

FUNCTIONS

FACTORIAL

$$N = 5$$

$$\text{ans} : \underline{120}$$

$$n! = n \times (n - 1) \times (n - 2) \times \dots \times 1$$

$$= 1 \times 2 \times 3 \times \dots \times n$$

$$3! = 3 \times 2 \times 1 = 6$$

$$5! = 5 \times 4 \times 3 \times 2 \times 1 = 120$$

```
int N;  
cin >> N;
```

N
5

```
int ans = 1;
```

```
for( int i=1 ; i <= N; i++ )
```

```
{
```

```
ans * = i;
```

```
}
```

```
cout << ans;
```

ans i
y 1
x 2
x 3
x 4
x 5
x 6
120

BINOMIAL COEFFICIENT

$${}^n C_r = \frac{n!}{r!(n-r)!}$$

Input $n = 5$
 $r = 2$

$${}^5 C_2 = \frac{5!}{2! \times 3!} = \frac{120}{2 \times 6} = 10$$

if : n and r

o/p : ${}^n C_r = \frac{n!}{r!(n-r)!}$

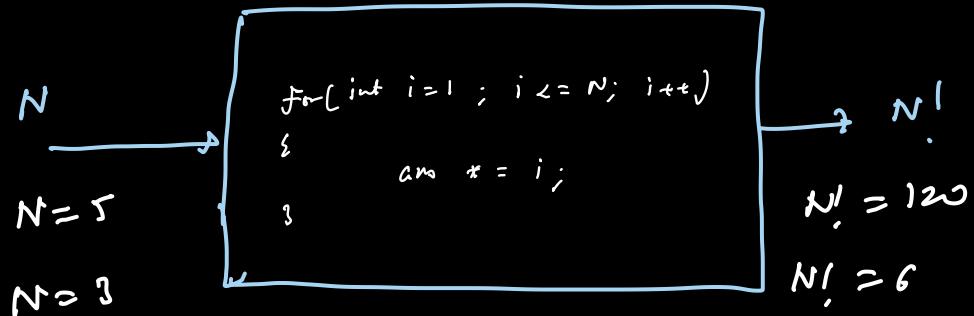
```
int N, R;
```

```
cin >> N >> R;
```

```
int nFact = 1;
```

```
for( int i=1 ; i<=N; i++ )
```

```
{  
    nFact * = i;  
}
```



$N!$

```

int rFact = 1;
for( int i=1 ; i <= R ; i++ )
{
    rFact * = i;
}

```

$$r!$$

```

int nrFact = 1;
for( int i=1 ; i <=  $\frac{N-R}{2}$  ; i++ )
{
    nrFact * = i;
}

```

$$(N-R)!$$

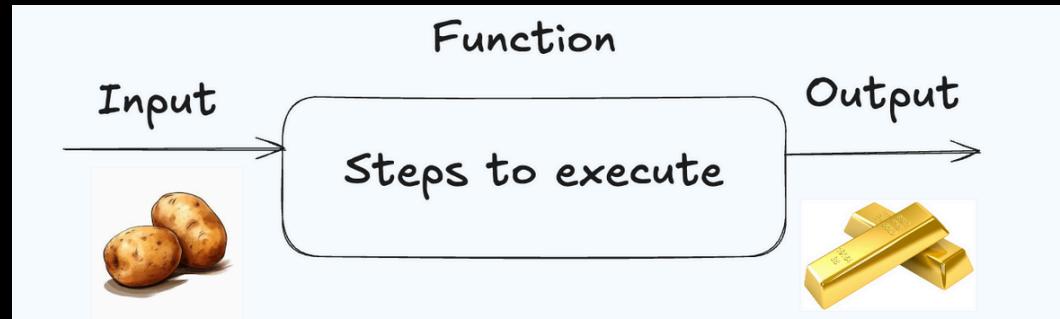
```

cout << nrFact / (rFact * nrFact) ;

```

FUNCTIONS

- Set of statements
- Write only once
- Reuse it multiple times
- Makes code:
 - Cleaner
 - Shorter
 - Easier to debug



FUNCTION SYNTAX

```
return_type function_name(parameters)
{
    // function body
    return value;
}
```

- Return type → what the function gives back
- Function name
- Parameters → inputs
- Return statement

```
int factorial ( int N )
{
    int ans = 1;
    for( i=1; i<=N; i++ )
    {
        ans *= i;
    }
    return ans;
}
```

EXAMPLES

```
int sum2(int a, int b)
{
    return a + b;
}
```

```
int sum3(int a, int b, int c)
{
    return a + b + c;
}
```

```
int factorial(int n)
{
    int ans = 1;
    for(int i = 1; i <= n; i++)
    {
        ans *= i;
    }
    return ans;
}
```

EXAMPLES

```
void print1toN(int n)
{
    for(int i = 1; i <= n; i++)
    {
        cout << i << endl;
    }
}
```

1 2 3 4 5
* * * * ~~*~~
r r x r ~~x~~
r r * r ~~x~~
r r x r ~~x~~

```
void printSquare(int n, char ch)
{
    for(int i = 1; i <= n; i++)
    {
        for(int j = 1; j <= n; j++)
        {
            cout << ch;
        }
        cout << endl;
    }
}
```

FUNCTION RULES

- Number of Parameters Must Match
- Return Type Must Match
- Return Ends the Function *Call*
- A Function May or May Not Return
 - int, double, bool → returns value
 - void → prints only

return-type function-name (—)
{
 ;
 ;
 ;
}
return;

Factors

$12 \rightarrow 1, 2, 3, 4, 6, 12$ (6 factors)

Smallest Factor

(N)

$\rightarrow 1$

$15 \rightarrow 1, 3, 5, 15$ (4 factors)

Largest Factor

for(i=1; i<=N; i++)

{

if (i is a factor of N)

{

cout << i << " ";

}

}

N y.i == 0

divide N with i,
remainder = 0

1
2

$\boxed{1}$ 2 3 4 5 6 7 8 9 10 11 12

| |
|----|
| 3 |
| 4 |
| 6 |
| 12 |

1) Print Factors

2) Count Factors

Prime Numbers

Exactly 2 factors

1

N

1 is not a prime number

1 2 3 5 7 11 13 17 19 23
 ↓ ↓ ↓ ↓ ↓ ↗ ↗
 [1] [1,2] [1,3] [1,5] [1,7] [1,11] ---

$\textcircled{N} \rightarrow$ Prime or not

(N) → Print all prime numbers from 1 to N

isPrime(i)

$N = 10$

2 3 5 7

for ($i = 1; i \leq N; i++$)

{

if (i is prime)

{ cout << i << " ";

}

}

$N = 20$

2 3 5 7 11 13 17 19

