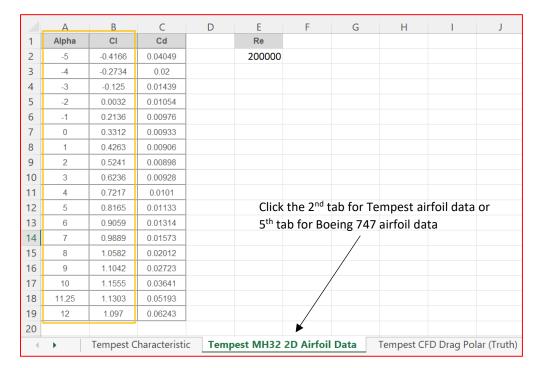


## Step 1A (Page 8 of main doc):

- 1. Lift Curve Comparison (CL vs  $\alpha$ ): Calculate and plot on the same figure the  $C_L$  vs.  $\alpha$  for the 2-D airfoil vs your approximation for a 3-D finite wing.
  - a. Compare and explain the data.
  - b. Make sure discuss the validity of your model based on fundamental aerodynamic concepts.

## Download and open Excel spreadsheet of provided data



Plot  $\alpha$  values on x-axis and  $C_1$  values on y-axis. This gives the plot for your 2D airfoil.

## Step 1B (Page 8 of main doc):

- 1. Lift Curve Comparison (CL vs  $\alpha$ ): Calculate and plot on the same figure the  $C_L$  vs.  $\alpha$  for the 2-D airfoil vs your approximation for a 3-D finite wing.
  - a. Compare and explain the data.
  - b. Make sure discuss the validity of your model based on fundamental aerodynamic concepts.

## Page 4 of main doc:

$$C_L = a \cdot (\alpha - \alpha_{L=0}) \qquad (2)$$

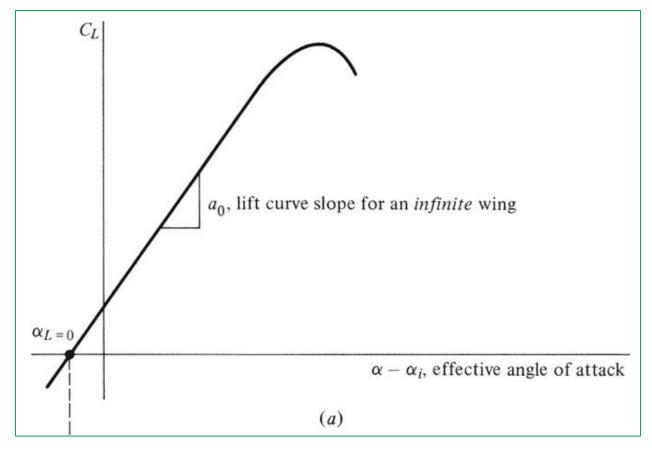
C<sub>L</sub> is ultimately what you want... break down quantities on right hand side until they are known.

$$C_L = \alpha \cdot (\alpha - \alpha_{L=0}) \qquad (2)$$

a is defined from Equation 1 in main doc:

$$a = \frac{dC_L}{d\alpha} = \frac{a_0}{1 + \frac{57.3 \cdot a_0}{\pi \cdot e \cdot AR}} \tag{1}$$

Figure 3 in main doc for reference:



a<sub>0</sub> is defined to be the linear slope of the given 2D data you just plotted in Step 1A

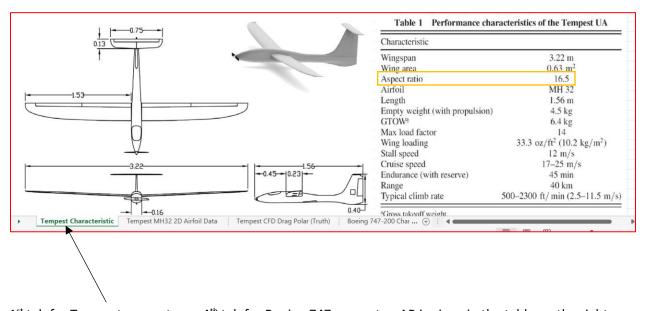
- 1. From what you just plotted, determine what region (i.e. what data points, or what "indices") can most accurately be represented as linear
- 2. On that region, do one of the following... you know how to do this... (from 2012 ofc)
  - Least squares fit
  - Polyfit (yes, you're actually allowed to use this in this class because easier = good!)
  - Some other linear interpolation method... they're really all the same

$$a = \frac{dC_L}{d\alpha} = \frac{a_o}{1 + \frac{57.3 \cdot a_o}{\pi \cdot e \cdot AR}} \qquad (1)$$

Where  $(a_o)$  is the 2-D airfoil lift curve slope in (1/deg) and (e) is the span efficiency factor. For whole aircraft, lift is not just generated by the wing along, but can also be generated by the fuselage and tail surfaces; however, for the purposes of this lab, we will be assuming that the Tempest's wing generates significantly more lift relative to the fuselage and tail and treat the finite wing lift as the total aircraft lift. Additionally, we will assume a span efficiency factor of e = 0.9. Also note that the formulation for the 3-D wing lift coefficient  $C_L$  only models the linear portion of the lift curve slope and not the nonlinear behavior near stall.

$$a = \frac{dC_L}{d\alpha} = \frac{a_o}{1 + \frac{57.3 \cdot a_o}{\pi \cdot e \cdot AR}} \tag{1}$$

Excel spreadsheet with provided data



1<sup>st</sup> tab for Tempest geometry or 4<sup>th</sup> tab for Boeing 747 geometry. AR is given in the table on the right.

Now all variables are known to determine the 3D lift-curve slope (a).

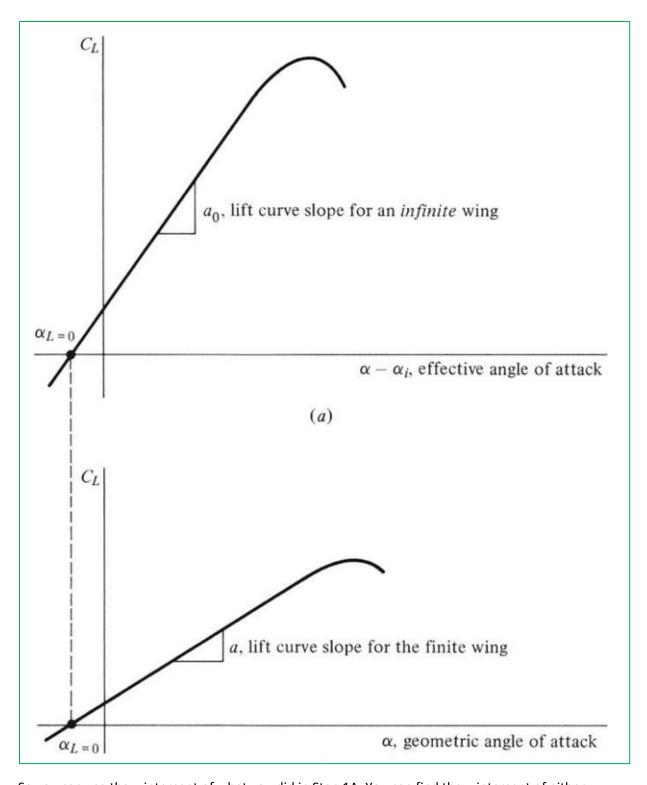
$$a = \frac{dC_L}{d\alpha} = \frac{a_0}{1 + \frac{57.3 \cdot a_0}{\pi \cdot e \cdot AR}} \tag{1}$$

$$C_L = \alpha \cdot (\alpha - \alpha_{L=0}) \qquad (2)$$

Literally just the vector of angle of attack values from the given data. i.e. same x-axis values, different lift coefficient from before.

$$C_L = a \cdot (\alpha - \alpha_{L=0}) \qquad (2)$$

 $\alpha_{L=0}$  is the angle of attack at which no lift is generated (i.e. the x-intercept, or root, of the  $C_L$  vs  $\alpha$  curve). We assume this value is exactly the same between 2D and 3D (as seen from the vertical dashed line in Figure 3)



So you can use the x-intercept of what you did in Step 1A. You can find the x-intercept of either

- The original, given data (least accurate)
- Your interpolation or best-fit line OF that data (more accurate)

Now plot C<sub>L</sub> on top of the previous one, with the same range of AOA values. This new one is for 3D wing.