
ECEN 4138 HW 1 Problem 1 Script

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By: Ian Faber, 09/05/2023

Housekeeping

```
clc; clear; close all;
```

Setup

```
m = 1; % kg
L = 1; % m
g = 9.8; % m/s^2

tspan = [0, 10]; % Simulate from 0 to 10 seconds

theta0 = deg2rad([1,5,25]); % deg -> rad
omega0 = deg2rad([0,0,0]); % deg/s -> rad/s

timeL = cell(1,length(theta0));
stateL = cell(1,length(theta0));
timeNL = cell(1,length(theta0));
stateNL = cell(1,length(theta0));

chartText = strings(length(theta0),1);
thetaText = strings(length(theta0),1);
omegaText = strings(length(theta0),1);

x0 = [theta0; omega0];
```

Simulate

```
for k = 1:length(theta0)

    x0 = [theta0(k); omega0(k)];

    chartText(k) = sprintf("Linear vs. Nonlinear Pendulum Simulation
\n \\theta_0 = %.3f^o and \\omega_0 = %.3f deg/s", rad2deg(theta0(k)),
rad2deg(omega0(k)));
    thetaText(k) = sprintf("\\theta vs. time");
    omegaText(k) = sprintf("\\omega vs. time");
```

```
[tL, sL] = ode45(@(t,state)pendulumEOM(t,state,g,0), tspan, x0); % Linear
EOM

[tNL, sNL] = ode45(@(t,state)pendulumEOM(t,state,g,1), tspan, x0); %
Nonlinear EOM

timeL{k} = tL;
stateL{k} = sL;

timeNL{k} = tNL;
stateNL{k} = sNL;

end

clear tL sL tNL sNL
```

Analyze

```
for k = 1:length(theta0)

    tL = timeL{:,k};
    sL = stateL{:,k};

    tNL = timeNL{:,k};
    sNL = stateNL{:,k};

    thetaL = sL(:,1);
    omegaL = sL(:,2);

    thetaNL = sNL(:,1);
    omegaNL = sNL(:,2);

    figure
    sgtitle(chartText(k))

    subplot(2,1,1)
    hold on; grid on;
    title(thetaText(k))
    plot(tL, rad2deg(thetaL), 'b-')
    plot(tNL, rad2deg(thetaNL), 'r-')
    xlabel("Time [sec]")
    ylabel("\theta [deg]")

    legend("Linear", "Nonlinear")

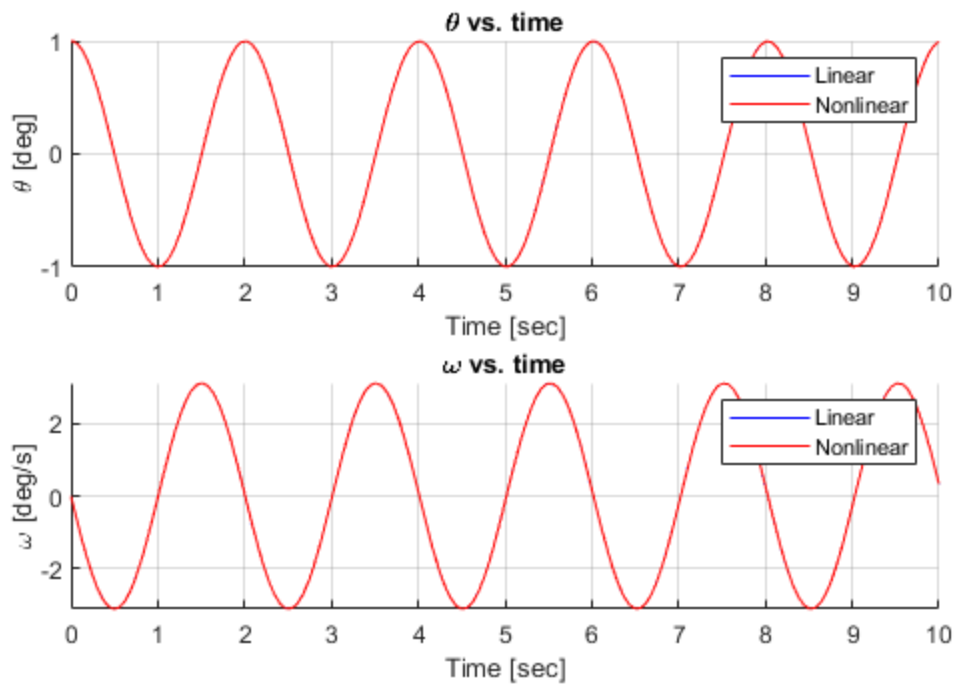
    subplot(2,1,2)
    hold on; grid on;
    title(omegaText(k))
    plot(tL, rad2deg(omegaL), 'b-')
    plot(tNL, rad2deg(omegaNL), 'r-')
    xlabel("Time [sec]")
    ylabel("\omega [deg/s]")
```

```
legend("Linear", "Nonlinear")
```

```
end
```

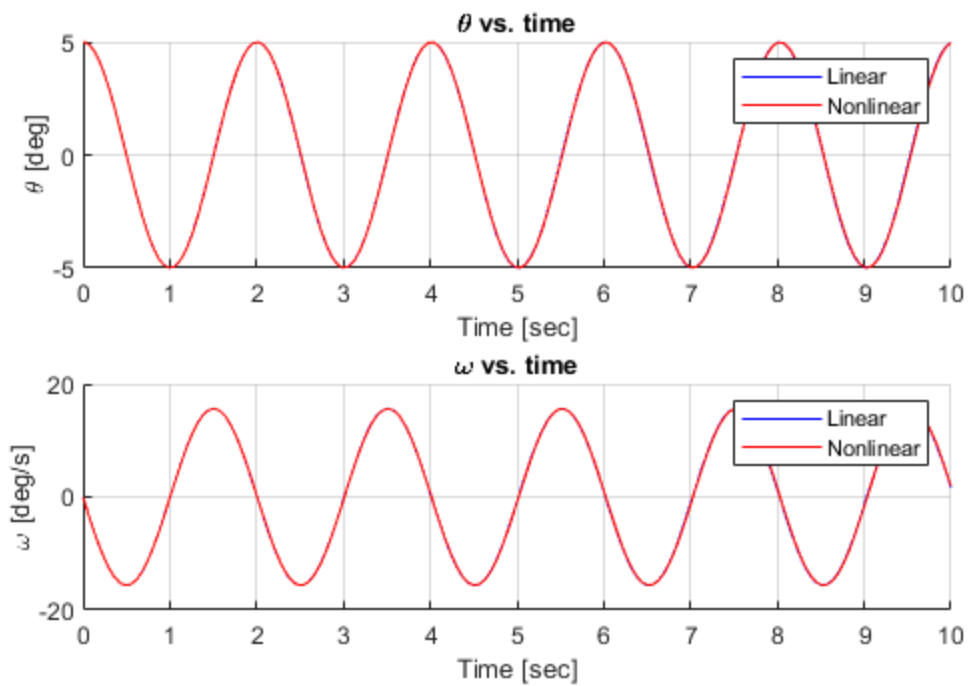
Linear vs. Nonlinear Pendulum Simulation

$\theta_0 = 1.000^\circ$ and $\omega_0 = 0.000$ deg/s



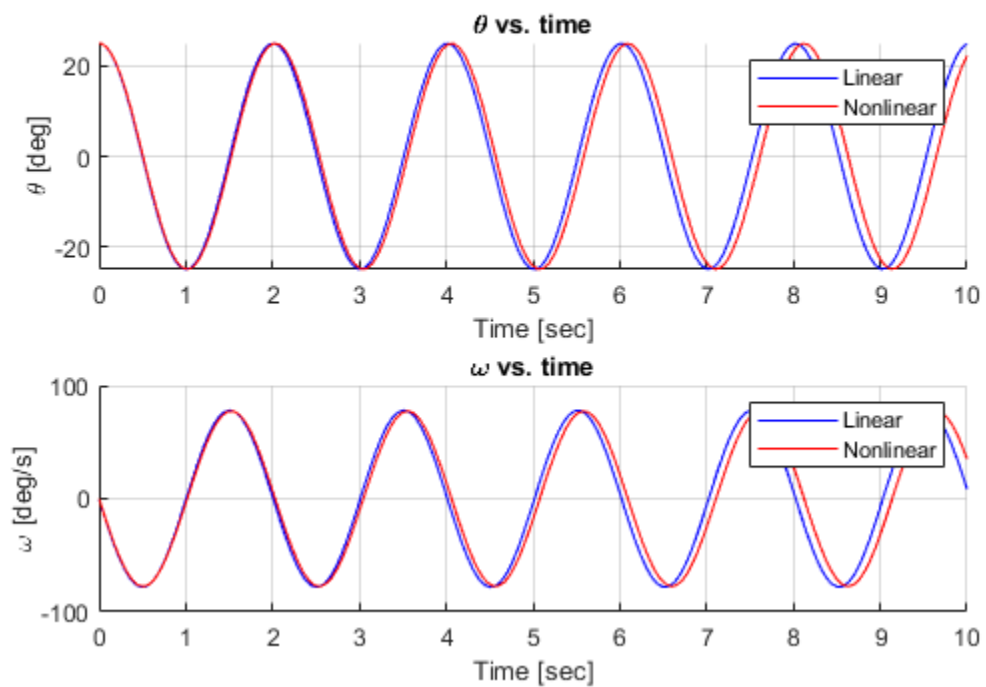
Linear vs. Nonlinear Pendulum Simulation

$$\theta_0 = 5.000^\circ \text{ and } \omega_0 = 0.000 \text{ deg/s}$$



Linear vs. Nonlinear Pendulum Simulation

$$\theta_0 = 25.000^\circ \text{ and } \omega_0 = 0.000 \text{ deg/s}$$



EOM function

```
function dX = pendulumEOM(t,X,g,config)
% EOM function for simulating a simple pendulum with ode45
% Inputs:
%     t: time [sec]
%     X: state vector
%         [ theta; omega ]
%     config: Type of EOM to simulate
%         0 = Linear, 1 = Nonlinear, defaults to linear if not 0 or 1
%
% Outputs:
%     dX: rate of change vector
%         [ omega; alpha ]
%
% By: Ian Faber, 09/05/2023
%

% Extract state variables
theta = X(1);
omega = X(2);

% Choose equation set to simulate
switch config
    case 0 % Linear
        alpha = -g*theta;
    case 1 % Nonlinear
        alpha = -g*sin(theta);
    otherwise % Dumb user
        alpha = -g*theta;
end

dX = [omega; alpha];

end
```

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