CSCB36 Term Test 5 Stephen Guo 1006313231

Question 4

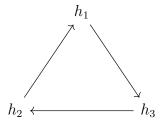
```
a) Define the domain D = {g<sub>1</sub>, g<sub>2</sub>, g<sub>3</sub>, g<sub>4</sub>}
let g<sub>1</sub> be beautiful, and calls g<sub>2</sub>
let g<sub>2</sub> be ugly, and calls g<sub>3</sub>
let g<sub>3</sub> be ugly, and calls g<sub>4</sub>
let g<sub>4</sub> be ugly, and calls g<sub>2</sub>
Let d = g<sub>1</sub>
Then (F<sub>1</sub> ∧ F<sub>2</sub> ∧ F<sub>2</sub>) is satisfied.
This is because d = g<sub>1</sub> is beautiful, so F<sub>1</sub> is satisfied.
g<sub>1</sub> calls g<sub>2</sub>, which is ugly.
g<sub>2</sub> calls g<sub>3</sub>, which is ugly.
g<sub>3</sub> calls g<sub>4</sub>, which is ugly.
g<sub>4</sub> calls g<sub>2</sub>, which is ugly.
So F<sub>2</sub> is satisfied
```

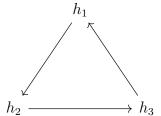
Lastly, no 2 functions call each other, so F_3 is satisfied

 $\therefore (F_1 \wedge F_2 \wedge F_2)$ is satisfied.

b) No, there does not exist a domain $\{h_1, h_2, h_3\}$ such that $(F_1 \wedge F_2 \wedge F_2)$ is satisfied.

Suppose to the contrary that there exist a domain $\{h_1, h_2, h_3\}$ such that $(F_1 \wedge F_2 \wedge F_2)$ is satisfied. In order for F_3 to be satisfied, then no 2 functions call each other, so we have either





Where a function points to the function it calls.

In order to sastify F_2 , then all functions must be ugly since all functions are called.

However, F_3 cannot be satisfied since no functions are beautiful. All functions are called because F_3 is satisfied.

Therefore our supposition was wrong, and there does not exist a domain $\{h_1, h_2, h_3\}$ such that $(F_1 \wedge F_2 \wedge F_2)$ is satisfied.