



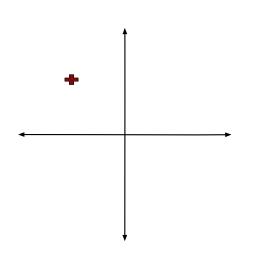
Why Language is Hard: Structure and Predictions

Introduction to Data Science Algorithms
Jordan Boyd-Graber and Michael Paul
STRUCTURED PREDICTION EXAMPLE

2D Example

Initially, weight vector is zero:

$$\vec{w}_1 = \langle 0, 0 \rangle \tag{1}$$



$$x_1 = \langle -2, 2 \rangle$$
 (2)
 $\hat{y}_1 = 0$ (3)
 $y_1 = +1$ (4)

$$\hat{y}_1 = 0 \tag{3}$$

$$y_1 = +1 \tag{4}$$

$$\vec{w}_{t+1} \leftarrow \vec{w}_t + y_t \vec{x}_t \tag{5}$$

$$\vec{w}_2 \leftarrow \tag{6}$$

$$\vec{w}_2 \leftarrow$$
 (6)

$$\vec{\mathbf{w}}_{t+1} \leftarrow \vec{\mathbf{w}}_t + \mathbf{y}_t \vec{\mathbf{x}}_t \tag{5}$$

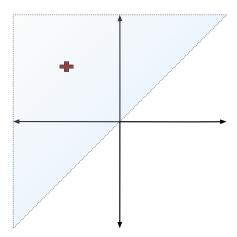
$$\vec{w}_2 \leftarrow \langle 0, 0 \rangle + \langle -2, 2 \rangle \tag{6}$$

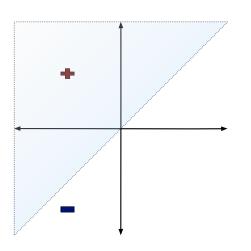
(7)

$$\vec{\mathbf{w}}_{t+1} \leftarrow \vec{\mathbf{w}}_t + \mathbf{y}_t \vec{\mathbf{x}}_t \tag{5}$$

$$\vec{w}_2 \leftarrow \langle 0, 0 \rangle + \langle -2, 2 \rangle \tag{6}$$

$$\vec{w}_2 = \langle -2, 2 \rangle \tag{7}$$





$$x_2 = \langle -2, -3 \rangle$$
 (8)
 $\hat{y}_2 = +4 + -6 = -2$ (9)

$$\hat{y}_2 = +4 + -6 = -2 \qquad (9)$$

$$y_2 = -1$$
 (10)

$$\vec{w}_{t+1} \leftarrow \vec{w}_t \tag{11}$$

$$\vec{w}_2 \leftarrow \tag{12}$$

$$y_2 \leftarrow$$
 (12)

$$\vec{w}_{t+1} \leftarrow \vec{w}_t \tag{11}$$

$$\vec{w}_2 \leftarrow \langle -2, 2 \rangle \tag{12}$$

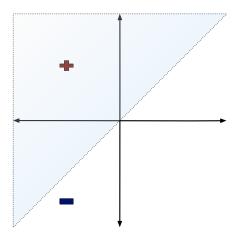
$$\vec{v}_2 \leftarrow \langle -2, 2 \rangle \tag{12}$$

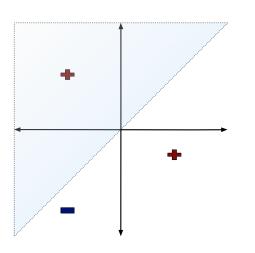
(13)

$$\vec{\mathbf{w}}_{t+1} \leftarrow \vec{\mathbf{w}}_t \tag{11}$$

$$\vec{w}_2 \leftarrow \langle -2, 2 \rangle \tag{12}$$

$$\vec{\mathbf{w}}_2 = \langle -2, 2 \rangle \tag{13}$$





$$x_3 = \langle 2, -1 \rangle$$
 (14)
 $\hat{y}_3 = -4 + -2 = -6$ (15)

$$\hat{y}_3 = -4 + -2 = -6$$
 (15)

$$y_3 = +1$$
 (16)

$$\vec{w}_{t+1} \leftarrow \vec{w}_t + y_t \vec{x}_t \tag{17}$$

$$\vec{w}_3 \leftarrow \tag{18}$$

$$\dot{V}_3 \leftarrow$$
 (18)

$$\vec{\mathbf{w}}_{t+1} \leftarrow \vec{\mathbf{w}}_t + y_t \vec{\mathbf{x}}_t \tag{17}$$

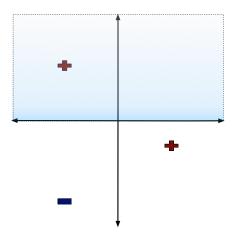
$$\vec{w}_3 \leftarrow \langle -2, 2 \rangle + \langle 2, -1 \rangle \tag{18}$$

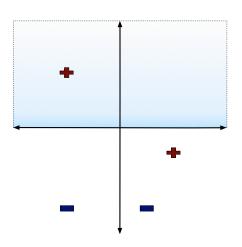
(19)

$$\vec{\mathbf{w}}_{t+1} \leftarrow \vec{\mathbf{w}}_t + \mathbf{y}_t \vec{\mathbf{x}}_t \tag{17}$$

$$\vec{w}_3 \leftarrow \langle -2, 2 \rangle + \langle 2, -1 \rangle \tag{18}$$

$$\vec{w}_3 = \langle 0, 1 \rangle \tag{19}$$





$$x_4 = \langle 1, -4 \rangle$$
 (20)
 $\hat{y}_4 = -4$ (21)
 $y_4 = -1$ (22)

$$\hat{y}_4 = -4 \tag{21}$$

$$y_4 = -1$$
 (22)

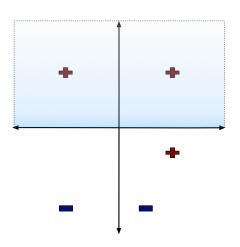
$$\vec{w}_4 \leftarrow$$
 (23)

$$\vec{w}_4 \leftarrow \vec{w}_3 \tag{23}$$

$$\vec{w}_4 \leftarrow \vec{w}_3 \tag{23}$$

$$\vec{w}_4 = \langle 0, 1 \rangle \tag{24}$$

$$Y_4 = \langle 0, 1 \rangle \tag{24}$$



$$x_5 = \langle 2, 2 \rangle$$
 (25)
 $\hat{y}_5 = 2$ (26)
 $y_5 = +1$ (27)

$$\hat{y}_5 = 2$$
 (26)

$$y_5 = +1$$
 (27)

$$\vec{w}_5 \leftarrow$$
 (28)

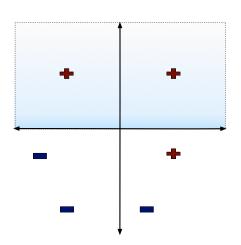
$$\vec{w}_5 \leftarrow \vec{w}_4 \tag{28}$$

(29)

$$\vec{w}_5 \leftarrow \vec{w}_4 \tag{28}$$

$$\vec{w}_5 = \langle 0, 1 \rangle \tag{29}$$

$$v_5 = \langle 0, 1 \rangle$$
 (29)



$$x_6 = \langle 2, 2 \rangle$$
 (30)
 $\hat{y}_6 = 2$ (31)
 $y_6 = +1$ (32)

$$\hat{y}_6 = 2$$
 (31)

$$y_6 = +1$$
 (32)

$$\vec{w}_6 \leftarrow$$
 (33)

$$\vec{w}_6 \leftarrow \vec{w}_5 \tag{33}$$

$$\vec{w}_6 \leftarrow \vec{w}_5 \tag{33}$$

$$\vec{w}_6 = \langle 0, 1 \rangle \tag{34}$$

$$\vec{V}_6 = \langle 0, 1 \rangle$$
 (34)

answer₀ the₁ question₂

$$S = \frac{VB}{PRO} \begin{pmatrix} \\ \\ \\ \\ NN \end{pmatrix}$$
(35)

$$w_{START, VB} + w_{VB, answer} = 0.00 + 0.00 = 0.00$$

answer₀ the₁ question₂

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 \\ 0.00 \\ NN \end{pmatrix}$$
(35)

$$w_{START, DET} + w_{DET, answer} = 0.00 + 0.00 = 0.00$$

answer₀ the₁ question₂

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 \\ 0.00 \\ NN \end{pmatrix}$$
(35)

$$w_{START, PRO} + w_{PRO, answer} = 0.00 + 0.00 = 0.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 0.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ \end{pmatrix} \tag{35}$$

$$w_{START, NN} + w_{NN, answer} = 0.00 + 0.00 = 0.00$$

answer₀ the₁ question₂

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.00 \end{pmatrix}$$
(35)

$$\delta_0(VB) + w_{VB, VB} + w_{VB, the} = 0.00 + 0.00 + 0.00 = 0.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \end{pmatrix}$$
 (35)

$$\delta_0(VB) + w_{VB, DET} + w_{DET, the} = 0.00 + 0.00 + 0.00 = 0.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \end{pmatrix}$$
(35)

$$\delta_0(VB) + w_{VB, PRO} + w_{PRO, the} = 0.00 + 0.00 + 0.00 = 0.00$$

$$\delta = \begin{array}{c} \text{vB} \\ VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ \end{array} \right) \tag{35}$$

$$\delta_0(VB) + w_{VB, NN} + w_{NN, the} = 0.00 + 0.00 + 0.00 = 0.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \end{pmatrix}$$
(35)

$$\delta_1(VB) + w_{VB, VB} + w_{VB, question} = 0.00 + 0.00 + 0.00 = 0.00$$

$$\delta = \begin{array}{c} \text{vB} \\ \text{VB} \\ \text{DET} \\ \text{PRO} \\ \text{NN} \end{array} \begin{pmatrix} 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ \end{array} \right) \tag{35}$$

$$\delta_1(VB) + w_{VB, DET} + w_{DET, question} = 0.00 + 0.00 + 0.00 = 0.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \end{pmatrix}$$
(35)

$$\delta_1(VB) + w_{VB, PRO} + w_{PRO, question} = 0.00 + 0.00 + 0.00 = 0.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0 \end{pmatrix}$$
(35)

$$\delta_1(VB) + w_{VB, NN} + w_{NN, question} = 0.00 + 0.00 + 0.00 = 0.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \end{pmatrix}$$
(35)

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \end{pmatrix}$$
(35)

Backpointers

$$\beta = \begin{array}{ccc} & \text{the}_1 & \text{question}_2 \\ \text{VB} & VB & VB \\ \text{PRO} & VB & VB \\ \text{NN} & VB & VB \\ VB & VB & VB \\ \end{array}$$
(36)

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \end{pmatrix}$$
(35)

Backpointers

the₁ question₂

$$\beta = \begin{cases}
VB & VB \\
DET & VB \\
PRO & VB \\
VB & VB \\
VB & VB
\end{cases}$$
(36)

Decoding Sentence 1

Scores

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 \end{pmatrix}$$
(35)

Backpointers

$$\beta = \begin{cases} VB & VB \\ \end{cases}$$
(36)

Reconstruction: VB VB VB

Prediction: VB VB VB

Prediction: VB VB VB

Prediction: VB VB VB

Gold Features

(DET, the) (DET, NN)

(VB, DET)

(NN, question)

Shared Features

(START, VB)

(VB, answer)

Predicted Features

(VB, the)

(VB, question)

(VB, VB)

Prediction: VB VB VB

Gold Features
(DET, the) (DET, NN)
(VB, DET)
(NN, question)

Shared Features (START, VB) (VB, answer) Predicted Features (VB, the) (VB, question) (VB, VB)

New feature vector: (DET, NN): 1.00; (DET, the): 1.00; (NN, question): 1.00; (VB, DET): 1.00; (VB, VB): -2.00; (VB, question): -1.00; (VB, the): -1.00

Prediction: VB VB VB

Gold Features
(DET, the) (DET, NN)
(VB, DET)
(NN, question)

Shared Features (START, VB) (VB, answer) Predicted Features (VB, the) (VB, question) (VB, VB)

```
    New feature vector: (DET, NN): 1.00; (DET, the): 1.00; (NN, question): 1.00; (VB, DET): 1.00; (VB, VB): -2.00; (VB, question): -1.00; (VB, the): -1.00
```

$$S = \frac{VB}{PRO} \begin{pmatrix} VB & \\ DET & \\ PRO & \\ NN \end{pmatrix}$$
 (37)

$$w_{START, VB} + w_{VB, question} = 0.00 + -1.00 = -1.00$$

w_{START, DET} + w_{DET, question} =
$$0.00 + 0.00 = 0.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} -1.00 \\ 0.00 \\ NN \end{pmatrix}$$
 question₀ the₁ answer₂ answer₂ (37)

$$w_{START, PRO} + w_{PRO, question} = 0.00 + 0.00 = 0.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} -1.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ \end{array}$$
 (37)

$$w_{START, NN} + w_{NN, question} = 0.00 + 1.00 = 1.00$$

$$\delta = \begin{array}{c} \text{question}_0 & \text{the}_1 & \text{answer}_2 \\ VB \\ DET \\ PRO \\ NN \\ \end{array} \begin{array}{c} -1.00 \\ 0.00 \\ 0.00 \\ 1.00 \\ \end{array}$$

$$\delta_0(NN) + w_{NN, VB} + w_{VB, the} = 1.00 + 0.00 + -1.00 = 0.00$$

$$\delta = \begin{array}{c} \text{question}_0 & \text{the}_1 & \text{answer}_2 \\ VB \\ OET \\ PRO \\ NN \\ \end{array} \begin{array}{c} -1.00 & 0.00 \\ 0.00 \\ 0.00 \\ 1.00 \\ \end{array}$$

$$\delta_0(NN) + w_{NN, DET} + w_{DET, the} = 1.00 + 0.00 + 1.00 = 2.00$$

$$\delta = \begin{array}{c} \text{question}_0 & \text{the}_1 & \text{answer}_2 \\ VB \\ OET \\ PRO \\ NN \\ \end{array} \begin{pmatrix} -1.00 & 0.00 \\ 0.00 & 2.00 \\ 0.00 \\ 1.00 \\ \end{array} \right) \tag{37}$$

$$\delta_0(NN) + w_{NN, PRO} + w_{PRO, the} = 1.00 + 0.00 + 0.00 = 1.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} -1.00 & 0.00 \\ 0.00 & 2.00 \\ 0.00 & 1.00 \\ 1.00 \end{pmatrix}$$
 (37)

$$\delta_0(DET) + w_{DET, NN} + w_{NN, the} = 0.00 + 1.00 + 0.00 = 1.00$$

$$\delta = \begin{array}{c} \text{question}_0 & \text{the}_1 & \text{answer}_2 \\ VB \\ \delta = \begin{array}{c} VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} -1.00 & 0.00 \\ 0.00 & 2.00 \\ 0.00 & 1.00 \\ 1.00 & 1.00 \\ \end{array} \right) \tag{37}$$

$$\delta_1(DET) + w_{DET, VB} + w_{VB, answer} = 2.00 + 0.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} -1.00 & 0.00 & 2.00 \\ 0.00 & 2.00 \\ 0.00 & 1.00 \\ 1.00 & 1.00 \\ \end{pmatrix} \tag{37}$$

$$\delta_1(DET) + w_{DET, DET} + w_{DET, answer} = 2.00 + 0.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{question}_0 & \text{the}_1 & \text{answer}_2 \\ VB \\ DET \\ PRO \\ NN \\ \end{array} \begin{pmatrix} -1.00 & 0.00 & 2.00 \\ 0.00 & 2.00 & 2.00 \\ 0.00 & 1.00 \\ 1.00 & 1.00 \\ \end{array} \right) \tag{37}$$

$$\delta_1(DET) + w_{DET, PRO} + w_{PRO, answer} = 2.00 + 0.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{question}_0 & \text{the}_1 & \text{answer}_2 \\ VB \\ DET \\ PRO \\ NN \\ \end{array} \begin{pmatrix} -1.00 & 0.00 & 2.00 \\ 0.00 & 2.00 & 2.00 \\ 0.00 & 1.00 & 2.00 \\ 1.00 & 1.00 \\ \end{array} \right) \tag{37}$$

$$\delta_1(DET) + w_{DET, NN} + w_{NN, answer} = 2.00 + 1.00 + 0.00 = 3.00$$

$$\delta = \begin{array}{c} \text{question}_0 & \text{the}_1 & \text{answer}_2 \\ VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} -1.00 & 0.00 & 2.00 \\ 0.00 & 2.00 & 2.00 \\ 0.00 & 1.00 & 2.00 \\ 1.00 & 1.00 & 3.00 \\ \end{pmatrix} \tag{37}$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} -1.00 & 0.00 & 2.00 \\ 0.00 & 2.00 & 2.00 \\ 0.00 & 1.00 & 2.00 \\ 1.00 & 1.00 & 3.00 \end{pmatrix}$$
(37)

Backpointers

$$B = \begin{array}{c} \text{the}_1 & \text{answer}_2 \\ \text{VB} & NN & DET \\ \text{DET} & NN & DET \\ \text{PRO} & NN & DET \\ \text{NN} & DET \\ DET & DET \end{array}$$
 (38)

$$\delta = \frac{VB}{PRO} \begin{pmatrix} -1.00 & 0.00 & 2.00 \\ 0.00 & 2.00 & 2.00 \\ 0.00 & 1.00 & 2.00 \\ 1.00 & 1.00 & 3.00 \end{pmatrix}$$
(37)

Backpointers

the₁ answer₂

$$\beta = \begin{array}{c}
VB \\
DET \\
PRO \\
NN \end{array} \begin{array}{c}
NN \\
DET \\
NN \\
DET \\
DET
\end{array}$$
(38)

Decoding Sentence 2

Scores

$$\delta = \frac{VB}{PRO} \begin{pmatrix} -1.00 & 0.00 & 2.00 \\ 0.00 & 2.00 & 2.00 \\ 0.00 & 1.00 & 2.00 \\ 1.00 & 1.00 & 3.00 \end{pmatrix}$$
(37)

Backpointers

$$\beta = \begin{array}{c} \text{the}_1 & \text{answer}_2 \\ \text{VB} & NN & DET \\ \text{DET} & NN & DET \\ \text{PRO} & NN & DET \\ \text{NN} & DET \\ DET & DET \end{array}$$
 (38)

Reconstruction: NN DET NN

Prediction: NN DET NN

Prediction: NN DET NN

Prediction: NN DET NN

Gold Features

(VB, DET) (START, VB)

(VB, question)

Shared Features

(DET, the) (DET, NN)

(NN, answer)

Predicted Features

(START, NN)

(NN, question)

(NN, DET)

Prediction: NN DET NN

Gold Features (VB, DET) (START, VB) (VB, question)

Shared Features (DET, the) (DET, NN) (NN, answer) Predicted Features (START, NN) (NN, question) (NN, DET)

New feature vector: (DET, NN): 1.00; (DET, the): 1.00; (NN, DET): -1.00;
 (VB, DET): 2.00; (VB, VB): -2.00; (VB, the): -1.00; (START, NN): -1.00;
 (START, VB): 1.00

Prediction: NN DET NN

Gold Features (VB, DET) (START, VB) (VB, question)

Shared Features (DET, the) (DET, NN) (NN, answer) Predicted Features (START, NN) (NN, question) (NN, DET)

New feature vector: (DET, NN): 1.00; (DET, the): 1.00; (NN, DET): -1.00; (VB, DET): 2.00; (VB, VB): -2.00; (VB, the): -1.00; (START, NN): -1.00; (START, VB): 1.00

$$\delta = \frac{VB}{PRO} \begin{pmatrix} VB & \\ DET & \\ NN \end{pmatrix}$$
 (39)

$$w_{START, VB} + w_{VB, you} = 1.00 + 0.00 = 1.00$$

$$5 = \frac{VB}{PRO} \begin{pmatrix} 1.00 \\ NN \end{pmatrix}$$
 (39)

$$w_{\text{START, DET}} + w_{\text{DET, you}} = 0.00 + 0.00 = 0.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 1.00 \\ 0.00 \\ NN \end{pmatrix}$$
 (39)

$$w_{\text{START, PRO}} + w_{\text{PRO, you}} = 0.00 + 0.00 = 0.00$$

$$5 = \frac{VB}{PRO} \begin{pmatrix} 1.00 \\ 0.00 \\ NN \end{pmatrix}$$
 (39)

$$w_{\text{START, NN}} + w_{\text{NN, you}} = -1.00 + 0.00 = -1.00$$

$$\delta = \begin{array}{c} \text{you}_0 & \text{demand}_1 & \text{the}_2 & \text{delay}_3 \\ VB & 1.00 & \\ O.00 & 0.00 & \\ NN & -1.00 & \\ \end{array} \right)$$
(39)

$$\delta_0(DET) + w_{DET, VB} + w_{VB, demand} = 0.00 + 0.00 + 0.00 = 0.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 \\ 0.00 \\ 0.00 \\ -1.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_0(VB) + w_{VB, DET} + w_{DET, demand} = 1.00 + 2.00 + 0.00 = 3.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 \\ 0.00 & 3.00 \\ 0.00 \\ -1.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_0(VB) + w_{VB, PRO} + w_{PRO, demand} = 1.00 + 0.00 + 0.00 = 1.00$$

$$\delta = \begin{array}{c} \text{VB} \\ \text{VB} \\ \text{DET} \\ \text{PRO} \\ \text{NN} \end{array} \begin{pmatrix} 1.00 & 0.00 \\ 0.00 & 3.00 \\ 0.00 & 1.00 \\ -1.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_0(VB) + w_{VB, NN} + w_{NN, demand} = 1.00 + 0.00 + 0.00 = 1.00$$

$$\delta = \begin{array}{c} \text{VB} \\ \text{VB} \\ \text{DET} \\ \text{PRO} \\ \text{NN} \end{array} \begin{pmatrix} 1.00 & 0.00 \\ 0.00 & 3.00 \\ 0.00 & 1.00 \\ -1.00 & 1.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_1(DET) + w_{DET, VB} + w_{VB, the} = 3.00 + 0.00 + -1.00 = 2.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 & 2.00 \\ 0.00 & 3.00 \\ 0.00 & 1.00 \\ -1.00 & 1.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_1(DET) + w_{DET, DET} + w_{DET, the} = 3.00 + 0.00 + 1.00 = 4.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 & 2.00 \\ 0.00 & 3.00 & 4.00 \\ 0.00 & 1.00 \\ -1.00 & 1.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_1(DET) + w_{DET, PRO} + w_{PRO, the} = 3.00 + 0.00 + 0.00 = 3.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 & 2.00 \\ 0.00 & 3.00 & 4.00 \\ 0.00 & 1.00 & 3.00 \\ -1.00 & 1.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_1(DET) + w_{DET, NN} + w_{NN, the} = 3.00 + 1.00 + 0.00 = 4.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 & 2.00 \\ 0.00 & 3.00 & 4.00 \\ 0.00 & 1.00 & 3.00 \\ -1.00 & 1.00 & 4.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_2(DET) + w_{DET, VB} + w_{VB, delay} = 4.00 + 0.00 + 0.00 = 4.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 & 2.00 & 4.00 \\ 0.00 & 3.00 & 4.00 \\ 0.00 & 1.00 & 3.00 \\ -1.00 & 1.00 & 4.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_2(VB) + w_{VB, DET} + w_{DET, delay} = 2.00 + 2.00 + 0.00 = 4.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 & 2.00 & 4.00 \\ 0.00 & 3.00 & 4.00 & 4.00 \\ 0.00 & 1.00 & 3.00 \\ -1.00 & 1.00 & 4.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_2(DET) + w_{DET, PRO} + w_{PRO, delay} = 4.00 + 0.00 + 0.00 = 4.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 & 2.00 & 4.00 \\ 0.00 & 3.00 & 4.00 & 4.00 \\ 0.00 & 1.00 & 3.00 & 4.00 \\ -1.00 & 1.00 & 4.00 \\ \end{pmatrix} \tag{39}$$

$$\delta_2(DET) + w_{DET, NN} + w_{NN, delay} = 4.00 + 1.00 + 0.00 = 5.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 & 2.00 & 4.00 \\ 0.00 & 3.00 & 4.00 & 4.00 \\ 0.00 & 1.00 & 3.00 & 4.00 \\ -1.00 & 1.00 & 4.00 & 5.00 \\ \end{pmatrix} \tag{39}$$

Decoding Sentence 3

Scores

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 & 2.00 & 4.00 \\ 0.00 & 3.00 & 4.00 & 4.00 \\ 0.00 & 1.00 & 3.00 & 4.00 \\ -1.00 & 1.00 & 4.00 & 5.00 \\ \end{pmatrix} \tag{39}$$

Backpointers

$$\beta = \begin{array}{cccc} & \text{demand}_1 & \text{the}_2 & \text{delay}_3 \\ \text{VB} & DET & DET & DET \\ \text{PRO} & VB & DET & VB \\ \text{NN} & VB & DET & DET \\ \end{array}$$
 (40)

Decoding Sentence 3

Scores

$$\delta = \begin{array}{c} VB \\ VB \\ PRO \\ NN \end{array} \begin{pmatrix} 1.00 & 0.00 & 2.00 & 4.00 \\ 0.00 & 3.00 & 4.00 & 4.00 \\ 0.00 & 1.00 & 3.00 & 4.00 \\ -1.00 & 1.00 & 4.00 & 5.00 \\ \end{pmatrix} \tag{39}$$

Backpointers

$$\beta = \begin{array}{cccc} & \text{demand}_1 & \text{the}_2 & \text{delay}_3 \\ \text{VB} & DET & DET & DET \\ \text{PRO} & VB & DET & VB \\ \text{NN} & VB & DET & DET \\ \end{array}$$
 (40)

Decoding Sentence 3

Scores

$$\delta = \begin{array}{c} \text{you}_0 & \text{demand}_1 & \text{the}_2 & \text{delay}_3 \\ VB & 1.00 & 0.00 & 2.00 & 4.00 \\ 0.00 & 3.00 & 4.00 & 4.00 \\ 0.00 & 1.00 & 3.00 & 4.00 \\ -1.00 & 1.00 & 4.00 & 5.00 \\ \end{array} \right) \tag{39}$$

Backpointers

$$\beta = \begin{array}{ccc} & \text{demand}_1 & \text{the}_2 & \text{delay}_3 \\ \text{VB} & DET & DET & DET \\ \text{PRO} & VB & DET & VB \\ \text{NN} & VB & DET & DET \\ \end{array}$$
 (40)

Reconstruction: VB DET DET NN

Prediction: VB DET DET NN

Prediction: VB DET DET NN

Prediction: VB DET DET NN

Gold Features

(VB, demand) (PRO, you) (START, PRO)

(PRO, VB)

Shared Features

(DET, the) (DET, NN)

(VB, DET)

(NN, delay)

Predicted Features

(DET, DET)

(START, VB)

(DET, demand)

(VB, you)

Prediction: VB DET DET NN

Gold Features

(VB, demand) (PRO, you) (START, PRO) (PRO, VB)

Shared Features (DET, the) (DET, NN) (VB, DET) (NN, delay)

Predicted Features (DET, DET) (START, VB) (DET, demand) (VB, you)

New feature vector: (DET, DET): -1.00; (DET, NN): 1.00;
(DET, demand): -1.00; (DET, the): 1.00; (NN, DET): -1.00;
(PRO, VB): 1.00; (PRO, you): 1.00; (VB, DET): 2.00; (VB, VB): -2.00;
(VB, demand): 1.00; (VB, the): -1.00; (VB, you): -1.00; (START, NN): -1.00; (START, PRO): 1.00

Prediction: VB DET DET NN

Gold Features

(VB, demand) (PRO, you) (START, PRO) (PRO, VB)

Shared Features (DET, the) (DET, NN) (VB, DET) (NN, delay)

Predicted Features (DET, DET) (START, VB) (DET, demand) (VB, you)

```
New feature vector: (DET, DET): -1.00; (DET, NN): 1.00;
(DET, demand): -1.00; (DET, the): 1.00; (NN, DET): -1.00;
(PRO, VB): 1.00; (PRO, you): 1.00; (VB, DET): 2.00; (VB, VB): -2.00;
(VB, demand): 1.00; (VB, the): -1.00; (VB, you): -1.00; (START, NN):
-1.00; (START, PRO): 1.00
```

$$S = \begin{cases} VB \\ DET \\ PRO \\ NN \end{cases}$$
 (41)

$$w_{START, VB} + w_{VB, you} = 0.00 + -1.00 = -1.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} VB & -1.00 \\ NN & \\ \end{pmatrix}$$
 (41)

$$w_{\text{START, DET}} + w_{\text{DET, you}} = 0.00 + 0.00 = 0.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} \text{you}_0 & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ -1.00 & & & \\ 0.00 & & & \\ NN & & & \\ \end{pmatrix} \tag{41}$$

$$w_{\text{START, PRO}} + w_{\text{PRO, you}} = 1.00 + 1.00 = 2.00$$

$$\delta = \begin{array}{c} \text{you}_0 & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ VB & -1.00 & \\ DET & 0.00 & \\ NN & 2.00 & \\ \end{array} \right) \tag{41}$$

$$w_{\text{START, NN}} + w_{\text{NN, you}} = -1.00 + 0.00 = -1.00$$

$$\delta = \begin{array}{c} \text{you}_0 & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ VB & -1.00 & \\ DET & 0.00 & \\ PRO & 2.00 & \\ NN & -1.00 & \\ \end{array} \right) \tag{41}$$

$$\delta_0(PRO) + w_{PRO, VB} + w_{VB, delay} = 2.00 + 1.00 + 0.00 = 3.00$$

$$\delta = \begin{array}{c} \text{VB} \\ \text{VB} \\ \text{DET} \\ \text{PRO} \\ \text{NN} \end{array} \begin{pmatrix} -1.00 & 3.00 \\ 0.00 \\ 2.00 \\ -1.00 \\ \end{pmatrix} \tag{41}$$

$$\delta_0(PRO) + w_{PRO, DET} + w_{DET, delay} = 2.00 + 0.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{you}_0 & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ VB \\ OET \\ PRO \\ NN \\ \end{array} \begin{pmatrix} -1.00 & 3.00 \\ 0.00 & 2.00 \\ 2.00 \\ -1.00 \\ \end{pmatrix} \tag{41}$$

$$\delta_0(PRO) + w_{PRO, PRO} + w_{PRO, delay} = 2.00 + 0.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{you}_0 & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ VB \\ OET \\ PRO \\ NN \\ \end{array} \begin{pmatrix} -1.00 & 3.00 \\ 0.00 & 2.00 \\ 2.00 & 2.00 \\ -1.00 \\ \end{pmatrix} \tag{41}$$

$$\delta_0(PRO) + w_{PRO, NN} + w_{NN, delay} = 2.00 + 0.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{you}_0 & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ VB \\ DET \\ PRO \\ NN \\ \end{array} \begin{pmatrix} -1.00 & 3.00 \\ 0.00 & 2.00 \\ 2.00 & 2.00 \\ -1.00 & 2.00 \\ \end{pmatrix} \tag{41}$$

$$\delta_1(PRO) + w_{PRO, VB} + w_{VB, the} = 2.00 + 1.00 + -1.00 = 2.00$$

$$\delta = \begin{array}{c} \text{VB} \\ \text{VB} \\ \text{DET} \\ \text{PRO} \\ \text{NN} \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 \\ 0.00 & 2.00 \\ 2.00 & 2.00 \\ -1.00 & 2.00 \\ \end{pmatrix} \tag{41}$$

$$\delta_1(VB) + w_{VB, DET} + w_{DET, the} = 3.00 + 2.00 + 1.00 = 6.00$$

$$\delta = \begin{array}{c} \text{VB} \\ \text{VB} \\ \text{DET} \\ \text{PRO} \\ \text{NN} \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 \\ 0.00 & 2.00 & 6.00 \\ 2.00 & 2.00 \\ -1.00 & 2.00 \\ \end{pmatrix} \tag{41}$$

$$\delta_1(VB) + w_{VB, PRO} + w_{PRO, the} = 3.00 + 0.00 + 0.00 = 3.00$$

$$\delta = \begin{array}{c} VB \\ VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 \\ 0.00 & 2.00 & 6.00 \\ 2.00 & 2.00 & 3.00 \\ -1.00 & 2.00 \\ \end{pmatrix} \tag{41}$$

$$\delta_1(VB) + w_{VB, NN} + w_{NN, the} = 3.00 + 0.00 + 0.00 = 3.00$$

$$\delta = \begin{array}{c} \text{VB} \\ \text{VB} \\ \text{DET} \\ \text{PRO} \\ \text{NN} \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 \\ 0.00 & 2.00 & 6.00 \\ 2.00 & 2.00 & 3.00 \\ -1.00 & 2.00 & 3.00 \\ \end{array} \right) \tag{41}$$

$$\delta_2(DET) + w_{DET, VB} + w_{VB, demand} = 6.00 + 0.00 + 1.00 = 7.00$$

$$\delta = \begin{array}{c} \text{VB} \\ \text{VB} \\ \text{DET} \\ \text{PRO} \\ \text{NN} \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 & 7.00 \\ 0.00 & 2.00 & 6.00 \\ 2.00 & 2.00 & 3.00 \\ -1.00 & 2.00 & 3.00 \\ \end{pmatrix} \tag{41}$$

$$\delta_2(DET) + w_{DET, DET} + w_{DET, demand} = 6.00 + -1.00 + -1.00 = 4.00$$

$$\delta = \begin{array}{c} VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 & 7.00 \\ 0.00 & 2.00 & 6.00 & 4.00 \\ 2.00 & 2.00 & 3.00 \\ -1.00 & 2.00 & 3.00 \\ \end{pmatrix} \tag{41}$$

$$\delta_2(DET) + w_{DET, PRO} + w_{PRO, demand} = 6.00 + 0.00 + 0.00 = 6.00$$

$$\delta = \begin{array}{c} \text{VB} \\ \text{VB} \\ \text{DET} \\ \text{PRO} \\ \text{NN} \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 & 7.00 \\ 0.00 & 2.00 & 6.00 & 4.00 \\ 2.00 & 2.00 & 3.00 & 6.00 \\ -1.00 & 2.00 & 3.00 & \end{array} \right) \tag{41}$$

$$\delta_2(DET) + w_{DET, NN} + w_{NN, demand} = 6.00 + 1.00 + 0.00 = 7.00$$

$$\delta = \begin{array}{c} \text{VB} \\ \text{VB} \\ \text{DET} \\ \text{PRO} \\ \text{NN} \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 & 7.00 \\ 0.00 & 2.00 & 6.00 & 4.00 \\ 2.00 & 2.00 & 3.00 & 6.00 \\ -1.00 & 2.00 & 3.00 & 7.00 \\ \end{pmatrix} \tag{41} \label{eq:delta_scale}$$

Scores

$$\delta = \begin{array}{c} \text{you}_0 & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 & 7.00 \\ 0.00 & 2.00 & 6.00 & 4.00 \\ 2.00 & 2.00 & 3.00 & 6.00 \\ -1.00 & 2.00 & 3.00 & 7.00 \\ \end{pmatrix} \tag{41}$$

Backpointers

$$\beta = \begin{array}{cccc} & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ \text{VB} & PRO & PRO & DET \\ \text{PRO} & PRO & VB & DET \\ \text{PRO} & VB & DET \\ \text{NN} & PRO & VB & DET \\ \end{array} \right) \tag{42}$$

Scores

$$\delta = \begin{array}{c} \text{you}_0 & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 & 7.00 \\ 0.00 & 2.00 & 6.00 & 4.00 \\ 2.00 & 2.00 & 3.00 & 6.00 \\ -1.00 & 2.00 & 3.00 & 7.00 \\ \end{pmatrix} \tag{41}$$

Backpointers

$$\beta = \begin{array}{cccc} & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ \text{VB} & \begin{array}{cccc} PRO & PRO & DET \\ PRO & PRO & DET \\ PRO & VB & DET \\ PRO & VB & DET \\ PRO & VB & DET \end{array} \right) \tag{42}$$

Scores

$$\delta = \begin{array}{c} \text{you}_0 & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ VB \\ \delta = \begin{array}{c} VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} -1.00 & 3.00 & 2.00 & 7.00 \\ 0.00 & 2.00 & 6.00 & 4.00 \\ 2.00 & 2.00 & 3.00 & 6.00 \\ -1.00 & 2.00 & 3.00 & 7.00 \\ \end{pmatrix} \tag{41}$$

Backpointers

$$\beta = \begin{array}{cccc} & \text{delay}_1 & \text{the}_2 & \text{demand}_3 \\ \text{VB} & PRO & PRO & DET \\ \text{PRO} & PRO & VB & DET \\ \text{PRO} & PRO & VB & DET \\ \text{PRO} & PRO & PRO$$

Reconstruction: PRO VB DET VB

Prediction: PRO VB DET VB

Prediction: PRO VB DET VB

Prediction: PRO VB DET VB

Gold Features (DET, NN) (NN, demand) Shared Features
(VB, delay)
(DET, the) (VB, DET)
(PRO, you)
(START, PRO)
(PRO, VB)

Predicted Features (DET, VB) (VB, demand)

Prediction: PRO VB DET VB

Gold Features (DET, NN)

(NN, demand)

Shared Features

(VB, delay) (DET, the) (VB, DET) (PRO, you) (START, PRO) (PRO, VB)

Predicted Features

(DET, VB) (VB, demand)

New feature vector: (DET, DET): -1.00; (DET, NN): 2.00;
(DET, VB): -1.00; (DET, demand): -1.00; (DET, the): 1.00; (NN, DET):
-1.00; (NN, demand): 1.00; (PRO, VB): 1.00; (PRO, you): 1.00; (VB, DET): 2.00; (VB, VB): -2.00; (VB, the): -1.00; (VB, you): -1.00; (START, NN): -1.00; (START, PRO): 1.00

- Correct answer: PRO VB DET NN
- Prediction: PRO VB DET VB

Gold Features (DET, NN)

(NN, demand)

Shared Features (VB, delay) (DET, the) (VB, DET) (PRO, you) (START, PRO) (PRO, VB)

Predicted Features (DET, VB) (VB, demand)

```
New feature vector: (DET, DET): -1.00; (DET, NN): 2.00;
(DET, VB): -1.00; (DET, demand): -1.00; (DET, the): 1.00; (NN, DET):
-1.00; (NN, demand): 1.00; (PRO, VB): 1.00; (PRO, you): 1.00; (VB, DET): 2.00; (VB, VB): -2.00; (VB, the): -1.00; (VB, you): -1.00; (START, NN): -1.00; (START, PRO): 1.00
```

what₀ silence₁ can₂ show₃

$$\delta = \frac{VB}{PRO} \begin{pmatrix} \\ \\ \\ NN \end{pmatrix}$$
(43)

$$w_{START, VB} + w_{VB, what} = 0.00 + 0.00 = 0.00$$

$$\tilde{D} = \frac{VB}{PRO} \begin{pmatrix} 0.00 \\ 0.00 \\ NN \end{pmatrix}$$
 (43)

$$w_{START, DET} + w_{DET, what} = 0.00 + 0.00 = 0.00$$

$$\mathcal{S} = \frac{VB}{PRO} \begin{pmatrix} 0.00 \\ 0.00 \\ NN \end{pmatrix}$$
 what₀ silence₁ can₂ show₃
$$0.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.00$$
 (43)

$$w_{START, PRO} + w_{PRO, what} = 1.00 + 0.00 = 1.00$$

$$\tilde{S} = \frac{VB}{PRO} \begin{pmatrix} 0.00 \\ 0.00 \\ 1.00 \\ NN \end{pmatrix}$$
 what₀ silence₁ can₂ show₃
$$\begin{pmatrix} 0.00 \\ 0.00 \\ 1.00 \\ \end{pmatrix}$$
 (43)

$$w_{START, NN} + w_{NN, what} = -1.00 + 0.00 = -1.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 \\ 0.00 \\ 1.00 \\ NN \end{pmatrix}$$
 (43)

$$\delta_0(PRO) + w_{PRO, VB} + w_{VB, silence} = 1.00 + 1.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{what}_0 & \text{silence}_1 & \text{can}_2 & \text{show}_3 \\ VB & 0.00 & 2.00 \\ O.00 & 0.00 \\ PRO & 1.00 \\ NN & -1.00 \end{array} \right) \tag{43}$$

$$\delta_0(VB) + w_{VB, DET} + w_{DET, silence} = 0.00 + 2.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{what}_0 & \text{silence}_1 & \text{can}_2 & \text{show}_3 \\ VB & 0.00 & 2.00 \\ O.00 & 2.00 \\ PRO & 1.00 \\ NN & -1.00 \end{array} \right) \tag{43}$$

$$\delta_0(PRO) + w_{PRO, PRO} + w_{PRO, silence} = 1.00 + 0.00 + 0.00 = 1.00$$

$$\delta = \begin{array}{c} \text{what}_0 & \text{silence}_1 & \text{can}_2 & \text{show}_3 \\ VB & 0.00 & 2.00 & \\ DET & 0.00 & 2.00 & \\ PRO & 1.00 & 1.00 & \\ NN & -1.00 & \\ \end{array} \right) \tag{43}$$

$$\delta_0(DET) + w_{DET, NN} + w_{NN, silence} = 0.00 + 2.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{what}_0 & \text{silence}_1 & \text{can}_2 & \text{show}_3 \\ VB & 0.00 & 2.00 & \\ DET & 0.00 & 2.00 & \\ PRO & 1.00 & 1.00 & \\ NN & -1.00 & 2.00 & \\ \end{array} \right) \tag{43}$$

$$\delta_1(PRO) + w_{PRO, VB} + w_{VB, can} = 1.00 + 1.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{what}_0 & \text{silence}_1 & \text{can}_2 & \text{show}_3 \\ VB & 0.00 & 2.00 & 2.00 \\ \hline \textit{DET} & 0.00 & 2.00 \\ \hline \textit{PRO} & 1.00 & 1.00 \\ \textit{NN} & -1.00 & 2.00 \\ \end{array} \right) \tag{43}$$

$$\delta_1(VB) + w_{VB, DET} + w_{DET, can} = 2.00 + 2.00 + 0.00 = 4.00$$

$$\delta = \begin{array}{c} \text{what}_0 \quad \text{silence}_1 \quad \text{can}_2 \quad \text{show}_3 \\ VB \\ \delta = \begin{array}{c} O.00 \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 0.00 & 2.00 & 2.00 \\ 0.00 & 2.00 & 4.00 \\ 1.00 & 1.00 \\ -1.00 & 2.00 \\ \end{pmatrix} \tag{43}$$

$$\delta_1(VB) + w_{VB, PRO} + w_{PRO, can} = 2.00 + 0.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{what}_0 \quad \text{silence}_1 \quad \text{can}_2 \quad \text{show}_3 \\ VB \\ \delta = \begin{array}{c} O.00 \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 0.00 & 2.00 & 2.00 \\ 0.00 & 2.00 & 4.00 \\ 1.00 & 1.00 & 2.00 \\ -1.00 & 2.00 \\ \end{array} \right) \tag{43}$$

$$\delta_1(DET) + w_{DET, NN} + w_{NN, can} = 2.00 + 2.00 + 0.00 = 4.00$$

$$\delta = \begin{array}{c|cccc} & \text{what}_0 & \text{silence}_1 & \text{can}_2 & \text{show}_3 \\ \hline VB & 0.00 & 2.00 & 2.00 \\ \hline DET & 0.00 & 2.00 & 4.00 \\ \hline PRO & 1.00 & 1.00 & 2.00 \\ \hline NN & -1.00 & 2.00 & 4.00 \\ \hline \end{array} \right) \tag{43}$$

$$\delta_2(NN) + w_{NN, VB} + w_{VB, show} = 4.00 + 0.00 + 0.00 = 4.00$$

$$\delta = \begin{array}{c} \text{What}_0 \quad \text{silence}_1 \quad \text{can}_2 \quad \text{show}_3 \\ VB \\ \delta = \begin{array}{c} O.00 \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 0.00 & 2.00 & 2.00 & 4.00 \\ 0.00 & 2.00 & 4.00 \\ 1.00 & 1.00 & 2.00 \\ -1.00 & 2.00 & 4.00 \\ \end{pmatrix} \tag{43}$$

$$\delta_2(VB) + w_{VB, DET} + w_{DET, show} = 2.00 + 2.00 + 0.00 = 4.00$$

$$\delta = \begin{array}{c} \text{what}_0 & \text{silence}_1 & \text{can}_2 & \text{show}_3 \\ VB & 0.00 & 2.00 & 2.00 & 4.00 \\ 0.00 & 2.00 & 4.00 & 4.00 \\ PRO & 1.00 & 2.00 & 4.00 \\ NN & -1.00 & 2.00 & 4.00 \\ \end{array} \right) \tag{43}$$

$$\delta_2(DET) + w_{DET, PRO} + w_{PRO, show} = 4.00 + 0.00 + 0.00 = 4.00$$

$$\delta = \begin{array}{c} \text{what}_0 \quad \text{silence}_1 \quad \text{can}_2 \quad \text{show}_3 \\ VB \\ \delta = \begin{array}{c} O.00 \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 0.00 & 2.00 & 2.00 & 4.00 \\ 0.00 & 2.00 & 4.00 & 4.00 \\ 1.00 & 1.00 & 2.00 & 4.00 \\ -1.00 & 2.00 & 4.00 \\ \end{pmatrix} \tag{43}$$

$$\delta_2(DET) + w_{DET, NN} + w_{NN, show} = 4.00 + 2.00 + 0.00 = 6.00$$

$$\delta = \begin{array}{c} \text{what}_0 \quad \text{silence}_1 \quad \text{can}_2 \quad \text{show}_3 \\ VB \\ \delta = \begin{array}{c} O.00 \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 0.00 & 2.00 & 2.00 & 4.00 \\ 0.00 & 2.00 & 4.00 & 4.00 \\ 1.00 & 1.00 & 2.00 & 4.00 \\ -1.00 & 2.00 & 4.00 & 6.00 \\ \end{pmatrix} \tag{43}$$

Scores

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 2.00 & 2.00 & 4.00 \\ 0.00 & 2.00 & 4.00 & 4.00 \\ 1.00 & 1.00 & 2.00 & 4.00 \\ NN & -1.00 & 2.00 & 4.00 & 6.00 \end{pmatrix}$$
(43)

Backpointers

$$\beta = \begin{cases} \text{vB} & \text{can}_2 & \text{show}_3 \\ \text{VB} & PRO & PRO & NN \\ \text{VB} & VB & VB \\ PRO & VB & DET \\ NN & PRO & VB & DET \\ \end{pmatrix}$$
(44)

Scores

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 2.00 & 2.00 & 4.00 \\ 0.00 & 2.00 & 4.00 & 4.00 \\ 1.00 & 1.00 & 2.00 & 4.00 \\ NN & -1.00 & 2.00 & 4.00 & 6.00 \end{pmatrix}$$
(43)

Backpointers

$$\beta = \begin{array}{ccc} \text{silence}_1 & \text{can}_2 & \text{show}_3 \\ \text{VB} & \begin{array}{ccc} PRO & PRO & NN \\ VB & VB & VB \\ PRO & VB & DET \\ NN & \begin{array}{ccc} DET & DET & DET \\ \end{array} \end{array} \right) \tag{44}$$

Scores

$$\delta = \begin{array}{c} \text{what}_0 \quad \text{silence}_1 \quad \text{can}_2 \quad \text{show}_3 \\ VB \\ O.00 \quad 2.00 \quad 2.00 \quad 4.00 \\ 0.00 \quad 2.00 \quad 4.00 \quad 4.00 \\ 1.00 \quad 1.00 \quad 2.00 \quad 4.00 \\ -1.00 \quad 2.00 \quad 4.00 \quad 6.00 \\ \end{array} \right) \tag{43}$$

Backpointers

silence₁ can₂ show₃

$$\beta = \begin{array}{cccc} VB & PRO & PRO & NN \\ DET & VB & VB & VB \\ PRO & VB & DET \\ NN & DET & DET & DET \end{array}$$
(44)

Reconstruction: PRO VB DET NN

Correct answer: PRO NN VB VB

Prediction: PRO VB DET NN

Correct answer: PRO NN VB VB

Prediction: PRO VB DET NN

Correct answer: PRO NN VB VB

Prediction: PRO VB DET NN

Gold Features

(VB, show) (VB, can) (PRO, NN) (NN, silence) (NN, VB) (VB, VB) Shared Features (START, PRO)

(PRO, what)

Predicted Features
(DET, can)
(NN, show)
(VB, silence)
(DET, NN) (VB, DET)
(PRO, VB)

- Correct answer: PRO NN VB VB
- Prediction: PRO VB DET NN

Gold Features

(VB, show) (VB, can) (PRO, NN) (NN, silence) (NN, VB) (VB, VB) Shared Features (START, PRO) (PRO, what)

Predicted Features

(DET, can) (NN, show) (VB, silence) (DET, NN) (VB, DET) (PRO, VB)

New feature vector: (DET, DET): -1.00; (DET, NN): 1.00; (DET, VB): -1.00; (DET, can): -1.00; (DET, demand): -1.00; (DET, the): 1.00; (NN, DET): -1.00; (NN, VB): 1.00; (NN, demand): 1.00; (NN, show): -1.00; (NN, silence): 1.00; (PRO, NN): 1.00; (PRO, you): 1.00; (VB, DET): 1.00; (VB, VB): -1.00; (VB, can): 1.00; (VB, show): 1.00; (VB, silence): -1.00; (VB, the): -1.00; (VB, you): -1.00; (START, NN): -1.00; (START, PRO): 1.00

- Correct answer: PRO NN VB VB
- Prediction: PRO VB DET NN

Gold Features

(VB, show) (VB, can) (PRO, NN) (NN, silence) (NN, VB) (VB, VB) Shared Features (START, PRO) (PRO, what)

Predicted Features

(DET, can) (NN, show) (VB, silence) (DET, NN) (VB, DET) (PRO, VB)

```
New feature vector: (DET, DET): -1.00; (DET, NN): 1.00; (DET, VB): -1.00; (DET, can): -1.00; (DET, demand): -1.00; (DET, the): 1.00; (NN, DET): -1.00; (NN, VB): 1.00; (NN, demand): 1.00; (NN, show): -1.00; (NN, silence): 1.00; (PRO, NN): 1.00; (PRO, you): 1.00; (VB, DET): 1.00; (VB, VB): -1.00; (VB, can): 1.00; (VB, show): 1.00; (VB, silence): -1.00; (VB, the): -1.00; (VB, you): -1.00; (START, NN): -1.00; (START, PRO): 1.00
```

what₀ show₁ can₂ silence₃

$$\delta = \frac{VB}{PRO} \begin{pmatrix} \\ \\ \\ NN \end{pmatrix}$$
(45)

$$w_{START, VB} + w_{VB, what} = 0.00 + 0.00 = 0.00$$

$$w_{START, DET} + w_{DET, what} = 0.00 + 0.00 = 0.00$$

$$\tilde{S} = \frac{VB}{PRO} \begin{pmatrix} 0.00 \\ 0.00 \\ NN \end{pmatrix}$$
 what₀ show₁ can₂ silence₃
$$0.00 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.00$$
 (45)

$$w_{START, PRO} + w_{PRO, what} = 1.00 + 0.00 = 1.00$$

$$\tilde{S} = \frac{VB}{PRO} \begin{pmatrix} 0.00 \\ 0.00 \\ 1.00 \\ NN \end{pmatrix}$$
 (45)

$$w_{\text{START, NN}} + w_{\text{NN, what}} = -1.00 + 0.00 = -1.00$$

$$\delta = \begin{array}{c} \text{What}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB & 0.00 & \\ DET & 0.00 & \\ PRO & 1.00 & \\ NN & -1.00 & \\ \end{array} \right) \tag{45}$$

$$\delta_0(PRO) + w_{PRO, VB} + w_{VB, show} = 1.00 + 0.00 + 1.00 = 2.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 2.00 \\ 0.00 & 0.00 \\ 1.00 & 0.00 \\ -1.00 \end{pmatrix}$$
 (45)

$$\delta_0(VB) + w_{VB, DET} + w_{DET, show} = 0.00 + 1.00 + 0.00 = 1.00$$

$$\delta = \frac{VB}{PRO} \begin{pmatrix} 0.00 & 2.00 \\ 0.00 & 1.00 \\ 1.00 \\ NN \end{pmatrix}$$
 (45)

$$\delta_0(PRO) + w_{PRO, PRO} + w_{PRO, show} = 1.00 + 0.00 + 0.00 = 1.00$$

$$\delta = \begin{array}{c} \text{What}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB & 0.00 & 2.00 \\ O.00 & 1.00 \\ PRO & 1.00 & 1.00 \\ NN & -1.00 \end{array} \right) \tag{45}$$

$$\delta_0(PRO) + w_{PRO, NN} + w_{NN, show} = 1.00 + 1.00 + -1.00 = 1.00$$

$$\delta = \begin{array}{c} \text{What}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB & 0.00 & 2.00 \\ O.00 & 1.00 \\ PRO & 1.00 & 1.00 \\ NN & -1.00 & 1.00 \\ \end{array} \right) \tag{45}$$

$$\delta_1(NN) + w_{NN, VB} + w_{VB, can} = 1.00 + 1.00 + 1.00 = 3.00$$

$$\delta = \begin{array}{c} \text{What}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB & 0.00 & 2.00 & 3.00 \\ 0.00 & 1.00 & \\ PRO & 1.00 & 1.00 \\ NN & -1.00 & 1.00 \\ \end{array} \right) \tag{45}$$

$$\delta_1(VB) + w_{VB, DET} + w_{DET, can} = 2.00 + 1.00 + -1.00 = 2.00$$

$$\delta = \begin{array}{c} \text{What}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB \\ \delta = \begin{array}{c} O.00 & 2.00 & 3.00 \\ 0.00 & 1.00 & 2.00 \\ PRO \\ NN & -1.00 & 1.00 \\ \end{array} \right) \tag{45}$$

$$\delta_1(VB) + w_{VB, PRO} + w_{PRO, can} = 2.00 + 0.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{what}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB \\ \delta = \begin{array}{c} O.00 & 2.00 & 3.00 \\ 0.00 & 1.00 & 2.00 \\ PRO \\ NN & -1.00 & 1.00 \end{array} \right) \tag{45}$$

$$\delta_1(VB) + w_{VB, NN} + w_{NN, can} = 2.00 + 0.00 + 0.00 = 2.00$$

$$\delta = \begin{array}{c} \text{What}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB \\ 0.00 & 2.00 & 3.00 \\ 0.00 & 1.00 & 2.00 \\ 1.00 & 1.00 & 2.00 \\ NN & -1.00 & 1.00 & 2.00 \\ \end{array} \right) \tag{45}$$

$$\delta_2(NN) + w_{NN, VB} + w_{VB, silence} = 2.00 + 1.00 + -1.00 = 2.00$$

$$\delta = \begin{array}{c} \text{What}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB & 0.00 & 2.00 & 3.00 & 2.00 \\ 0.00 & 1.00 & 2.00 & \\ PRO & 1.00 & 1.00 & 2.00 \\ NN & -1.00 & 1.00 & 2.00 \\ \end{array} \right) \tag{45}$$

$$\delta_2(VB) + w_{VB, DET} + w_{DET, silence} = 3.00 + 1.00 + 0.00 = 4.00$$

$$\delta = \begin{array}{c|ccccc} & \text{what}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB & 0.00 & 2.00 & 3.00 & 2.00 \\ \hline DET & 0.00 & 1.00 & 2.00 & 4.00 \\ PRO & 1.00 & 1.00 & 2.00 \\ NN & -1.00 & 1.00 & 2.00 \\ \end{array} \right) \tag{45}$$

$$\delta_2(VB) + w_{VB, PRO} + w_{PRO, silence} = 3.00 + 0.00 + 0.00 = 3.00$$

$$\delta = \begin{array}{c} \text{What}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB \\ \delta = \begin{array}{c} O.00 & 2.00 & 3.00 & 2.00 \\ 0.00 & 1.00 & 2.00 & 4.00 \\ 1.00 & 1.00 & 2.00 & 3.00 \\ -1.00 & 1.00 & 2.00 & \end{array} \right) \tag{45}$$

$$\delta_2(VB) + w_{VB, NN} + w_{NN, silence} = 3.00 + 0.00 + 1.00 = 4.00$$

$$\delta = \begin{array}{c|ccccc} & \text{what}_0 & \text{show}_1 & \text{can}_2 & \text{silence}_3 \\ VB & 0.00 & 2.00 & 3.00 & 2.00 \\ \hline 0.00 & 1.00 & 2.00 & 4.00 \\ PRO & 1.00 & 1.00 & 2.00 & 3.00 \\ NN & -1.00 & 1.00 & 2.00 & 4.00 \\ \end{array} \right) \tag{45}$$

Decoding Sentence 6

Scores

$$\delta = \begin{array}{c} VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 0.00 & 2.00 & 3.00 & 2.00 \\ 0.00 & 1.00 & 2.00 & 4.00 \\ 1.00 & 1.00 & 2.00 & 3.00 \\ -1.00 & 1.00 & 2.00 & 4.00 \\ \end{pmatrix} \tag{45}$$

Backpointers

$$\beta = \begin{cases} \text{Show}_1 & \text{can}_2 & \text{silence}_3 \\ \text{VB} & PRO & NN & NN \\ \text{VB} & VB & VB \\ PRO & VB & VB \\ PRO & VB & VB \\ PRO & VB & VB \\ \end{cases}$$
(46)

Decoding Sentence 6

Scores

$$\delta = \begin{array}{c} VB \\ DET \\ PRO \\ NN \end{array} \begin{pmatrix} 0.00 & 2.00 & 3.00 & 2.00 \\ 0.00 & 1.00 & 2.00 & 4.00 \\ 1.00 & 1.00 & 2.00 & 3.00 \\ -1.00 & 1.00 & 2.00 & 4.00 \\ \end{pmatrix} \tag{45}$$

Backpointers

$$\beta = \begin{cases} VB & Show_1 & can_2 & silence_3 \\ VB & PRO & NN & NN \\ VB & VB & VB \\ PRO & VB & VB \\ \end{cases}$$
(46)

Decoding Sentence 6

Scores

$$\delta = \begin{array}{c} VB \\ DET \\ NN \end{array} \begin{pmatrix} 0.00 & 2.00 & 3.00 & 2.00 \\ 0.00 & 1.00 & 2.00 & 4.00 \\ 1.00 & 1.00 & 2.00 & 3.00 \\ -1.00 & 1.00 & 2.00 & 4.00 \\ \end{pmatrix} \tag{45}$$

Backpointers

$$\beta = \frac{\text{VB}}{\text{PRO}} \begin{pmatrix} PRO & NN & NN \\ VB & VB & VB \\ PRO & PRO & VB & VB \\ PRO & VB & VB \end{pmatrix}$$

$$(46)$$

Reconstruction: PRO NN VB DET

Correct answer: PRO NN VB VB

Prediction: PRO NN VB DET

Correct answer: PRO NN VB VB

Prediction: PRO NN VB DET

Correct answer: PRO NN VB VB

Prediction: PRO NN VB DET

Gold Features

(VB, silence)

(VB, VB)

Shared Features

(NN, show) (VB, can) (PRO, NN) (NN, VB)

(START, PRO)

(PRO, what)

Predicted Features

(DET, silence)

(VB, DET)

- Correct answer: PRO NN VB VB
- Prediction: PRO NN VB DET

Gold Features

(VB, silence) (VB, VB)

Shared Features

(NN, show) (VB, can) (PRO, NN) (NN, VB) (START, PRO) (PRO, what)

Predicted Features

(DET, silence) (VB, DET)

```
New feature vector: (DET, DET): -1.00; (DET, NN): 1.00; (DET, VB): -1.00; (DET, can): -1.00; (DET, demand): -1.00; (DET, silence): -1.00; (DET, the): 1.00; (NN, DET): -1.00; (NN, VB): 1.00; (NN, demand): 1.00; (NN, show): -1.00; (NN, silence): 1.00; (PRO, NN): 1.00; (PRO, you): 1.00; (VB, can): 1.00; (VB, show): 1.00; (VB, the): -1.00; (VB, you): -1.00; (START, NN): -1.00; (START, PRO): 1.00
```

- Correct answer: PRO NN VB VB
- Prediction: PRO NN VB DET

Gold Features

(VB, silence) (VB, VB)

Shared Features

(NN, show) (VB, can) (PRO, NN) (NN, VB) (START, PRO) (PRO, what)

Predicted Features

(DET, silence) (VB, DET)

```
New feature vector: (DET, DET): -1.00; (DET, NN): 1.00; (DET, VB): -1.00; (DET, can): -1.00; (DET, demand): -1.00; (DET, silence): -1.00; (DET, the): 1.00; (NN, DET): -1.00; (NN, VB): 1.00; (NN, demand): 1.00; (NN, show): -1.00; (NN, silence): 1.00; (PRO, NN): 1.00; (PRO, you): 1.00; (VB, can): 1.00; (VB, show): 1.00; (VB, the): -1.00; (VB, you): -1.00; (START, NN): -1.00; (START, PRO): 1.00
```