

More Algorithms

Course: CPSC 1150
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Example 2

- Write an algorithm that given a value for the height of triangle (eg. H), it draws a triangle with the given height H like following:

H

5

```
*
**
***
****
*****
```

```
      *
     ***
    *****
   ********
  *********
 *****
```

```
*
**
* *
*  *
*   *
*****
```

```
      *
     * *
    *  *
   *   *
  *    *
 *****
```

8

```
*
**
***
****
*****
*****
*****
*****
*****
*****
```

```
      *
     ***
    *****
   ********
  **********
 *****
  **********
 *****
  **********
 *****
  **********
 *****
```

```
*
**
* *
*  *
*   *
*    *
*     *
*      *
*       *
*****
```

```
      *
     * *
    *  *
   *   *
  *    *
 *     *
*      *
*       *
*        *
*****
```

Exercise A

H

5

```
*  
**  
***  
****  
*****
```

START

get H from user input

$n \leftarrow 1$

Repeat while $n \leq H$:

print n of '*' in a new line

$n \leftarrow n + 1$

8

```
*  
**  
***  
****  
*****  
*****  
*****  
*****  
*****
```

END

Exercise B

H
5

```
  *
 ***
*****
*****
*****
```

START

Input H from user input
line $\leftarrow 1$

Repeat while line $\leq H$:

print (H-line) spaces in a new line

n $\leftarrow 2 \cdot \text{line} - 1$

print n of '*' in the same line

line $\leftarrow \text{line} + 1$

8

```
  *
 ***
*****
*****
*****
*****
*****
*****
*****
```

END

Exercise C

H
5 START

```
*
**
* *
*  *
*****
```

get H from user input

print * in a new line

$n \leftarrow 2$

8

```
*
**
* *
*  *
*   *
*    *
*     *
*      *
*****
```

Repeat while $n < H$:

 print '*' in a new line

 print $n-2$ spaces in the same line

 print '*' in the same line

$n \leftarrow n + 1$

print n of '*' in the new line

END

Exercise D

H

5

```
      *
     * *
    * * *
   * * * *
  * * * * *
```

8

```
      *
     * *
    * * *
   * * * *
  * * * * *
 * * * * * *
* * * * * * *
```

START

read H from user input

line \leftarrow 1

space \leftarrow H – line

print space of ' ' in a new line

print '*' in the same line

line \leftarrow 2

Repeat while line < H:

 space \leftarrow H – line

 print space of ' ' in a new line

 print '*' in the same line

 space \leftarrow (2*line – 1) – 2

 print space of ' ' in the same line

 print '*' in the same line

 line \leftarrow line + 1

print (2*line – 1) of '*' in a new line

END

Example 3

Algorithm: Find average of a class for an exam.

(Define terms)

Let numOfStudents be the number of the students in the class.

Let grade be the grade of each students.

START

$numOfStudents \leftarrow 0$

$total \leftarrow 0$

Repeat for all students

 read *grade* of the student.

$total \leftarrow total + grade$

 Increment *numOfStudents* by 1

$average \leftarrow total / numOfStudents$

print average

END

Example 4

Algorithm: Find number of the students passed or failed in a class

(Define terms)

Let *passed* be the number of the students passed.

Let *failed* be the number of the students failed.

Let *grade* be the grade of each students in the exam.

START

passed \leftarrow 0

failed \leftarrow 0

Repeat for all students

 read *grade* of the student.

 If *grade* \geq 50 Then

passed \leftarrow *passed*+1

 Otherwise

failed \leftarrow *failed*+1

print *passed* and *failed*

END

Working on Digits of a Number

Write an algorithm that given an integer number, it finds the sum of all its digits. For example, if the number is 3056, then the algorithm prints 14.

- To separate the last digits of a number from the rest, use remainder (%) by 10
 - $3056 \% 10 \rightarrow 6$
- To get the rest of digits use integer divide (//) by 10
 - $3056 // 10 \rightarrow 305$
- **Note:** finding integer division is done implicitly or explicitly in different programming languages. But use // to show integer division in the algorithms.

Similar Examples

- Write an algorithm that given a number, it prints true if the sum of its odd digits equals to its even digits. Otherwise it prints false.

For example, given 12045 it prints true, but given 3127 prints false.

Similar Examples

- Write an algorithm that gets a number and it produces another number with reverse order of the digits in the original number. The leading zeros are ignored.

Original Number	The Result
12365	56321
7601	1067
980	89
370000	73

Example 5 - Factorial

The factorial of a number \mathbf{x} , $\mathbf{x}!$ is the product of all integers from 1 up to and including \mathbf{x}

- e.g. $10! = 10(9)(8)(7)\dots(3)(2)(1) = ?$

$$4! = 4(3)(2)(1) = 24$$

- Write an algorithm to compute $\mathbf{x}!$ (use flowchart and pseudo-code to show your algorithm)

Pseudo code for Factorial

Algorithm: Find $n!$ (Factorial of n)

(Define terms)

Let n be the number input by user

Let $factorial_n$ be the factorial of n

START

1. Input n
2. $factorial_n \leftarrow 1$
3. Repeat while $n > 0$
 - 3.1 $factorial_n \leftarrow factorial_n * n$
 - 3.2 $n \leftarrow n - 1$
4. print $factorial_n$

END

Test using Trace Table

n	$factorial_n$	Output
5	1	

Example 6 - Fibonacci

The Fibonacci sequence is the sequence of integers such that every number in the sequence is the sum of the previous two numbers in the sequence.

- e.g. 1, 1, 2, 3, 5, 8, 13, 21, ...
- Write an algorithm to display the first X values of the Fibonacci sequence. (use flowchart and pseudo-code to show your algorithm)

Pseudo code for Fibonacci

Algorithm: Print first x Fibonacci numbers

(Define terms)

0.1 Let x be the number input defined by user.

Test using Trace Table

START

1. Input x

2. $num1 \leftarrow 0$

3. $num2 \leftarrow 1$

4. $newNum \leftarrow 1$

5. $counter \leftarrow 0$

6. Print $newNum$,

7. Repeat while $x \geq counter$

7.1 $newNum \leftarrow num1 + num2$

7.2 Print $newNum$,

7.3 $num1 \leftarrow num2$

7.4 $num2 \leftarrow newNum$

7.5 $counter \leftarrow counter + 1$

END

x	num1	num2	newNum	counter	output
5					

Is this algorithm Correct?