

## ButterRoti ICPC Team Notebook (2017-18)

## Contents

<b>1</b>	<b>Sublime</b>	<b>1</b>
1.1	Build . . . . .	1
1.2	Snippet . . . . .	1
<b>2</b>	<b>Combinatorial optimization</b>	<b>1</b>
2.1	Lowest Common Ancestor . . . . .	1
2.2	Auxiliary Tree . . . . .	2
2.3	Articulation Point and Bridges . . . . .	2
2.4	Biconnected Components . . . . .	2
2.5	2-SAT . . . . .	4
2.6	Dinic's Max Flow . . . . .	4
2.7	Min Cost Max Flow . . . . .	5
2.8	Global Min Cut . . . . .	6
2.9	Bipartite Matching . . . . .	7
2.10	Hopcraft-Karp . . . . .	7
2.11	Hungarian . . . . .	8

## 1 Sublime

## 1.1 Build

```
{
"cmd": ["g++ -std=c++14 -g -Wall '${file}' &&
        timeout 15s '${file_path}/./a.out'<'${file_path}
        '/input.txt'>'${file_path}/output.txt'"],
"shell":true
}
```

## 1.2 Snippet

```
#include <bits/stdc++.h>

using namespace std;

template<typename T> using V = vector<T>;
template<typename T, typename V> using P = pair<T,
V>;
template<typename T> using min_heap =
priority_queue<T, V<T>, greater<T>>;

using LL = long long;
using ll = LL;
using LD = long double;
using ld = long double;

#define fi first
```

```
#define ff first
#define se second
#define ss second
#define pp push_back
#define pb pp
#define endl '\n'
#define SYNC std::ios::sync_with_stdio(false);
        cin.tie(NULL);
#define ALL(v) v.begin(), v.end()
#define FOR0(i,n) for(int i=0, _##i=(n); i<_##i;
        ++i)
#define FOR(i,l,r) for(int i=(l), _##i=(r); i<_##i
        ; ++i)
#define FORD(i,l,r) for(int i=(r), _##i=(l); --i>=
        _##i; )
#define rep(i,a) FOR0(i, a)
#define repn(i,a) FOR(i, 1, a + 1)
#define REP(i, n) rep(i, n)
#define REPN(i, n) repn(i, n)
#define SZ(a) ((int)((a).size()))
#define mp make_pair
#define dzx cerr << "here";
#define her cerr << "HERE "
#define pii pair<int,int>
#define ii pii
#define en(v) * (--v.end())

const int MOD = (int)1e9 + 7, inf = 0x3f3f3f3f;
const ll INF = 0x3f3f3f3f3f3f3f3f;

int32_t main() {SYNC;

        return 0;
}
```

## 2 Combinatorial optimization

## 2.1 Lowest Common Ancestor

```
// 0-based vertex indexing. memset to -1
int log(int t) {
    int res = 1;
    for(; 1 << res <= t; res++);
    return res;
}
```

```

int lca(int u , int v){
    if(h[u] < h[v]) swap(u , v);
    int L = log(h[u]);
    for(int i = L - 1; i >= 0; i--){
        if(par[u][i] + 1 && h[u] - (1 << i) >= h[v]){
            u = par[u][i];
        }
    }
    if(v == u) return u;
    for(int i = L - 1; i >= 0; i--){
        if(par[u][i] + 1 && par[u][i] != par[v][i]){
            u = par[u][i]; v = par[v][i];
        }
    }
    return par[u][0];
}

```

## 2.2 Auxiliary Tree

```

//std::vector<int> a contains vertices to form the
//aux t
sort(ALL(a), [](const int & a, const int & b) ->
    bool{
        return st[a] < st[b];
    });
set<int> s(a);
for(int i = 0, k = (int)a.size(); i + 1 < k; i++){
    int v = lca(a[i], a[i + 1]);
    if(s.find(v) == s.end())
        a.push_back(v);
    s.insert(v);
}

sort(ALL(a), [](const int & a, const int & b) ->
    bool{
        return st[a] < st[b];
    });

stack<int> S;
S.push(a[0]);

auto anc = [](int & a, int & b) -> bool{
    return st[b] >= st[a] && en[b] <= en[a];
};

for(int i = 1; i < (int)a.size(); i++){

```

```

    while(!anc(S.top(), a[i])) S.pop();
    G[S.top()].pp(a[i]);
    G[a[i]].pp(S.top());
    S.push(a[i]);
}
//G is the Aux tree

```

## 2.3 Articulation Point and Bridges

```

#include <bits/stdc++.h>

using namespace std;
const int N = 50;
int dis[N], low[N], par[N], AP[N], vis[N], tits;
void update(int u , int i, int child) {
    //For Cut Vertices
    if(par[u] != -1 && low[i] >= dis[u]) AP[u] =
        true;
    if(par[u] == -1 && child > 1) AP[u] = true;

    //For Finding Cut Bridge
    if(low[i] > dis[u]){
        //articulation bridge found.
    }
}

void dfs(int u){
    vis[u] = true;
    low[u] = dis[u] = (++tits); int child = 0;
    for(int i : g[u]) {
        if(!vis[i]){
            child++;
            par[i] = u;
            dfs(i);
            low[u] = min(low[u] , low[i]);
            update(u, i, child);
        }
        else if(i != par[u]) {
            low[u] = min(low[u] , dis[i]);
        }
    }
}

```

## 2.4 Biconnected Components

```

#include <bits/stdc++.h>

```

```

using namespace std;
const int N = (int)2e5 + 10;

vector<vector<int>> tree, g;
bool isBridge[N << 2], vis[N];
int Time, arr[N], U[N], V[N], cmpno, comp[N];
vector<int> temp; //temp stores component values

int adj(int u, int e){
    return (u == U[e] ? V[e] : U[e]);
}

int find_bridge(int u , int edge){
    vis[u] = true;
    arr[u] = Time++;
    int x = arr[u];

    for(auto & i : g[u]){
        int v = adj(u, i);
        if(!vis[v]){
            x = min(x, find_bridge(v, i));
        }
        else if(i != edge){
            x = min(x, arr[v]);
        }
    }

    if(x == arr[u] && edge != -1){
        isBridge[edge] = true;
    }
    return x;
}

void dfs1(int u){
    int current = cmpno;
    queue<int> q;
    q.push(u);
    vis[u] = 1;
    temp.push_back(current);

    while(!q.empty()){
        int v = q.front();
        q.pop();
        comp[v] = current;

        for(auto & i : g[v]) {
            int w = adj(v, i);

```

```

            if(vis[w]) continue;
            if(isBridge[i]){
                cmpno++;
                tree[current].push_back(cmpno);
                tree[cmpno].push_back(current);
                dfs1(w);
            }
            else{
                q.push(w);
                vis[w] = 1;
            }
        }
    }
}

int main(){
    int n, m;
    cin >> n >> m;
    g.resize(n + 2); tree.resize(n + 2);

    for(int i = 0; i < m; i ++){
        cin >> U[i] >> V[i];
        g[U[i]].push_back(i);
        g[V[i]].push_back(i);
    }

    cmpno = Time = 0;
    memset(vis, false, sizeof vis);

    for(int i = 0; i < n; i ++){
        if(!vis[i]){
            find_bridge(i , -1);
        }
    }

    memset(vis, false, sizeof vis);
    cmpno = 0;

    for(int i = 0; i < n; i ++){
        if(!vis[i]){
            temp.clear();
            cmpno++;
            dfs1(i);
        }
    }
}

```

## 2.5 2-SAT

```

class sat_2{
public:
    int n, m, tag;
    V<V<int>> g, grev;
    V<bool> val;
    V<int> st;
    V<int> comp;

    sat_2(){}
    sat_2(int n) : n(n), m(2 * n), tag(0), g(m + 1),
        grev(m + 1), val(n + 1) {}

    void add_edge(int u, int v) { //u or v
        auto make_edge = [&](int a, int b) {
            if(a < 0) a = n - a;
            if(b < 0) b = n - b;
            g[a].pp(b);
            grev[b].pp(a);
        };

        make_edge(-u, v);
        make_edge(-v, u);
    }

    void truth_table(int u, int v, V<int> t) {
        for(int i = 0; i < 2; i++) for(int j = 0; j <
            2; j++) {
            if(!t[i * 2 + j])
                add_edge((2 * (i ^ 1) - 1) * u, (2 * (j ^
                    1) - 1) * v);
        }
    }

    void dfs(int u, V<V<int>> & G, bool first) {
        comp[u] = tag;
        for(int & i : G[u]) if(comp[i] == -1)
            dfs(i, G, first);
        if(first) st.push_back(u);
    }

    bool satisfiable() {
        tag = 0; comp.assign(m + 1, -1);
        for(int i = 1; i <= m; i++) {
            if(comp[i] == -1)

```

```

            dfs(i, g, true);
        } reverse(ALL(st));

        tag = 0; comp.assign(m + 1, -1);
        for(int & i : st) {
            if(comp[i] != -1) continue;
            tag++;
            dfs(i, grev, false);
        }

        for(int i = 1; i <= n; i++) {
            if(comp[i] == comp[i + n]) return false;
            val[i] = comp[i] > comp[i + n];
        }

        return true;
    }
};

```

## 2.6 Dinic's Max Flow

```

// from stanford notebook
struct edge {
    int u, v;
    ll c, f;
    edge() {}
    edge(int _u, int _v, ll _c, ll _f = 0): u(_u), v
        (_v), c(_c), f(_f) {}
};

int n;
vector<edge> edges;
vector<vector<int>> g;
vector<int> d, pt;

void addEdge(int u, int v, ll c, ll f = 0) {
    g[u].emplace_back(edges.size());
    edges.emplace_back(edge(u, v, c, f));
    g[v].emplace_back(edges.size());
    edges.emplace_back(edge(v, u, 0, 0));
}

bool bfs(int s, int t) {
    queue<int> q({s});
    d.assign(n+1, n+2);
    d[s] = 0;
    while(!q.empty()) {
        int u = q.front(); q.pop();

```

```

    if (u == t) break;
    for(int k : g[u]) {
        edge &e = edges[k];
        if(e.f < e.c && d[e.v] > d[e.u] + 1){
            d[e.v] = d[e.u] + 1;
            q.push(e.v);
        }
    }
}
return d[t] < n+2;
}

ll dfs(int u, int t, ll flow = -1) {
    if(u == t || !flow) return flow;
    for(int &i = pt[u]; i < (int)(g[u].size()); i++)
    {
        edge &e = edges[g[u][i]], &oe=edges[g[u][i]^1];
        if(d[e.v] == d[e.u] + 1) {
            ll amt = e.c - e.f;
            if (flow != -1 && amt > flow) amt = flow;
            if(ll pushed = dfs(e.v,t,amt)) {
                e.f += pushed;
                oe.f -= pushed;
                return pushed;
            }
        }
    }
    return 0;
}

ll flow(int s, int t) {
    ll ans = 0;
    while(bfs(s,t)) {
        pt.assign(n+1, 0);
        while(ll val = dfs(s,t)) ans += val;
    }
    return ans;
}

```

## 2.7 Min Cost Max Flow

```

int tt=0;
class CostFlowGraph{
public:
    struct Edge{

```

```

        int v,f,c;
        Edge(){}
        Edge(int v,int f,int c):v(v),f(f),c(c){}
    };
    V<V<int>> > g;
    V<Edge> e;
    V<int> pot;
    int n, flow, cost;
    CostFlowGraph(int sz) {
        n=sz;
        g.resize(n);
        pot.assign(n,0);
        flow=0;
        cost=0;
    }
    void clear() {
        flow=0;cost=0;
        for(int i=0;i<(int)e.size();i++) {
            e[i].f+=e[i^1].f;
            e[i^1].f=0;
        }
    }
    void addEdge(int u,int v,int cap,int c) {
        g[u].pb((int)e.size());
        e.pb(Edge(v, cap, c));
        g[v].pb((int)e.size());
        e.pb(Edge(u, 0, -c));
    }
    void assignPots(int s) {
        priority_queue<pii,V<pii>,greater<pii>> q;
        V<int> npot(n,inf);
        q.push({s,0});
        while(!q.empty()) {
            auto cur=q.top();q.pop();
            if(npot[cur.fi]<=cur.se)
                continue;
            npot[cur.fi]=cur.se;
            for(auto i:g[cur.fi]) if(e[i].f>0){
                int cst=pot[cur.fi]-pot[e[i].v]+e[i].c;
                q.push({e[i].v,cst+cur.se});
            }
        }
        for(int i=0;i<n;i++) if(npot[i]!=inf) {
            pot[i]+=npot[i];
        }
    }
}

```

```

void dfs(int t, V<bool> &v, V<int> &stk) {
    auto cur=stk.back();
    v[e[cur].v]=1;
    if(e[stk.back()].v==t)
        return ;
    for(auto i:g[e[cur].v]) if(!v[e[i].v] && e[i].
        f>0 && (pot[e[cur].v]-pot[e[i].v]+e[i].c)
        ==0) {
        stk.pb(i);
        dfs(t,v,stk);
        if(e[stk.back()].v==t)
            return ;
    }
    stk.pop_back();
}

int augment(int s,int t){
    V<bool> v(n,false);
    vector<int> stk;
    if(g[s].size()==0)
        return 0;
    stk.pb(g[s][0]^1);
    dfs(t,v,stk);
    if(stk.empty())
        return 0;
    int mx=inf;
    for(int i=1;i<(int)stk.size();i++)
        mx=min(mx,e[stk[i]].f);
    for(int i=1;i<(int)stk.size();i++){
        e[stk[i]].f-=mx;
        e[(stk[i])^1].f+=mx;
    }
    return mx;
}

void mcf(int s,int t){
    int cur=0;
    do{
        flow+=cur;
        cost+=(pot[t]-pot[s]);
        assignPots(s);
        cur=augment(s,t);
    }while(cur);
}
};

```

```

// Adj mat. Stoer-Wagner min cut algorithm.
// Running time:O(|V|^3)
typedef vector<int> VI;
typedef vector<VI> VVI;

const int INF = 1000000000;

pair<int, VI> GetMinCut(VVI &weights) {
    int N = weights.size();
    VI used(N), cut, best_cut;
    int best_weight = -1;

    for (int phase = N-1; phase >= 0; phase--) {
        VI w = weights[0];
        VI added = used;
        int prev, last = 0;
        for (int i = 0; i < phase; i++) {
            prev = last;
            last = -1;
            for (int j = 1; j < N; j++)
                if (!added[j] && (last == -1 || w[j] > w[last]))
                    last = j;
            if (i == phase-1) {
                for (int j = 0; j < N; j++) weights[prev][j] +=
                    weights[last][j];
                for (int j = 0; j < N; j++) weights[j][prev] =
                    weights[j][last];
                used[last] = true;
                cut.push_back(last);
                if (best_weight == -1 || w[last] < best_weight)
                    {
                        best_cut = cut;
                        best_weight = w[last];
                    }
            } else {
                for (int j = 0; j < N; j++)
                    w[j] += weights[last][j];
                added[last] = true;
            }
        }
        return make_pair(best_weight, best_cut);
    }
}

```

```

int main() {
    int N;

```

```

cin >> N;
for(int i = 0; i < N; i++) {
    int n, m;
    cin >> n >> m;
    VVI weights(n, VI(n));
    for (int j = 0; j < m; j++) {
        int a, b, c;
        cin >> a >> b >> c;
        weights[a-1][b-1] = weights[b-1][a-1] = c;
    }
    pair<int, VI> res = GetMinCut(weights);
    cout << "Case #" << i+1 << ": " << res.first
    << endl;
}
}

```

## 2.9 Bipartite Matching

```

// maximum cardinality bipartite matching using
// augmenting paths.
// assumes that first n elements of graph
// adjacency list belong to the left vertex set.
int n;
vector<vector<int>> graph;
vector<int> match, vis;

int augment(int l) {
    if(vis[l]) return 0;
    vis[l] = 1;
    for(auto r: graph[l]) {
        if(match[r]==-1 || augment(match[r])) {
            match[r]=l; return 1;
        }
    }
    return 0;
}

int matching() {
    int ans = 0;
    for(int l = 0; l < n; l++) {
        vis.assign(n, 0);
        ans += augment(l);
    }
    return ans;
}

```

## 2.10 Hopcraft-Karp

```

#define MAX 100001
#define NIL 0
#define INF (1<<28)

vector< int > G[MAX];
int n, m, match[MAX], dist[MAX];
// n: number of nodes on left side, nodes are
// numbered 1 to n
// m: number of nodes on right side, nodes are
// numbered n+1 to n+m
// G = NIL[0] 1 G1[G[1---n]] 1 G2[G[n+1---n+m]]

bool bfs() {
    int i, u, v, len;
    queue< int > Q;
    for(i=1; i<=n; i++) {
        if(match[i]==NIL) {
            dist[i] = 0;
            Q.push(i);
        }
        else dist[i] = INF;
    }
    dist[NIL] = INF;
    while(!Q.empty()) {
        u = Q.front(); Q.pop();
        if(u!=NIL) {
            len = G[u].size();
            for(i=0; i<len; i++) {
                v = G[u][i];
                if(dist[match[v]]==INF) {
                    dist[match[v]] = dist[u] + 1;
                    Q.push(match[v]);
                }
            }
        }
    }
    return (dist[NIL]!=INF);
}

bool dfs(int u) {
    int i, v, len;
    if(u!=NIL) {

```

```

    len = G[u].size();
    for(i=0; i<len; i++) {
        v = G[u][i];
        if(dist[match[v]]==dist[u]+1) {
            if(dfs(match[v])) {
                match[v] = u;
                match[u] = v;
                return true;
            }
        }
    }
    dist[u] = INF;
    return false;
}
return true;
}

int hopcroft_karp() {
    int matching = 0, i;
    // match[] is assumed NIL for all vertex in G
    while(bfs())
        for(i=1; i<=n; i++)
            if(match[i]==NIL && dfs(i))
                matching++;
    return matching;
}

```

## 2.11 Hungarian

```

// Min cost BPM via shortest augmenting paths
// O(n^3).Solves 1000x1000 in ~1s
// cost[i][j] = cost for pairing left node i with
// right node j
// Lmate[i] = index of right node that left node
// i pairs with
// Rmate[j] = index of left node that right node
// j pairs with
// The values in cost[i][j] may be +/- . To
// perform
// maximization, negate cost[i][j].
typedef vector<double> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;

double MinCostMatching(const VVD &cost, VI &Lmate,
    VI &Rmate) {

```

```

    int n = int(cost.size());

    // construct dual feasible solution
    VD u(n);
    VD v(n);
    for (int i = 0; i < n; i++) {
        u[i] = cost[i][0];
        for (int j = 1; j < n; j++) u[i] = min(u[i],
            cost[i][j]);
    }
    for (int j = 0; j < n; j++) {
        v[j] = cost[0][j] - u[0];
        for (int i = 1; i < n; i++) v[j] = min(v[j],
            cost[i][j] - u[i]);
    }

    // construct primal solution satisfying
    // complementary slackness
    Lmate = VI(n, -1);
    Rmate = VI(n, -1);
    int mated = 0;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            if (Rmate[j] != -1) continue;
            if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10)
            {
                Lmate[i] = j;
                Rmate[j] = i;
                mated++;
                break;
            }
        }
    }

    VD dist(n);
    VI dad(n);
    VI seen(n);

    // repeat until primal solution is feasible
    while (mated < n) {

        // find an unmatched left node
        int s = 0;
        while (Lmate[s] != -1) s++;

        // initialize Dijkstra
        fill(dad.begin(), dad.end(), -1);

```



```

fill(seen.begin(), seen.end(), 0);
for (int k = 0; k < n; k++)
    dist[k] = cost[s][k] - u[s] - v[k];

int j = 0;
while (true) {

    // find closest
    j = -1;
    for (int k = 0; k < n; k++) {
if (seen[k]) continue;
if (j == -1 || dist[k] < dist[j]) j = k;
    }
    seen[j] = 1;

    // termination condition
    if (Rmate[j] == -1) break;

    // relax neighbors
    const int i = Rmate[j];
    for (int k = 0; k < n; k++) {
if (seen[k]) continue;
const double new_dist = dist[j] + cost[i][k] -
    u[i] - v[k];
if (dist[k] > new_dist) {
    dist[k] = new_dist;
    dad[k] = j;
}
    }
}

```

```

// update dual variables
for (int k = 0; k < n; k++) {
    if (k == j || !seen[k]) continue;
    const int i = Rmate[k];
    v[k] += dist[k] - dist[j];
    u[i] -= dist[k] - dist[j];
}
u[s] += dist[j];

// augment along path
while (dad[j] >= 0) {
    const int d = dad[j];
    Rmate[j] = Rmate[d];
    Lmate[Rmate[j]] = j;
    j = d;
}
Rmate[j] = s;
Lmate[s] = j;

mated++;

double value = 0;
for (int i = 0; i < n; i++)
    value += cost[i][Lmate[i]];

return value;
}

```

---