

# N-Body Simulations with REBOUND

Lab course protocol

Group 3+10

Pratyush Singh,  
Proshmit Dasputpa,  
Erasył Telman

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Eberhard Karls Universität Tübingen

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## Abstract

This is optional, but never longer than half a page.

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# 1 Introduction

Very short summary what the experiment is about and why the subject plays a role in astronomy/astrophysics.

## 2 Theory

### 2.1 Classical N-Body Problem

### 2.2 Time Integrators

#### 2.2.1 Leapfrog

#### 2.2.2 IAS15

#### 2.2.3 WHFast

#### 2.2.4 Gragg-Bulirsch-Stoer

### 2.3 REBOUND

## 3 Experiment

### 3.1 Two Body Problem

We use the simple two body problem to test various integrators in REBOUND (Leapfrog, IAS15, WHFast, Gragg-Bulirsch-Stoer) and compare the quality of the resulting outputs. We also test the quality of the results as we change the timestep from 1 to  $10^{-6}$

In a two body problem we simulate a moon orbiting a planet, or a planet orbiting a star. The energy and the angular momentum of the system will

remain constant. They are given as:

$$E = -\mu \frac{GM}{2a} \quad (1)$$

$$L = \mu \sqrt{GMa(1 - e^2)} \quad (2)$$

Where  $\mu = \frac{m_1 m_2}{M}$  is the reduced mass of the system and  $M = m_1 + m_2$  is the total mass.

From the above equations we can derive that the semi major axis and the eccentricity of the system should also remain constant when we simulate the system.

### 3.2 Three Body Problem and Stability of the Planet System

### 3.3 Jupiter and Kirkwood Gaps

### 3.4 Resonant Capture of a Planet

## 4 Conclusions

An important section in which you should critically review the experiment and its results. Mention also parts that did not work out as expected, but keep a neutral to positive view. This can span from a few sentences to half a page.

## References

- [1] Brown B, Aaron M (2001) The politics of nature. In: Smith J (ed) The rise of modern genomics, 3rd edn. Wiley, New York, p 234–295
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- [3] Slifka MK, Whitton JL (2000) Clinical implications of dysregulated cytokine production. J Mol Med, doi: 10.1007/s001090000086
- [4] Smith J, Jones M Jr, Houghton L et al (1999) Future of health insurance. N Engl J Med 965:325–329
- [5] South J, Blass B (2001) The future of modern genomics. Blackwell, London

## Appendix

### Code

Please attach here your original handwritten notes and other documents created during the experiment.