ButterRoti ICPC Team Notebook (2017-18)

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1 Sublime

1.1 Build

```
{
"cmd": ["g++ -std=c++14 -g -Wall '${file}' &&
    timeout 15s '${file_path}/./a.out'<'${file_path}
    }/input.txt'>'${file_path}/output.txt'"],
"shell":true
}
```

1.2 Snippet

```
using 1d = long double;
#define fi first
#define ff first
#define se second
#define ss second
#define pp push_back
#define pb pp
#define endl '\n'
#define SYNC std::ios::sync_with_stdio(false);
   cin.tie(NULL);
#define ALL(v) v.begin(), v.end()
#define FOR0(i,n) for(int i=0, ##i=(n); i< ##i;
#define FOR(i,1,r) for(int i=(1), _##i=(r); i<_##i
   ; ++i)
#define FORD(i,1,r) for(int i=(r), _##i=(1); --i>=
  ##i; )
#define rep(i,a) FORO(i, a)
#define repn(i,a) FOR(i, 1, a + 1)
#define REP(i, n) rep(i, n)
#define REPN(i, n) repn(i, n)
#define SZ(a) ((int)((a).size()))
#define mp make pair
#define dzx cerr << "here";
#define her cerr << "HERE "
#define pii pair<int,int>
#define ii pii
#define en(v) *(--v.end())
const int MOD = (int)1e9 + 7, inf = 0x3f3f3f3f3f;
const 11 INF = 0x3f3f3f3f3f3f3f3f;
int32_t main() {SYNC;
    return 0;
```

2 Combinatorial optimization

2.1 Lowest Common Ancestor

```
// 0-based vertex indexing. memset to -1
int log(int t) {
  int res = 1;
```

```
for(; 1 << res <= t; res++);
  return res;
}
int lca(int u , int v) {
  if(h[u] < h[v]) swap(u , v);
  int L = log(h[u]);
  for(int i = L - 1; i >= 0; i--) {
    if(par[u][i] + 1 && h[u] - (1 << i) >= h[v])
        u = par[u][i];
  }
  if(v == u) return u;
  for(int i = L - 1; i >= 0; i--) {
    if(par[u][i] + 1 && par[u][i] != par[v][i]) {
        u = par[u][i]; v = par[v][i];
    }
  return par[u][0];
}
```

2.2 Heavy-Light Decomposition

```
int n;
V < V < P < int >> > q;
V<int> values;
V<int> depth;
V<int> size;
V<int> hchild:
V<V<int> > chains;
V<int> head;
V<int> cmap,idmap;
V<int> parent;
V<P<int> > Edges;
V<Seatree> trees;
void dfs(int u,int p) {
  parent[u]=p;
  depth[u] = depth[p] +1;
  size[u]=1;
  int hs=0, hv=-1;
  for(auto v:q[u]) if(v.fi!=p){
    dfs(v.fi,u);
    values[v.fi]=v.se;
    size[u] += size[v.fi];
    if(size[v.fi]>hs) {
      hv=v.fi;
      hs=size[v.fi];;
```

```
hchild[u]=hv;
void form(int u,int p) {
  cmap[u] = (int) chains.size() -1;
  idmap[u] = (int) chains.back().size();
  if(chains.back().size()==0) {
    head.pb(u);
  chains.back().pb(values[u]);
  if (hchild[u]!=-1)
    form(hchild[u],u);
  for(auto v:g[u]) if(v.fi!=p && v.fi!=hchild[u])
    chains.pb({});
    form(v.fi,u);
void build() {
  for (int i=0;i<chains.size();i++) {</pre>
    trees.pb(Segtree(chains[i]));
int query(int u,int v) {
  int r=0:
  while (u!=v)
    if(cmap[v] == cmap[u]) {
      if (depth[v] < depth[u])</pre>
         swap(v,u);
      r=max(r, trees[cmap[v]].query(idmap[u]+1,
         idmap[v]);
      v=u:
    else{
      if (depth[head[cmap[v]]] < depth[head[cmap[u]</pre>
         ]]])
        swap(v,u);
      int h=head[cmap[v]];
      int hid=idmap[h];
      int vid=idmap[v];
      r=max(r, trees[cmap[v]].query(hid, vid));
      v=parent[h];
  return r;
```

```
void update(int idx,int val){
  auto p=Edges[idx-1];
  int v=p.se;
  if(depth[p.se]<depth[p.fi])
    v=p.fi;
  trees[cmap[v]].update(idmap[v],val);
}</pre>
```

2.3 Auxiliary Tree

```
//std::vector<int> a contains vertices to form the
    aux t
sort(ALL(a), [](const int & a, const int & b) ->
  bool{
  return st[a] < st[b];</pre>
});
set < int > s (a);
for (int i = 0, k = (int) a.size(); i + 1 < k; i++) {
  int v = lca(a[i], a[i + 1]);
  if(s.find(v) == s.end())
    a.push back(v);
  s.insert(v);
sort(ALL(a), [](const int & a, const int & b) ->
  bool {
  return st[a] < st[b];</pre>
});
stack<int> S;
S.push(a[0]);
auto anc = [](int & a, int & b) -> bool{
  return st[b] >= st[a] && en[b] <= en[a];
};
for(int i = 1; i < (int)a.size(); i++){</pre>
  while(!anc(S.top(), a[i])) S.pop();
  G[S.top()].pp(a[i]);
  G[a[i]].pp(S.top());
  S.push(a[i]);
//G is the Aux tree
```

2.4 Articulation Point and Bridges

```
#include <bits/stdc++.h>
using namespace std;
const int N = 50;
int dis[N], low[N], par[N], AP[N], vis[N], tits;
void update(int u , int i, int child) {
  //For Cut Vertices
  if (par[u] != -1 \&\& low[i] >= dis[u]) AP[u] =
    true;
  if (par[u] == -1 && child > 1) AP[u] = true;
  //For Finding Cut Bridge
  if(low[i] > dis[u]){
    //articulation bridge found.
void dfs(int u) {
  vis[u] = true;
  low[u] = dis[u] = (++tits); int child = 0;
  for(int i : q[u]) {
    if(!vis[i]){
      child++;
      par[i] = u;
      dfs(i);
      low[u] = min(low[u], low[i]);
      update(u, i, child);
    else if(i != par[u]) {
      low[u] = min(low[u], dis[i]);
```

2.5 Biconnected Components

```
#include <bits/stdc++.h>
using namespace std;
const int N = (int)2e5 + 10;

vector<vector<int>> tree, g;
bool isBridge[N << 2], vis[N];
int Time, arr[N], U[N], V[N], cmpno, comp[N];</pre>
```

```
vector<int> temp; //temp stores component values
int adj(int u, int e) {
  return (u == U[e] ? V[e] : U[e]);
int find_bridge(int u , int edge) {
  vis[u] = true;
  arr[u] = Time++;
 int x = arr[u];
  for(auto & i : q[u]) {
    int v = adj(u, i);
    if(!vis[v]){
      x = min(x, find bridge(v, i));
    else if(i != edge){
      x = min(x, arr[v]);
  if(x == arr[u] && edge != -1) {
    isBridge[edge] = true;
  return x;
void dfs1(int u) {
  int current = cmpno;
  queue<int> q;
  q.push(u);
  vis[u] = 1;
  temp.push back(current);
  while(!q.emptv()){
    int v = q.front();
    q.pop();
    comp[v] = current;
    for (auto & i : q[v]) {
      int w = adj(v, i);
      if(vis[w])continue;
      if(isBridge[i]){
        cmpno++;
        tree[current].push back(cmpno);
        tree[cmpno].push_back(current);
        dfs1(w);
```

```
else{
        q.push(w);
        vis[w] = 1;
int main(){
  int n, m;
 cin >> n >> m;
 q.resize(n + 2); tree.resize(n + 2);
 for(int i = 0; i < m; i ++) {
    cin >> U[i] >> V[i];
    q[U[i]].push back(i);
    q[V[i]].push back(i);
  cmpno = Time = 0;
 memset(vis, false, sizeof vis);
 for (int i = 0; i < n; i ++) {
    if(!vis[i]){
      find bridge(i, -1);
 memset (vis, false, sizeof vis);
  cmpno = 0;
 for (int i = 0; i < n; i ++) {
    if(!vis[i]){
      temp.clear();
      cmpno++;
      dfs1(i);
```

2.6 2-SAT

class sat_2{
public:
 int n, m, tag;

```
V<V<int>> q, grev;
V<bool> val;
V<int> st;
V<int> comp;
sat_2(){}
sat_2(int n) : n(n), m(2 * n), tag(0), g(m + 1),
    grev(m + 1), val(n + 1) { }
void add_edge(int u, int v) { //u or v
  auto make_edge = [&](int a, int b) {
    if(a < 0) a = n - a;
    if(b < 0) b = n - b;
    g[a].pp(b);
    grev[b].pp(a);
  };
  make edge (-u, v);
  make_edge(-v, u);
void truth_table(int u, int v, V<int> t) {
  for (int i = 0; i < 2; i ++) for (int j = 0; j <
      2; † ++) {
    if(!t[i * 2 + j])
      add_edge((2 * (i ^1) - 1) * u, (2 * (j ^1) )
         1) -1) * v);
 }
void dfs(int u, V<V<int>> & G, bool first) {
  comp[u] = tag;
  for (int & i : G[u]) if (comp[i] == -1)
    dfs(i, G, first);
  if(first) st.push_back(u);
bool satisfiable() {
  tag = 0; comp.assign(m + 1, -1);
  for (int i = 1; i <= m; i ++) {</pre>
    if(comp[i] == -1)
      dfs(i, q, true);
  }reverse(ALL(st));
  tag = 0; comp.assign(m + 1, -1);
  for(int & i : st) {
    if(comp[i] != -1) continue;
```

```
tag++;
    dfs(i, grev, false);
}

for(int i = 1; i <= n; i ++) {
    if(comp[i] == comp[i + n]) return false;
    val[i] = comp[i] > comp[i + n];
}

return true;
}
};
```

2.7 Dinic's Max Flow

```
// from stanford notebook
struct edge {
  int u, v;
  11 c, f;
  edge() { }
  edge(int _u, int _v, ll _c, ll _f = 0): u(_u), v
    (_v), c(_c), f(_f) { }
} ;
int n;
vector<edge> edges;
vector<vector<int> > q;
vector<int> d, pt;
void addEdge(int u, int v, ll c, ll f = 0) {
  g[u].emplace back(edges.size());
  edges.emplace_back(edge(u,v,c,f));
  g[v].emplace_back(edges.size());
  edges.emplace_back(edge(v,u,0,0));
bool bfs(int s, int t) {
  queue<int> q({s});
  d.assign(n+1, n+2);
  d[s] = 0;
  while(!q.empty()) {
    int u = q.front(); q.pop();
    if (u == t) break;
    for(int k : g[u]) {
      edge &e = edges[k];
      if(e.f < e.c && d[e.v] > d[e.u] + 1){
        d[e.v] = d[e.u] + 1;
        q.push(e.v);
```

```
return d[t] < n+2;</pre>
ll dfs(int u, int t, ll flow = -1) {
  if(u == t || !flow) return flow;
  for(int &i = pt[u]; i < (int)(g[u].size()); i++)</pre>
    edge &e = edges[q[u][i]], &oe=edges[q[u][i
       ]^1];
    if(d[e.v] == d[e.u] + 1) {
      11 \text{ amt} = e.c - e.f;
      if (flow != -1 \&\& amt > flow) amt = flow;
      if(ll pushed = dfs(e.v,t,amt)) {
        e.f += pushed;
        oe.f -= pushed;
        return pushed;
  return 0;
11 flow(int s, int t) {
  11 \text{ ans} = 0;
  while(bfs(s,t)) {
    pt.assign(n+1, 0);
    while(ll val = dfs(s,t)) ans += val;
  return ans;
```

2.8 Min Cost Max Flow

```
int tt=0;
class CostFlowGraph{
public:
    struct Edge{
        int v,f,c;
        Edge() {}
        Edge(int v,int f,int c):v(v),f(f),c(c) {}
    };
    V<V<int> > g;
    V<Edge> e;
```

```
V<int> pot;
int n, flow, cost;
CostFlowGraph(int sz) {
  n=sz;
  q.resize(n);
  pot.assign(n,0);
  flow=0;
  cost=0;
void clear(){
  flow=0; cost=0;
  for (int i=0; i < (int) e.size(); i++) {</pre>
    e[i].f+=e[i^1].f;
    e[i^1].f=0;
void addEdge(int u,int v,int cap,int c) {
  q[u].pb((int)e.size());
  e.pb(Edge(v,cap,c));
  g[v].pb((int)e.size());
  e.pb (Edge (u, 0, -c));
void assignPots(int s) {
  priority_queue<pii, V<pii>, greater<pii>> q;
  V<int> npot(n,inf);
  q.push({s,0});
  while(!q.empty()){
    auto cur=q.top();q.pop();
    if(npot[cur.fi] <= cur.se)</pre>
      continue;
    npot[cur.fi]=cur.se;
    for(auto i:q[cur.fi]) if(e[i].f>0){
      int cst=pot[cur.fi]-pot[e[i].v]+e[i].c;
      q.push({e[i].v,cst+cur.se});
  for (int i=0; i < n; i++) if (npot[i]!=inf) {</pre>
    pot[i] +=npot[i];
void dfs(int t, V<bool> &v, V<int> &stk) {
  auto cur=stk.back();
  v[e[cur].v]=1;
  if(e[stk.back()].v==t)
    return ;
  for(auto i:q[e[cur].v]) if(!v[e[i].v] && e[i].
```

```
f>0 && (pot[e[cur].v]-pot[e[i].v]+e[i].c)
       ==0)
      stk.pb(i);
      dfs(t,v,stk);
      if(e[stk.back()].v==t)
        return ;
    stk.pop back();
  int augment(int s,int t){
    V<bool> v(n, false);
    vector<int> stk;
    if(g[s].size()==0)
      return 0;
    stk.pb(q[s][0]^1);
    dfs(t,v,stk);
    if(stk.empty())
      return 0;
    int mx=inf;
    for (int i=1; i < (int) stk.size(); i++)</pre>
      mx=min(mx,e[stk[i]].f);
    for (int i=1; i < (int) stk.size(); i++) {</pre>
      e[stk[i]].f-=mx;
      e[(stk[i])^1].f+=mx;
    return mx;
  void mcf(int s,int t) {
    int cur=0;
    do{
      flow+=cur;
      cost+=(pot[t]-pot[s]);
      assignPots(s);
      cur=augment(s,t);
    }while(cur);
};
```

2.9 Global Min Cut

```
// Adj mat. Stoer-Wagner min cut algorithm.
// Running time:O(|V|^3)
typedef vector<int> VI;
typedef vector<VI> VVI;
const int INF = 1000000000;
```

```
pair<int, VI> GetMinCut(VVI &weights) {
  int N = weights.size();
  VI used(N), cut, best cut;
  int best weight = -1;
  for (int phase = N-1; phase >= 0; phase--) {
    VI w = weights[0];
    VI added = used;
    int prev, last = 0;
    for (int i = 0; i < phase; i++) {</pre>
      prev = last;
      last = -1;
      for (int j = 1; j < N; j++)</pre>
  if (!added[\dot{j}] && (last == -1 || w[\dot{j}] > w[last]))
      last = j;
      if (i == phase-1) {
  for (int j = 0; j < N; j++) weights[prev][j] +=</pre>
     weights[last][j];
  for (int j = 0; j < N; j++) weights[j][prev] =</pre>
     weights[prev][j];
  used[last] = true;
  cut.push_back(last);
  if (best_weight == -1 || w[last] < best_weight)</pre>
    best cut = cut;
    best weight = w[last];
      } else {
  for (int j = 0; j < N; j++)
    w[i] += weights[last][j];
  added[last] = true;
      }
  return make pair (best weight, best cut);
int main() {
  int N;
  cin >> N;
  for (int i = 0; i < N; i++) {
    int n, m;
    cin >> n >> m;
    VVI weights(n, VI(n));
    for (int j = 0; j < m; j++) {
```

```
int a, b, c;
    cin >> a >> b >> c;
    weights[a-1][b-1] = weights[b-1][a-1] = c;
}
pair<int, VI> res = GetMinCut(weights);
cout << "Case #" << i+1 << ": " << res.first
    << endl;
}
}</pre>
```

2.10 Bipartite Matching

```
// maximum cardinality bipartite matching using
   augmenting paths.
// assumes that first n elements of graph
   adjacency list belong to the left vertex set.
vector<vector<int>> graph;
vector<int> match, vis;
int augment(int 1) {
  if(vis[1]) return 0;
  vis[1] = 1;
 for(auto r: graph[1]) {
    if (match[r] == -1 | | augment (match[r])) {
      match[r]=1; return 1;
  return 0;
int matching() {
  int ans = 0;
 for(int 1 = 0; 1 < n; 1++) {
    vis.assign(n, 0);
    ans += augment(1);
  return ans;
```

2.11 Hopcraft-Karp

```
#define MAX 100001
#define NIL 0
#define INF (1<<28)</pre>
```

```
vector< int > G[MAX];
int n, m, match[MAX], dist[MAX];
// n: number of nodes on left side, nodes are
  numbered 1 to n
// m: number of nodes on right side, nodes are
  numbered n+1 to n+m
// G = NIL[0] } G1[G[1--n]] } G2[G[n+1--n+m]]
  11
bool bfs() {
    int i, u, v, len;
    queue< int > Q;
    for (i=1; i<=n; i++) {
        if (match[i] == NIL) {
            dist[i] = 0;
            Q.push(i);
        else dist[i] = INF;
    dist[NIL] = INF;
    while(!Q.empty()) {
        u = Q.front(); Q.pop();
        if(u!=NIL) {
            len = G[u].size();
            for (i=0; i<len; i++) {</pre>
                v = G[u][i];
                if (dist[match[v]] == INF) {
                     dist[match[v]] = dist[u] + 1;
                     Q.push (match[v]);
    return (dist[NIL]!=INF);
bool dfs(int u) {
    int i, v, len;
    if(u!=NIL) {
        len = G[u].size();
        for (i=0; i<len; i++) {</pre>
            v = G[u][i];
            if (dist[match[v]] == dist[u] + 1) {
                 if (dfs (match[v])) {
                     match[v] = u;
```

2.12 Hungarian

```
// Min cost BPM via shortest augmenting paths
// O(n^3). Solves 1000x1000 in ~1s
// cost[i][j] = cost for pairing left node i with
   right node j
// Lmate[i] = index of right node that left node
  i pairs with
// Rmate[i] = index of left node that right node
  j pairs with
// The values in cost[i][j] may be +/-. To
  perform
// maximization, negate cost[][].
typedef vector<double> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
double MinCostMatching(const VVD &cost, VI &Lmate,
   VI &Rmate) {
  int n = int(cost.size());
 // construct dual feasible solution
 VD u(n);
 VD v(n);
 for (int i = 0; i < n; i++) {
```

```
u[i] = cost[i][0];
  for (int j = 1; j < n; j++) u[i] = min(u[i],
     cost[i][i]);
for (int j = 0; j < n; j++) {
  v[j] = cost[0][j] - u[0];
  for (int i = 1; i < n; i++) v[j] = min(v[j]),
     cost[i][j] - u[i]);
// construct primal solution satisfying
   complementary slackness
Lmate = VI(n, -1);
Rmate = VI(n, -1);
int mated = 0;
for (int i = 0; i < n; i++) {</pre>
  for (int j = 0; j < n; j++) {
    if (Rmate[j] != -1) continue;
    if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10)
  Lmate[i] = j;
  Rmate[j] = i;
  mated++;
  break:
VD dist(n);
VI dad(n);
VI seen(n);
// repeat until primal solution is feasible
while (mated < n) {</pre>
  // find an unmatched left node
  int s = 0;
  while (Lmate[s] !=-1) s++;
  // initialize Dijkstra
  fill(dad.begin(), dad.end(), -1);
  fill(seen.begin(), seen.end(), 0);
  for (int k = 0; k < n; k++)
    dist[k] = cost[s][k] - u[s] - v[k];
  int j = 0;
```

```
while (true) {
  // find closest
  \dot{1} = -1;
  for (int k = 0; k < n; k++) {
if (seen[k]) continue;
if (j == -1 \mid | dist[k] < dist[j]) j = k;
  seen[j] = 1;
  // termination condition
  if (Rmate[j] == -1) break;
  // relax neighbors
  const int i = Rmate[j];
  for (int k = 0; k < n; k++) {
if (seen[k]) continue;
const double new_dist = dist[j] + cost[i][k] -
    u[i] - v[k];
if (dist[k] > new_dist) {
  dist[k] = new_dist;
  dad[k] = j;
// update dual variables
for (int k = 0; k < n; k++) {
  if (k == j || !seen[k]) continue;
  const int i = Rmate[k];
  v[k] += dist[k] - dist[j];
  u[i] = dist[k] - dist[j];
u[s] += dist[j];
// augment along path
while (dad[j] >= 0) {
  const int d = dad[j];
  Rmate[j] = Rmate[d];
  Lmate[Rmate[j]] = j;
  j = d;
Rmate[j] = s;
Lmate[s] = j;
mated++;
```

```
double value = 0;
for (int i = 0; i < n; i++)
  value += cost[i][Lmate[i]];
return value;
}</pre>
```

3 Data Structures

3.1 Implicit Treap

```
//1-based with lazy-updates, range sum query
struct node {
    int val, sum, lazy, prior, size;
    node *1, *r;
};
const int N = 2e5;
node pool[N]; int poolptr=0;
typedef node* pnode;
int sz(pnode t) { return t?t->size:0; }
void upd_sz(pnode t) { if(t) t \rightarrow size = sz(t \rightarrow 1) +
   1 + sz(t->r);
void lazy(pnode t) {
    if(!t || !t->lazy) return;
    t->val+=t->lazv;
    t \rightarrow sum + = t \rightarrow lazy * sz(t);
    if(t->1)t->1->lazy+=t->lazy;
    if(t->r)t->r->lazy+=t->lazy;
    t \rightarrow lazy = 0;
void reset(pnode t) {
    if(t) t->sum=t->val;
void combine(pnode& t, pnode l, pnode r) {
    if(!l || !r) return void(t=l?l:r);
    t \rightarrow sum = 1 \rightarrow sum + r \rightarrow sum;
void operation(pnode t) {
    if(!t) return;
    reset(t);
    lazy(t->1); lazy(t->r);
    combine (t, t->1, t); combine (t, t, t->r);
```

```
void split(pnode t, pnode& l, pnode& r, int pos,
  int add = 0) {
    if(!t) return void(l=r=NULL);
   lazy(t); int curr_pos = add + sz(t->1);
    if(curr_pos<pos) split(t->r,t->r,r,pos,
      curr pos+1), l=t;
    else split (t->1,1,t->r,pos,add), r=t;
   upd_sz(t); operation(t);
void merge(pnode& t, pnode l, pnode r) {
    lazy(l); lazy(r);
    if(!l || !r) t = l?l:r;
    else if(l->prior > r->prior) merge(l->r,l->r,r
      ),t=1;
    else merge(r->1, 1, r-> 1), t=r;
   upd sz(t); operation(t);
pnode init(int val) {
   pnode ret = & (pool[poolptr++]);
   ret->prior = rand(); ret->size = 1;
    ret->val = val; ret->sum = val; ret->lazy = 0;
```

```
return ret;
int guery(pnode t, int 1, int r) {
    pnode L, mid, R;
    split(t, L, mid, 1-1); split(mid, t, R, r-1);
    int ans = t->sum;
    merge(mid, L, t); merge(t, mid, R);
    return ans;
void upd(pnode t, int l, int r, int val) {
    pnode L, mid, R;
    split(t, L, mid, l-1); split(mid, t, R, r-1);
    t->lazy += val;
    merge(mid, L, t); merge(t, mid, R);
void insert(pnode& t, ll val, int pos) {
    pnode 1;
    split(t,l,t,pos-1); merge(l,l,init(val));
      merge(t, l, t);
```