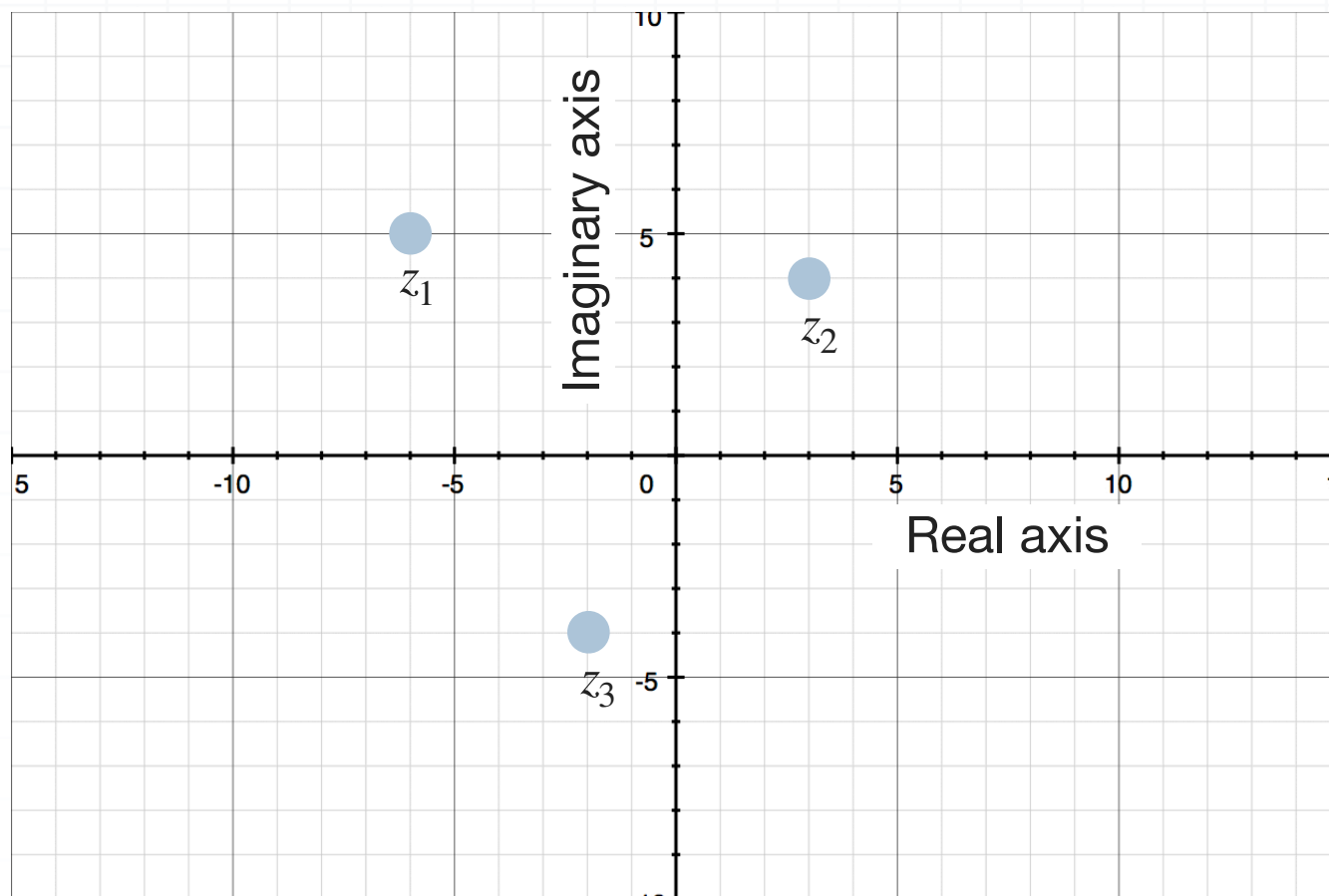


**Topic:** Graphing complex numbers

**Question:** Which three complex numbers are represented in the graph?

**Answer choices:**

- A  $3 - 4i$ ,  $2 + 4i$ , and  $-5 + 6i$
- B  $-2 - 4i$ ,  $3 + 4i$ , and  $-6 + 5i$
- C  $5 + 6i$ ,  $2 + 4i$ , and  $-3 - 4i$
- D  $3 + 4i$ ,  $-6 - 5i$ , and  $-4 - 2i$



**Solution: B**

The point  $z_1$  is 6 units to the left of the vertical axis and 5 units above the horizontal axis, so it's the complex number  $-6 + 5i$ .

The point  $z_2$  is 3 units to the right of the vertical axis and 4 units above the horizontal axis, so it's the complex number  $3 + 4i$ .

The point  $z_3$  is 2 units to the left of the vertical axis and 4 units below the horizontal axis, so it's the complex number  $-2 - 4i$ .

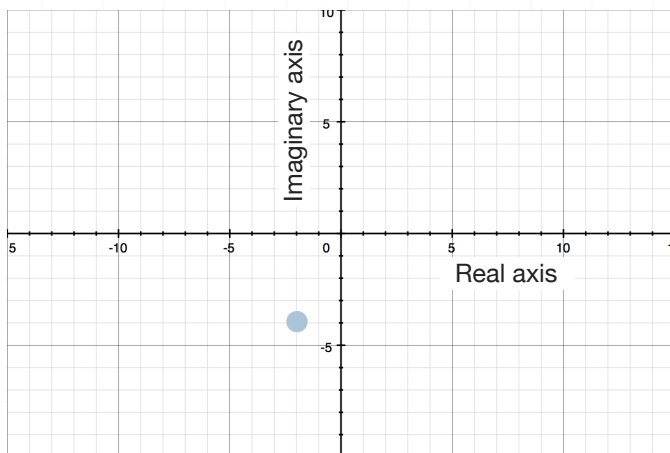


**Topic:** Graphing complex numbers

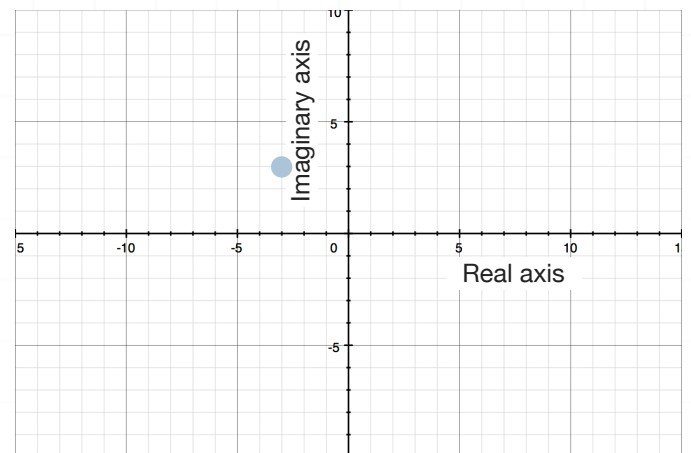
**Question:** Which graph shows the difference of  $-8 + 5i$  and  $-6 + 9i$   $((-8 + 5i) - (-6 + 9i))$ ?

**Answer choices:**

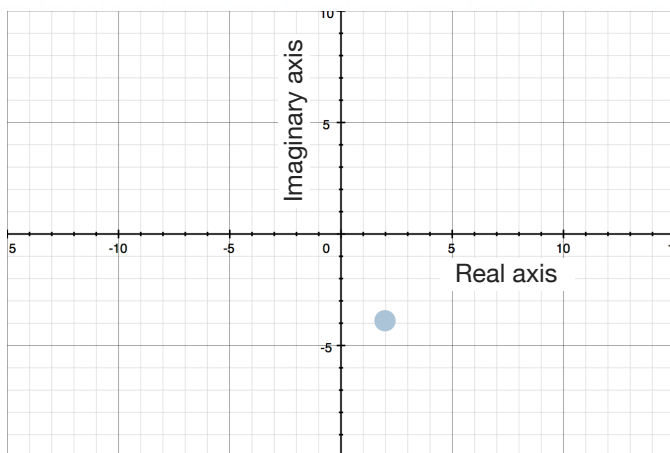
A



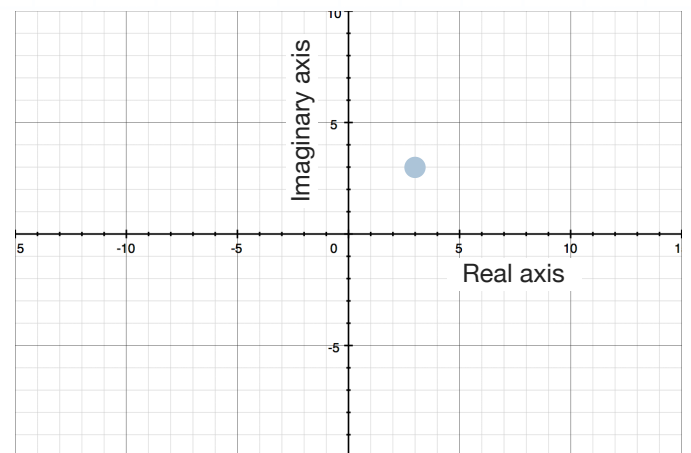
B



C



D



**Solution: A**

First, we'll compute the difference of the complex numbers.

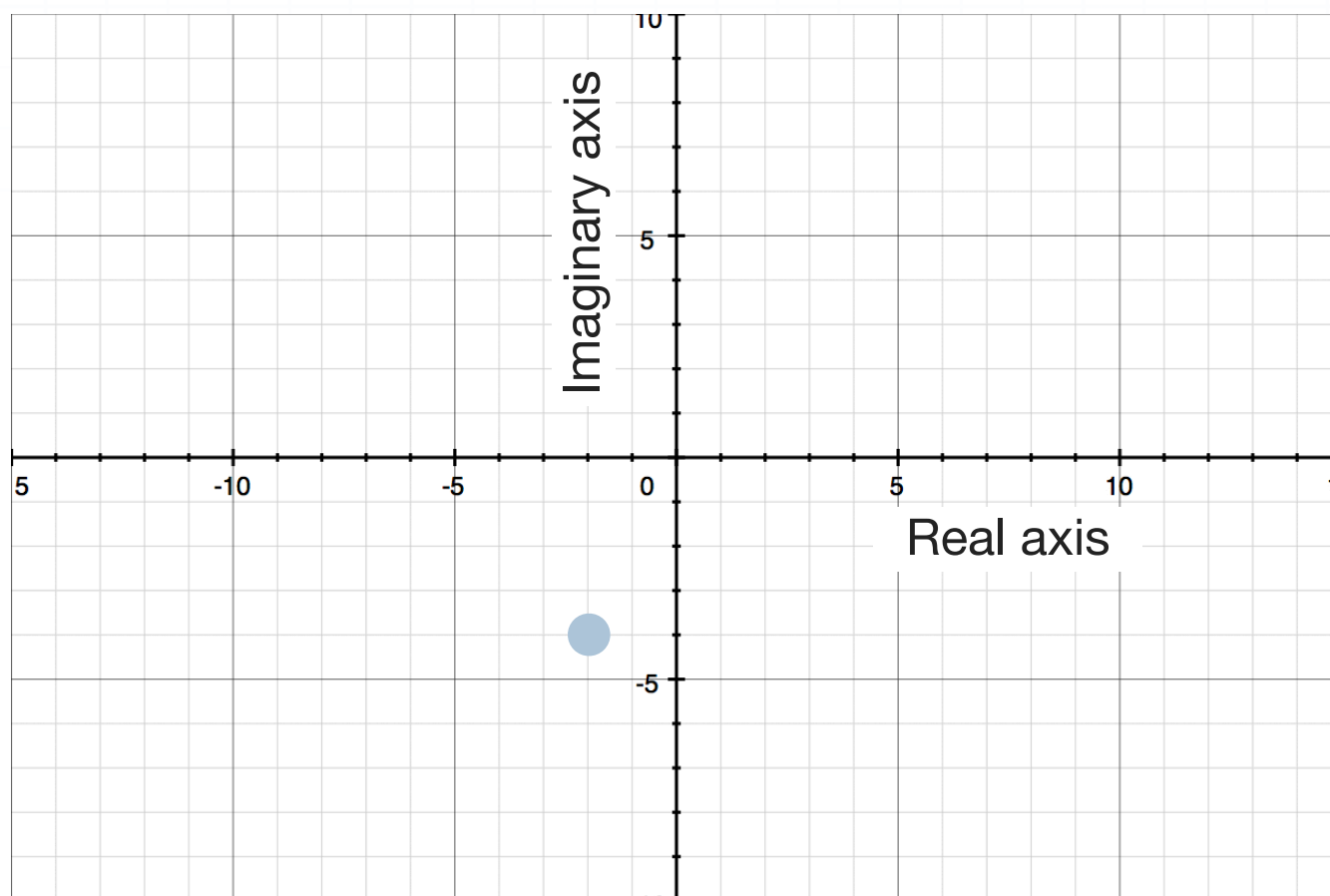
$$(-8 + 5i) - (-6 + 9i)$$

$$(-8 - (-6)) + (5 - 9)i$$

$$(-8 + 6) + (5 - 9)i$$

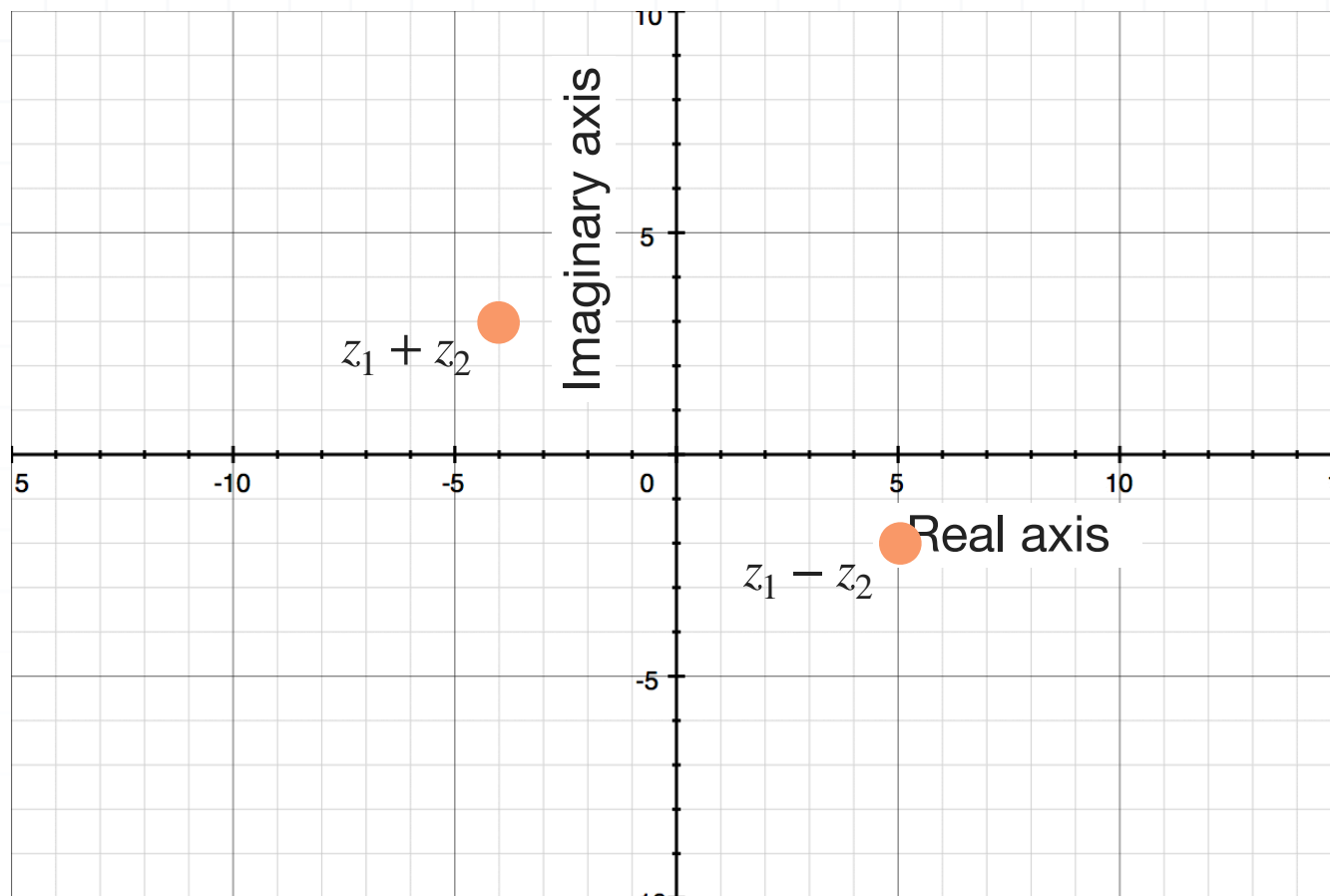
$$-2 - 4i$$

The real part of their difference is  $-2$ , and the imaginary part is  $-4$ . This means that the difference should be graphed 2 units to the left of the vertical axis and 4 units below the horizontal axis.



## Topic: Graphing complex numbers

**Question:** The points on the graph are the sum  $z_1 + z_2$  and difference  $z_1 - z_2$  of two  $z_1$  and  $z_2$ . Use a system of equations to find  $z_1$  and  $z_2$ .



### Answer choices:

- A  $z_1 = (5/2) - (1/2)i$  and  $z_2 = (1/2) + (1/2)i$
- B  $z_1 = (3/2) + (7/2)i$  and  $z_2 = -(5/2) - (3/2)i$
- C  $z_1 = (1/2) + (1/2)i$  and  $z_2 = -(9/2) + (5/2)i$
- D  $z_1 = (7/2) - (3/2)i$  and  $z_2 = (5/2) + (1/2)i$



**Solution: C**

The points on the graph are  $z_1 + z_2 = -4 + 3i$  and  $z_1 - z_2 = 5 - 2i$ . We'll set up this system of equations:

$$z_1 + z_2 = -4 + 3i$$

$$z_1 - z_2 = 5 - 2i$$

Add the two equations together to eliminate  $z_2$ .

$$z_1 + z_2 = -4 + 3i$$

$$z_1 + z_2 + (z_1 - z_2) = -4 + 3i + (5 - 2i)$$

$$z_1 + z_2 + z_1 - z_2 = -4 + 3i + 5 - 2i$$

$$2z_1 = 1 + i$$

$$z_1 = \frac{1}{2} + \frac{1}{2}i$$

Substitute  $z_1$  back into one of the other equations to find  $z_2$ .

$$z_1 + z_2 = -4 + 3i$$

$$\frac{1}{2} + \frac{1}{2}i + z_2 = -4 + 3i$$

$$z_2 = -4 + 3i - \frac{1}{2} - \frac{1}{2}i$$

$$z_2 = -\frac{9}{2} + \frac{5}{2}i$$

