

The Distribution of Wealth in a Life-Cycle Model with Durables

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1 Introduction

The main goal of this paper is to show how modeling durables in an incomplete markets life-cycle model where agents face idiosyncratic income shocks and thus accumulate precautionary savings can help to explain how agents accumulate wealth over the life-cycle. Such models provide the basis for the analysis of redistributive policies. They shed light on the underlying mechanisms leading to unequal distributions of wealth and consumption. In order to improve policy making it is crucial in understanding these mechanisms.

My starting point is a classical life-cycle model with incomplete markets such as Hintermaier and Koeniger (2011) use. A majority of the literature focuses on models with only one asset, net worth. However, as Fernández-Villaverde and Krueger (2011) show, modeling durables has a big impact on life-cycle savings. Others such as Díaz and Luengo-Prado (2010) show how modelling durables affect the wealth distribution. My thesis contributes to this literature and shows that modeling durables (is either important or unimportant) in order to reproduce the wealth distribution. And thus sheds light on the importance of durables as important driver of the net-worth accumulation. The data I use is directly obtained from Hintermaier and Koeniger (2011). The prime age sample entails 26 to 55 years old. The empirical net-worth distribution I am using consists of distributions for three age groups: 26-35, 36-45 and 46-55. The data is thus particularly suitable to examine how changes in parameters affect different age-groups in an adverse manner. I will therefore put a stronger focus on these differences and thus contribute to the literature on net worth particularly in this point.

2 Literature Overview

THIS SECTION WILL BE SPLIT UP INTO INTRODUCTION, FACTS AND GENERATING A WEALTH DISTRIBUTION

Investigate empirical predictions of the life-cycle incomplete markets model (Gourinchas and Parker (2002); Cagetti (2003); Castaneda, Diaz-Gimenez, and Rios-Rull (2003); Yang (2009); Kaplan and Violante (2010); Hintermaier and Koeniger (2011)), thus contribute to the literature that (note copy paste.... demonstrate that a plausibly parameterized version of their models can quantitatively explain empirical findings as arising from rational choices of consumers facing an increasing wage profile and income uncertainty.) The model is based on the classic income-fluctuation problem in which the consumer faces a stochastic income process and decides in every period how much to save and how much to consume. Important contributions to the literature are Deaton (1991), Carroll (1992,1997), Gourinchas and Parker (2002). (note copy paste... Following Bewley (1986), this problem has been embedded by Huggett

(1993) and Aiyagari (1994) into a general equilibrium framework, giving rise to the endogenous determination of the interest rate as well as a nontrivial income, wealth, and consumption distribution at equilibrium.) (Note copy paste... Furthermore, this paper relates to other literature such as: Endogenous borrowing constraint: The specification of the borrowing constraint in Fernández-Villaverde and Krueger (2011) is adapted from the recent endogenous incomplete-markets literature: Kehoe and Levine (1993), Kocherlakota (1996), Krueger and Perri (1999, 2006), and Alvarez and Jermann (2000). Lustig (2004) also has a model with durable assets and an endogenous borrowing constraint to explain the equity premium puzzle, however agents have full access to Arrow securities and are infinitely lived. Literature on optimal portfolio choice in the presence of consumer durables: Grossman and Laroque (1990), Eberly (1994), Chah et al. (1995), and Flavin and Yamashita (2002).)

Note: missing citations, not all of the above are cited properly!!!!

Literature on wealth distribution!!!!

3 Facts about the wealth distribution

4 Research strategy

4.1 The issue with the richest

In the following I explain the strategy I use to shed light on the effect of different parametrisations on the wealth distribution as well as the life-cycle behavior of consumers.

As I will further discuss below, one crucial driver of heterogeneity, which manifests itself through different portfolio holdings in these models, is the income process. Permanent uninsurable income shocks lead to different choices in the accumulation of assets and eventually lead to a wealth distribution. Hence, the modeling of the income process is crucial.

Two general approaches can be distinguished. For one, there is the approach to closely match the individual income process and hence calibrating the income process independantly of wealth distributional aspects. Hintermaier and Koeniger (2011) or Hintermaier and Koeniger (2016) estimate age effects from the data and then take the variance of the residuals to retrieve the income shocks. The big plus of such an approach is to closely model the income process on a micro level. Changes in determinants of this process can thus be directly incorporated in the analysis. The downside is, that such models are not able to match the top part of the wealth distribution Fella and De Nardi (2017). Another approach commonly used in the literature is thus to calibrate

the income process to match features of the income- as well as the wealth distribution at the same time. This approach is based on a paper from Castaneda et al. (2003). (OR ADDING PARETO SHAPED TAIL PIKETTY AND SAEZ 2003) It entails modeling extreme income shocks in order to provoke precautionary savings to match the vast accumulation of assets by the very top of the wealth distribution. Due to the problem mentioned above, more recent literature dealing with the empirical validity of bewley-type models for the wealth distribution have further investigated the reproducibility of the high concentration of wealth for the richest. De Nardi and Yang (2014) show that adding voluntary bequests and intergenerational transmission of earnings drastically improves the model's prediction for the empirical cross-sectional differences in wealth at retirement as well as their correlation with lifetime incomes. Krusell and Smith (1998) were the first to point out that a stochastic discount factor across dynasties can account for the variance of the cross-sectional distribution of wealth and does increase the wealth concentration among the richest. Other approaches are: A heterogeneous interest rates (Benhabib, Bisin, and Luo, 2015), a richer earnings process (De Nardi, Fella, and Pardo, 2016) or entrepreneurship (Cagetti and De Nardi, 2009). Although these additional modeling features are able to better approximate the right tail of the wealth distribution, they still fail to produce a satisfying representation.¹

I will thus chose the former strategy. Since calibrating the income process separately from the wealth distribution and thus reproducing a more realistic modeling of income risk does not allow for a representation of the right tail of the wealth distribution I focus on the distribution up to the 9th percentile. As Hintermaier and Koeniger (2011) argue this strategy is robust if general equilibrium feedback effects on the consumers excluded do not adversely affect the result.

4.2 Prime Age Sample

Moreover, I will focus on consumers aged between 26 and 55, where income risk plays an important role for the accumulation of savings.

5 Generating a wealth distribution

In the following section I discuss the economic model considered and outline the most important considerations made within the literature. Firstly, I discuss the life-cycle modeling and the literature, which applies life-cycle and to be more exact imperfect markets models in the context of wealth distributions. Secondly, I present my modeling

¹For a more indebted review of this literature see (Fella and De Nardi, 2017)

choices and solution methods applied for this particular problem.

5.1 Modeling Literature

5.2 The Model

Before going into a more detailed description of the model at hand it is important to understand the modelling choice. Why a life-cycle model with an imperfect market structure? Why include durables as an additional asset choice to the more standard approach, which does summarize all assets in a one period bond, such as for example Hintermaier and Koeniger (2011)?

To answer the first question I will mainly refer to the the literature. The second will be discussed in a more detailed manner in the following section, which treads the life-cycle profiles and especially the importance of modeling durables.

5.2.1 Imperfect market structure

The choice of an exogenously determined imperfect market structure allows for a straight forward answer. It comes down to the economic question one poses. The aim here is to demonstrate that such a model can quantitatively explain the empirical net-wealth distribution in the US. The role the imperfect market structure, entering as a limited choice of assets to fully insure against idiosyncratic wage shocks, poses, is thus to produce an endogenous wealth distribution. The savings are first and foremost driven by a precautionary motive to insure for future wage shocks. Knowing that the income may drop in the future consumers save today to achieve a more stable consumption across their life. In a complete market framework consumers could perfectly diversify away idiosyncratic risks (Tideman and Weber, 2010) (and thus would not build a buffer stock of savings for future shocks.) (???????? is this exact?????) The hypothesis of the complete market framework has been rejected by the vast majority of empirical research (Tideman and Weber, 2010). Deaton and Paxson (1994) show that the life cycle profile of consumption inequality is increasing with age, a fact that would be inconsistent with complete markets. Moreover, the assuming away markets, where individuals can trade contingent claims to insure themselves against the idiosyncratic wage shocks is justified by moral hazard problems (Fernández-Villaverde and Krueger, 2011). While in some rare cases - such as when only studying aggregates, it may still be sufficient to consider a complete market framework, when considering wealth-distributive questions, the imperfect market assumption is both necessary from a theoretical perspective and well-founded from an empirical perspective. It remains to discuss the whether it makes sens to treat distributive issues from a life-cycle point of view.

5.2.2 Life-Cycle

As Deaton and Paxson (1994) show, consumption inequality seems to vary with age. Further empirical research does support these findings, indicating that some of the differences in earnings, income, and wealth across households can be attributed to differences in the household's age Rios-Rull, Kuhn, et al. (2016) (FIND BETTER REFERENCES?). Hintermaier and Koeniger (2011) Show that the average net-wealth increases with wealth and that the dispersion of wealth falls with age. Moreover, there is a vast theoretical literature using a different versions of the life-cycle model to discuss distributive questions. Gourinchas and Parker (2002); Cagetti (2003); Castaneda et al. (2003); Yang (2009); Kaplan and Violante (2010);Hintermaier and Koeniger (2011) (CITE MORE RECENT LITERATURE!!!) while there are also some that use infinite horizon models....

Finally, the choice to study the empirical validity of a life-cycle model, which produces a net-wealth distribution arising from rational choices of consumers subject to income uncertainty, moreover allows for a detailed analysis of consumption and savings behavior over a person's live-cycle. A coherent framework incorporating the behavior of household's over their lifespan is paramount for the study of re-distributive policies. (Cite....) These factors thus support the choice of a life-cycle model.

5.2.3 Partial Equilibrium

Last but not least, partial equilibrium as modeling choice has to be discussed briefly. (????????????????)

(copy paste from hintermaier 2011 Note that we assume that changes in the domestic supply of assets do not affect do not affect the interest rate. As in a small-open economy, this price is determined exogenously (on the world markets.) ²)

5.2.4 The Income Process

Kaplan and Violante (2010) discuss various features of the income process in more detail.

5.3 Why model durables? How do durables affect savings?

1. Fernández-Villaverde and Krueger (2011)

²This assumption is not restrictive for our purposes since we observe the price in our ex post analysis for the period 1983-2007. Hence, the supply of assets and the observed price suffice to determine the equilibrium asset quantities. This allows us to be agnostic about the price elasticity of asset demand.

- (a) empirical observation that durables constitute a large fraction of households' asset holdings - hh hold 35% of their total assets in durables and only 28% in equity (flow of funds account 2nd quarter)
- (b) the life-cycle pattern of nondurable consumption may be closely related to the life-cycle pattern of the accumulation of durables and thus any abstraction to net wealth may severely bias the study of asset accumulation (and life-cycle profile of nondurable consumption)

5.3.1 Consumer's Problem

As established above, the baseline model in question is a life-cycle model with an imperfect market structure. I closely follow Hintermaier and Koeniger (2010).³ While their algorithm allows for both a live-cycle and infinite-horizon models, the example model presented in their paper uses the latter. For reasons discussed above, I will in this case opt for a live-cycle formulation. Finally, the baseline model does not include adjustment costs. These are considered in a later section of the model.

There is a continuum of risk averse consumers with a finite time horizon. At age 90 consumers die with certainty, younger consumers between the age of 26 and 90 may die with probability $\pi_j < 1$ at age j . Until retirement the labor income of each individual i y_{ij} is stochastic. After the age 65 is completed, they retire with certainty and receive individual-specific retirement benefits b_i .⁴ Consumers derive utility from a durable good d and a non-durable good c . The utility function $U(c, d)$ is strictly concave, increasing and non-separable in c and d (REALLY??? When not??? all three true???). In each period consumption c_j , the durable good d_{j+1} and the financial risk-free asset a_{j+1} are chosen after receiving the income. Agents then derive utility from consumption and durable services, before the assets pay returns. While the liquid assets return an interest rate r durables depreciate at rate δ . As previously discussed, such a market structure implies that markets are incomplete and agents will accumulate a buffer stock in order to save for rainy days. The ex-ante identical consumers thus will thus, depending on their income trajectory, end up with different portfolios of the endogenous state variables. The model is therefore suited to match empirical facts about net worth positions since it does produce an endogenous distribution of portfolios, which differs in age and income. Moreover, (THE ADVANTAGE OF DURABLES) besides providing services and thus allowing consumers to derive utility from durables, their durability implies, that they may be used as collateral. It is assumed that all credit needs to be collateralized.⁵

³In order to facilitate comparability, I will closely follow the notation used in their paper.

⁴The construction of these benefits is discussed in the Appendix.

⁵About 85% of household debt in the Survey of Consumer Finances 2004 is secured by collat-

The collateral constraint takes the form:

$$\underbrace{\mu(1 - \delta)d_{j+1} + \gamma y}_{\text{collateral}} \geq -(1 + r)a_{j+1} \quad (1)$$

where \underline{y} is the minimum labor income realization ⁶ and $\mu \in [0, 1)$ and $\gamma \in [0, 1)$ are the respective fractions of the durable stock and of minimum labor income, which can be collateralized. ⁷

It is useful to rewrite the constraint in terms of total wealth and future durable holdings. Total wealth available to a consumer in each period is

$$x_j \equiv (1 + r)a_j + (1 - \delta)d_j, \quad (2)$$

rewritten the constraint then looks like this:

$$x_{j+1} \geq -\gamma \underline{y} + (1 - \mu)(1 - \delta)d_{j+1} \quad (3)$$

One now sees that total wealth needs to be larger than the negative value of the minimum fraction of income that can be collateralized and the fraction of wealth which cannot be used as collateral. Furthermore, under the assumption that $\mu < 1$ d_{j+1} is determined for a given x_{j+1} , when the constraint binds.

Although in my baseline model they are set to 0, I also consider the case where durables can only be adjusted with some costs:

$$\Psi(d_{t+1}, d_t) = \frac{\alpha}{2} \left(\frac{d_{t+1} - (1 - \delta)d_t}{d_t} \right)^2 d_t. \quad (4)$$

8

Finally, the specification of the budget constraint, follows from the above:

$$a_{j+1} + d_{j+1} + c_j + \Psi(d_{t+1}, d_t) = x_j + y_j \quad (5)$$

eral.(Hintermaier and Koeniger, 2010)

⁶CHECK THIS WITH CODE!!!

⁷It is important to note that this constraint guarantees full repayment by consumers and thus acts as non-bankruptcy constraint. This is assured by the timing assumptions made above –The lender does know the financial portfolio choice (a_{j+1}, d_{j+1}) and the minimum of the support of the income distribution \underline{y} , however future individual income draws y_{j+1} do remain obscure to him. Finally, note that only choices in j determine, whether the constraint is binding or not.

⁸(Hintermaier and Koeniger, 2010) use the same specification, which is based on the investment literature (COPY PASTE(see, for example, ?,p.192)). Costs are differntiable in d_{t+1} and d_t . Moreover, by letting the durable stock depreciate, consumers can avoid these costs. In this particular specification, adjustment costs do not affect the collateral constraint, as it is assumed that these costs do not have an impact on the sales of collateral seized by lenders. NOTE (Hintermaier and Koeniger, 2010) EXPLAIN IN APPENDIX VERSION WHERE THIS IS THE CASE.

The recursive formulation of the household problem I will proceed by depicting the case prior to retirement. (SPECIFY RETIREMENT CASE!!!) We let T^r denote the first period of retirement. The Bellman equation prior to retirement, if $j < T^r$ thus is:

$$v_j(x_j, d_j, y_j) = \max_{a_{j+1}, d_{j+1}} \left[U(\underbrace{x_j + y_j - a_{j+1} - d_{j+1} - \Psi(d_{t+1}, d_t)}_{c_j}, d_j) + \hat{v}_j(x_{j+1}, d_{j+1}, y_j) \right] \quad (6)$$

where the expected next period value function is discounted by the product of the probability of survival $(1 - \pi_j)$ and the discount factor β

$$\hat{v}_j(x_{j+1}, d_{j+1}, y_j) \equiv \beta(1 - \pi_j)E_j v_{j+1}(x_{j+1}, d_{j+1}, y_{j+1}),^9 \quad (7)$$

with the constraints:

$$a_{j+1} + d_{j+1} + c_j + \Psi(d_{t+1}, d_t) = x_j + y_j, \quad (8)$$

$$x_{j+1} = (1 + r)a_{j+1} + (1 - \delta)d_{j+1}, \quad (9)$$

$$x_{j+1} \geq -\gamma \underline{y} + (1 - \mu)(1 - \delta)d_{j+1}, \quad (10)$$

(WHAT HAPPENS WITH MIN Y IN RETIREMENT???)

$$d_{j+1} \geq d_{min}, \quad (11)$$

FROM RED PAPER HELP TO SPECIFY CASE WITH RETIREMENT!!! We specify our model in discrete time. Rearranging the budget constraint, consumption of individual i with age j is

$$c_{ij} = \begin{cases} (1 + r)a_{i,j-1} - a_{ij} + y_{ij} & \text{if } j < T^r, \\ (1 + r)a_{i,j-1} - a_{ij} + b(z_{i,T^r-1}) & \text{if } j \geq T^r, \end{cases} \quad (12)$$

where $b(z_{i,T^r-1})$ are the retirement benefits. These benefits depend on the last realization of labor income before retirement z_{i,T^r-1} as we explain further in the next section. Defining cash-on-hand as

$$x_{ij} = \begin{cases} (1 + r)a_{i,j-1} + y_{ij} & \text{if } j < T^r, \\ (1 + r)a_{i,j-1} + b(z_{i,T^r-1}) & \text{if } j \geq T^r, \end{cases} \quad (13)$$

we can write the Bellman equation as

$$V_j(x_{ij}, y_{ij}) = \max_{a_{ij} \geq 0} [u(\underbrace{x_{ij} - a_{ij}}_{c_{ij}}) + \beta(1 - \delta_j)E_j V_{j+1}(x_{i,j+1}, y_{i,j+1})], \quad (14)$$

where we restrict the choice of assets to $a_{ij} \geq 0$, as motivated in the previous section.)

6 Calibration

The calibration strategy demands to be in line with the aim of the paper - discussing the importance of modeling durables in context of the distribution of net worth. It is thus crucial to satisfy a high degree of comparability with other work dealing with net-worth distributions. Moreover, the calibration ought to replicate some features of the data, without containing too much information on the features the model is asked to show. (CITE SOME BOOK/ PAPER). In order to give insight on the underlying parameters of the cross-section of inequality I will thus proceed in the following way. As discussed above, I base the parametrisation of model on Hintermaier and Koeniger (2011) and apply the algorithm introduced by Hintermaier and Koeniger (2010) to solve the model with durables.

6.1 The income process

As discussed above the income process is an important driver of the accumulation of savings in the form of precautionary savings. Its calibration does thus decisively influence the outcome. Hintermaier and Koeniger (2011) use the SCF cross sections to construct a measure for labor earnings risk before retirement purging labor earnings from age effects for consumers between age 26 and age 65. The authors assume that log of earnings y_{ij} of individual i at age j before retirement is additively separable in a deterministic age polynomial ϕ_j and an idiosyncratic income shock z_{ij} :¹⁰

$$y_{ij} = \phi_j + z_{ij}$$

,

where the shock z_{ij} follows an AR(1) process

$$z_{ij} = \rho z_{i,j-1} + \epsilon_{ij}$$

After retirement the income process is deterministic. Thus, each individual receives retirement benefits from social security, the level of which is determined by the last period's income resulting in a replacement ratio of benefits over gross income of 52% for

¹⁰This approach is quite standard in the literature (see others! NEWERS THAN YANG AND KAPLAN VIOLANTE)

the median income in the last period before retirement. The approximation takes into account the US social security legislation(<http://www.ssa.gov>).¹¹ The age polynomial ϕ_j is obtained by regression the log of earnings on a quartic age polynomial in each survey year of the SCF data between ages 26 and 65.¹² The then obtained standard deviation of the residuals are used to calibrate the distribution of earnings shocks z_{ij} , with the assumption that the shocks are drawn from a normal distribution. This means that in the calibration to the SCF 1983, $z_{1983} \sim \mathcal{N}(0, 0.498)$, and in the calibration to the SCF 2004, $z_{2004} \sim \mathcal{N}(0, 0.607)$. (POSSIBLY COMPARE THIS RISK TO OTHER STUDIES ALSO SEE KRUEGER AND PERRI 2006) The calculations for the experience premium displays a concave relationship between the base age and the rising age it is compared to. Moreover, the experience premium has risen since the 1980s. The autocorrelation of the log-earnings shocks are calibrates as $\rho = 0.95$, which implies a variance for the innovations of $\epsilon_{ij} = 0.048$. (HERE ALSO COMPARE TO OTHER, MORE RECENT LITERATURE) The AR(1) process for z_{ij} is then approximated by a Markov chain with 21 income states via the Rouwenhorst method.

Finally, the authors adjust for growth in life-cycle income to convert the cross-sectional age-earnings pattern into life-cycle profiles considering a growth factor of $1.015^{age-baseage}$, where the base age is a reference age to make income units comparable across cohorts of different years.

The choice for the comparison of the SCF 2004 with the SCF 1983 is motivated by the fact that both surveys have been undertaken at similar points in the business cycle.

Controlling for the age distribution is another important determinant for the dynamics!

It is worth noting that the smallest income is larger than 0!!!!

Income Process LOOK AT GOURINCHAS and PARKER(2002) AND AT THE ADDA and COOPER BOOK!

1. (Fernández-Villaverde and Krueger, 2011) stochastic labor income process up to age 65, where they impose mandatory retirement. Differs from other specifications such as Abowd and Card (1989), Carroll (1992), or Gourinchas and Parker (2002) in two aspects:

¹¹The reader may consult Hintermaier and Koeniger (2011) for a more detailed discription of the calibration of the retirement benefits.

¹²The table in appendix A displays the experience obtained by Hintermaier and Koeniger (2011).

- (a) do not allow labor income to go to zero- very low probability Carroll (1992) estimates it at 0.003 for a year. However, its effects on the intertemporal allocations are quite big, since hh will not borrow any positive amount since they might face a lifelong sequence of zero labor income and might be unable to consume a positive amount and repay their debt in some period. (Moreover, argument of public income-support programs in the US -> labor in the model is after-tax, after-government transfer labor income.
- (b) unit root in AR process is not imposed (is something that is debated -> they show that their results are not very sensitive toward this issue -> increase ρ toward unity (LOOK AT STORESLETTEN ET AL: (2001) -> do not reject unit root.

2. Check Hintermaier and Koeniger (2010) and Hintermaier and Koeniger (2011)

6.2 Utility parameters

I consider a utility function that is non-separable in durable- and non-durable consumption, strictly increasing in both consumption types, strictly concave and obeying the INADA-Conditions with respect to nondurable consumption. It is the same class of preferences as Hintermaier and Koeniger (2010), which is commonly used in the literature considering durable and non-durable consumption (CITE MORE).¹³

$$U(c, d) = \frac{\psi(c, d)^{1-\sigma} - 1}{1-\sigma} \quad \text{where} \quad \psi(c, d) = c^\theta (d + \epsilon_d)^{1-\theta}, \quad (15)$$

where I assume $\epsilon_d > 0$, which thus indicates a number small enough to be irrelevant for the quantitative exercise at hand but nonetheless larger than zero. The CRRA utility function with the Cobb-Douglas specification of the consumption index, thus allows for zero consumption of durables, while the INADA-Condition ensures that people always consume some non-durables, i.e. intuitively this means consumers cannot survive without food, but are allowed to survive without houses and cars.¹⁴ (WHAT IS THE CONSEQUENCE OF OMITTING THE EPSILON????

(Fernández-Villaverde and Krueger, 2011) utility from death is normalized to 0 ??????????

The risk-aversion σ typically takes values from 1-5 in the literature (Yang, 2009). Following the aforementioned author I use $\sigma = 1.5$ as estimated by Attanasio, Banks, Meghir, and Weber (1999) and Gourinchas and Parker (2002) from consumption data.

¹³Note that this choice is in line with a more generic formulation of the utility function (Fernández-Villaverde and Krueger, 2011).

¹⁴For the recursive problem it means that when allowing the potentially optimal choice $d' = d_{min}$, the constraint for minimal durable holdings needs to be accounted for explicitly, as the INADA-Conditions do not implicitly exclude zero durable consumption.

The discount factor β and the weight on non-durable consumption θ are calibrated to match the average net-worth holding and average durable holding of the prime age population up to the 90th percentile, respectively. The data moments are 2.95 for the durable holdings and 2.39 for the net-worth in terms of median labor-income. TO MATCH HOW EXACT: SHOW WITH SMALL TABLE (BE CAREFUL TO BE SPECIFIC ENOUGH!) To calibrate the two parameters I solved the for a grid of (??????) for θ and a grid of (???????) for β . The choice to match the 90th percentile and the population from 26 to 55 years old is motivated by the fact that calibrating the model for the whole data-set would lead to overestimating the net-worth holdings of the prime sample –as is both the population above 55 years of age and above the 90th percentile hold more wealth on average than in the prime age sample. The estimation procedure is explained in more detail in appendix B.

Table 1: This table depicts the parameter estimates matching the average durable holdings and average total worth of the prime age population in the data.

Parameters	Baseline	Alternative
β	0.991	??
θ	0.761	???

(BE MINDFUL OF THE FACT THAT HINTERMAIER 2016 HAS 0.76 FOR HOUSING - SAME SAMPLE!!!!!!) The estimation results are somewhat different from what other authors with similar models have obtained. (NOTE DIFFERENCE INF HORIZON AND LIFE CYCLE) Fern andez-Villaverde and Krueger (2011) estimate a weight on non-durable consumption of 0.81, Yang (2009) 0.8615 and Hintermaier and Koeniger (2010) 0.8092. (CITE NEWER STUDIES) Whereas studies solely considering housing, obtain estimates more closely to mine (CITE THESE STUDIES). This should, however, not be surprising, as I used data moments which correspond to the means of the above defined prime-age sample, contrary to these other studies, who calibrated their to the whole sample. D  az and Luengo-Prado (2010) among others, show that the empirical portfolio composition changes over life-time, as will be discussed more in detail below. Young households take on credit to invest in durables and older households accumulate assets to finance retirement. The fraction of durables of total wealth, as the two data moments show 2.95/2.39 is larger than one for the prime-age sample, since the average liquid assets are negative. Where as for the whole sample the fraction of average durable holdings in terms of average total wealth 4.45/6.33 is smaller than one (Hintermaier and Koeniger, 2010). The estimated discount factor β is quite similar to the one in Hintermaier and Koeniger (2011).

6.3 Further inputs

As is common in the literature dealing with the period of the great moderation and supported by empirical evidence, the interest rate r is set to 4%. (CITING LITERATURE). As discussed above, this partial equilibrium approach entails the assumption of a small open economy. Furthermore, I set the loan-to-value ratio $\mu = 0.8$. Although commonly used in the literature, this is a rather conservative assumption for the loan-to-value ratio: CAPLIN ET AL (1997) claim that it is almost impossible for a hh to obtain a house without paying at least 10%, moreover (OTHER AUTHOR IN HINTERMAIER2010 max LTV). However, this will allow me to investigate the effects of recent years, which lead to a relaxation of the LTV (IacovielloandPavan 2013) or (THAT OTHER PAPER ABOUT THE DENSITIES OF LTV). Finally, as in Hintermaier and Koeniger (2010) $\gamma = 0.97$ is chosen to be smaller than 1 in order to assure positive consumption at the smallest gridpoint of next periods net-worth x' . The probabilities of death as in Hintermaier and Koeniger (2011) are taken from Table 1 of the decennial life tables 1979-1982 and 1999-2001 for the calibration of 1983 and 2004, respectively.¹⁵ (COMMENT ON WHY THESE ARE IMPORTANT!)

7 Numerical algorithm

The problem above does not provide a closed-form solution (CITE!!!!) and thus the solution has to be approximated numerically. Hintermaier and Koeniger (2010) offer a solution for problems of this type. They expand the endogenous gridpoints method (EGM) proposed by Carroll (2006) for a problem with two states and thus providing a very efficient algorithm to solve models with durables and collateralized debt. As their algorithm is formulated recursively, it is well suited to solve life-cycle models.¹⁶ I iterate over the policy function starting in period $j = T$ where the consumer sells all liquid assets and durables (TIME ASSUMPTION OF DURABLES IS IMPORTANT HERE - agents retrieve utility from the durable stock before it is sold, and can consume afterwards????) to consume them before death. It thus holds that $x' = d' = a' = 0$ and thus the initial consumption policy is $c(x, d_j, y_{kj}) = x + y_{j,k}$ (NOTE CASE WITHOUT ADC). Each iteration n on the policy function then gives the the solution for the period $T - n$, where in my case $n = 65$ which corresponds to ages 90 to 26.

The exogenous grids for d and x are chosen as follows:

¹⁵They are published by the National Center for Health Statistics at http://www.cdc.gov/nchs/products/life_tables.htm.

¹⁶Solving such models has been considered particularly expensive and challenging, as durables enter as additional state (if non-separability utility from durables and non-durable or adjustment costs are allowed for) and durables increase the dimensionality of the portfolio choice.(Hintermaier and Koeniger, 2010)

(NOTE THAT ALGORITHM MUST BE CHANGED FOR CASE WITH ADJUSTMENT COSTS)

For each period $t < T-1$, the algorithm proceeds as follows. In a first step it maps x' into d' and in a second step it solves for the current choice c and state x from optimal future combinations (x', d') . Moreover, the values for the exogenous grid are chosen such that the results are not affected. (BE MORE PRECISE INDICATE DIFFERENCES BETWEEN POST/PRE RETIREMENT (expectation)!

7.0.1 Comparing the simulation output with SCF data

Data (Initializing DATA + probability of death (PLOT!))

8 Life-Cycle Profiles

As discussed above, the choice of a life-cycle model is mainly motivated by the fact, that age plays an important role in questions related to wealth distribution and in particular to the net-wealth distribution. This section will give insight into the accumulation of wealth by agents over their lifetime. As we will see, this also affects consumption. Fernández-Villaverde and Krueger (2011) have pointed out that it is paramount to consider durables in order to properly model the life-cycle profile of consumption, which is hump shaped. The first section discusses empirical results as well as life-cycle profiles produced by models from theoretical research. In the second section I will produce and comment on the life-cycle profile of my baseline model and then go over to a more detailed investigation of certain factors in the third section.

LOOK AT GOURINCHAS and PARKER (2002) for more insight

8.1 Life-Cycle profiles in the data and theoretical literature

This section discusses a number of important issues discussed by the theoretical literature related to empirical patterns. I thereby focus on issues discussed in relation to durables.

8.1.1 Consumption smoothing

The standard life-cycle model with complete financial markets predicts, that individuals smooth consumption over their lifetimes and across states of the world.¹⁷ This is true if the one period utility function and the time discount factor are constant. As households

¹⁷NEED TO FIND GOOD REFERENCES!!! SEE also: Further empirical literature about the life-cycle profile of consumption observed in cross-sectional micro data: Blundell et al. (1994), Attanasio and Browning (1995), Attanasio and Weber (1995), Gourinchas and Parker (2002).

will then choose consumption plans in order to equate marginal utility across time and states of the world. Potentially they might do this with some growth rate, depending on the relative size of the real interest rate and the discount factor. (COPY PASTE (Fernández-Villaverde and Krueger, 2011): "Under CRRA (Constant Relative Risk Aversion), period utility consumption growth itself should be constant across time. With complete markets, consumption smoothing can be achieved through the transfer of contingent claims across periods and states. (this statement relies on the further assumption that leisure and consumption are separable in the period utility function.") However, the data shows that consumption of both, non-durables and durables, is hump shaped over the life-cycle.¹⁸ (amongst others CITE MORE). As these authors point out it is important, especially for policy considerations, such as social security reforms, public provision of saving incentives, or welfare consequences of progressive taxation, as these will vary by age group. Fernández-Villaverde and Krueger (2011) show that 50% of the consumption hump can be accounted for by adjustment through family size. However, the other 50% can only be explained by including durables. Namely, if the period utility function is separable in nondurable consumption and durable consumption, the real interest rate will be equal to the time discount factor and remain constant over time. It thus follows that optimizing households will buy the desired stock of durables early in life and then only replace depreciation from there on. However, as the data shows, durable consumption is hump shaped, which is consistent with work, which has documented liquidity constraints in the purchases of consumption durables¹⁹ or argued that it is vital to consider nonseparabilities in the utility function²⁰.

In this first section, Fernández-Villaverde and Krueger (2011) thus contradict Blundell et al. (1994), Attanasio and Browning (1995) and Attanasio et al. (1999), who argue that if one adjusted the consumption data for changes in household size (which is also hump-shaped over the life-cycle) the hump in life cycle consumption disappears.

Income tracking consumption (COPY PASTE :Deaton (1992) provides an overview for the literature answering this question. The main stylized fact emerging in this literature was that consumption seems to track income over the life cycle, changing only when income changes and not when it becomes known that income will change, as economic theory predicts. was interpreted as indication for liquidity constraints or

¹⁸In the Consumer Expenditure Survey (CEX), when the head of household is 50, the average household spends 63% more when he or she is 25 and 70% more when he or she is 65 (Fernández-Villaverde and Krueger, 2011).

¹⁹NOTE COPY PASTE FROM FV& K2011 Eberly (1994); Alessie et al. 1997; Barrow and McGranahan (2000); Attanasio et al. (2005)

²⁰NOTE COPY PASTE FROM FV& K2011 Attanasio and Weber (1995)

other financial market imperfections. The empirical observation that consumption initially underresponds to income shocks and then adjusts with a delay. Flavin (1985), Campbell and Deaton (1989), Jappelli and Pistaferri (2010))

8.1.2 Portfolio Composition

As Fernández-Villaverde and Krueger (2011) point out households' portfolio composition do vary over the lifetime. Young households only little liquid assets and hold most of their wealth in consumer durables, whereas later in life, they accumulate big amounts of financial assets to save up for retirement. Durables make up 35% of the aggregate composition of wealth, while equity only accounts for 28% (Fernández-Villaverde and Krueger, 2011). The same authors thus show that these facts can better be accounted for, when one considers liquid assets and durables separately, instead of combining them in one asset such as net worth. The interaction of the two assets thus is able to reproduce the observed pattern in the data. Where the consumer durables provide both consumption and collateral services as well as an endogenous borrowing constraint.

8.2 Profiles predicted by the model

In the following section I will discuss the baseline life-cycle profiles produced by the model more in detail and compare it to other work and empirical results presented therein. I will mainly focus on two aspects discussed in the literature. The consumption and income profiles and comparing the asset profiles, which entails a discussion about portfolio allocations over the life-cycle.

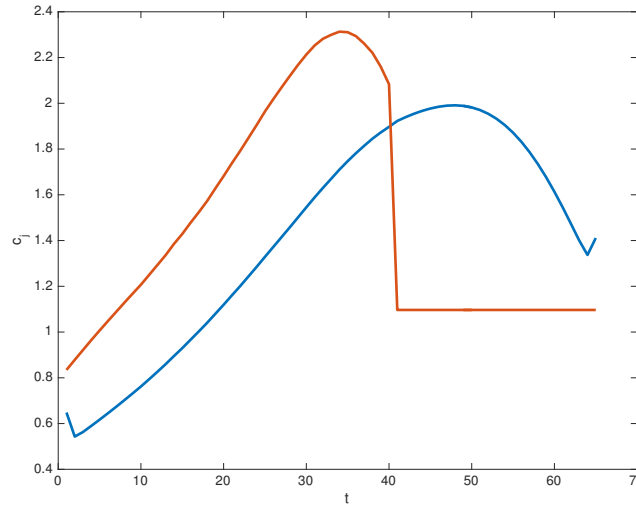
The life-cycle presented in figure 1 and figure 2 show averages of the variables of interest over the simulated population of 100000 consumers aged between 26 and 90. With the exception of net-labor earnings all variables are in units of average net-labor earnings per adult-equivalent. (BE MORE PRECISE HERE)

8.3 Income and Consumption

Income Figure 1 shows the hump of the income profile arising by construction as the process is determined exogenously. Note that this hump shaped profile arises from the experience premium captured by the estimated age polynomial as well as economic growth, up to age 65. Consumers earnings rise until the age of 49, when they reach the maximum log net-income equivalent of 2.3131. Afterwards the experience premium decreases, as the experience factor is dominated by a decrease in productivity to the age of 65, where consumers earn 2.0834, thus around 10% less than when they are at their top. At this point the average income decreases sharply, as every consumer retires

after the age of 65 and receives deterministic retirement benefits from then on, with an average of 1.0966. ²¹

Figure 1: Average Income and Consumption over the Life-Cycle



Consumption is in terms of average net labor-earning equivalents and the labor earnings are as calibrated, the log of net labor earnings-equivalents????? JUST VERY STANDARD! NEEDS TO BE UPDATED

Consumption Figure ?? show the life-cycle profile of consumption. The peak is around retirement, with a size that is about 125% bigger than at the age of 26. (NOTE Fern  ndez-Villaverde and Krueger (2011) are only at 40% !!!!!!!). Consumption increases in the early part of life, mainly due to two reasons. Note that both depend on the presence of durable goods. First of all, since durables also generate utility, it is optimal to stock durables and compromise on the consumption of nondurables. Secondly, when the stock of durables is built, due to the nonseparabilities in the utility function, the marginal utility from nondurable consumption is higher, since at that point households are better endowed in durables. (SHOW THIS MATHEMATICALLY!!!) Following Fern  ndez-Villaverde and Krueger (2011) (COPY PASTE: the hump shape in nondurable consumption is not per se due to buffer stock behavior as in Carroll (1992) or Gourinchas and Parker (2002), since households, when they have accumulated durables can use it as collateralizable insurance against idiosyncratic labor shocks as their borrowing capacity increases in their durable holdings.

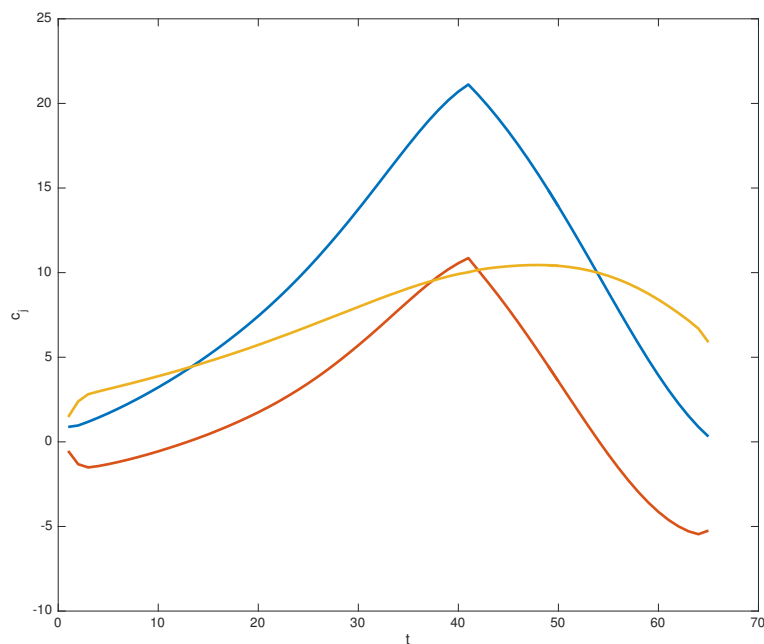
Note that the increase of consumption late in life is due to lifetime uncertainty. As they are never entirely shure at what point they will die, they hold a small buffer even

²¹Following Hintermaier and Koeniger (2011) the growth adjustment is neglected for the retirement period, therefore the curve does not increase for ages 66 to 90. (CHECK IF WOULD HAVE AN EFFECT! OR IS THERE A REASON FOR THIS???)

when retired and subject to deterministic income. As survival probabilities become very small in the last periods, or next to zero. They consume.

Also, since the income increase displayed here is perfectly forecastable (the means of the shocks are 0), this model does display excess sensitivity of consumption to income (income tracking consumption too closely SEE LITERATURE!!!!), which contradicts the predictions of the basic life-cycle model.²²

Figure 2: Average Asset Holdings over the Life-Cycle



NEED TO INDICATE THE MEASURES. JUST VERY STANDARD! NEEDS TO BE UPDATED

Wealth Portfolio ADD FIGURE COMBINING THE THREE? As they are young households borrow as much as possible to accumulate durables. As they get older they start to increase both financial assets and their nondurable consumption. Since households can use their durables to loosen their borrowing constraint the accumulation of liquid assets occurs for life-cycle and not for insurance purposes??????????? The model reproduces a few important factors of the life-cycle composition of wealth:

1. (COPY PASTE (Fernández-Villaverde and Krueger, 2011): Young households save and thus net worth becomes positive at the age of 35 (MINE IS NEVER NEGATIVE!!!) but they do not save in financial assets, but rather accumulate consumer durables.

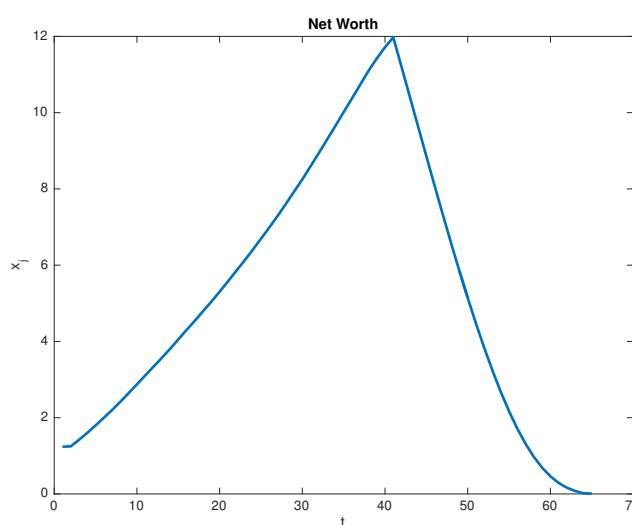
²²See DEATON (1992) for a review

2. As the households get older, they do start accumulating more assets, which are important in retirement. They do hold a lot of net worth until high ages in order to insure against living too long. Elderly households seem to overaccumulate assets. (Seems not to be the case in my model!!!)

Figure 3 shows how net net worth evolves over the life-cycle.

Yang (2009) also shows that young households to virtually own no liquid financial assets, but hold the majority of their wealth as housing. As they age, they shift their portfolios to financial assets.

Figure 3: Average Net Worth over the Life-Cycle



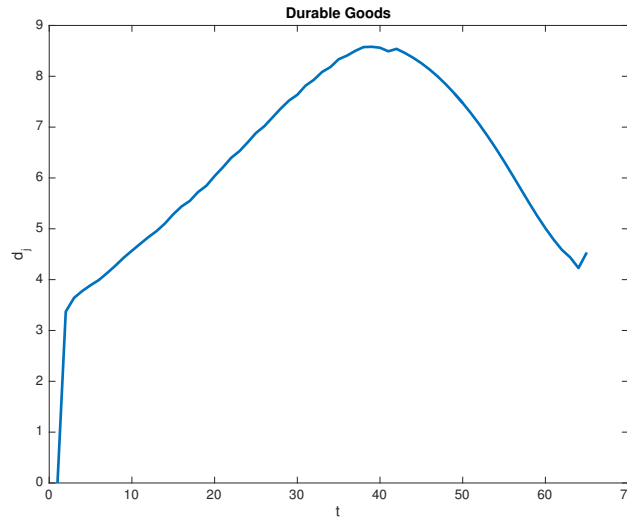
NEED TO INDICATE THE MEASURES. JUST VERY STANDARD! NEEDS TO BE UPDATED

Durables Note that the durables are rather different from (Fernández-Villaverde and Krueger, 2011) (COPY PASTE: Consumer durables: the stock follows a hump shape, differing from a complete-markets model where the desired stock is built up in the first period and only an amount equal to depreciation is spent each period thereafter. Comparing durable consumption (model) and durable expenditure (the data): the model generates a pattern of consumer durables that somehow diverges from the observed pattern: there is a big peak in the first years and then it falls, even though it is possible to see something of a hump after the first spike. One possible explanation is that in the data young families obtain bequests, which in large part come as consumer durables. A second possible explanation is the endogenous formation of households in the data. In our model, all households enter their active economic life at age 20, a time period where they want to build up the desired stock of capital. In the data, however, economically active (in the sense of our model) households are created endogenously

due to differences in marriage timing and education. This endogeneity smooths out the first big spike of durable expenditures in the data and leads to the pattern of life-cycle durables expenditure reported in section 2. (this divergence between data and model may also indicate that our borrowing constraint is specified too loosely, allowing households to invest in consumer durables at too rapid a pace when young.)

Yang (2009) shows that modelling adjustment costs is important to account for the slow downsizing of durables (housing in his case) as agents get older. Since the high transaction costs for trading houses prevents the households from decreasing their stock quickly later in life. He also shows that when agents are young they build a housing stock and compromise on non-housing consumption. Moreover, as they age they start to decrease non-housing consumption because time the time preference is higher than the interest rate and mortality rates are increasing along the life cycle.

Figure 4: Average Durable Holdings over the Life-Cycle



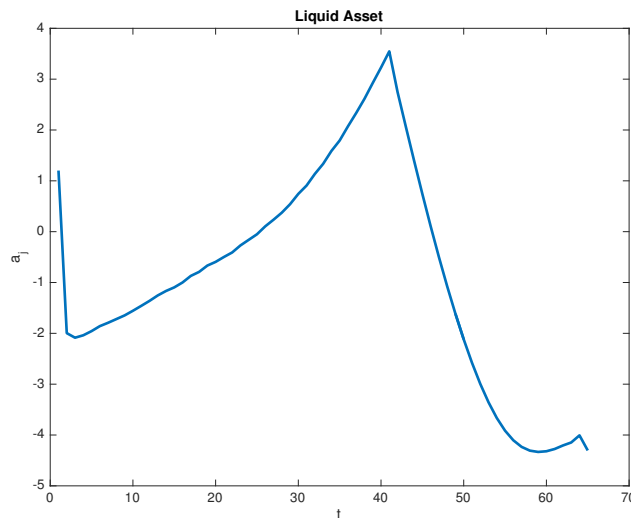
NEED TO INDICATE THE MEASURES. JUST VERY STANDARD! NEEDS TO BE UPDATED

Assets

8.4 What drives the life-cycle profiles within the model?

Yang (2009) investigates the quantitative relevance of transaction costs, borrowing constraints and bequest motives. He shows (COPY PASTE: that borrowing constraints are essential in explaining the accumulation of housing assets early in life, the existence of transaction costs is crucial in explaining the slow downsizing of housing profile later in life.) Moreover, he shows that the bequest motives play a role in determining total lifetime wealth, but not the housing profile!!!! Certain features Yang (2009) has abstracted from and his justification:

Figure 5: Average Asset Holdings over the Life-Cycle



NEED TO INDICATE THE MEASURES. JUST VERY STANDARD! NEEDS TO BE UPDATED

1. no inter-vivos transfers (parents lend children money if they need some), data from Health and Retirement Study suggest that these transfers are fairly small, this would lead to higher durable and non-durable consumption
2. yang uses exogenous borrowing constraints and not endogenous ones. Fernández-Villaverde and Krueger (2011) compare the two and show that life-cycle profiles are identical. only exception, with endogenous borrowing constraints net worth of average young agents is slightly negative
3. no housing rental market
4. no health shocks for elderly, which might be important for accumulation of wealth stock

What I want to look at:

1. Check if income uncertainty zero
2. Check what happens when death proba is always zero
3. Use Ad-Hoc constraint
4. With adjustment costs!

9 Creating a cross-section from simulated life-cycle profiles

10 What features of the Wealth Distribution are explained by the model?

In the previous section we have seen what durables may contribute. Since they do have an impact on life-cycle consumption it seems likely that they will affect the wealth distribution created by the model in one way or the other. In the first part of this chapter I will discuss certain features of the wealth distribution that the baseline model is able to capture. In a second part I will conduct experiments on some parameter changes and analyze how this affects the wealth distribution. Namely, I will drop the adjustment costs, then simulate a model where durables do not provide any utility to provide an insight for the importance of durables. Moreover, I will try different versions of the borrowing constraint, remove the probability of death and finally look at some features of the income process.

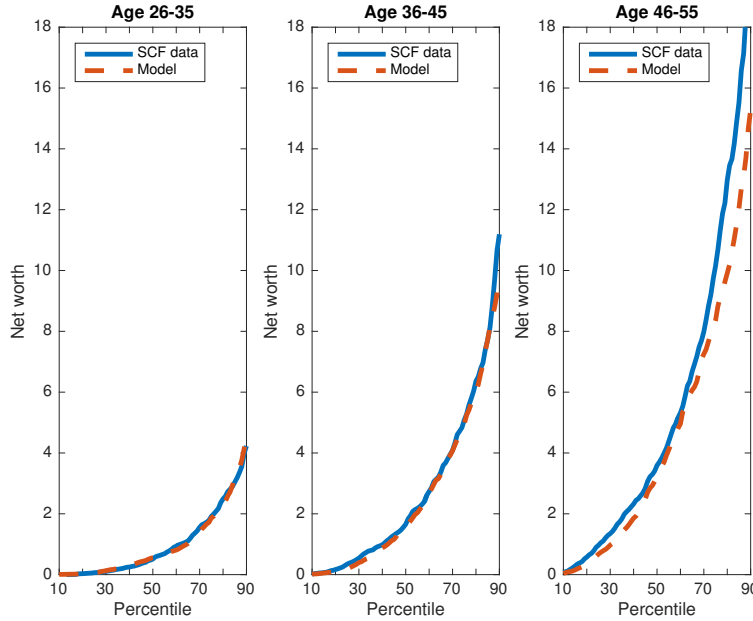
10.1 Model Predictions

10.1.1 Up to the 90th percentile

Figure 6 shows the net-wealth distribution for three different age groups from the 10th to the 90th percentile. The blue represents the SCF-Data from the year 2004 and the dotted orange line shows the distribution reproduced by the model. Table 2 shows the corresponding gini-indices. The ones for the SCF-Data are directly taken from Hintermaier and Koeniger (2011) whereas the model indices and averages are calculated from the net-wealth distribution resulting from the model simulation.²³ The evidence suggests that the model does manage to reproduce a decent representation of the wealth distribution. For the youngest age group it does underpredict inequality, while for the other two the model does quite accurately reproduce the ginis. While one may argue about the precision it is evident, that it reproduces a known feature (AS DISCUSSED IN THE FACTS PART) of the empirical distribution, namely that while average wealth holdings increase with age, the concentration of wealth holdings decreases. The means are such that the model slightly overpredicts average net-worth

²³As I allow for negative net-worth holdings in the model, the gini-indices have to be normalized, as otherwise indices of a magnitude larger than 1 were possible. I hereby follow Chen, Tsaur, and Rhai (1982). Note that this may slightly bias the gini-indices compared to the ones calculated without normalization. BE MORE PRECISE!!!

Figure 6: Average Durable Holdings over the Life-Cycle



CHANGE THE BLOODY COLOURS!!!! IT IS THE SAME AS IN HINTER-MAIERS! NEED TO INDICATE THE MEASURES. JUST VERY STANDARD! NEEDS TO BE UPDATED

holdings for the youngest group and slightly underpredicts net-worth for the other two age groups.

10.1.2 The full distribution and the issue with the tails of the distribution

Figure 7 shows the full distribution of the three age groups. Note that the scale of the y-axis varies between the age groups and compared to 6 in order to illustrate the whole outline of the empirical distribution. In comparison to the previous graph, two differences immediately meet the eye. For one, the model is not able to correctly predict the lowest part of the distribution. While in the model the poorest agents' net-worth holdings are around 0 for all ages, the SCF-Data displays negative values, which are more pronounced for the two younger generations. The second notable difference is the top of the distribution. Clearly, the model is unable to generate high enough savings for the richest 10%. This is a known problem in the literature.²⁴

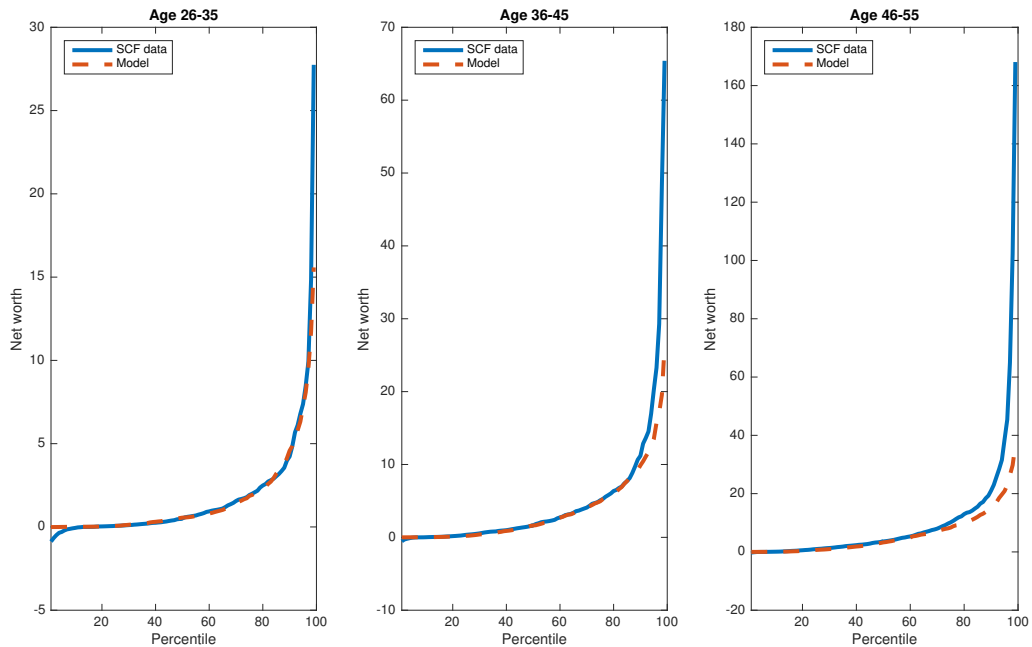
The richest One of the reasons is that people in the later stages of their lives do not have enough incentives to accumulate assets. The main driving forces during their

²⁴See Fella and De Nardi (2017) for a review and modeling choices that are able to deal with this issue.

Table 2: As Table 6 in Hintermaier and Koeniger (2011) this Table shows the Gini and Means for the distribution of different age groups up to and with the 90th percentile of the net-worth distribution.

	Data	Model
Age 26-35		
Mean	0.80	0.8350
Gini coefficient	0.713	0.6255
Age 36-45		
Mean	2.36	2.2657
Gini coefficient	0.596	0.5943
Age 46-55		
Mean	4.81	3.9695
Gini coefficient	0.564	0.5522

Figure 7: Average Durable Holdings over the Life-Cycle



CHANGE THE BLOODY COLOURS!!!! IT IS THE SAME AS IN HINTER-
MAIERS! NEED TO INDICATE THE MEASURES. JUST VERY STANDARD!
NEEDS TO BE UPDATED. NOTE THAT THE LOWEST PART OF THE DIS-
TRIBUTION IS NOT VISIBLE!

life-cycle is the accumulation of assets for retirement as well as precautionary savings, i.e. to be able to deal with wage shocks. However, as the agent approaches death, the incentive to substitute assets for consumption becomes stronger and stronger. As seen in the life-cycle profiles REFERENCE GRAPH, the point where agents start decumulating liquid assets and durables with 65, when entering the retirement period. There are different ways in dealing with this issue. One approach is to model a bequest motive. Agents will thus draw utility from the capital stock remaining at the time of death and therefore tend to accumulate more and longer over the life-cycle (CITE DE NARDI!). Another way is to model extreme income risk. (Castaneda et al., 2003) calibrates the income process to match the ginis of both the income as well as the net-worth distribution. The resulting income states contain an extreme income state of a magnitude about 100 times larger than the second state and 1000 times larger than the worst state. The issue with this approach is that the income process then is not founded on micro-data of the income, which may be counterproductive for policy recommendation.

MAYBE INCLUDE GRAPH WITH SAVING RATE FROM DE NARDI

The poorest The main reason for the poor reproduction of the lowest 10% is the calibration. When Hintermaier and Koeniger (2011) estimated their preference parameters they did not consider all observation with negative net-worth as their estimation approach did not permit for negative values.

10.1.3 Relative degrees of inequality

So far I have only discussed net-worth in the distribution section. However, the model does also reproduce a distribution of consumption as well as the two assets, which make up net-worth, independently. Moreover, there is the distribution of earnings, which is endogenously determined. It is well known that heterogeneous agent models of this type are able to reproduce the ordinal ranking of inequalities for consumption, income and net-worth in line with empirical evidence. Aiyagari (1994) shows that the model reproduces the (COPY PASTE: empirical plausible relative degrees of inequality), where consumption exhibits the least inequality, followed by income and capital is most unequal. (NOTE AIYAGARI IS A INFINITE HORIZON MODEL)

Table 3 displays the gini indices produced by the model and the one found in the data.²⁵ The model manages to match the ordering for the different inequalities only considering the types of the assets as well as net-worth. Moreover, it also shows that the consump-

²⁵The empirical indices for durables, liquid assets and net worth are taken from Hintermaier and Koeniger (2010) and the index for income from Hintermaier and Koeniger (2011)

Table 3: Gini indices for the different distributions					
	Consumption	Income	Durables	Liquid Assets	Net Worth
Model	0.3250	0.4062	0.3678	0.9523	0.6674
Data	????	0.427	0.67	0.97	0.81

tion inequality is lowest. However, it does not manage to show that durables are more concentrated than income. Díaz and Luengo-Prado (2010) show, in a model with housing, that this may be overcome by explicitly modeling a rental market. Housing makes up the biggest part of durables (CITE AND SHOW NUMBERS). As a consequence of rental markets, wealth poor households will decide to rent instead of owning, thus satisfying their durable consumption needs without being able to benefit from the collateral value of the durable object. As the rented object does not account for the housing part of the durable holdings, wealth poor will hold less durables and thus the gini index of durables increases, while, as Díaz and Luengo-Prado (2010) show, the other indices change only slightly and are only marginally affected. As I will show below. The concentration on durables largely depends on the persistence of the earning process. A change in the income process thus helps to improve on the prediction of the gini index of durables by the model.

10.2 Different Parameters

10.2.1 Adjustment Costs

Yang (2009) shows and explains the impact of the adjustment costs on the life-cycle profiles:

1. Transaction Costs and Borrowing constraints
 - (a) Helps to slow down decrease of non-housing consumption later in life
 - (b) Comparing ratio of housing to non-housing consumption
 - i. Without transaction costs, ratio becomes flatter over the life cycle
 - ii. ratio is increasing early in life since borrowing constraints bind more likely than later in life
 - iii. borrowing constraints are essential in explaining accumulation of housing assets early in life
 - (c) average life cycle profiles of financial assets and total net worth
 - i. the evolution of wealth portfolio over the life cycle is similar

- ii. shift from financial assets to housing assets when transaction costs are reduced

(d) small effect on net worth profile!!!

2. explains that it is not that important in explaining the net worth distribution!

Díaz and Luengo-Prado (2010) Interaction Between Adjustment Costs and the Collateral Constraint Effect of zero adjustment costs: Home ownership rate rises to 89%, the Gini indices of houses and financial assets increase significantly for the group of homeowners Gini index of houses for total pop falls from 0.58 to 0.52 in the benchmark economy Since houses are liquid, fraction of wealth held increases as houses increases for all wealth quintiles (although relatively more for the poor) thus effect on overall wealth distribution is minimal With lower adjustment costs, houses are liquid and there is less need to accumulate financial assets for precautionary reasons Zero down payment it follows that households accumulate less financial assets because they are not required to keep a down payment

10.2.2 Durables

10.2.3 Collateral Constraint

10.2.4 Income Process

In connection with the relative degrees of inequality:

Moreover, Hintermaier and Koeniger (2010) and Díaz and Luengo-Prado (2010) both show that a modeling of persistent earnings is necessary to reproduce higher inequality in the durables and thus to more closely match the data.

10.2.5 Determinants

What I can look at

1. Diaz and Luengo-Prado(2010)

- (a) the role of superstars and how it affects other results
- (b) interaction between adjustment costs and the collateral constraint
- (c) the role of persistent earnings

What are the savings motives? Hence why do households accumulate wealth?

1. Kaymak and Poschke (2015): the relative strength of each motive depends on a household's productivity

- (a) precautionary savings motive to insure against life-cycle income risk

- (b) consumption smoothing motive to save for retirement
- (c) bequest motive to endow estates for their offsprings

10.2.6 The literature

10.2.7 Implementing Castañeda

11 Conclusion

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A Experience Premium

Table 4: The annualized experience premium of labor income at ages 36, 46 and 56 relative to age 26.

Source: Corresponds to Table 4 in Hintermaier and Koeniger (2011) and displays the results of the authors' calculation based on SCF Data.

Annualized experience premium		1983	2004
Age -26:	10 years	1.81%	2.60%
	20 years	1.33%	2.18%
	30 years	0.99%	1.83%

B Estimation

Due to my estimation strategy, to estimate the model for the prime age sample and thus excluding consumers, which are situated in the top 10% of the wealth distribution, the means estimation does not suffer from the bias Cagetti (2003) puts forward.

ADDA and COOPER: Model is just identified. Choice of weighting matrix imp when model is overidentified.

The moment condition holds for both moments:

$$E(d_i - D(\beta_0, \theta_0)) = 0$$

$$E(d_i - X(\beta_0, \theta_0)) = 0$$

where D and X are the average of durable stock and net worth holdings of the prime age population respectively. As a consequence, the simulated method of moments can be applied (Duffie and Singleton, 1993).

Therefore I look for

$$\hat{\Theta} = \arg \min [(m(\Theta) - \nu)' I (m(\Theta) - \nu)]$$

where Θ is a vector containing β and θ , m contains the simulated moments for a specific Θ and $\nu = [2.95, 2.39]$ the empirical counterpart.

$\hat{\beta}$ and $\hat{\theta}$ that

Heathcote et al. (2010): (COPY PASTE: As Christiano and Eichenbaum argue, the exact identification strategy allows for a clear separation between what the model is

restricted to match and what it is designed to explain. The exactly identified strategy amounts to a weighting matrix that sets positive and equal weight only on certain moments, based on the investigator's prior about the (first-order) dimensions of the data that the model should fit.)