

Eric Larsen  
A02176917

aerofeels.usu.edu/mach up 6

$$R_h = \frac{b_w}{c_w} \quad c_w = \frac{s}{b} \quad \frac{b^2}{s} = -R_A$$

MAE 5510 : Exercise Set 2

Group	Eric L.				
Date					
Leader					
Member					
Member					
Member					

For the following problems, we will consider a version of the British Spitfire with the following geometric and aerodynamic characteristics:

$\bar{c}_w = 6.625$   
 $R_k = 5.569$   
 $R_{Ah} = 3.652$

$S_w = 244 \text{ ft}^2$	$b_w = 36.83 \text{ ft}$	$C_{L_w, \alpha} = 4.62$	$\alpha_{L0_w} = -2.2^\circ$	$C_{m_{h, \alpha}} = -0.053$
$S_h = 31 \text{ ft}^2$	$b_h = 10.64 \text{ ft}$	$C_{L_h, \alpha} = 4.06$	$\epsilon_e = 0.60$	$C_{m_{h, \delta_e}} = -0.55$
$W = 8,375 \text{ lbf}$		$l_h - l_w = 18.16 \text{ ft}$		

Assume that the center of gravity lies at the quarter-chord of the main wing, the horizontal stabilizer has a symmetric airfoil, and that the main wing and horizontal stabilizer have zero twist.

2.1 The main wing of the British Spitfire has an elliptic planform. From lifting-line theory, the lift coefficient produced on an elliptic wing with zero twist can be computed from

$$C_L = C_{L, \alpha} (\alpha - \alpha_{L0})_{\text{root}} \quad (1)$$

where

$$C_{L, \alpha} = \frac{\tilde{C}_{L, \alpha}}{[1 + \tilde{C}_{L, \alpha} / (\pi R_A)]} \quad \left[ 1 + \frac{2\pi}{\pi(5.569)} \right] \quad (2)$$

Assuming the main wing has a thin airfoil, compute the lift on the main wing at 5 deg angle of attack and a velocity of 200 mph at sea level.

$\rho_{SL} = 0.0023769$   
 $\tilde{C}_{L, \alpha} = 2\pi$   
 $C_{L, \alpha} = 4.62$   
 $V_{\infty} = 293.33 \text{ ft/s}$

$$C_L = 4.62 (5^\circ + 2.2^\circ)$$

$$C_L = 4.62 \left( 7.2 \cdot \frac{\pi}{180} \right) = 0.5805$$

$$L = 0.5805 \cdot \left( \frac{1}{2} \rho V_{\infty}^2 S_w \right) = 0.5805 (0.5 \cdot 0.0023769 \cdot 293.33^2 \cdot 244)$$

$$L_w = 14,483.913 \text{ lbf}$$

2.2 The horizontal stabilizer on the British Spitfire has an elliptic planform. Assuming it uses a thin airfoil, compute the lift on the horizontal stabilizer at 5 deg angle of attack and a velocity of 200 mph at sea level without any influence from the main wing.

$\alpha = 5^\circ$   
 $\epsilon_d = 0$   
 $\alpha_{L0_h} = 0^\circ$

$$C_{L_h} = C_{L_h, \alpha} (\alpha - \alpha_{L0_h} - \epsilon_d) = C_{L_h} = 4.06 \left( 5 \cdot \frac{\pi}{180} \right) = 0.3543$$

$$L_h = 0.354302 \cdot \left( \frac{1}{2} \cdot 0.0023769 \cdot 293.33^2 \cdot 31 \right) = 1123.1214 \text{ lbf}$$

Acru

2.3 Using MachUp 4, compute the lift produced on the main wing at 5 deg angle of attack and a velocity of 200 mph at sea level. Assume that the airfoil used on the main wing is thin and has a zero-lift angle of attack of  $-2.2^\circ$ . The root chord of an elliptic wing can be computed from

$$c_{root} = \frac{4b}{\pi R_A} \quad \frac{4 \cdot 36.83}{\pi 5.559} = 8.43558$$

Compare this result to that in problem 2.1.

$$C_{L_{root}} = 0.8809$$

2.1  
 $L = 14,483$

$C_{L_A} \quad L = 14,483 //$

same result.

2.4 Using MachUp 4, compute the lift produced on the horizontal stabilizer at 5 deg angle of attack and a velocity of 200 mph at sea level. Compare this result to that in problem 2.3.

$$C_{root} = \frac{4 \cdot 10.64}{\pi (3.652)} = 3.7096$$

$$C_{L_h} = 0.3545$$

2.3  $L_h = 1123.12 \text{ lbf}$

$$L_h = 1123.755 \text{ lbf}$$

this result is slightly higher

2.5 Using MachUp 4, compute the lift produced on the main wing and horizontal stabilizer at 5 deg angle of attack and a velocity of 200 mph at sea level when the horizontal stabilizer is placed a distance of  $l_h - l_w = 18.16 \text{ ft}$  aft of the main wing. Compare this result to that in problems 2.1 - 2.4. Discuss your results.

$$C_{L_h} = \frac{0.01054}{0.01054} \cdot \frac{S_w}{S_h} = 0.08296$$

$$C_{L_w} \rightarrow 0.19878$$

$$L_w = 4958.696$$

$$L_h = 33.4046$$

Lift is drastically wrong from previous results, much lower.

Be sure it is an issue w/ the code. Should be more than main wing but less than combination due to downwash effects on H.S.

2.6 Using the simplified analysis for estimating the downwash, estimate the downwash on the horizontal as a function of the lift coefficient on the main wing.

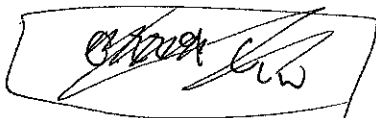
$$\epsilon_D(\bar{x}, \bar{y}, 0) = \frac{k_v k_p k_s}{k_b} \frac{C_{LW}}{R_{AW}} = \frac{k_v}{k_b} \frac{C_{LW}}{R_{AW}}$$

$$k_v = 1.0$$

$$k_b = \frac{\pi}{4}$$

$$k_p = 0.46$$

$$\frac{1.0}{\frac{\pi}{4}} = \frac{4}{\pi} \cdot \frac{C_{LW}}{R_{AW}} = \frac{4}{3.1415} \cdot 5.559 =$$



$$\frac{1.0}{\frac{\pi}{4}} = \frac{4}{\pi} \cdot \frac{C_{LW}}{R_{AW}} = \frac{4}{3.1415} \cdot 5.559 =$$

$$1.2556 \approx$$

$$\frac{1.0}{\frac{\pi}{4}} = \frac{4}{\pi} \cdot \frac{C_{LW}}{R_{AW}} = \frac{4}{3.1415} \cdot 5.559 =$$

$$\epsilon_D = 0.229 C_{LW}$$

$$\epsilon_D = 0.10534 C_{LW}$$

$$\frac{k_v k_p k_s}{k_b R_{AW}} C_{LW, \alpha}$$

$$\epsilon_D = \left[ \epsilon_D + \epsilon_{D, \alpha} \alpha \right]$$

$$\epsilon_{D, \alpha} = 0.10534 C_{LW, \alpha}$$

$$\alpha_{ow} \quad \alpha_{ol}$$

2.7 Using the results of 2.6, find the mounting angle of the main wing and horizontal stabilizer required for the aircraft to be trim in steady-level flight at sea level at a velocity of 200 mph with zero elevator deflection and zero angle of attack. Compare your results to those from problem 1.13. Discuss your results.

$$\alpha = 0 \quad \alpha = 0 \quad \gamma = 0 \quad 200 \text{ mph} = 293.33 \text{ ft/s}$$

$$C_{LW} = 1.16$$

$$C_{LW} = - \left[ C_{LW} - \frac{C_{LW}}{C_{LW}} C_{LW} (\alpha_{ow} - \alpha_{ol}) \right] - \frac{S_h}{S_w} \frac{C_{LW}}{C_{LW}} C_{LW} (\alpha_{oh} - 0.229 C_{LW})$$

$$C_{LW}$$

$$C_{LW}$$

$$\epsilon_D$$

$$\epsilon_D = 4.62 (\alpha_{ow} - 0.053)$$

$$C_{LW} = 0.1774$$

$$\alpha_{oh} = -0.00875 \text{ rad}$$

$$\alpha_{oh} = -0.502 \text{ degrees}$$

$$C_{LW}$$

lowers the required angle of mounting of aircraft.

$$0.158259 = 4.62 \alpha_{ow} + 0.51582 (\alpha_{oh} - \epsilon_D)$$

$$\frac{-0.053 + \epsilon_D}{1.4139} = \alpha_{oh}$$

$$C_{LW}$$

$$0.067819 = 2.24 \alpha_{ow} + 0.51582 \alpha_{oh}$$

$$-0.22856 = 4.62 \alpha_{ow} + 1.4139 \alpha_{oh}$$

$$\alpha_{ow} = 0.277 \quad \alpha_{oh} = -1.067$$

$$C_{Lw,\alpha} = 4.62$$

2.8 Compute the aircraft static margin. Compare your results to those from problem 1.14. Discuss your results.

$$C_{m,\alpha} = \frac{-L_w}{C_w} C_{Lw,\alpha} - \frac{S_{h,h}}{S_{w,cw}} \eta_h C_{Lh,\alpha} (1 - \epsilon_{d,\alpha})$$

$$C_{L,\alpha} = C_{Lw,\alpha} + \frac{S_h}{S_w} \eta_h C_{Lh,\alpha} (1 - \epsilon_{d,\alpha})$$

$$\epsilon_{d,\alpha} = 0.10534 C_{Lw,\alpha}$$

$$\epsilon_{d,\alpha} = 0.10534 (4.62) = \underline{0.48667}$$

need to solve.

$$C_{L,\alpha} = 4.62 + \frac{31}{244} 4.06 (1 - 0.48667) = 4.8847$$

$$C_{m,\alpha} = \frac{-L_w}{C_w} C_{Lw,\alpha} - \frac{31 \cdot 18.16}{244 \cdot 36.83} 4.06 (1 - 0.48667) = -0.72580$$

$$-\frac{C_{m,\alpha}}{C_{L,\alpha}} = \frac{-0.7258}{4.8847} = 0.1485 = \underline{14.86\%}$$

Reduced the static margin greatly.

2.9 If the main wing and horizontal stabilizer both have zero mounting angles, compute the angle of attack and elevator deflection required to trim the aircraft in a steady climb at an altitude of 5,000 ft and a climb angle of 20 deg at a speed of 200 mph. Include the effects of downwash and compare your results to those from problem 1.15. Discuss your results.

$$\alpha_{cw} = \alpha_{ch} = 0$$

$$\varphi = 0.002048$$

$$\begin{bmatrix} C_{L,\alpha} & C_{L,\delta_e} \\ C_{m,\alpha} & C_{m,\delta_e} \end{bmatrix} \begin{bmatrix} \alpha \\ \delta_e \end{bmatrix} = \begin{bmatrix} C_L - C_{L0} \\ -C_{m0} \end{bmatrix}$$

has effects of  $\epsilon_d$

Need  $\epsilon_{d0}$ ??

$$C_{L,\alpha} = 4.8847$$

$$C_{m,\alpha} = -0.72580$$

$$C_{L,\delta_e} = 0.309492$$

$$C_{m,\delta_e} = -0.879084$$

$$\begin{bmatrix} 4.8847 & 0.309492 \\ -0.72580 & -0.879084 \end{bmatrix}$$

$$= \begin{bmatrix} -0.98 \\ 0.198 \end{bmatrix}$$

$$\begin{bmatrix} 0.366066 - 0.177395 \\ 0.09053 \end{bmatrix}$$

Wing

$$\epsilon_{d0} = 4.62 (\alpha_{cw} - 0.030)$$

$$\epsilon_{d0} = -0.17556$$

$$-C_{m0} = \frac{L_w}{C_w} C_{Lw,\alpha} (\alpha_{cw} - \alpha_{row}) - \left[ C_{mw} + \frac{S_{h,h}}{S_{w,cw}} \eta_h C_{Lh,\alpha} (\alpha_{ch} - \alpha_{row} - \epsilon_{d0}) \right]$$

$$\frac{S_{h,h}}{S_{w,cw}} \eta_h C_{Lh,\alpha} (\alpha_{ch} - \alpha_{row} - \epsilon_{d0})$$

$$-C_{m0} = - \left[ -0.053 - \frac{31 \cdot 18.16}{244 \cdot 36.83} 4.06 (-0.177556) \right]$$

$$-4 [-0.053 + 0.2510] = 0.198$$

$$\alpha = -0.1966 \quad \delta_e = -0.0678$$

2.10 Using MachUp 4, compute the global inviscid lift, drag, and pitching-moment coefficients about the origin for the aircraft at angles of attack of 4, 5, and 6 deg.

Angle of Attack [deg]	$C_L$	$C_{Di}$	$C_m$
4.0	0.3596	0.0138	-0.0574
5.0	0.4450	0.0181	-0.0464
6.0	0.5308	0.0234	-0.0358

$$C_{L,\alpha} \approx 0.0856$$

$$C_{m,\alpha} = 0.011$$

$$C_{Di,\alpha} \approx 0.0048$$

2.11 Using the results of problem 2.10, find the location of the aerodynamic center ( $x_{ac}, y_{ac}$ ) using the general relations for the aerodynamic center. Compare your results to that which would be obtained from the simplified analysis in problem 2.8. Discuss your findings.

find  $x_{ac}, y_{ac}$

$$C_A = C_D$$

$$C_L = C_N$$

$$C_m = C_{m0}$$

$$C_{L,\alpha} = C_{D,\alpha} = \frac{0.0234 - 0.0138}{2 \left( \frac{\pi}{180} \cdot 1 \right)} = 0.275 \text{ (rad)}$$

$$C_{D,\alpha} = \frac{C_D(\alpha + \Delta\alpha) - C_D(\alpha) + C_D(\alpha - \Delta\alpha)}{\Delta\alpha^2} = 3.282$$

$$C_{L,\alpha} = 0.27502$$

$$C_{m,\alpha} = 0.61879$$

$$C_{L,\alpha} = 4.9045$$

$$C_{m,\alpha} = -1.3131$$

$$C_{L,\alpha\alpha} = 1.3131$$

$$\frac{x_{ac}}{c_{ref}} = \frac{C_{D,\alpha} C_{m,\alpha\alpha} - C_{m,\alpha} C_{D,\alpha\alpha}}{C_{L,\alpha} C_{D,\alpha\alpha} - C_{D,\alpha} C_{L,\alpha\alpha}} = \frac{-2.392}{15.735} = \boxed{-0.15202}$$

$$\frac{y_{ac}}{c_{ref}} = \frac{C_{L,\alpha} C_{m,\alpha\alpha} - C_{m,\alpha} C_{L,\alpha\alpha}}{C_{L,\alpha} C_{D,\alpha\alpha} - C_{D,\alpha} C_{L,\alpha\alpha}} = \frac{-7.2526}{15.735} = \boxed{-0.4609}$$

not the same as before

Because I got a +  $C_{m,\alpha}$  so it would be not stable at all.