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Project Title: Predicting Evolving Graphs from an Inverse Perspective

In searching through the application of inverse problems in my field of interest, I stumbled upon the use of inverse techniques in generating evolving graphs<sup>1</sup>. In particular, the range of two vertices in the graph is computed based upon the current state of the graph. Our input  $x$  would be the range of the two systems, the model  $A$  (which is generally approximated) is given as some way to view the range as a probability distribution. Finally, our solution  $b$  is the graph in its current state. Given  $b$  and approximating for  $A$ , the researchers sought to approximate what possible range values  $x$  could hold for the graph.

Given this application of inverse problems in graph theory, I feel that I could apply similar logic to evolving graphs. The paper focused on only one potential way of modeling  $A$ , which greatly impacted the results that could be derived. Given that not all graphs have similar ranges, my project plans on experimenting with other approximations for  $A$  in order to find a suitable solution range  $x$ . The paper also applied this knowledge by performing simulations on the evolving graphs using this data. Similarly, my project aims to try out these approximations for  $x$  by running simulations to determine if the evolving graphs seem to be reasonable predictions for what has already occurred.

By doing this project, I hope to learn a lot of information in my field - including more about evolving graphs, random algorithms, and large-scale graph programming. I also hope to apply some of the skills I've learned in this course to a problem that interests me. In evaluating its success, I mostly plan on looking at a few datasets (likely related to hyperlink networks) and seeing if my predictions for  $x$  result in a reasonable evolving graph that applies to some problems. I also hope to try out some other methods for approximating  $A$  and completing the inverse problem, even if not many of them lead to a successful approximation.

I plan to write a bit of software in either MATLAB or python when it comes to running tests on the approximations. However, I first plan on attempting solving the inverse problem using various techniques to see what I can derive analytically. I am hopeful that I can find at least a couple of reasonable approximations for the data.

Finally, if this project ends up being far too daunting, I may also be open to writing part of the regularization toolkit in python. But I do hope to at least attempt this project for now and learn a lot from it.

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<sup>1</sup> <https://royalsocietypublishing.org/doi/pdf/10.1098/rspa.2009.0456#purchaseArea>