

**FUNCTIONS**

# FACTORIAL

$$n! = n \times (n - 1) \times (n - 2) \times \dots \times 1$$

$$= 1 \times 2 \times 3 \times \dots \times n$$

$$3! = 3 \times 2 \times 1 = 6$$

$$5! = 5 \times 4 \times 3 \times 2 \times 1 = 120$$

$$N = 5$$

$$\text{ans} : \underline{120}$$

```
int N;  
cin >> N;
```

```
int ans = 1;
```

```
for (int i = 1; i <= N; i++)
```

```
{
```

```
    ans *= i;
```

```
}
```

```
cout << ans;
```

N  
5

ans

1

~~1~~

~~2~~

~~6~~

~~24~~

120

i

1

~~2~~

~~2~~

~~6~~

~~24~~

6

# BINOMIAL COEFFICIENT

$${}^nC_r = \frac{n!}{r!(n-r)!}$$

Input

$$n = 5$$
$$r = 2$$

$${}^5C_2 = \frac{5!}{2! \times 3!} = \frac{120}{2 \times 6} = 10$$

i/p:  $n$  and  $r$

o/p:  ${}^nC_r = \frac{n!}{r!(n-r)!}$

```
int N, R;
```

```
cin >> N >> R;
```

```
int nFact = 1;
```

```
for(int i=1; i <= N; i++)
```

```
{
```

```
    nFact * = i;
```

```
}
```

N

N=5

N=3

```
for(int i=1; i <= N; i++)
```

```
{
```

```
    ans * = i;
```

```
}
```

N!

N! = 120

N! = 6

N!

```
int rFact = 1;
```

```
for( int i=1 ; i <= R ; i++)  
{  
    rFact * = i;  
}
```

R!

```
int nrFact = 1;
```

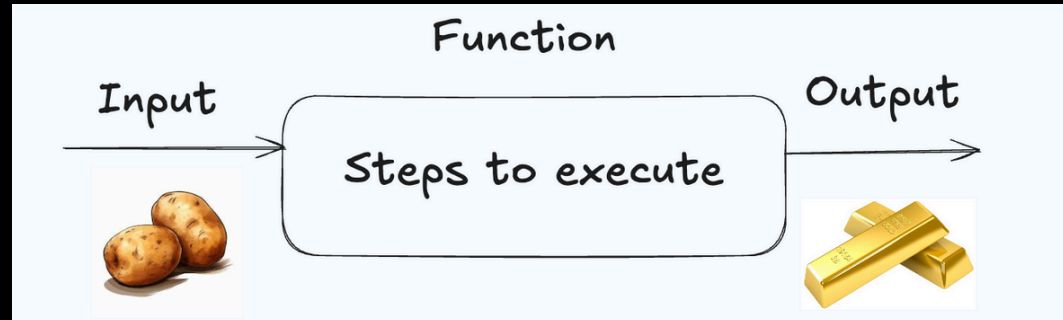
```
for( int i=1 ; i <= N-R ; i++)  
{  
    nrFact * = i;  
}
```

(N-R)!

```
cout << nFact / (rFact * nrFact) ;
```

# FUNCTIONS

- Set of statements
- Write only once
- Reuse it multiple times
- Makes code:
  - Cleaner
  - Shorter
  - Easier to debug



# FUNCTION SYNTAX

```
return_type function_name(parameters)
{
    // function body
    return value;
}
```

- Return type → what the function gives back
- Function name
- Parameters → inputs
- Return statement

```
int factorial ( int N )
{
    int ans = 1;
    for ( i = 1; i <= N; i++ )
    {
        ans *= i;
    }
    return ans;
}
```



# EXAMPLES

```
int sum2(int a, int b)
{
    return a + b;
}
```

```
int sum3(int a, int b, int c)
{
    return a + b + c;
}
```

```
int factorial(int n)
{
    int ans = 1;
    for(int i = 1; i <= n; i++)
    {
        ans *= i;
    }
    return ans;
}
```

# EXAMPLES

```
void print1toN(int n)
{
    for(int i = 1; i <= n; i++)
    {
        cout << i << endl;
    }
}
```

```
void printSquare(int n, char ch)
{
    for(int i = 1; i <= n; i++)
    {
        for(int j = 1; j <= n; j++)
        {
            cout << ch;
        }

        cout << endl;
    }
}
```

```
x x x x x
x x x x x
x x x x x
x x x x x
x x x x x
```

# FUNCTION RULES

- Number of Parameters Must Match
- Return Type Must Match
- Return Ends the Function *Call*
- A Function May or May Not Return
  - int, double, bool → returns value
  - void → prints only

*return-type*    *function-name* ( *\_\_\_\_\_* )  
{  
    \_\_\_\_\_  
    \_\_\_\_\_  
    \_\_\_\_\_  
    *return;*  
}

Factors

12  $\rightarrow$  1, 2, 3, 4, 6, 12 (6 factors)

15  $\rightarrow$  1, 3, 5, 15 (4 factors)

Smallest Factor

$N \rightarrow 1$

Largest Factor

$N$

$N \% i == 0$

Divide  $N$  with  $i$ ,  
remainder = 0

For( $i = 1$ ;  $i \leq N$ ;  $i++$ )

{

if (  $i$  is a factor of  $N$  )

{

cout <<  $i$  << " " ;

}

}

1  
2

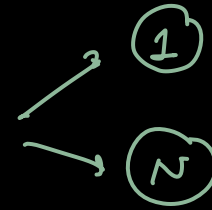
1  
~~2~~ ~~3~~ ~~4~~ ~~5~~ ~~6~~ ~~7~~ 8 9 10 11 12

3  
 4  
 6  
 12

- 1) Print Factors
- 2) Count Factors

Prime Numbers

Exactly 2 factors



1 is not a prime number

1 2 3 5 7 11 13 17 19 23  
 ↓ ↓ ↓ ↓ ↓ ↓  
 [1] [1,2] [1,3] [1,5] [1,7] [1,11] ---

N → Prime or not

(N)  $\rightarrow$  Print all prime numbers from 1 to N

```
isPrime(i) ←  
for (i = 1; i ≤ N; i++)  
{  
    if (i is Prime)  
    {  
        cout << i << " ";  
    }  
}
```

N = 10

2 3 5 7

N = 20

2 3 5 7 11 13 17 19

