# CS 560: Homework 5(b)

#### **Eric Stevens**

#### **Question 1**

If the social security number of person x is the same as the social security number of person y then y are the same person. From KB we should be able to conclude that  $\phi(johnsmith)$  and  $\phi(johnwsmith)$  are the same individual.

#### **Question 2**

Reflexive, Symmetric, and Transitive:

- X = X
- $X = Y \leftarrow Y = X$
- $X = Z \leftarrow X = Y \land Y = Z$

#### **Axiom Schema:**

•  $ssn(X) = ssn(Y) \leftarrow X = Y$  (we wont have to use this)

## **Question 3**

? johnsmith = johnwsmith

yes ← johnsmith = johnwsmith

- Use:  $X = Y \leftarrow ssn(X) = ssn(Y)$
- **Sub:** {X/johnsmith, Y/johnwsmith}

yes ← ssn(johnsmith) = ssn(johnwsmith)

- Use: X = Z ← X = Y ^ Y = Z
- **Sub:** {X/ssn(johnsmith), Z/johnwsmith}

yes ← ssn(johnsmith) = Y1 ^ Y1 = ssn(johnwsmith)

- Use:
- Sub: {Y1/123456789}

yes  $\leftarrow$  ssn(johnsmith) = 123456789  $^{\land}$  123456789 = ssn(johnwsmith)

- **Use:** ssn(johnsmith) = 123456789
- Sub: {}

```
    yes ← 123456789 = ssn(johnwsmith)
    Use: X = Y ← Y = X
    Sub: {X/123456789, Y/ssn(johnwsmith)}
    yes ← ssn(johnwsmith) = 123456789
    Use: ssn(johnwsmith) = 123456789
    Sub: {}
```

#### **Question 4**

yes ←

The book does not clearly specify the liberties that may be taken when using paramodulation. While it may not be of utility in a fully fleged RSA, there is a way to hack your way to a paramodulation style solution in this case.

```
rule: ssn(johnwsmith) => 123456789

yes ← johnsmith = johnwsmith

• Use: X = Y ← ssn(X) = ssn(Y)

• Sub: {X/johnsmith, Y/johnwsmith}

yes ← ssn(johnsmith) = ssn(johnwsmith)

• Rewrite: ssn(johnwsmith) => 123456789

yes ← ssn(johnsmith) = 123456789

• Use: ssn(johnsmith) = 123456789

• Sub: {}
```

In general, if you are allowed to choose when and where rewrites take place then you can use paramodulation to solve this problem.

### **Question 5**

The below code does not function properly. It appears to be function properly until the point where an atom is resolved that causes one of the delayed notequal atoms atoms to be grounded to a constant that will make it evealuate to false. I have run out of time to solve this problem.

```
In [2]:
          1
             def prove(query,kb):
          2
          3
                 vars = findvariables(query,[])
          4
                 print("Vars in query are %s" % vars)
          5
                 answer = [['yes']+vars]+query
          6
                 print("Initial answer clause is %s" % prettyclause(answer))
          7
          8
                 # the initial frontier is a list whose only element is the initial
          9
                 # answer clause
         10
                 frontier = [answer]
         11
         12
                 while frontier:
         13
                     # give answer clause fresh variables
         14
                     answer = frontier[0]
         15
                     if len(answer) == 1:
         16
                         yesatom = answer[0]
                         str = "Proof:"
         17
         18
                          for var, val in zip(vars, yesatom[1:]):
                              str += " %s=%s" % (var,prettyexpr(val))
         19
         20
                         print(str)
         21
                         return True
         22
         23
                     print("Trying to prove : %s" % prettyclause(answer))
         24
                     # give it fresh variables
         25
                     answer = freshvariables(answer)
                     print("\n after fresh vars : %s" % prettyclause(answer))
         26
         27
         28
                     neighbors = []
         29
         30
                     i=1
         31
                     while delay(answer[i]):
         32
                         print(i)
         33
                         i+=1
         34
                         if i > 1000: break
         35
         36
                     print("\n\n EVALUATING ANSWER ATOM: ", answer[i],"\n\n")
         37
         38
                     if answer[i][0] == 'notequal':
         39
         40
                          if notequal(answer[i]):
         41
                              print(" \n using notequal rule\n" )
         42
                              # create answer clause
         43
                              answercopy = answer[0:i]+answer[i+1:] # changed answer
         44
                              # apply substitution
         45
                              answercopy = substitute(answercopy, subs)
         46
                              print(" result: "+prettyclause(answercopy))
         47
                              neighbors.append(answercopy)
         48
                         else:
         49
                              return False
         50
         51
                     else:
                         for rule in kb:
         52
         53
                              subs = \{\}
         54
                              if not unify(rule[0],answer[i],subs): #changed answer ;
         55
                                  print('FAILED TO UNIFY ',rule[0], answer[i])
         56
                                  continue
         57
                              print('UNIFYing ',rule[0], answer[i])
```

```
58
                    print(" \n using rule %s\n" % prettyclause(rule))
59
                    print(" proven by %s with %s\n" % (rule[0], subs))
60
                    # create answer clause
                    answercopy = answer[0:i]+rule[1:]+answer[i+1:] # change
61
62
                    # apply substitution
63
                    answercopy = substitute(answercopy, subs)
64
                    print(" result: "+prettyclause(answercopy))
65
                    neighbors.append(answercopy)
66
                    break
67
            frontier = neighbors+frontier[1:]
            #print('New Front: %s' % prettyclause([frontier]))
68
69
            print('\n\n')
70
        return False
71
72
   def notequal(predicate):
73
        if predicate[0] == 'notequal':
74
            if not unify(predicate[1],predicate[2],{}): return True
75
            if predicate[1] == predicate[2]: return False
76
        return True
77
78
   def delay(predicate):
79
        if predicate[0] == 'notequal':
80
            if not unify(predicate[1],predicate[2],{}): return False
81
            if predicate[1] == predicate[2]: return False
82
            else: return True
83
        # predicate is not 'notequal'
84
        return False
85
86
```

```
In [4]:
          1
             kb = [
          2
                  [['block', 'red1']],
          3
                  [['block', 'red2']],
          4
                  [['block', 'red3']],
                 [['block', 'red4']],
[['block', 'red5']],
          5
          6
                  [['block', 'red6']],
          7
          8
                  [['block', 'red7']],
          9
                  [['block', 'gre1']],
                 [['block', 'gre2']],
         10
         11
                  [['block', 'gre3']],
                  [['block', 'blu1']],
         12
         13
                  [['block', 'blu2']],
                 [['block', 'yel1']],
         14
                 [['block', 'bla1']],
         15
                  [['color', 'red1', 'red']],
         16
                  [['color', 'red2', 'red']],
         17
                  [['color', 'red3', 'red']],
         18
         19
                  [['color', 'red4', 'red']],
                 [['color', 'red5', 'red']],
         20
         21
                  [['color', 'red6', 'red']],
                  [['color', 'red7', 'red']],
         22
         23
                  [['color', 'gre1', 'green']],
                 [['color', 'gre2', 'green']],
         24
                 [['color', 'gre3', 'green']],
         25
                  [['color', 'blu1', 'blue']],
         26
                  [['color', 'blu2', 'blue']],
         27
                  [['color', 'yell', 'yellow']],
         28
         29
                  [['color', 'bla1', 'black']],
         30
         31
                  [['mct', ['s','0'], ['p','Block','nil']], ['block', 'Block']],
         32
         33
                  [['mct', ['s','X'],'NewTower'],
         34
         35
                      ['notequal', 'X','0'],
                      ['mct', 'X', 'Tower'],
         36
                      ['unify', 'Tower', ['p', 'Top', 'US']],
         37
                      ['notequal', 'TopColor', 'BlockColor'],
         38
         39
                      ['differentfromlist', 'Block', 'Tower'],
                      ['color', 'Top', 'TopColor'],
         40
                      ['block', 'Block'],
['color', 'Block', 'BlockColor'],
         41
         42
                      ['unify','NewTower',['p','Block','Tower']]
         43
         44
                  ],
         45
                  [['differentfromlist', 'X', ['p','Y','nil']],
         46
         47
                      ['notequal', 'X', 'Y']
         48
                  ],
         49
         50
                  [['differentfromlist', 'X', ['p', 'Top', 'Rest']],
                      ['notequal', 'X', 'Top'],
         51
         52
                      ['differentfromlist','X','Rest']
         53
                  ],
         54
         55
         56
         57
                  [['unify', 'X', 'X']],
```

58 59 ] 60

# **Question 5 Critique**

My KB is correct other than my base case for differentfromlist. I could not figure out how to represent an empty list and my guess was wrong. My solution is stylistically very different than the solution manual, but the operation of the code seems to be very similar. I believe I have a bug somewhere and I have not been able to find it. When running the code the operations I would expect to take place occur. I think I have some misunderstanding about the way this operation works. Also, I would like to apologize for the Python file I submitted, the code blocks are out of order as I was working on it in Jupyter where I can run block out of order. I am submitting the file that has code blocks reordered so that they can run.

### **Question 6**

```
step1(impliedby(impliedby(A,B),impliedby(C,D)),TopOutput) :-
    !,
    %write("made double implied\n"),
    step1(impliedby(A,B),OutputAB),
    step1(impliedby(C,D),OutputCD),
    TopOutput = or(OutputAB, not(OutputCD)).
step1(impliedby(X,impliedby(Y,Z)),Output) :-
    !,
    %write("made iRight\n"),
    step1(impliedby(Y,Z), Output2),
    Output = or(X, not(Output2)).
step1(impliedby(impliedby(X,Y),Z),Output) :-
    !,
    %write("made iLeft\n"),
    step1(impliedby(X,Y),Output2),
    Output = or(Output2, not(Z)).
step1(impliedby(X,Y),Output) :-
    !,
    %write("made iSingel\n"),
    Output = or(X, not(Y)).
step1(and(X,Y),TopOutput) :-
    !,
    %write("made AND\n"),
    step1(X,OutputX),
    step1(Y,OutputY),
    TopOutput = and(OutputX,OutputY).
step1(or(X,Y),TopOutput) :-
    !,
    %write("made OR\n"),
    step1(X,OutputX),
    step1(Y,OutputY),
    TopOutput = or(OutputX,OutputY).
step1(not(X),TopOutput) :-
    !,
    %write("made NOT\n"),
    step1(X,OutputX),
    TopOutput = not(OutputX).
step1(X,Output) :-
    %write("made Generalized\n"),
    Output = X.
```

```
findall(X,step1(impliedby(d,e),X),L1),
    write(L1), nl,
    findall(X,step1(impliedby(d,not(e)),X),L2),
    write(L2), nl,
    findall(X,step1(impliedby(d,impliedby(e,f)),X),L3),
    write(L3), nl,
    findall(X,step1(impliedby(impliedby(a,b),impliedby(e,f)),X),L
4),
    write(L4), nl,
    findall(X,step1(and(a,(or(b,or(c,(not(impliedby(d,e))))))),X),L
5),
    write(L5), nl.
/**
RESULTS:
?- test1.
[or(d,not(e))]
[or(d,not(not(e)))]
[or(d,not(or(e,not(f))))]
[or(or(a,not(b)),not(or(e,not(f))))]
[and(a,or(b,or(c,not(or(d,not(e))))))]
true.
**/
```

# **Question 6 Self Assesment**

While the answer I gave results in the correct solution in terms of the test cases, it has unnecessary complexity. The cases of impliedby are wrong. They should be consolidated into a single expression that captures all of the cases that they capture together, as is done in the solution. In the other expressions I am using the = expression for explicit unification where the provided solution implies unification in the head of the clauses.