Homework 1

- 0.1:
 - (a) all positive odd number
 - (b) all even number
 - (c) all positive even number
 - (d) all positive number that is multiple of 6
 - (e) palindrome number with only 0s and 1s
 - (f) empty set
- 0.2:
 - (a) $\{n \mid n = 1 \text{ or } 10 \text{ or } 100\}$
 - (b) $\{n \mid n \in \mathbb{N} \text{ and } n > 5\}$
 - (c) $\{n \mid n \in \mathbb{Z} \text{ and } n < 5\}$
 - $(d) \{aba\}$
 - (e) $\{\epsilon\}$
 - (f) {}
- 0.3:
 - (a) No
 - (b) Yes
 - (c) $\{x, y, z\}$
 - $(d) \{x, y\}$
 - (e) $\{\langle x, x \rangle, \langle x, y \rangle, \langle y, x \rangle, \langle y, y \rangle, \langle z, x \rangle, \langle z, y \rangle\}$
 - (f) $\{\{\}, \{x\}, \{y\}, \{x,y\}\}$
- 0.4:

Select one element from A and one from B forms A x B, so there are a*b elements in the set.

• 0.5:

Each element in C can either be in or not in an element in power set of C. The number of elements is 2^c .

• 0.6:

- (a) 7
- (b) Range = {6, 7}, domain = {n | n \ge 1 and n \le 5 where n \in \mathbb{Z}}
- (c) 6
- (d) Domain = $\{n \mid n \ge 1 \text{ and } n \le 5 \text{ where } n \in \mathbb{Z}\}$

Range =
$$\begin{cases} \{10\} & \text{if } X = 1\\ \{6, 7, 8, 9, 10\} & \text{if } X = 2\\ \{7, 8, 9\} & \text{if } X = 3\\ \{6, 7, 8, 9, 10\} & \text{if } X = 4\\ \{6\} & \text{if } X = 5 \end{cases}$$

- (e) 8
- 0.7:
 - (a)

	1	2	3
1	V	V	
2	V	V	V
3		V	V

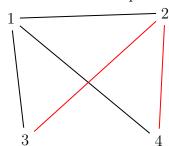
(b)

	1	2	3
1	V	V	
2		V	
3			V

(c)

	1	2	3
1	V	V	
2	V	V	
3			

• 0.8: Red line indicates path from node 3 to node 4



$$deg(1) = 3$$
, $deg(2) = 3$, $deg(3) = 2$, $deg(4) = 2$

• 0.9:

G = (V, E) where

 $V = \{1,2,3,4,5,6\}, E = \{\{1,4\},\{1,5\},\{1,6\},\{2,4\},\{2,5\},\{2,6\},\{3,4\},\{3,5\},\{3,6\}\}\}$