# **Sparsity for Long-Context LLM Inference**

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#### 1. Introduction

Background Long-context large language models (LLMs) have achieved significant advancements across various fields. However, they face computational challenges due to high memory demands, particularly when the context window extends to lengths as large as 128K or even 1 million tokens. The self-attention mechanism, a core component in transformers, exhibits quadratic computational complexity with respect to sequence length, becoming a substantial bottleneck in managing such extended contexts. Efficient techniques are essential for practical deployment, especially for tasks that require lengthy contexts, such as dialogue systems, document summarization, and question answering.

Importance of Sparsity Introducing sparsity is crucial for handling these large-scale computations. By selectively reducing attention calculations, activating specific parameters, and optimizing key-value (KV) caching mechanisms, sparsity techniques enable models to retain essential information while minimizing computational costs. For example, SPARSEK(Lou et al., 2024) Attention optimizes sparse attention by limiting the number of key-value pairs each query attends to, achieving linear time complexity during generation and offering notable memory efficiency. This efficiency is increasingly critical for models like LLaMA and GPT-4, which are often deployed on resource-constrained devices.

**Objective and Contribution** This report aims to survey key sparsity techniques—specifically focusing on attention sparsity, activation sparsity, model structure sparsity, and KV cache optimization—to address the inference challenges in long-context LLMs. Each of these techniques represents a different approach to reducing computational load, preserving memory, and enhancing inference efficiency without the need for extensive retraining.

### 2. Problem Formulation

Challenges of Long-Context LLM Inference Managing long sequences in LLMs demands substantial computational resources. Due to the quadratic complexity of the attention mechanism, computation time and memory requirements increase exponentially with sequence length. For instance, a LLaMA-65B model requires approximately 365GB of KV cache memory for a batch size of 128 and a sequence length

of 2048, which is nearly three times larger than the model's parameters. Although techniques like KV cache eviction have been proposed, they often lead to performance degradation when important tokens are inadvertently removed, resulting in context loss.

Defining Sparsity and Its Goals Sparsity involves selectively activating only the most critical parts of the model's computations or storage. Attention sparsity reduces the number of tokens each query attends to; activation sparsity deactivates unnecessary neurons; model structure sparsity prunes less critical components like attention heads or layers; and KV cache optimization focuses on retaining only essential tokens in memory to manage long-context dependencies. The ultimate goal is to balance memory usage and computational cost without compromising the model's ability to accurately process long contexts.

## 3. Techniques for Introducing Sparsity

### 3.1. Attention Sparsity

Sparse Attention Mechanisms Techniques such as SPARSEK(Lou et al., 2024) improve efficiency by reducing the quadratic complexity of self-attention to linear. SPARSEK(Lou et al., 2024) utilizes a differentiable top-K mask operator that allows each query to attend to only a fixed number of key-value pairs, thereby achieving constant memory usage and linear computational complexity during inference. Similarly, Low-Rank Approximation for Sparse Attention(Song et al., 2024) employs low-rank projections to approximate the attention map, selecting only the most relevant tokens for computation, which leads to reduced memory usage and enhanced speed.

Query-Aware Techniques Quest(Tang et al., 2024b) introduces a dynamic, query-dependent method by identifying critical tokens based on the current query vector. By selecting only the top-K pages relevant to each query, Quest(Tang et al., 2024b) minimizes the number of tokens processed in each attention calculation, significantly accelerating self-attention and achieving a 7.03× reduction in latency.

### 3.2. Activation Sparsity

**Dynamic ReLU-based Sparsity** TurboSparse(Song et al., 2024) optimizes activation sparsity using a novel dynamic

ReLU (dReLU) function that deactivates certain neurons based on the input, reducing unnecessary calculations without requiring additional fine-tuning. This selective deactivation effectively lowers both the number of active neurons and the overall computational load during inference.

**Top-K Sparsification** Q-Sparse(Wang et al., 2024) applies top-K sparsification to activations, enabling a fully sparse model where only the most critical activations are computed. This method scales well, providing efficiency gains in both computation and input/output operations, making it suitable for managing large models under limited computational budgets.

### 3.3. Model Structure Sparsity

Layer and Attention Head Pruning Techniques such as Mixture-of-Experts (MoE) selectively activate attention heads and layers based on task requirements. This approach reduces the number of active components during inference, significantly lowering resource demands without major loss in accuracy. LoRA-Sparse(Song et al., 2024) also demonstrates that removing redundant attention heads can further improve computational efficiency without sacrificing performance.

### 3.4. KV Cache Techniques

Eviction H2O (Heavy-Hitter Oracle)(Zhang et al., 2023) retains only the most important tokens (heavy hitters) in the KV cache by analyzing accumulated attention scores. This strategy prioritizes tokens that contribute the most to downstream attention computations, reducing memory usage while maintaining inference quality.

Merging CaM(Tang et al., 2024a) and D2O(Wan et al., 2024) introduce merging strategies that combine tokens slated for eviction with others based on attention score similarity. By retaining essential information while compressing less critical data, these methods minimize performance degradation even with significant reductions in the KV cache.

### 4. Challenges and Open Questions

#### 4.1. Challenges of Sparsity

Balancing Sparsity and Accuracy A key challenge is balancing computational efficiency with model accuracy. While techniques like LoRA-Sparse (Song et al., 2024) demonstrate that sparse attention can sometimes enhance performance, there is a risk of diminishing returns or even accuracy degradation if sparsity is applied too aggressively. Designing optimal sparsity patterns is crucial to ensure the model efficiently focuses on important information without overlooking critical details.

Hardware Limitations Existing hardware architectures are often optimized for dense matrix operations. Sparse computations may not fully leverage the capabilities of current hardware, potentially reducing the expected computational gains. This hardware-software mismatch poses a significant challenge in realizing the practical benefits of sparsity in LLMs

**Training Complexity** Sparse models may require specialized training strategies, increasing the complexity and cost of training. Ensuring convergence and stability during training with sparsity constraints is an open question that demands further research. Additionally, integrating sparsity into the training process without introducing significant overhead is a non-trivial task.

Generalization Across Tasks Designing sparsity mechanisms that generalize well across different tasks and data types is challenging. Models may need to be tailored for specific applications, limiting their versatility and increasing development efforts. Achieving a balance between task-specific optimization and general applicability remains an open question.

#### 4.2. Future Research Directions

Future research could focus on developing adaptive sparsity mechanisms that dynamically adjust based on input context length or specific task requirements, further optimizing model efficiency while maintaining performance. This includes exploring self-adjusting sparsity techniques to accommodate the dynamic nature of textual information relevance and investigating new sparse attention algorithms that reduce computational complexity—such as those based on locality-sensitive hashing or low-rank approximations—to uncover novel methods that maintain performance with reduced computational overhead.

Designing specialized hardware accelerators optimized for sparse computations can help bridge the gap between theoretical efficiency gains and practical implementations. Collaboration between hardware designers and machine learning researchers could lead to architectures that better support sparse operations. Exploring hybrid methods that integrate sparsity across attention mechanisms, activation functions, and KV cache management may yield new insights into efficient long-context LLM deployment, providing a holistic approach to efficiency by leveraging sparsity at multiple levels of the model architecture.

Developing supportive tools and frameworks would lower the barrier to research and application in this area, facilitating experimentation with sparse models and accelerating adoption in practical settings. Theoretical analysis of how sparsity affects the model's expressive power and generalization performance can provide deeper insights and guide the development of more effective sparsity techniques. Understanding the fundamental limits and capabilities of sparse models is crucial for informed advancement. Finally, validating sparse models in real-world applications and gathering feedback can inform iterative improvements, ensuring that the models meet practical needs and revealing unforeseen challenges and opportunities to guide future research directions.

### 5. Conclusion

Sparsity techniques in attention, activation, model structure, and KV cache management play a crucial role in optimizing inference in long-context LLMs. By selectively reducing computational load and memory usage, these techniques enable efficient processing without significant loss of accuracy. Future research could explore more adaptive, task-aware sparsity techniques and further investigate sparsity for diverse LLM architectures. Such advancements will help scale these models for real-world applications that demand efficient long-context processing.

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