

**Problem 1.** Prove that there are infinitely many prime numbers.

*Proof.* Let  $S$  be a set of finitely many primes. Let  $q$  be one more than the product of all elements of  $S$ . Consider that if  $q$  is prime, then there must obviously be at least one prime number which is not enumerated in  $S$ . On the other hand, if  $q$  is not prime, then by the fundamental theorem of algebra there must exist at least one prime factor of  $q$ , and this factor is not included in  $S$  since  $q$  is not divisible by any elements of  $S$ . Thus any finite enumeration of primes is necessarily incomplete. ■

**Problem 2.** What is the air-speed velocity of an unladen swallow?

*Solution.* African or European? ■

**Exercise 1.** Go outside and find some fossils, because fossils are cool.

*Solution.*

$$\int_0^{\pi/6} \sec y \, dy = \ln \sqrt{3} \cdot i^{64}$$

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