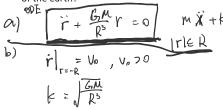
You are designing a gravity train that will travel along a diametric path through the centre of the earth. Assume the mass and radius of earth are M and R, respectively. The force acting on the train with mass m at position r from the centre of the earth is given where G is the gravitational constant. $\mathcal{F} = \frac{GM_{in}}{r^2}$

- Find a differential equation for the position of the train with respect to the centre of a) earth.
- Assume the train starts at the surface of the earth with downwards speed v_0 . Determine the position and velocity of the train as functions of time.
- How far can the gravity train reach from the centre of the earth? What is it's maximum speed?
- Assume the gravity train starts at rest. How long will it take to reach the other side





$$\frac{\Gamma(k)^{2} - R \cos(kt) + \frac{V_{0}}{k} \sin(kt)}{\pi \left(\frac{V_{0}}{k} \right)^{2} \sin(kt) + \tan^{2}\frac{V_{0}}{\rho k}}$$

According to Einstein's theory of special relativity, the kinetic energy of an $\frac{mc^2}{mc^2}$ $\frac{mc}{\sqrt{1-\frac{v^2}{c^2}}} - mc^2 \text{ where } c \text{ is}$ object with rest mass m and speed v is given by $K = \frac{1}{2} \left(\frac{1}{2} \right)^{n}$

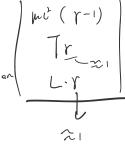
the speed of light.

- a) Find a second order Maclaurin polynomial for K as a function of $\frac{v^2}{2}$ for the kinetic energy.
- Derive the classical form of kinetic energy by only considering first order
- Assume $v \leq v_1$ for some v_1 . Find an upper bound for the error in the second order Maclaurin polynomial. c)
- Graph the first prdpr, second order, and exact forms of K.

$$V = \frac{mc^2}{\sqrt{1-v^2/c^2}} - mc^2$$
when $V/c = 1$

$$\begin{array}{lll}
\text{Fe} & \text{Fin} & \text{F$$

Grauss's law



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$$\gamma(\sigma) = \frac{1}{\sqrt{1-\sigma}} = \frac{2\sigma}{\sqrt{\frac{\gamma(\sigma)}{N!}}} \cdot \sigma^{N}$$

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