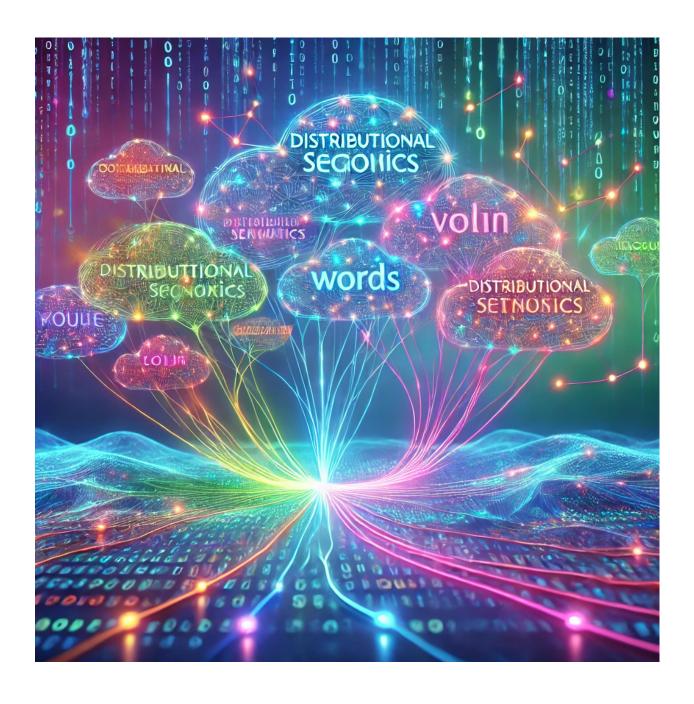
Introduction to Natural Language Processing, Assignment 2

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Contents

1	Distributional Semantics			
		Raw Co-occurrence Vectors		
		Prediction Based Word Vectors	4	
4	TOb	ic wodering		

1 Distributional Semantics

1.1 Raw Co-occurrence Vectors

Given the following raw co-occurrence counts of words with contexts jealous (c_1) and gossip (c_2) :

	c_1 (jealous)	$c_2(\text{gossip})$
w_1	2	5
w_2	3	0
w_3	4	0
w_4	0	4

1. Compute the TF-IDF Weighted Co-occurrence Matrix

Use the following formulas:

$$\operatorname{tf}(w,c) = \log\left(\frac{\operatorname{freq}(w,c)}{\max_{w'}\operatorname{freq}(w',c)} + 1\right)$$

$$\mathrm{idf}(c) = \log\left(\frac{|V|}{|\{w \in V : \mathrm{freq}(w,c) > 0\}|}\right)$$

Where |V| = 4.

TF:

- $\operatorname{tf}(w_1, c_1) = \log\left(\frac{2}{4} + 1\right) = 0.176$
- $tf(w_2, c_1) = \log(\frac{3}{4} + 1) = 0.243$
- $tf(w_3, c_1) = log(\frac{4}{4} + 1) = 0.301$
- $\operatorname{tf}(w_4, c_1) = \log\left(\frac{0}{4} + 1\right) = 0$
- $\operatorname{tf}(w_1, c_2) = \log\left(\frac{5}{5} + 1\right) = 0.301$
- $\operatorname{tf}(w_2 c_2) = \log\left(\frac{0}{5} + 1\right) = 0$
- $\operatorname{tf}(w_3, c_2) = \log\left(\frac{0}{5} + 1\right) = 0$
- $tf(w_4, c_2) = log(\frac{4}{5} + 1) = 0.255$

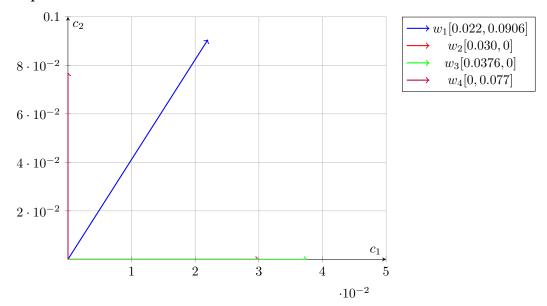
IDF:

- $idf(c_1) = log(\frac{4}{3}) = 0.125$
- $idf(c_2) = log(\frac{4}{2}) = 0.301$

TF-IDF

- $tf\text{-}idf(w_1, c_1) = 0.176 \cdot 0.125 = 0.022$
- $tf\text{-}idf(w_2, c_1) = 0.243 \cdot 0.125 = 0.030$
- $tf\text{-}idf(w_3, c_1) = 0.301 \cdot 0.125 = 0.0376$
- $tf\text{-}idf(w_4, c_1) = 0 \cdot 0.125 = 0$
- $tf\text{-}idf(w_1, c_2) = 0.301 \cdot 0.301 = 0.0906$
- $tf\text{-}idf(w_2, c_2) = 0 \cdot 0.301 = 0$
- $tf\text{-}idf(w_3, c_2) = 0 \cdot 0.301 = 0$
- $tf\text{-}idf(w_4, c_2) = 0.255 \cdot 0.301 = 0.077$

2. Represent Each Word as a TF-IDF Vector



3. Compute the Euclidean Distance Between:

$$d(x,y) = \sqrt{\sum_{i=1}^{n} (x_i - y_i)^2}$$

(a)
$$w_1$$
 and $w_2 \to d(w_1, w_2) = \sqrt{(0.022 - 0.030)^2 + (0.0906 - 0)^2} = 0.091$

(b)
$$w_2$$
 and $w_3 \to d(w_1, w_2) = \sqrt{(0.0307 - 0.0376)^2 + (0 - 0)^2} = 0.0076$

4. Discussion

Based on the Euclidean distances computed, evaluate whether Euclidean distance is an appropriate measure for capturing the relationships between the words.

Answer: Is not a valid option because the Euclidean Distance is affected by vectors length.

1.2 Prediction Based Word Vectors

• Why does Word2Vec use separate input vectors (u_w) and output vectors (v_w) for each word, and how does this benefit the model's performance?

Answer: Two random vectors (of dimension $d \ll |V|$) assigned to each word:

- $-u_w \rightarrow$ the "input" vector of the word w, when it is used to predict another word.
- $-v_w \rightarrow$ the "output" vector of the word w, when it is the one being predicted.
- What are the primary differences between the Skip-Gram and Continuous Bag-of-Words (CBOW) models in Word2Vec, and in what scenarios might one outperform the other?

Answer:

- Skip-Gram predicts each context words from the center word. More efficient with less amounts
 of data.
- CBOW predicts the center word from the whole context. Faster, more efficient with big amounts
 of data
- How does negative sampling improve the efficiency of training Word2Vec models compared to using the full softmax function?

Answer: Denominator in softmax sums over words in V_N , instead of the whole $V \to N << |V|$

• How does the choice of window size in Word2Vec affect the type of semantic relationships the model captures?

Answer:

- Small windows \rightarrow more sintactic relationships catched
- Big windows \rightarrow more semantic relationships catched
- What strategies canWord2Vec employ to handle out-of-vocabulary (OOV) words, and what are the implications of these strategies?

Answer: Tokenization: enrich word embeddings with subword information (low frequency "token" and "ization" more frequent). Learn subwords vectors (char n-grams) along with word-level embeddings.

2 Topic Modeling

Consider a simple corpus with the following characteristics:

- Vocabulary (V): {apple, banana, cherry}
- Number of Topics (K): 2
- Number of Documents (M): 2

The initial topic distributions over words (ϕ_k) and document distributions over topics (θ_m) are randomly initialized as follows:

$$\phi_1 = \begin{bmatrix} \frac{1}{3} \frac{1}{3} \frac{1}{3} \end{bmatrix}, \quad \phi_2 = \begin{bmatrix} \frac{1}{3} \frac{1}{3} \frac{1}{3} \end{bmatrix}$$

$$\theta_1 = \begin{bmatrix} \frac{1}{2} \frac{1}{2} \end{bmatrix}, \quad \theta_2 = \begin{bmatrix} \frac{1}{2} \frac{1}{2} \end{bmatrix}$$

Documents

• Document 1: apple, banana

• Document 2: banana, cherry

Steps to Solve

1. Compute Topic Assignment Probabilities

For each word in each document, compute the probability of assigning it to each topic using the current ϕ and θ values. Specifically, calculate:

$$P(z_{mn} = k) \propto \phi_k[w] \times \theta_m[k]$$

for each word w in document m.

2. Assign New Topics

Based on the probabilities computed earlier, assign a new topic to each word in each document. Assume you sample deterministically by choosing the topic with the higher probability.

3. Update Distributions

Update the ϕ_k and θ_m distributions based on the new topic assignments. Compute the new probabilities:

$$P(w|k) = \frac{C(w,k)}{\sum_{w'} C(w',k)}$$

$$P(k|d) = \frac{C(k,d)}{\sum_{k'} C(k',d)}$$

where C(w, k) is the count of word w assigned to topic k across all documents, and C(k, d) is the count of topic k in document d.