

Appendix A: Bits-per-ATP and Negentropy Conversion

1. From Thermodynamics to Information

The free energy of ATP hydrolysis represents the work potential per molecule. At 37 °C (310 K), the energy cost of erasing one bit of information—the Landauer limit—is:

$$E_{\text{bit}} = kT \ln 2 = (1.38 \times 10^{-23})(310)(0.693) = 2.96 \times 10^{-21} \text{ J} \cdot \text{bit}^{-1}.$$

Thus every 2.96×10^{-21} J of free energy can, in principle, sustain one bit of order.

2. Bits per ATP

The physiological ΔG_{ATP} varies from -45 to $-60 \text{ kJ} \cdot \text{mol}^{-1}$ depending on phosphorylation potential:

bits per ATP = $(|\Delta G_{\text{ATP}}| / N_A) / E_{\text{bit}}$, where N_A is Avogadro's number.

$\Delta G_{\text{ATP}} \text{ (kJ} \cdot \text{mol}^{-1})$	$\text{J} \cdot \text{molecule}^{-1}$	$\text{bits} \cdot \text{ATP}^{-1}$
-60	9.96×10^{-20}	33.6
-55	9.14×10^{-20}	30.8
-50	8.30×10^{-20}	28.0
-45	7.47×10^{-20}	25.2

As $[\text{Pi}]$ rises and ΔG_{ATP} becomes less negative ($-60 \rightarrow -45 \text{ kJ} \cdot \text{mol}^{-1}$), the usable information content per ATP molecule falls by roughly 25% (~ 8 bits).

3. Information Throughput of the Heart

At rest, the myocardium synthesizes $\approx 7.4 \text{ W}$ of ATP ($\sim 1.4 \times 10^{20} \text{ molecules} \cdot \text{s}^{-1}$). With 28–34 bits per molecule, this corresponds to $\approx 4.2 \times 10^{21} \text{ bits} \cdot \text{s}^{-1}$. Ion pumps capture $\sim 3 \text{ W}$ of this organized energy ($\sim 40\%$ of total), yielding gradient information throughput $\approx 1.7 \times 10^{21} \text{ bits} \cdot \text{s}^{-1}$.

4. Biological Interpretation

Each bit represents one state decision—e.g., a pump choosing Na^+ vs K^+ exchange or a channel opening event. As ΔG_{ATP} declines, fewer bits of reliable order can be maintained per unit energy, leading to phase desynchronization and arrhythmia.

5. Key Take-Home Equation

Negentropic throughput = $(|\Delta G_{\text{ATP}}| / kT \ln 2) \times \text{ATP turnover rate}$.

This identity links chemical energy, information flow, and physiological order into one measurable continuum—from molecular biophysics to cardiac rhythm stability.