

Tutorial 5

Question 1

For each English sentence on the left, there is a corresponding logical sentence on the right, but *not necessarily the one across from it*. Work out which English sentence corresponds to which propositional logic sentence, and hence determine the meaning (in English) of each proposition symbol.

English

There is a Wumpus at (0, 1).

If the agent is at (0, 1) and there is a Wumpus at (0, 1),
then the agent is not alive.

The agent is at (0, 0) and there is no Wumpus at (0, 1).

The agent is at (0, 0) or (0, 1), but not both.

Propositional Logic

$(C \vee B) \wedge (\neg C \vee \neg B)$

$C \wedge \neg D$

$\neg A \vee \neg(B \wedge D)$

D

Question 2

Consider a vocabulary with only four propositions, A , B , C , and D . How many models are there for the following sentences?

- a. $B \vee C$.
- b. $\neg A \vee \neg B \vee \neg C \vee \neg D$.
- c. $(A \Rightarrow B) \wedge A \wedge \neg B \wedge C \wedge D$.
- d. $(A \wedge B) \vee (C \wedge D)$.
- e. $B \Rightarrow (A \wedge B)$.

Question 3

According to some political pundits, a person who is radical (R) is electable (E) if he/she is conservative (C), but otherwise is not electable.

- a. Which of the following are correct representations of this assertion?
 - (i) $(R \wedge E) \iff C$
 - (ii) $R \Rightarrow (E \iff C)$
 - (iii) $R \Rightarrow ((C \Rightarrow E) \vee \neg E)$