

Statistical Quality Control :- Applications of statistics to ~~or~~ assure quality of products or items which are outcomes of modern large scale manufacturing process.

Quality of a product or an item is its fitness towards a definite use. Non-conformance means falling short of given specifications or standards. ~~And~~ An instance of non-conformance of an item is called non-conformity. An item containing one or more non-conformities is a non-conforming product or item.

Quality control :-

- (1) Process control.
- (2) Product control.

1. Process control : It attempts to ~~assure~~ <sup>ensure</sup> that a manufacturing process produces a minimum number of non-conforming products.

Tools for Process control

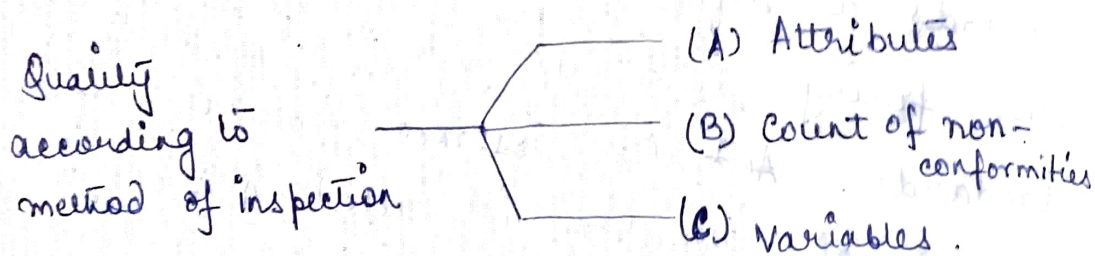
- Control charts developed by W. A. Shewart
- 2. Product control : It attempts to ensure quality of product/item to the consumer, irrespective of the quality.

maintained by the manufacturer. Generally speaking, it relates to input materials and finished products.

### Tools:-

- Sampling Inspection Plans (SIP) by F. G. Dodge and F. H. Romig.

## Classification of Quality



A. Attributes :- Eg: A finished TV picture tube classified as functioning or non-functioning.

B. Count of non-conformities :- Spots or pores counted on a finished roll of paper.

C. Variables :-<sup>Eg:</sup> Diameter measured of a finished bowl.

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### CONTROL CHARTS FOR ATTRIBUTES :-

Process → Manufacturing electric bulbs

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graph LR; A[Process → Manufacturing electric bulbs] --- B1(( )); B1 --- B2[ ]; B1 --- B3[ ]; B2 --- B2a["conforming"]; B3 --- B3a["non-conforming"];
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\* Shewart Control Charts :- The key concept in shewart's control charts is rational subgrouping. Variation in quality characteristics is inherent in any process. This variation is due to two kinds of causes :-

- i) Variation due to chance cause, known as random variation.
- ii) Variation due to assignable causes, known as systematic variation.

The aim of shewart's control chart technique is to separate out the assignable causes from the chance causes in order to take investigative and corrective measure. Chance causes are considered allowable, and the assignable causes preventable. The approaches to divide a group of products from a given process into a number of subgroups such that variation within each subgroup is due to random causes alone but

forming such subgroups are  
the variations, between ~~or~~ subgroups if  
it exists is due to assignable causes.  
The process is said to be in control if the  
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Hint  
 Shewhart's Control Charts based on rational subgroups given a process distribution with process parameter  $\theta$ :

SUBGROUPS :  $m$  subgroups of items each of size  $n$  are collected from the process in such a way that variation within the subgroups are due to random causes only and variation between the subgroups are due to <sup>assignable</sup> systematic causes. We consider a statistic

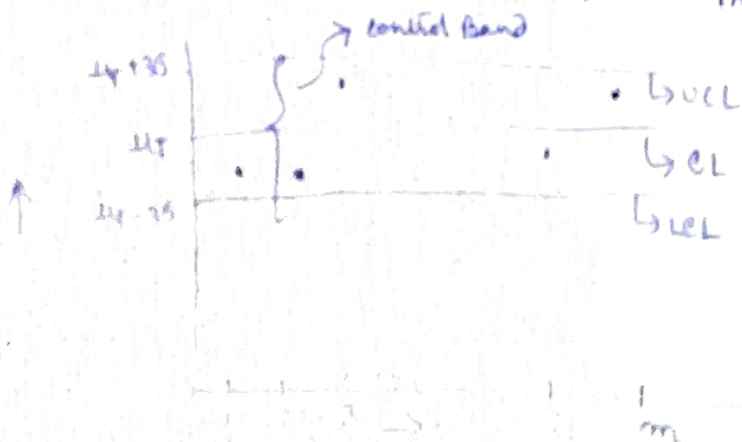
$$T = T(X_1, X_2, \dots, X_n)$$

$$\mu_T = E(T) = \mu(\theta)$$

$$\sigma_T^2 = \text{var}(T) = \sigma^2(\theta)$$

Subgroups: 1, 2, ..., i, ..., m

Statistic values:  $T_1, T_2, \dots, T_i, \dots, T_m$

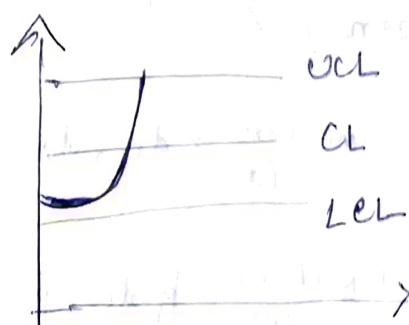




(b) If the control limits, LCL & UCL are lower and upper control lines respectively. The process is said to be in control if :-  
 (i) the observations lie within the control band  
 (ii) the observations do not show any definite pattern of variation.  
 (iii) the observations are within the control band, otherwise it is out of control.



Figure



Trend

## CONTROL CHART FOR ATTRIBUTES

Example 5: manufacturing of electric

conforming  
 non-conforming

## Process Distribution

number of defective items  
 $p$  is the probability that

manufactured by the process  
 is non-conforming.  $p$  is the  
 $X \sim \text{Ber}(p)$