Northeastern University



CS5200 - DBMSSpring 2025

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Mar 27, 2025

Homework 6 Solution

Problem 1. Consider the following schedule...

$$r_1(A), r_2(B), w_1(A), w_1(B), r_2(C), w_1(A), c_1, r_3(B), w_3(B), c_3, w_2(C), c_2$$

Assume that all writes to A, B, and C prior to the operations above have already committed. Provide an answer, with justification, for each of the following questions.

- a. Is this schedule serial?
- b. Is this schedule conflict serializable?
- c. Is this schedule recoverable?
- d. Is this schedule cascadeless?

Problem 1. Solution

$$T_1: r_1(A), \ w_1(A), \ w_1(B), \ w_1(A), c_1$$

$$T_2: r_2(B), \ r_2(C), \ w_2(C), \ c_2$$

$$T_3: r_3(B), \ w_3(B), \ c_3$$

- a. No.
 - Operations from T1, T2, and T3 are interleaved, for example, T2 read B after T1 starts.
- b. Yes.
 - $-r_2(B)$ read B before $w_1(B)$, T2 -> T1
 - $-r_2(B)$ read B before $w_3(B)$, T2 -> T3
 - $w_1(B)$ before $r_3(B)$ and $w_3(B)$, T1 -> T3
 - T2 -> T1 -> T3
- c. Yes.
 - T2 reads B which was written by T1
 - T2 commits after T1, so it's correct
 - T3 also reads from T1 and commits after T1
- d. No.
 - T2 reads B written by T1 before commits, so it's a dirty read

Problem 2. Consider the following transactions...

$$T_1: r(B), \ r(A), \ w(A)$$

$$T_2: r(B), \ w(B), \ r(A)$$

List all schedules that are conflict equivalent to serial schedule (T_2, T_1) .

Problem 2. Solution

$$r_2(B), w_2(B), r_2(A), r_1(B), r_1(A), w_1(A)$$

- The following schedules are conflict equivalent to the serial schedule (T2, T1):
- $r_2(B)$, $w_2(B)$, $r_2(A)$, $r_1(B)$, $r_1(A)$, $w_1(A)$
- $r_2(B)$, $w_2(B)$, $r_1(B)$, $r_2(A)$, $r_1(A)$, $w_1(A)$
- These maintain the necessary conflict orderings:
- $w_2(B)$ before $r_1(B)$
- $r_2(A)$ before $w_1(A)$

Problem 3. Consider the following schedule...

$$r_3(C)$$
, $r_1(A)$, $w_3(C)$, $r_2(A)$, $r_1(C)$, $r_2(B)$, $w_2(B)$, $r_1(B)$, $w_1(A)$

Answer each of the following questions.

- a. Construct a precedence graph for this schedule.
- b. Is this schedule conflict serializable? If so, list all conflict-equivalent serial schedule(s). If not, provide justification.

Problem 3. Solution

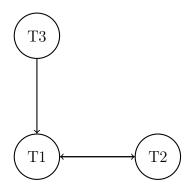
$$T_1: r_1(A), r_1(C), r_1(B), w_1(A)$$

$$T_2: r_2(A), r_2(B), w_2(B)$$

$$T_3: r_3(C), \ w_3(C)$$

(a) Precedence Graph

- T3 \rightarrow T1: $w_3(C)$ occurs before $r_1(C)$ (write-read conflict on C)
- T2 \rightarrow T1: $r_2(A)$ before $w_1(A \text{ (read-write conflict on A)})$
- T1 \rightarrow T2: $r_1(B)$ before $w_2(B)$ (read-write conflict on B)



(b) Is the schedule conflict serializable?

No, the schedule is not conflict serializable because the precedence graph contains a cycle:

$$T2 \rightarrow T1 \rightarrow T2$$

This cycle implies that there is no equivalent serial schedule.