

MEASURE THEORY AND INTEGRATION

MATH 320, YALE UNIVERSITY, FALL 2022

These are lecture notes for MATH 320, “Measure Theory and Integration” taught by Charlie Smart at Yale University during the fall of 2022. These notes are not official, and have not been proofread by the instructor for the course. These notes live in my lecture notes respository at

<https://github.com/Eph97/Eph97/Math320>.

If you find any errors, please open a bug report describing the error, and label it with the course identifier, or open a pull request so I can correct it.

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SYLLABUS

Syllabus

Instructor	Prof. Charlie Smart, charlie.smart@yale.edu
Lecture	MW 11:35 AM–12:50 PM, Hum 207
Recitation	TBA
Textbook	Real & Complex Analysis
Midterms	TBD
Final	TBD

1 2022-08-31

Following the universal rule for first class, we covered the syllabus and logistics. We then dove into review on the Riemann integral to motivate measure theory. Prof. Smart seemed much more comfortable talking about math than logistics.

1.1 *Course Plan*

- Review Riemann Int
- Abstract Measure Theory (Majority of class)
- Applications in Probability
- Apps in Dynamics
- Some brief apps in geometry

Problem 1.1. The Riemann Integral

Works for most functions of interest but notably

1. Is not closed under important limits
2. It is hard to eneralize to new geometries.