CS 161 Computer Security

Exam Prep 5

Q1 The Red Hood (15 points)

Jason Todd decides to launch a communications channel in order to securely communicate with the Red Hood Gang over an insecure channel. Jason wants to test different schemes in his attempt to attain confidentiality and integrity.

Notation:

- ullet M is the message Jason sends to the recipient.
- K_1 , K_2 , and K_3 are secret keys known to only Jason and the recipient.
- ECB, CBC, and CTR represent block cipher encryption modes for a secure block cipher.
- Assume that CBC and CTR mode are called with randomly generated IVs.
- *H* is SHA2, a collision-resistant, one-way hash function.
- HMAC is the HMAC construction from lecture.

Decide whether each scheme below provides confidentiality, integrity, both, or neither. For all question parts, the ciphertext is the value of C; t is a temporary value that is not sent as part of the ciphertext.

Q1.1 (3 points)

$$t = \mathsf{CBC}(K_1, M)$$
 $C_1 = \mathsf{ECB}(K_2, t)$ $C_2 = \mathsf{HMAC}(K_3, t)$ $C = (C_1, C_2)$

- O Confidentiality only
- O Integrity only
- Both confidentiality and integrity
- O Neither confidentiality nor integrity

Solution: This is a typical encrypt-then-MAC scheme with a twist: Instead of including the ciphertext t directly, the ciphertext (but not the MAC) is additionally encrypted with ECB mode. Even though both the HMAC and ECB leak information about t, t doesn't leak information about the plaintext, so the scheme is confidential. The HMAC over t ensures that the input passed to CBC decryption can't be tampered with, so the scheme maintains integrity.

Q1.2 (3 points)

$$t = \mathsf{ECB}(K_1, M)$$
 $C_1 = \mathsf{CBC}(K_2, t)$ $C_2 = \mathsf{HMAC}(K_3, t)$ $C = (C_1, C_2)$

- Confidentiality only
- Integrity only
- O Both confidentiality and integrity
- O Neither confidentiality nor integrity

Solution: Notice that t leaks information about the message because it uses insecure ECB mode. C_2 then leaks information about t, which leaks information about the plaintext, so confidentiality is lost (in this case, C_2 is deterministic). However, because the HMAC is computed over t, which is decryptable to the message, integrity is maintained.

Q1.3 (3 points)

$$C_1 = \mathsf{ECB}(K_1, M)$$
 $C_2 = H(K_2 || C_1)$ $C = (C_1, C_2)$

- O Confidentiality only
- O Integrity only
- O Both confidentiality and integrity
- Neither confidentiality nor integrity

Solution: C_1 leaks information about M it uses insecure ECB mode, so confidentiality is lost. C_2 does not maintain integrity as it vulnerable to length extension attacks—an attacker could forge $C_2' = H(K_2 || C_1 || x)$ and $C_1' = C_1 || x$, which would be accepted by anyone verifying the hash.

Q1.4 (3 points) For this subpart only, assume that i a monotonically, increasing counter incremented per message.

$$C_1 = \mathsf{CTR}(K_1, M)$$
 $C_2 = \mathsf{HMAC}(i, H(C_1))$ $C = (C_1, C_2)$

Clarification issued during exam: Assume that the counter, i, starts at 0.

- Confidentiality only
- O Integrity only
- O Both confidentiality and integrity
- O Neither confidentiality nor integrity

Solution: Because i is a known value, the key to the HMAC can be predicted, and the scheme does not maintain integrity. However, since the ciphertext is encrypted with secure CTR mode, and the insecure HMAC is computed only over the ciphertext, the scheme maintains confidentiality.

Q1.5 (3 points) For this subpart only, assume that the block size of block cipher is n, the lengths of K_1 and K_2 are n, the length of M must be 2n, and the length of the hash produced by H is 2n.

$$C_1 = \mathsf{CBC}(K_1, K_2)$$
 $C_2 = M \oplus C_1 \oplus H(C_1)$ $C = (C_1, C_2)$

- O Confidentiality only
- O Integrity only
- O Both confidentiality and integrity
- Neither confidentiality nor integrity

Solution: Notice that the attacker already knows the value of C_1 since it is sent with the ciphertext. Because of this, the adversary can just compute $H(C_1)$ then $C_2 \oplus C_1 \oplus H(C_1)$ in order to recover M, so the scheme is not confidential. Additionally, there is no MAC, so the scheme does not have integrity.

Q2 PRNGs and Diffie-Hellman Key Exchange

(15 points)

Eve is an eavesdropper listening to an insecure channel between Alice and Bob.

- 1. Alice and Bob each seed a PRNG with different random inputs.
- 2. Alice and Bob each use their PRNG to generate some pseudorandom output.
- 3. Eve learns both Alice's and Bob's pseudorandom outputs from step 2.
- 4. Alice, without reseeding, uses her PRNG from the previous steps to generate a, and Bob, without reseeding, uses his PRNG from the previous steps to generate b.
- 5. Alice and Bob perform a Diffie-Hellman key exchange using their generated secrets (a and b). Recall that, in Diffie-Hellman, neither a nor b are directly sent over the channel.

(lear	en the internal state of) in order	ns, select the minimum number of to learn the Diffie-Hellman share of a PRNG between steps 3 and 4	d secret $g^{ab} \mod p$. Assume that		
Q2.1	(3 points) Alice and Bob both use a PRNG that outputs the same number each time.				
	(A) Neither PRNG	(C) Both PRNGs	(E) ——		
	(B) One PRNG	O(D) Eve can't learn the secret	(F) —		
Solution: Eve observes the PRNG outputs. Since both PRNGs output the same time, Eve also learns the values of a and b . She can use this to compute the $g^{ab} \mod p$ without compromising any PRNGs.					
Q2.2	(3 points) Alice uses a secure, r number each time.	ollback-resistant PRNG. Bob use	s a PRNG that outputs the same		
	(G) Neither PRNG	(I) Both PRNGs	(K) —		
	(H) One PRNG	(J) Eve can't learn the secret	(L) —		
	Solution: Eve observes Bob's PRNG output and learns the value of b . Alice will send $g^a \mod p$ in his half of the exchange. Eve can compute $(g^a)^b \mod p$ to learn the shared secret without compromising any PRNGs.				

Page 4 of 8

Q2.3	(3 points) Alice and Bob both use a secure, rollback-resistant PRNG.				
	(A) Neither PRNG	(C) Both PRNGs	(E) ——		
	(B) One PRNG	O(D) Eve can't learn the secret	(F) ——		
Solution: Eve only needs to compromise one PRNG to learn one of the secrets. For if Eve compromises Alice's PRNG, she learns a and can compute $(g^b)^a \mod p$ to shared secret (because Bob sends $g^b \mod p$ in his half of the exchange). Alternatic compromises Bob's PRNG, she learns b and can compute $(g^a)^b \mod p$ to learn secret (because Alice sends $g^a \mod p$ in her half of the exchange).					
For	the rest of the question, conside	r a different sequence of steps:			
1.	. Alice and Bob each seed a PRN	IG with different random inputs.			
2.	Alice uses her PRNG from the previous step to generate b .	e previous step to generate a , an	d Bob uses his PRNG from the		
3.	3. Alice and Bob perform a Diffie-Hellman key exchange using their generated secrets (a and b).				
4.	Alice and Bob, without reseedi	ng, each use their PRNG to gener	ate some pseudorandom outpu		
5.	Eve learns both Alice's and Bo	b's pseudorandom outputs from s	tep 2.		
As b	pefore, assume that Eve always l	earns the internal state of a PRNO	6 between steps 3 and 4.		
Q2.4	(3 points) Alice and Bob both u	use a secure, but not rollback-resis	stant PRNG.		
	(G) Neither PRNG	(I) Both PRNGs	(K) —		
	(H) One PRNG	(J) Eve can't learn the secret	(L) —		
	Solution: Because there is no rollback resistance, if Eve compromises one PRNG, Eve can deduce previous PRNG output and learn a secret (either a or b), which is enough to compute the shared secret (as in the previous part).				
Q2.5	(3 points) Alice and Bob both use a secure, rollback-resistant PRNG.				
	(A) Neither PRNG	(C) Both PRNGs	(E) ——		
	(B) One PRNG	(D) Eve can't learn the secret	(F) ——		
	_	promises both PRNGs, because that b (i.e. previous PRNG output).	•		

Q3 Bonsai (10 points)

EvanBot wants to store a file in an untrusted database that the adversary can read and modify.

Before storing the file, EvanBot computes a hash over the contents of the file and stores the hash separately. When retrieving the file, EvanBot re-computes a hash over the file contents, and, if the computed hash doesn't match the stored hash, then EvanBot concludes that the file has been tampered with.

Clarification during exam: Assume that EvanBot does not know if hashes or files have been modified in the untrusted datastore.

- Q3.1 (4 points) What assumptions are needed for this scheme to guarantee integrity on the file? Select all that apply.
 - (A) An attacker cannot tamper with EvanBot's stored hash
 - ☐ (B) EvanBot has a secret key that nobody else knows
 - \square (C) The file is at most 128 bits long
 - (D) EvanBot uses a secure cryptographic hash
 - \square (E) None of the above

☐ (F) ——

Solution: In order to guarantee integrity on this file, we need two assumptions to hold.

First, the attacker shouldn't be able to tamper with the stored hash. If they could, then the attacker could simply replace the file with an arbitrary file of the attacker's choice, and replace the original stored hash with a hash over this new file. EvanBot's check on the file would succeed.

If EvanBot had a secret key, then EvanBot could change the scheme to use a MAC using the secret key instead of a hash. However, since this scheme uses a hash, a secret key doesn't help us here.

The file being 128 bits long has no relevance to this question.

Finally, the hash must be a secure cryptographic hash. A quick counterexample: if EvanBot used a hash function that mapped every input to the hash value "1", then the attacker could choose an input of their choice, and the check on the hash would always succeed.

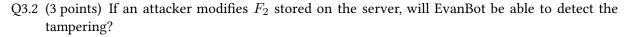
For the rest of this question, we refer to two databases: a *trusted database* that an adversary cannot read or modify, and an *untrusted database* that an adversary can read and modify.

Assume that H is a secure cryptographic hash function and || denotes concatenation.

EvanBot creates and stores four files, F_1 , F_2 , F_3 , and F_4 , in the untrusted database. EvanBot also computes and stores a hash on each file's contents in the untrusted database:

$$h_1 = H(F_1)$$
 $h_2 = H(F_2)$ $h_3 = H(F_3)$ $h_4 = H(F_4)$

Then, EvanBot stores $h_{root} = H(h_1 || h_2 || h_3 || h_4)$ in the trusted database.



 \bullet (G) Yes, because EvanBot can compute h_{root} and see it doesn't match the stored h_{root}

 \bigcirc (H) Yes, because EvanBot can compute h_2 and see it doesn't match the stored h_2

(I) No, because the hash doesn't use a secret key

 \bigcirc (J) No, because the attacker can re-compute h_2 to be the hash of the modified file

(K) —

(L) ---

Solution:

In this scheme, we have a trusted database that an adversary cannot read or modify. Because we have this trusted database, it's possible to ensure integrity through the use of hashes, despite them not being signed (like MAC's).

Let's walk through what happens if an attacker modifies F_2 . If the attacker modifies this file and nothing else, then it's easy for Bot to detect tampering: Bot just has to recompute a hash over F_2 and realize that it doesn't match h_2 .

However, an attacker can also modify h_2 to be the hash of the malicious file, since it's in the untrusted database. Because of this, in order to detect tampering, Bot has to use the only thing that the attacker doesn't have access to: h_{root} , which is stored in the trusted database.

Based on this information: the simplest way to verify the integrity of F_2 is to:

- 1. Recompute a hash over F_1 , F_2 , F_3 , and F_4 .
- 2. Recompute h_{root} using these hashes.
- 3. Compare this h_{root} to the stored version of h_{root} .

If the attacker modifies F_2 , then Bot will **always** be able to detect the tampering, since the check on the root hashes will fail.

Q3.3 (3 points) What is the of all four files?	(3 points) What is the minimum number of hashes EvanBot needs to compute to verify the int of all four files?				
(A) 1	O(C) 3	(E) 5			
(B) 2	(D) 4	(F) More than 5			

Solution:

Because the attacker has the ability to modify all files and hashes in the insecure database, Bot needs to make sure that the attacker hasn't modified any single file/hash pair. To do this, Bot need to follow the procedure discussed in Q3.2's solution - recompute a hash over each file (4 hashes in total), and recompute the root hash (1 hash in total).