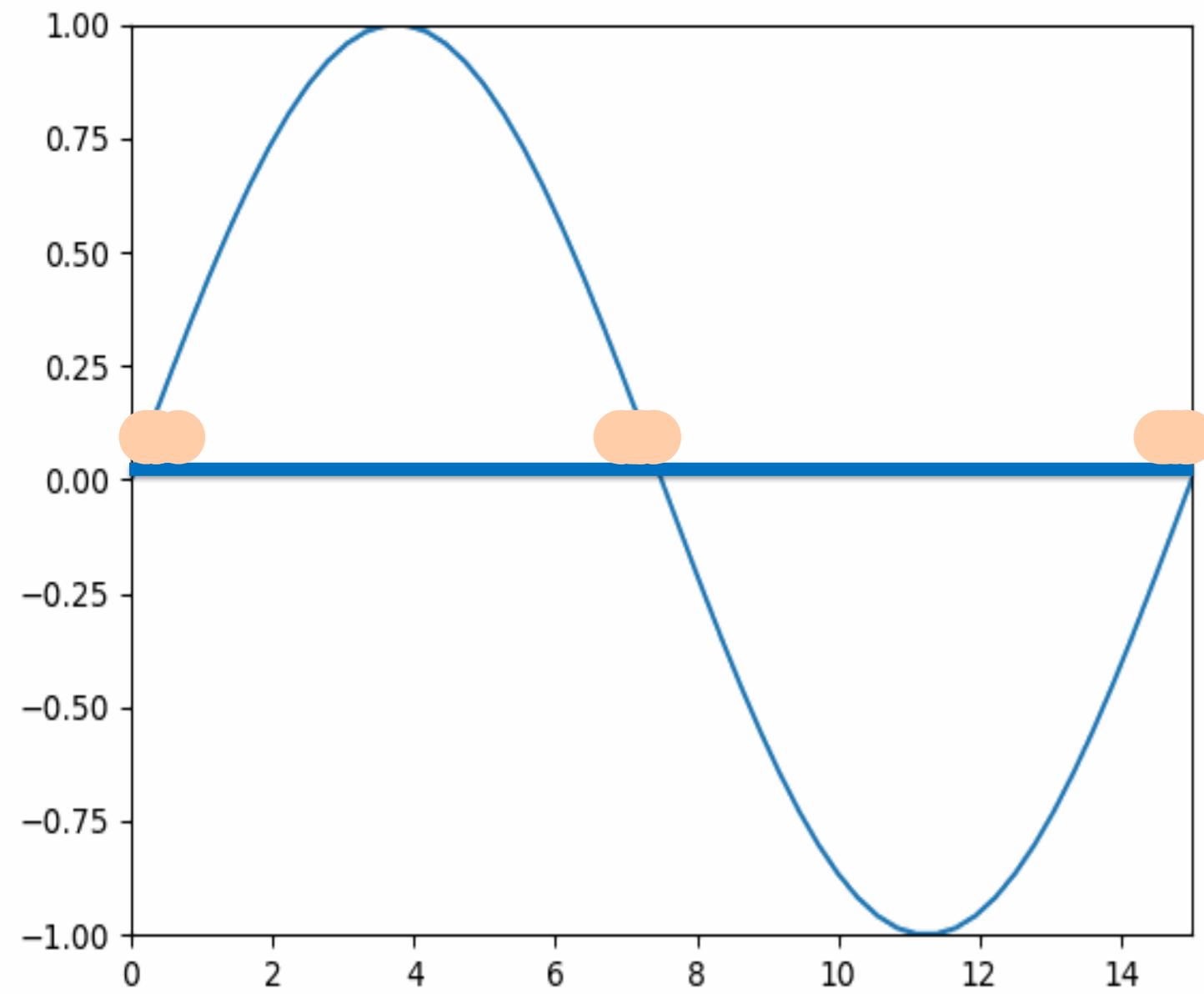
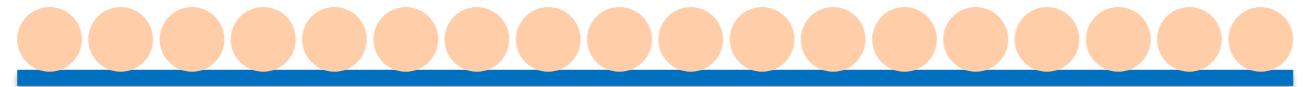


# Análisis modal como técnica revolucionaria dentro del SHM

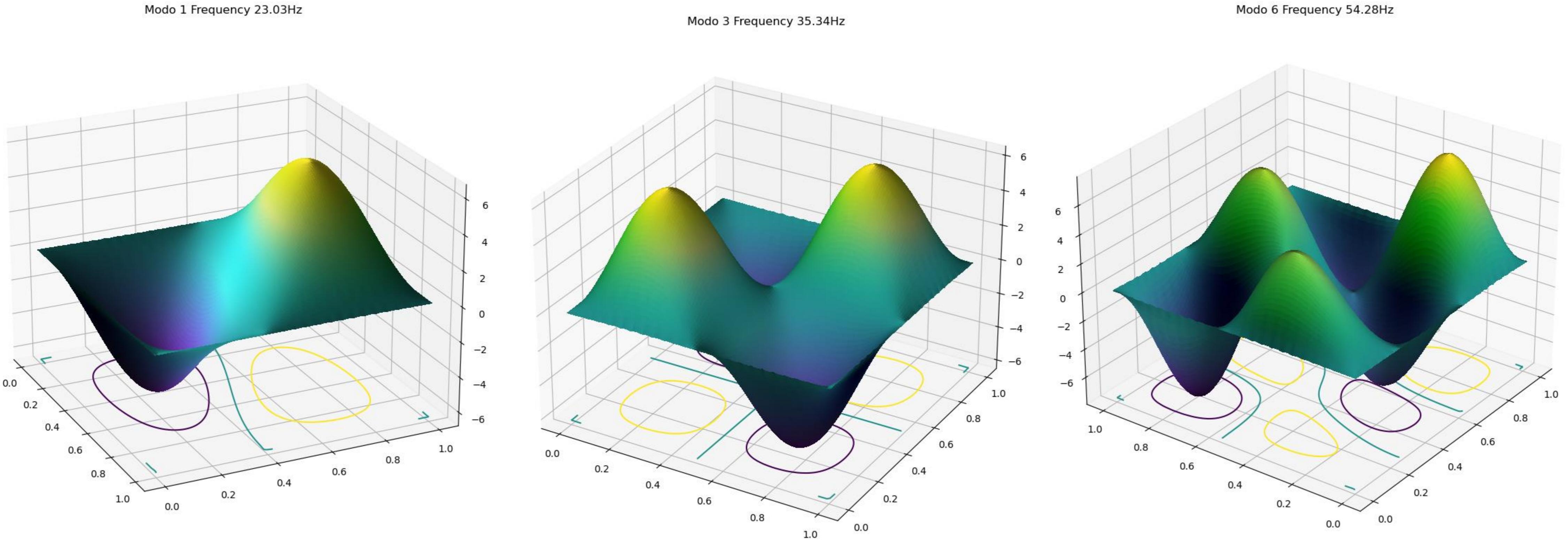


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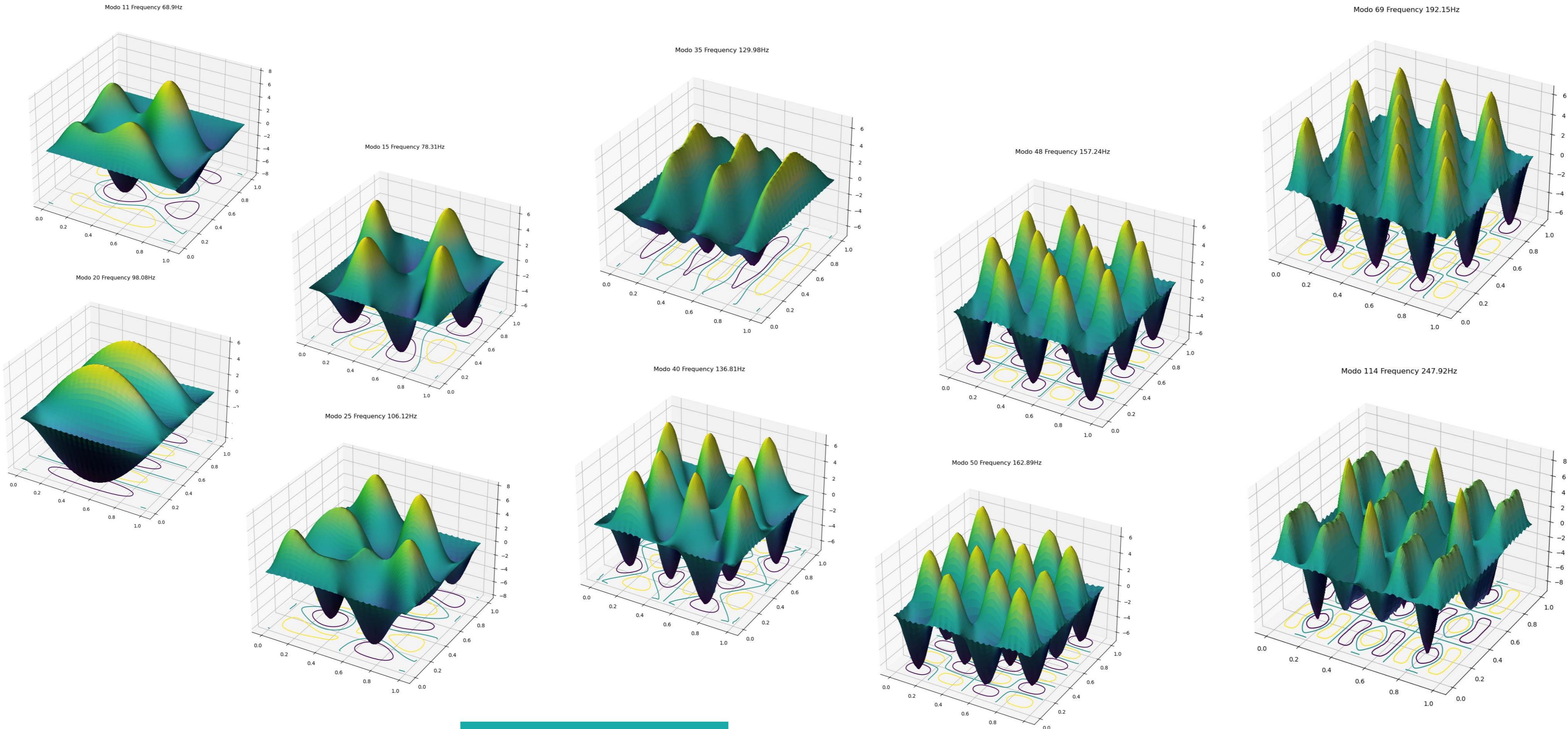
# Análisis modal como técnica revolucionaria dentro del SHM



# Análisis modal como técnica revolucionaria dentro del SHM



# Análisis modal como técnica revolucionaria dentro del SHM



Frecuencia

# Análisis modal como técnica revolucionaria dentro del SHM



<https://www.youtube.com/watch?v=wvJAGRUBF4w>



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## Análisis Modal como técnica revolucionaria dentro del SHM

Existen dos grandes variantes dentro del análisis modal:

- **Análisis Modal Experimental (EMA).** Las excitaciones de entrada son conocidas.
- **Análisis Modal Operational (OMA).** Las excitaciones de entrada son desconocidas.

