



Course Code : CST204  
Course Name : Data Structures  
Lecturer : Dr. Raja Majid Mehmood  
Academic Session : 2023/09  
Assessment Title : Assignment –  
Sorting, Search, and Graph Algorithms  
Submission Due Date : 28<sup>th</sup> December 2023

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Mark:

### **Own Work Declaration**

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Signature:



Date: 28<sup>th</sup> December 2023

## C++ Code

### Question 1:

```
#include <iostream>

#include <stack>

using namespace std;

int main() {

    //Input elements 85, 75, 95, 80
    int a[] = {85, 75, 95, 80}, n = 4;

    //Create original stack (st)
    stack<int> st;

    //Push the elements into the stack
    cout << "(1) push the elements ";
    for (int i = 0; i < n; i++) {
        cout << a[i] << ", ";
        st.push(a[i]);
    }

    cout << " onto the stack st." << endl;

    cout << "(2) the process of sorting elements of stack st is:" << endl;

    //Create a temporary extra stack (tmpst)
    stack<int> tmpst;
```

```

while (!st.empty()) {
    //Obtain the top element from the st and assign to tmp
    int tmp = st.top();

    //Pop out the element from the st
    st.pop();

    cout << "\tst: pop out " << tmp << "=>" << endl;

    //If stack tmpst is not empty
    while (!tmpst.empty()) {
        cout << "\t\ttmpst: get the top element " << tmpst.top() << endl;

        //Making sure to push tmpst top element until tmpst top element becomes
        smaller than tmp.
        if (tmpst.top() > tmp) {
            cout << "\t\t\tSince " << tmpst.top() << " > " << tmp << " tmpst: pop out "
            << tmpst.top() << endl;

            cout << "\t\t\tst: push " << tmpst.top() << endl;

            //Push the element from tmpst onto st
            st.push(tmpst.top());

            //Pop out tmpst element
            tmpst.pop();
        }
        else
        {
            cout << "\t\t\tSince " << tmpst.top() << " < " << tmp << ", exit the loop" <<
            endl;

            break;
        }
    }
}

```

```

    }

}

cout << "\t\ttmpst: push " << tmp << endl;

//If stack tmpst is empty, push tmp onto tmpst
tmpst.push(tmp);

cout << endl;

}

//If tmpst is not empty
while (!tmpst.empty()) {

    //Push remaining elements from tmpst to the st
    st.push(tmpst.top());

    //Pop the top element from tmpst
    tmpst.pop();

}

cout << "(3) the sorting of stack st ends." << endl;

cout << "(4) the popping sequence of st is: ";

while (!st.empty()) {

    //Print out the sorted numbers on screen
    cout << st.top() << " ";

    //Pop out the top element of st
    st.pop();

}

```

```
cout << endl;  
  
return 0;  
}
```

**Question 2 - Case A:**

```
#include <iostream>

#include <stdlib.h>

#include <time.h>

using namespace std;

class Node {
public:
    int val;
    int weight;
    Node* next;

    Node(int x, int w) //Constructor
    {
        val = x ;
        weight = w;
        next = NULL;
    }
};

class List {
public:
    Node* head;

    List(void) //Constructor
    {
```

```

        head = NULL;
    }

};

class Graph {
public:
    int vt;
    List* array;

    Graph(int vertices) //Constructor
    {
        vt = vertices;
        array = new List[vertices];
    }

    //addEdge is to add an edge between two vertices
    //source = source vertex, dest = destination vertex, x=weight of the edge
    void addEdge(int source, int dest, int x) {
        //Create new Node with given vertex(dest) and weight (x)
        Node* temp = new Node(dest, x);

        //Update next pointer of newly created Node object temp to point to current head
        of the adjacency list for source vertex
        temp->next = array[source].head;

        //Assign temp pointer to head member variable of the list object at index source
        in the array
        array[source].head = temp;
    }
}

```



```
//numEdge to count total number of edges in the graph

int numEdge() {
    int counter = 0;

    //To iterate over all vertices in the graph
    for (int i = 0; i < vt; i++) {
        //Declare temp and initialize with value of head member variable at index i in
array
        Node* temp = array[i].head;

        //Loop until there are no more Nodes
        while (temp != NULL) {
            temp = temp->next;
            counter++;
        }
    }

    return counter;
}
};
```

```
// Case A Sparse Graph - 100x100
```

```
int main(){
    int vertices = 1000;
    int edges;

    Graph gr(vertices);

    srand(time(0));
```

```
//Add edges with random source and destination vertices and random weight
for (int i = 0; i < (100 * 100); i++) {
    gr.addEdge(rand() % 1000, rand() % 1000, rand());
}

//Count total number of edges
edges = gr.numEdge();
cout << "The total number of edges for Case A is " << edges;
cout << endl;

return 0;
}
```

**Question 2 - Case B:**

```
#include <iostream>
#include <stdlib.h>
#include <time.h>
using namespace std;

class Node {
public:
    int val;
    int weight;
    Node* next;
```

```
Node(int x, int w) //Constructor
{
    val = x ;
    weight = w;
    next = NULL;
}
};
```

```
class List {
public:
    Node* head;

    List(void) //Constructor
    {
        head = NULL;
    }

};
```

```
class Graph {
public:
    int vt;
    List* array;

    Graph(int vertices) //Constructor
    {
        vt = vertices;
```

```

    array = new List[vertices];
}

//addEdge is to add an edge between two vertices

//source = source vertex, dest = destination vertex, x=weight of the edge
void addEdge(int source, int dest, int x) {
    //Create new Node with given vertex(dest) and weight (x)
    Node* temp = new Node(dest, x);
    //Update next pointer of newly created Node object temp to point to current head
    of the adjacency list for source vertex
    temp->next = array[source].head;
    //Assign temp pointer to head member variable of the list object at index source
    in the array
    array[source].head = temp;
}

//numEdge to count total number of edges in the graph
int numEdge() {
    int counter = 0;
    //To iterate over all vertices in the graph
    for (int i = 0; i < vt; i++) {
        //Declare temp and initialize with value of head member variable at index i in
        array
        Node* temp = array[i].head;
        //Loop until there are no more Nodes
        while (temp != NULL) {
            temp = temp->next;
            counter++;
        }
    }
}

```

```

    }

    }

    return counter;

}

};

// Case B Dense Graph - 600x600

int main(){

    int vertices = 1000;

    int edges;

    Graph gr(vertices);

    srand(time(0));

    //add edges with random source and destination vertices and random weight
    for (int i = 0; i < (600 * 600); i++) {

        gr.addEdge(rand() % 1000, rand() % 1000, rand());

    }

    //count total number of edges

    edges = gr.numEdge();

    cout << "The total number of edges for Case B is " << edges;

    cout << endl;

    return 0;

}

```

**Question 2 - Case C:**

```
#include <iostream>

#include <stdlib.h>

#include <time.h>

using namespace std;

class Node {
public:
    int val;
    int weight;
    Node* next;

    Node(int x, int w) //Constructor
    {
        val = x ;
        weight = w;
        next = NULL;
    }
};

class List {
public:
    Node* head;

    List(void) //Constructor
    {
```

```

        head = NULL;
    }

};

class Graph {
public:
    int vt;
    List* array;

    Graph(int vertices) //Constructor
    {
        vt = vertices;
        array = new List[vertices];
    }

    //addEdge is to add an edge between two vertices
    //source = source vertex, dest = destination vertex, x=weight of the edge
    void addEdge(int source, int dest, int x) {
        //Create new Node with given vertex(dest) and weight (x)
        Node* temp = new Node(dest, x);

        //Update next pointer of newly created Node object temp to point to current head
        of the adjacency list for source vertex
        temp->next = array[source].head;

        //Assign temp pointer to head member variable of the list object at index source
        in the array
        array[source].head = temp;
    }
}

```

```
//numEdge to count total number of edges in the graph

int numEdge() {
    int counter = 0;

    //To iterate over all vertices in the graph
    for (int i = 0; i < vt; i++) {
        //Declare temp and initialize with value of head member variable at index i in
        array
        Node* temp = array[i].head;

        //Loop until there are no more Nodes
        while (temp != NULL) {
            temp = temp->next;
            counter++;
        }
    }

    return counter;
}

};
```

```
// Case C Complete Graph - 1000 x 1000
```

```
int main(){
    int vertices = 1000;
    int edges;

    Graph gr(vertices);

    srand(time(0));
```



```
//Add edges with random source and destination vertices and random weight
for (int i = 0; i < 1000; i++) {
    for (int j = 0; j < 1000; j++) {
        gr.addEdge(i, j, rand());
    }
}

//Count total number of edges
edges = gr.numEdge();

cout << "The total number of edges for Case C is " << edges;

cout << endl;

return 0;
}
```

**Question 3:**

```
#include <iostream>

#include <stdlib.h>

#include <time.h>

#include <algorithm>

#include <cmath>

using namespace std;


// initialise array with random data

void generateRandom(int a[], int SIZE)

{

    for (int i = 0; i < SIZE; ++i)

    {

        a[i] = rand() % SIZE; // generate value in range from 0 to SIZE-1 inclusive

    }

}


// to sort an array

void doSortedList(int a[], int SIZE)

{

    sort(a, a + SIZE); //sort array a using the range from a's first element address to
a+SIZE address(last element)

}


// implement binary search and Count at every midpoint visit

int findByBinSearch(int key, int a[], int SIZE)
```

```

{
    int low = 0;
    int high = SIZE - 1;
    int mid;
    int counter = 0;

    while (low <= high)
    {
        counter++;
        mid = (low + high) / 2;

        if (a[mid] < key)
            low = mid + 1;
        else if (a[mid] > key)
            high = mid - 1;
        else
            break;
    }
    if (a[mid] != key)
        return -1;
    else
        return counter;
}

// implement sequential search and Count at every array-index visit
int findBySeqSearch(int key, int a[], int SIZE)
{

```

```

int n = SIZE;

int i;

int counter = 0;

for (i = 0; i < SIZE; i++)
{
    counter++;

    if (a[i] == key)
    {
        break;
    }

    else if (i == n - 1)
    {
        return -1;
    }
}

return i + 1;
}

int main()
{
    srand(time(0));

    //long long int is used to store large values of SIZE

    long long int SIZE = 10;

    cout << "\nSize\t\tComplexity-Sequential\tComplexity-
Binary\t\t(best/avg/worst)\n\t\t\t\t\t\t\tSeq. Cost\tBinary Cost\n\n";

    //Loop again to get different sizes.

    for (int i = 0; i < 8; i++)

```

```

{
    int* a = new int[SIZE];

    // call generateRandom()

    generateRandom(a, SIZE);


    // call doSortedList()

    doSortedList(a, SIZE);

    int searchNum = rand() % SIZE;


    // call both search functions and print information as in Table 1

    int sequence = findBySeqSearch(searchNum, a, SIZE);
    int binary = findByBinSearch(searchNum, a, SIZE);
    string scost, bcost;


    //Calculate sequence cost
    if (sequence == 1)
        scost = "best ";
    else if (sequence == SIZE)
        scost = "worst ";
    else if (sequence > 1 && sequence < SIZE)
        scost = "average ";
    else
        scost = "not found";


    //Calculate binary cost
    if (binary == 1)
        bcost = "best ";

```

```

else if (binary == floor(log2(SIZE)) || binary == floor(log2(SIZE) + 1))
    bcost = "worst ";
else if (binary > 1 && binary < floor(log2(SIZE)))
    bcost = "average ";
else
    bcost = "not found";

//Print out the values
cout << SIZE << "\t\t" << sequence << "\t\t" << binary << "\t\t" << scost <<
"\t\t" << bcost << endl;

SIZE = SIZE * 10;

// Free dynamically allocated memory
delete[] a;
}
return 0;
}

```

## Results and Discussion

### Question 1:

```
(1) push the elements 85,75,95,80, onto the stack st.
(2) the process of sorting elements of stack st is:
    st: pop out 80=>
        tmpst: push 80

    st: pop out 95=>
        tmpst: get the top element 80
            Since 80 < 95, exit the loop
        tmpst: push 95

    st: pop out 75=>
        tmpst: get the top element 95
            Since 95 > 75 tmpst: pop out 95
            st: push 95
        tmpst: get the top element 80
            Since 80 > 75 tmpst: pop out 80
            st: push 80
        tmpst: push 75

    st: pop out 80=>
        tmpst: get the top element 75
            Since 75 < 80, exit the loop
        tmpst: push 80

    st: pop out 95=>
        tmpst: get the top element 80
            Since 80 < 95, exit the loop
        tmpst: push 95

    st: pop out 85=>
        tmpst: get the top element 95
            Since 95 > 85 tmpst: pop out 95
            st: push 95
        tmpst: get the top element 80
            Since 80 < 85, exit the loop
        tmpst: push 85

    st: pop out 95=>
        tmpst: get the top element 85
            Since 85 < 95, exit the loop
        tmpst: push 95

(3) the sorting of stack st ends.
(4) the popping sequence of st is: 75 80 85 95
```

**Explanation:**

1. Initialize an array, 'a,' with a size of 4, and input the elements 85, 75, 95, 80 into it.
2. Create a stack named 'st' and push the elements of array 'a' onto the stack.
3. Establish a temporary stack, 'tmpst.'
4. Execute the outer while loop to iterate through stack 'st,' extracting elements from the top one by one for sorting.
5. Retrieve and store the top element of 'st' in the variable 'tmp' using the expression "int tmp = st.top();"
6. Pop the top element from 'st.'
7. Utilize the inner while loop to compare the top element of 'tmpst' with the current variable 'tmp,' ensuring the elements in 'tmpst' are arranged in descending order.
8. Print the top element of 'tmpst.'
9. If the top element of 'tmpst' is greater than 'tmp,' move it back to 'st' since it should be positioned after the current element.
10. If the top of 'tmpst' is not greater than 'tmp,' let it remain in 'tmpst' as it is already in the correct location and exit the loop.
11. After the inner loop, push the current element 'tmp' onto 'tmpst.'
12. Continue this process until all numbers in 'st' have been moved to 'tmpst' in a sorted manner.
13. If there are any remaining numbers in 'tmpst,' move them back to 'st' in sorted order using a similar process in the last while loop.
14. Finally, print the sorted numbers and pop out the elements of 'st.'



## Question 2:

### Case A

```
cd "/Users/honeyskoko/Library/Mobile Documents/com~apple~CloudDocs/XMUM
UNI/YEAR 2 SEM 1/Data Structures_CST204/Assignment/" && g++ Q2_CaseA.c
pp -o Q2_CaseA && "/Users/honeyskoko/Library/Mobile Documents/
com~apple~CloudDocs/XMUM UNI/YEAR 2 SEM 1/Data Structures_CST204/Assignment/"Q2_CaseA
The total number of edges for Case A is 10000
honeyskoko@MacBook-Pro Assignment %
```

### Explanation:

To determine the total number of edges for Case A, the process involves the addition of the specified size of weighted edges, which is  $100 \times 100$ . This is achieved through a for loop that generates random source and destination vertices along with weights. Subsequently, a counter is initialized to keep track of the cumulative number of edges. The algorithm iterates through all vertices in the graph using a for loop. For each node encountered in the linked list, the counter is incremented, and this process is reiterated until all nodes in the linked list are processed. This cycle is then repeated for the next vertex in the graph. Once all vertices have been processed, the final value of the counter, which is 10,000, is returned.

### Case B

```
cd "/Users/honeyskoko/Library/Mobile Documents/com~apple~CloudDocs/XMUM
UNI/YEAR 2 SEM 1/Data Structures_CST204/Assignment/" && g++ Q2_CaseB.cpp -o Q2_CaseB && "/Users/honeyskoko/Library/Mobile Documents/com~apple~CloudDocs/XMUM UNI/YEAR 2 SEM 1/Data Structures_CST204/Assignment/"Q2_CaseB
The total number of edges for Case B is 360000
honeyskoko@MacBook-Pro Assignment %
```

### Explanation:

To determine the total count of edges for Case B, the procedure involves adding the specified size of weighted edges, totalling  $600 \times 600$ , utilizing a for loop to systematically generate random source and destination vertices along with corresponding weights. A counter is then initialized to monitor the cumulative number of edges systematically. The algorithm iterates through all vertices in the graph using a for loop, incrementing the counter for each node encountered in the linked list until all nodes have been processed. Subsequently, the algorithm transitions to the next vertex, repeating the aforementioned steps. Upon completing the processing of all vertices, the final counter value, amounting to 360,000, is returned as the calculated total number of edges for Case B.

## Case C

```
cd "/Users/honeyskoko/Library/Mobile Documents/com~apple~CloudDocs/XMUM
UNI/YEAR 2 SEM 1/Data Struct%
honeyskoko@MacBook-Pro ~ % cd "/Users/honeyskoko/Library/Mobile Documen
ts/com~apple~CloudDocs/XMUM UNI/YEAR 2 SEM 1/Data Structures_CST204/Ass
ignment/" && g++ Q2_CaseC.cpp -o Q2_CaseC && "/Users/honeyskoko/Library
/Mobile Documents/com~apple~CloudDocs/XMUM UNI/YEAR 2 SEM 1/Data Struct
ures_CST204/Assignment/"Q2_CaseC
The total number of edges for Case C is 1000000
honeyskoko@MacBook-Pro Assignment %
```

### Explanation:

To determine the total number of edges for Case C, the method involves the summation of the specified size of weighted edges, set at 1000 x 1000, utilizing a for loop to generate random source and destination vertices with corresponding weights. A counter is initialized to systematically track the cumulative edge count as the algorithm iterates through all vertices in the graph. For each encountered node in the linked list, the counter increments iteratively until all nodes are processed. The algorithm then proceeds to the next vertex in the graph, repeating the steps. Once all vertices are processed, the final counter value of 1,000,000 is returned as the computed total number of edges for Case C.

### Question 3:

Size	Complexity-Sequential	Complexity-Binary	(best/avg/worst)			
			Seq. Cost	Binary Cost		
10	1	3	best		worst	
100	-1	-1	not found		not found	
1000	799	8	average		average	
10000	8875	10	average		average	
100000	-1	-1	not found		not found	
1000000	849447	17	average		average	
10000000				average		worst
100000000	1948692	23				
1000000000	83952272		27	average	average	worst

d)

### Explanation of Best, Average, Worst and Not Found Cases in Binary Search and Sequential Search

#### Binary Search

1. Best Case: The best-case scenario occurs when the target number is precisely situated at the middle index of the sorted array. In this case, the algorithm performs just a single comparison to identify the target number, representing the most efficient execution of binary search. The output table designates this scenario as the "best."

2. Average Case: The target number is located somewhere in the array but not necessarily at the middle index. With each comparison, the algorithm systematically eliminates approximately half of the remaining entries. While the average complexity is more favorable than the worst case, it is higher than the best case. The output table designates this scenario as the "average."
3. Worst Case: The worst-case scenario unfolds when the target number is positioned at either extreme end of the array, either the first or final index. In such instances, the algorithm necessitates the maximum number of comparisons to pinpoint the target. The worst-case complexity is represented by  $\log_2(\text{SIZE})$ , signifying the maximum number of iterations, where SIZE denotes the size of the array. The output table designates this scenario as the "worst."
4. Not Found Case: If the target element is not discovered during this process, the algorithm continues to iteratively refine the search space until it becomes an empty interval. In this situation, the algorithm returns a special value, represented as -1, signaling that the wanted value is not present in the sorted array.

### **Sequential Search**

1. Best Case: The target number is located at the first index of the sorted array, which the time complexity is the lowest as the algorithm needs to run only one time to compare. The output table indicates "best" for this.
2. Average Case: The target number is situated somewhere in the middle of the sorted array. The time complexity is higher than the best case but lower than the worst case. To locate the desired number, the algorithm must traverse approximately half of the array. The output table designates this scenario as "average."
3. Worst Case: The target number is located at the last index of the sorted array. In this case, the algorithm must explore the entire array and perform SIZE comparisons. This result is the highest time complexity among all cases. The output table indicates "worst" for this.
4. Not Found Case: If the target element is not encountered throughout this process, the algorithm concludes that the element is not present in the collection. To signify this absence, the algorithm commonly returns a special value, denoted as -1, indicating that the search did not locate the desired element in the given collection.

### Explanation of the Output Based on Table 1

1. Size = 10:
  - I. Complexity for sequential search is **1**. The **best** case as the target number is located at the first index.
  - II. Complexity for binary search is **3**. The **worst** case as the target number is found with the largest number of iterations.
2. Size = 100:
  - I. Complexity for sequential search is **-1**. The target number is **not found**.
  - II. Complexity for binary search is **-1**. The target number is **not found**.
3. Size = 1000:
  - I. Complexity for sequential search is **799**. The **average** case as the target number is located somewhere at the middle of the sorted array.
  - II. Complexity for binary search is **8**. The **average** case as the target number is located somewhere but not in the middle of the sorted array.
4. Size = 10000:
  - I. Complexity for sequential search is **8875**. The **average** case as the target number is located somewhere at the middle of the sorted array.
  - II. Complexity for binary search is **10**. The **average** case as the target number is located somewhere but not in the middle of the sorted array.
5. Size = 100000:
  - I. Complexity for sequential search is **-1**. The target number is **not found**.
  - II. Complexity for binary search is **-1**. The target number is **not found**.
6. Size = 1000000:
  - I. Complexity for sequential search is **849447**. The **average** case as the target number is located somewhere at the middle of the sorted array.
  - II. Complexity for binary search is **17**. The **average** case as the target number is located somewhere but not in the middle of the sorted array.
7. Size = 10000000:
  - I. Complexity for sequential search is **1948692**. The **average** case as the target number is located somewhere at the middle of the sorted array.
  - II. Complexity for binary search is **23**. The **worst** case as the target number is found with the largest number of iterations.
8. Size = 100000000:
  - I. Complexity for sequential search is **83952272**. The **average** case as the target number is located somewhere at the middle of the sorted array.
  - II. Complexity for binary search is **27**. The **worst** case as the target number is found with the largest number of iterations.

All in all, sequential search is more effective for smaller sizes due to its better sequential cost compared to binary search. It performs well in best and average cases, while binary search is preferable for larger sizes because it has a lower time complexity, making it more efficient in handling larger datasets, despite having more unfavourable worst-case scenarios.

**APPENDIX 1**

**MARKING RUBRICS**

Component Title	Assignment: Tasks 1 to 3			Percentage (%)	
Criteria	Score and Descriptors			Weight (%)	Marks
	(5)	(3-4)	(0-2)		
Task 1) Stack-based Sorting	Completed 100% of task requirements & Delivered on time, and in correct format & Student explained perfectly in results section	Completed 100% of task requirements & Delivered on time, and in correct format & Student has minor problem in explanation in result section	Completed less than 50% of the requirements. or Runtime issues or Does not comply with requirements (does something other than requirements). or Student does not explain enough in result section	5	
Task 2) Graph Data structure	Completed 100% of task requirements & Delivered on time, and in correct format & Student explained perfectly in results section	Completed 100% of task requirements & Delivered on time, and in correct format & Student has minor problem in explanation in result section	Completed less than 50% of the requirements. or Runtime issues or Does not comply with requirements (does something other than requirements). or Student does not explain enough in result section	5	
Task 3) Search Algorithms	Completed 100% of task requirements & Delivered on time, and in correct format & Student explained perfectly in results section	Completed 100% of task requirements & Delivered on time, and in correct format & Student has minor problem in explanation in result section	Completed less than 50% of the requirements. or Runtime issues or Does not comply with requirements (does something other than requirements). or Student does not explain enough in result section	5	
<b>TOTAL</b>				<b>15</b>	

Note to students: Please print out and attach this appendix together with the submission of coursework.