

On the top of the screen, you can use "View Options" / "Assistant" to make annotation.

I will answer your general questions at the beginning and then discuss some problems together.

Please feel free to ask any questions. You are encouraged to open your mic and camera to get to know each other.

The notes can be downloaded at <https://www.gutenberg.org/files/101010/101010-h/101010-h.pdf>

SCHOOL

$$E = \frac{1}{2} \epsilon_0 \frac{d^2 \phi}{dx^2} + \frac{1}{2} \epsilon_0 \frac{d^2 \psi}{dx^2}$$

$$\epsilon = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

the choice of ϵ depends on N .

RC circuit

- \square $R \Rightarrow$ resistor
- $\text{---} \text{---}$ $C \Rightarrow$ capacitor
- $\text{---} \text{---}$ $L \Rightarrow$ inductor
- $\text{---} \text{---}$ $V \Rightarrow$ voltage source

AC: alternating current

DC: direct current

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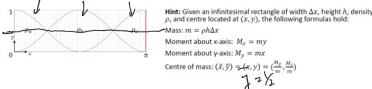
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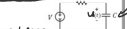
Module B1: Riemann Sums and Applications of Integration

Suppose we have a Werther's Original which has a top-down shape given by the three regions bounded by $x = 0$, $x = \pi$, $y = \sin^2 x$ and $y = \cos^2 x$ and has densities ρ_1, ρ_2, ρ_3 (see figure below). At which point (\bar{x}, \bar{y}) should you balance this candy such that it does not tip over (i.e., into/out of the page)?



Module C1: Introduction to ODEs

The circuit below contains a battery with constant voltage $V = 40$ V, a resistor with resistance $R = 10$ Ω , and a capacitor with capacitance $C = 0.01$ F. The voltage $u(t)$ of the capacitor at time t is given by the ODE: $RC \frac{du}{dt} + u = V$.



- How many initial values must we know in order to solve $\text{fohd}(t)$?
- Find the value $u(t)$ as $t \rightarrow \infty$.
- Verify that $u(t) = V + (V_0 - V)e^{-\frac{t}{RC}}$ for some constant V_0 is a solution to the ODE. What is the initial value $u(0)$ in terms of the variables in this solution?

R, C are constants, u is the potential of C .

$$RC \frac{du}{dt} + u = V$$

$$RC u' = V - u$$

$$u' = \frac{V - u}{RC}$$

$$e^{\frac{t}{RC}} u' + \frac{1}{RC} e^{\frac{t}{RC}} u = \frac{1}{RC} e^{\frac{t}{RC}} V$$

$$(e^{\frac{t}{RC}} u)' = \frac{V}{RC} e^{\frac{t}{RC}}$$

$$\text{let } k = V - u(0)$$

$$\text{ODE} \Rightarrow -RC \frac{dk}{dt} = k$$

$$\frac{dk}{dt} = -\frac{1}{RC} k$$

$$\Rightarrow k = C e^{-\frac{t}{RC}}$$

$$\Rightarrow u(t) = V - C e^{-\frac{t}{RC}}$$

IVP

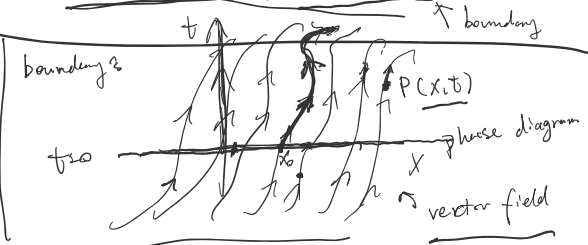
initial value problem

$\rightarrow q$

$\rightarrow t \rightarrow \infty$

Given a system, parameter x .

$$\Rightarrow x' = f(x, t), \quad x(t_0) = x_0$$

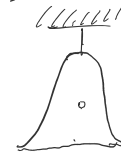


$$\frac{\int x \rho(x, y) dx dy}{\int \rho(x, y) dx dy} = \bar{x}$$

$$dm(x, y) = \rho(x, y) dx dy$$

$$\rho(x, y) \text{ has density } \rho(x, y)$$

Q2. $q \in t \rightarrow \infty$. $u \rightarrow V$
charging the capacitor



bell pitch = 640 Hz. A4

Now there is a small crack on the bell, is the pitch $\uparrow, \downarrow, \rightarrow$?

IVP, bdy.

Dirichlet Bdy \rightarrow Neumann Bdy.

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