## A Homework Assignment

**Problem 1.** Prove that there are infinitely many prime numbers.

*Proof.* Let S be a set of finitely many primes. Let q be one more than the product of all elements of S. Consider that if q is prime, then there must obviously be at least one prime number which is not enumerated in S. On the other hand, if q is not prime, then by the fundamental theorem of algebra there must exist at least one prime factor of q, and this factor is not included in S since q is not divisible by any elements of S. Thus any finite enumeration of primes is necessarily incomplete.

**Problem 2.** What is the air-speed velocity of an unladen swallow?

Solution. African or European?

**Exercise 3.** Go outside and find some fossils, because fossils are cool.