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RA: 168.813
RA: 168.880
RA: 170.453
RA: 169.259

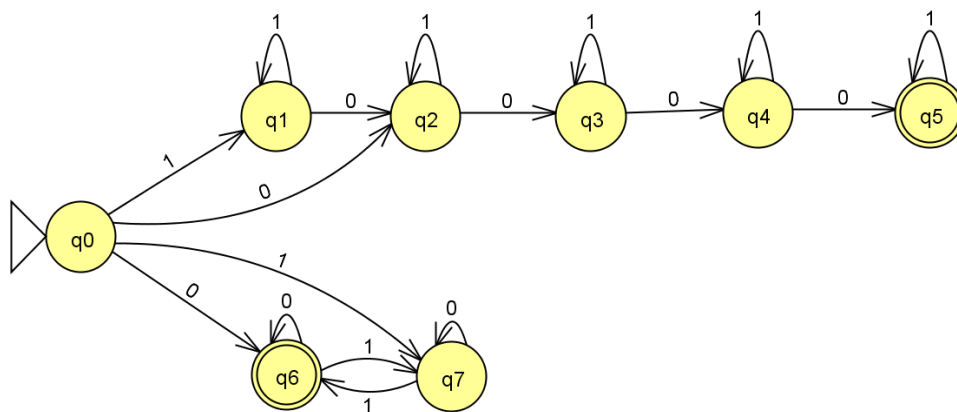
Projetos

LFA / Teoria da Computação

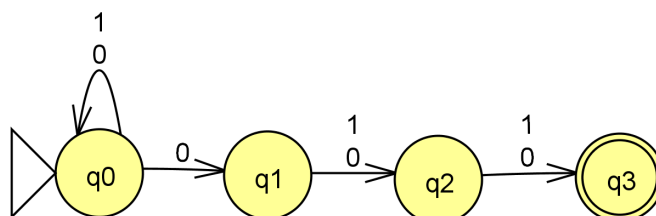
Projeto 03

∴ Projetar um NFA para as seguintes linguagens (considere $\Sigma = \{0, 1\}$).

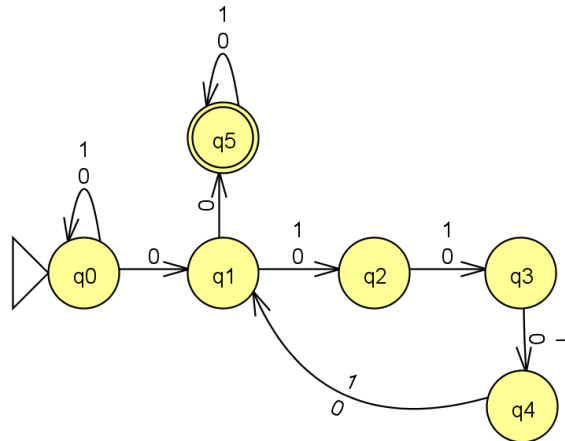
A) $L_1 = \{w \mid w \text{ contém exatamente 4 0's ou um número par de 1's}\}$ (8 estados)



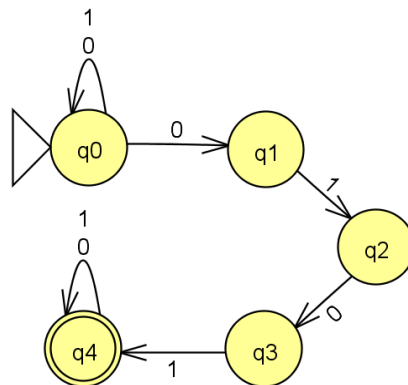
B) $L_2 = \{w \mid w \text{ possui o terceiro símbolo a partir da direita igual a 0}\}$ (4 estados)



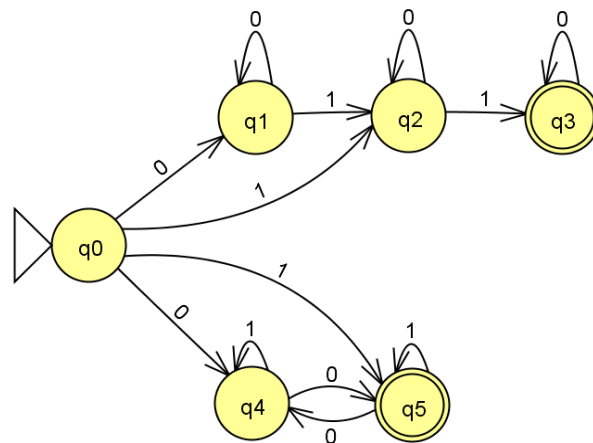
C) $L_3 = \{w \mid w \text{ possui dois 0's separados por um string de comprimento } 4i \text{ para algum } i \geq 0\}$ (6 estados)



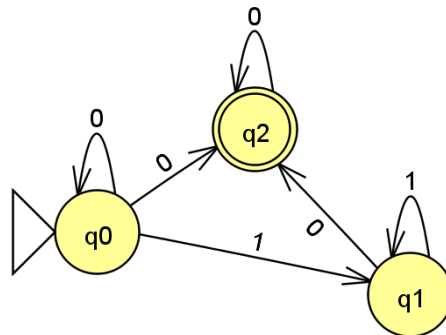
D) $L_4 = \{w \mid w \text{ contém a substring } 0101\}$ (5 estados)



E) $L_5 = \{w \mid w \text{ contém um número par de 0's ou exatamente dois 1's}\}$ (6 estados)



F) $L_6 = \{w \mid w = 0^*1^*0^*0\}$ (3 estados)²



² 0^* , por exemplo, significa que pode haver qualquer quantidade de 0's (inclusive nenhum).

∴ Função de Transição Estendida para NFAs

Para cada string, aplicar a função de transição estendida para verificar se a string pertence à

linguagem.

A) $L_1 \Rightarrow 00100, 1100$

$$\hat{\delta}(q_0, 00100) = \delta(\hat{\delta}(q_0, 0010), 0) = \delta(q_4, 0) \cup \delta(q_7, 0) = \{q_5\} \cup \{q_7\} = \{q_5, q_7\}$$

$$\hat{\delta}(q_0, 0010) = \delta(\hat{\delta}(q_0, 001), 0) = \delta(q_3, 0) \cup \delta(q_7, 0) = \{q_4\} \cup \{q_7\} = \{q_4, q_7\}$$

$$\hat{\delta}(q_0, 001) = \delta(\hat{\delta}(q_0, 00), 1) = \delta(q_3, 1) \cup \delta(q_6, 1) = \{q_3\} \cup \{q_7\} = \{q_3, q_7\}$$

$$\hat{\delta}(q_0, 00) = \delta(\hat{\delta}(q_0, 0), 0) = \delta(q_2, 0) \cup \delta(q_6, 0) = \{q_3\} \cup \{q_6\} = \{q_3, q_6\}$$

$$\hat{\delta}(q_0, 0) = \delta(\hat{\delta}(q_0, \epsilon), 0) = \delta(q_0, 0) = \{q_2, q_6\}$$

$$\hat{\delta}(q_0, \epsilon) = \{q_0\}$$

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$$\hat{\delta}(q_0, 1100) = \delta(\hat{\delta}(q_0, 110), 0) = \delta(q_2, 0) \cup \delta(q_6, 0) = \{q_3\} \cup \{q_6\} = \{q_3, q_6\}$$

$$\hat{\delta}(q_0, 110) = \delta(\hat{\delta}(q_0, 11), 0) = \delta(q_1, 0) \cup \delta(q_6, 0) = \{q_2\} \cup \{q_6\} = \{q_2, q_6\}$$

$$\hat{\delta}(q_0, 11) = \delta(\hat{\delta}(q_0, 1), 1) = \delta(q_1, 1) \cup \delta(q_7, 1) = \{q_1\} \cup \{q_6\} = \{q_1, q_6\}$$

$$\hat{\delta}(q_0, 1) = \delta(\hat{\delta}(q_0, \epsilon), 1) = \delta(q_0, 1) = \{q_1, q_7\}$$

$$\hat{\delta}(q_0, \epsilon) = \{q_0\}$$

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B) L2 => 0011, 0100

$$\begin{aligned}\hat{\delta}(q_0, 0011) &= \delta(\hat{\delta}(q_0, 001), 1) = \delta(q_0, 1) \cup \delta(q_2, 1) \cup \delta(q_3, 1) = \{q_0\} \cup \{q_3\} \cup \{\epsilon\} = \{q_0, q_3\} \\ \hat{\delta}(q_0, 001) &= \delta(\hat{\delta}(q_0, 00), 1) = \delta(q_0, 1) \cup \delta(q_1, 1) \cup \delta(q_2, 1) = \{q_0\} \cup \{q_2\} \cup \{q_3\} = \{q_0, q_2, q_3\} \\ \hat{\delta}(q_0, 00) &= \delta(\hat{\delta}(q_0, 0), 0) = \delta(q_0, 0) \cup \delta(q_1, 0) = \{q_0, q_1\} \cup \{q_2\} = \{q_0, q_1, q_2\} \\ \hat{\delta}(q_0, 0) &= \delta(\hat{\delta}(q_0, \epsilon), 0) = \delta(q_0, 0) = \{q_0, q_1\} \\ \hat{\delta}(q_0, \epsilon) &= \{q_0\}\end{aligned}$$

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$$\begin{aligned}\hat{\delta}(q_0, 0100) &= \delta(\hat{\delta}(q_0, 010), 0) = \delta(q_0, 0) \cup \delta(q_1, 0) \cup \delta(q_3, 0) = \{q_0, q_1\} \cup \{q_2\} \cup \{\epsilon\} = \{q_0, q_1, q_2\} \\ \hat{\delta}(q_0, 010) &= \delta(\hat{\delta}(q_0, 01), 0) = \delta(q_0, 0) \cup \delta(q_2, 0) = \{q_0, q_1\} \cup \{q_3\} = \{q_0, q_1, q_3\} \\ \hat{\delta}(q_0, 01) &= \delta(\hat{\delta}(q_0, 0), 1) = \delta(q_0, 1) \cup \delta(q_1, 1) = \{q_0\} \cup \{q_2\} = \{q_0, q_2\} \\ \hat{\delta}(q_0, 0) &= \delta(\hat{\delta}(q_0, \epsilon), 0) = \delta(q_0, 0) = \{q_0, q_1\} \\ \hat{\delta}(q_0, \epsilon) &= \{q_0\}\end{aligned}$$

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C) L3 => 0101, 0101101

$$\begin{aligned}\hat{\delta}(q_0, 0101) &= \delta(\hat{\delta}(q_0, 010), 1) = \delta(q_0, 1) \cup \delta(q_1, 1) \cup \delta(q_3, 1) = \{q_0, q_1\} \cup \{q_2\} \cup \{\epsilon\} = \{q_0, q_1, q_2\} \\ \hat{\delta}(q_0, 010) &= \delta(\hat{\delta}(q_0, 01), 0) = \delta(q_0, 0) \cup \delta(q_2, 0) = \{q_0, q_1\} \cup \{q_3\} = \{q_0, q_1, q_3\} \\ \hat{\delta}(q_0, 01) &= \delta(\hat{\delta}(q_0, 0), 1) = \delta(q_0, 1) \cup \delta(q_1, 1) = \{q_0\} \cup \{q_2\} = \{q_0, q_2\} \\ \hat{\delta}(q_0, 0) &= \delta(\hat{\delta}(q_0, \epsilon), 0) = \delta(q_0, 0) = \{q_0, q_1\} \\ \hat{\delta}(q_0, \epsilon) &= \{q_0\}\end{aligned}$$

✗ Não Aceito

$$\begin{aligned}\hat{\delta}(q_0, 0101101) &= \delta(\hat{\delta}(q_0, 010110), 1) = \delta(q_0, 1) \cup \delta(q_1, 1) \cup \delta(q_4, 1) \cup \delta(q_5, 1) = \{q_0\} \cup \{q_2\} \cup \{q_1\} \cup \{q_5\} = \{q_0, q_2, q_1, q_5\} \\ \hat{\delta}(q_0, 010110) &= \delta(\hat{\delta}(q_0, 01011), 0) = \delta(q_0, 0) \cup \delta(q_3, 0) \cup \delta(q_1, 0) = \{q_0, q_1\} \cup \{q_4\} \cup \{q_5\} = \{q_0, q_1, q_4, q_5\} \\ \hat{\delta}(q_0, 01011) &= \delta(\hat{\delta}(q_0, 0101), 1) = \delta(q_0, 1) \cup \delta(q_2, 1) \cup \delta(q_4, 1) = \{q_0\} \cup \{q_3\} \cup \{q_1\} = \{q_0, q_3, q_1\} \\ \hat{\delta}(q_0, 0101) &= \delta(\hat{\delta}(q_0, 010), 1) = \delta(q_0, 1) \cup \delta(q_1, 1) \cup \delta(q_3, 1) = \{q_0\} \cup \{q_2\} \cup \{q_4\} = \{q_0, q_2, q_4\} \\ \hat{\delta}(q_0, 010) &= \delta(\hat{\delta}(q_0, 01), 0) = \delta(q_0, 0) \cup \delta(q_2, 0) = \{q_0, q_1\} \cup \{q_3\} = \{q_0, q_1, q_3\} \\ \hat{\delta}(q_0, 01) &= \delta(\hat{\delta}(q_0, 0), 1) = \delta(q_0, 1) \cup \delta(q_1, 1) = \{q_0\} \cup \{q_2\} = \{q_0, q_2\} \\ \hat{\delta}(q_0, 0) &= \delta(\hat{\delta}(q_0, \epsilon), 0) = \delta(q_0, 0) = \{q_0, q_1\} \\ \hat{\delta}(q_0, \epsilon) &= \{q_0\}\end{aligned}$$

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D) L4 => 0001, 00101

$$\begin{aligned}\hat{\delta}(q_0, 0001) &= \delta(\hat{\delta}(q_0, 000), 1) = \delta(q_0, 1) \cup \delta(q_1, 1) = \{q_0\} \cup \{q_2\} = \{q_0, q_2\} \\ \hat{\delta}(q_0, 000) &= \delta(\hat{\delta}(q_0, 00), 0) = \delta(q_0, 0) \cup \delta(q_1, 0) = \{q_0, q_1\} \cup \{\epsilon\} = \{q_0, q_1\} \\ \hat{\delta}(q_0, 00) &= \delta(\hat{\delta}(q_0, 0), 0) = \delta(q_0, 0) \cup \delta(q_1, 0) = \{q_0, q_1\} \cup \{\epsilon\} = \{q_0, q_1, \epsilon\} \\ \hat{\delta}(q_0, 0) &= \delta(\hat{\delta}(q_0, \epsilon), 0) = \delta(q_0, 0) = \{q_0, q_1\} \\ \hat{\delta}(q_0, \epsilon) &= \{q_0\}\end{aligned}$$

✗ Não Aceito

$$\begin{aligned}\hat{\delta}(q_0, 00101) &= \delta(\hat{\delta}(q_0, 0010), 1) = \delta(q_0, 1) \cup \delta(q_1, 1) \cup \delta(q_3, 1) = \{q_0\} \cup \{q_2\} \cup \{q_4\} = \{q_0, q_2, q_4\} \\ \hat{\delta}(q_0, 0010) &= \delta(\hat{\delta}(q_0, 001), 0) = \delta(q_0, 0) \cup \delta(q_2, 0) = \{q_0, q_1\} \cup \{q_3\} = \{q_0, q_1, q_3\} \\ \hat{\delta}(q_0, 001) &= \delta(\hat{\delta}(q_0, 00), 1) = \delta(q_0, 1) \cup \delta(q_1, 1) = \{q_0\} \cup \{q_2\} = \{q_0, q_2\} \\ \hat{\delta}(q_0, 00) &= \delta(\hat{\delta}(q_0, 0), 0) = \delta(q_0, 0) \cup \delta(q_1, 0) = \{q_0, q_1\} \cup \{\epsilon\} = \{q_0, q_1\} \\ \hat{\delta}(q_0, 0) &= \delta(\hat{\delta}(q_0, \epsilon), 0) = \delta(q_0, 0) = \{q_0, q_1\} \\ \hat{\delta}(q_0, \epsilon) &= \{q_0\}\end{aligned}$$

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E) L5 => 0001, 0101

$$\begin{aligned}\hat{\delta}(q_0, \epsilon) &= \{q_0\} \\ \hat{\delta}(q_0, 0) &= \delta(\hat{\delta}(q_0, \epsilon), 0) = \{q_1, q_4\} \\ \hat{\delta}(q_0, 00) &= \delta(\hat{\delta}(q_0, 0), 0) = \delta(q_1, 0) \cup \delta(q_4, 0) = \{q_1, q_5\} \\ \hat{\delta}(q_0, 000) &= \delta(\hat{\delta}(q_0, 00), 0) = \delta(q_1, 0) \cup \delta(q_5, 0) = \{q_1, q_4\} \\ \hat{\delta}(q_0, 0001) &= \delta(\hat{\delta}(q_0, 000), 1) = \delta(q_1, 1) \cup \delta(q_4, 1) = \{q_2, q_4\}\end{aligned}$$

✗ Não Aceito

$$\begin{aligned}\hat{\delta}(q_0, \epsilon) &= \{q_0\} \\ \hat{\delta}(q_0, 0) &= \delta(\hat{\delta}(q_0, \epsilon), 0) = \{q_1, q_4\} \\ \hat{\delta}(q_0, 01) &= \delta(\hat{\delta}(q_0, 0), 1) = \delta(q_1, 1) \cup \delta(q_4, 1) = \{q_2, q_4\} \\ \hat{\delta}(q_0, 010) &= \delta(\hat{\delta}(q_0, 01), 0) = \delta(q_2, 0) \cup \delta(q_4, 0) = \{q_2, q_5\} \\ \hat{\delta}(q_0, 0101) &= \delta(\hat{\delta}(q_0, 010), 1) = \delta(q_2, 1) \cup \delta(q_5, 1) = \{q_3, q_5\}\end{aligned}$$

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F) L6 => 00110, 01010

$$\begin{aligned}\hat{\delta}(q_0, \epsilon) &= \{q_0\} \\ \hat{\delta}(q_0, 0) &= \delta(\hat{\delta}(q_0, \epsilon), 0) = \{q_0, q_2\} \\ \hat{\delta}(q_0, 00) &= \delta(\hat{\delta}(q_0, 0), 0) = \delta(q_0, 0) \cup \delta(q_2, 0) = \{q_0, q_2\} \\ \hat{\delta}(q_0, 001) &= \delta(\hat{\delta}(q_0, 00), 1) = \delta(q_0, 1) \cup \delta(q_2, 1) = \{q_1\} \\ \hat{\delta}(q_0, 0011) &= \delta(\hat{\delta}(q_0, 001), 1) = \delta(q_1, 1) = \{q_1\} \\ \hat{\delta}(q_0, 00110) &= \delta(\hat{\delta}(q_0, 0011), 0) = \delta(q_1, 0) = \{q_2\}\end{aligned}$$

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$$\begin{aligned}\hat{\delta}(q_0, \epsilon) &= \{q_0\} \\ \hat{\delta}(q_0, 0) &= \delta(\hat{\delta}(q_0, \epsilon), 0) = \{q_0, q_2\} \\ \hat{\delta}(q_0, 01) &= \delta(\hat{\delta}(q_0, 0), 1) = \delta(q_0, 1) \cup \delta(q_2, 1) = \{q_1\} \\ \hat{\delta}(q_0, 010) &= \delta(\hat{\delta}(q_0, 01), 0) = \delta(q_1, 0) = \{q_2\} \\ \hat{\delta}(q_0, 0101) &= \delta(\hat{\delta}(q_0, 010), 1) = \delta(q_2, 1) = \{\} \\ \hat{\delta}(q_0, 01010) &= \delta(\hat{\delta}(q_0, 0101), 0) = \{\}\end{aligned}$$

✗ Não Aceito