

# Sunspots Time Series

A Long Term Time Series Analysis



# What are Sunspots?

- Earth sized magnetic storms
- Correlated with the solar magnetic cycle
- Every time the Sun finishes an ~11 year cycle the magnetic poles swap places



## How does it affect Earth?

- Sunspots are correlated with Magnetic/Electrical disturbances.
- High sunspot activity is also correlated with high solar output.

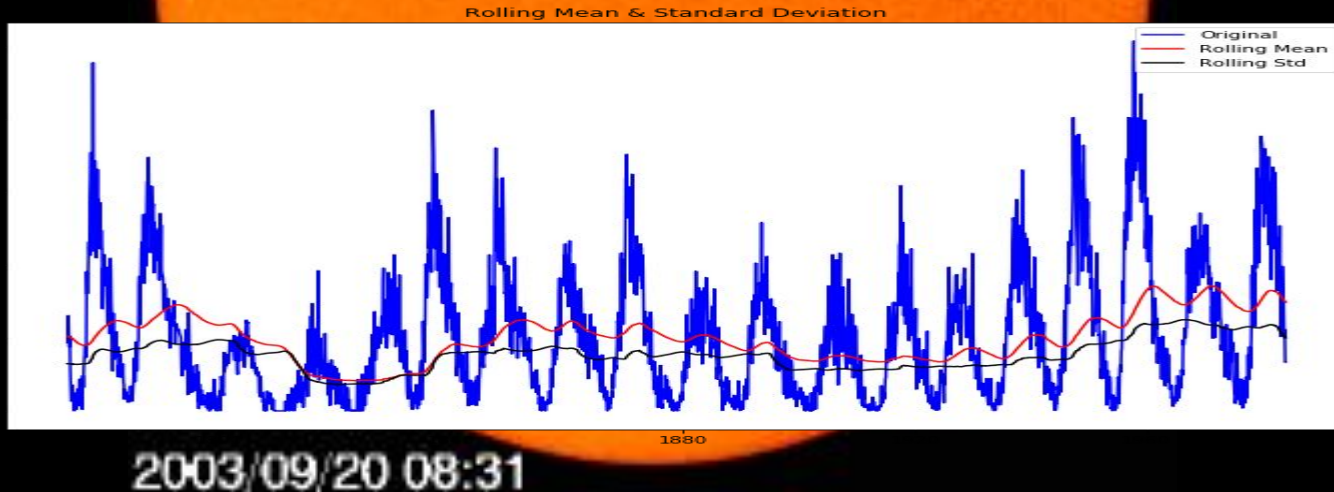


# The Data

2003/09/20 08:31

# The Data

- Number of sunspots per month since 1749

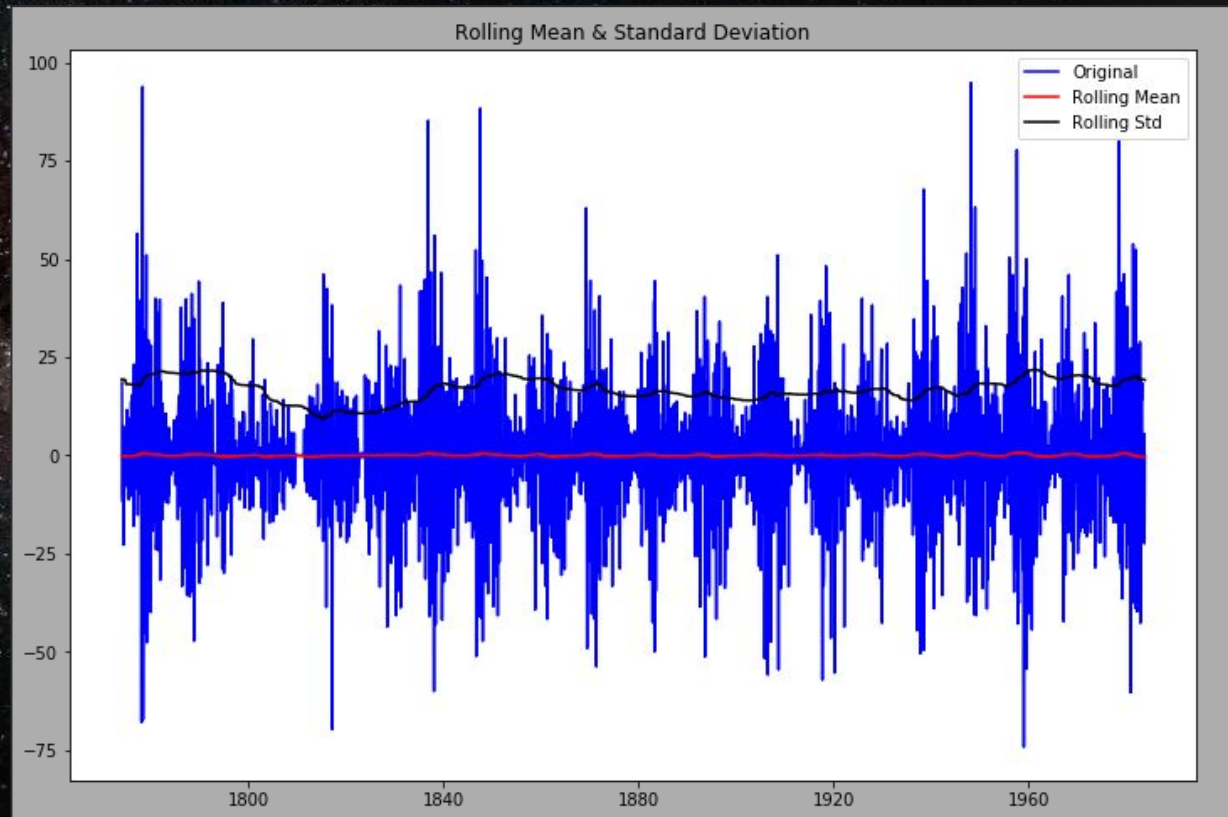


First Difference

Dickey-Fuller

p-value =

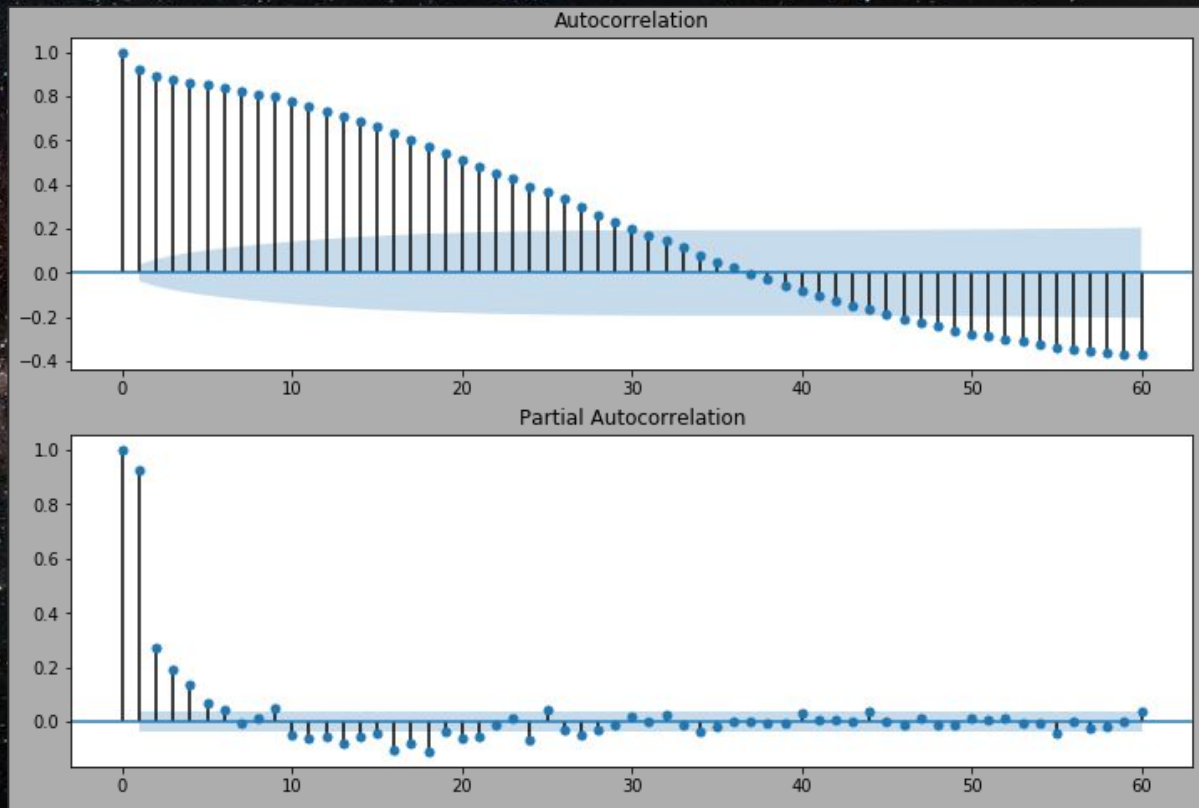
$5.2 \times 10^{-14}$



## ACF & PACF

Autocorrelation  
with original  
data

Partial  
autocorrelation  
with original  
data





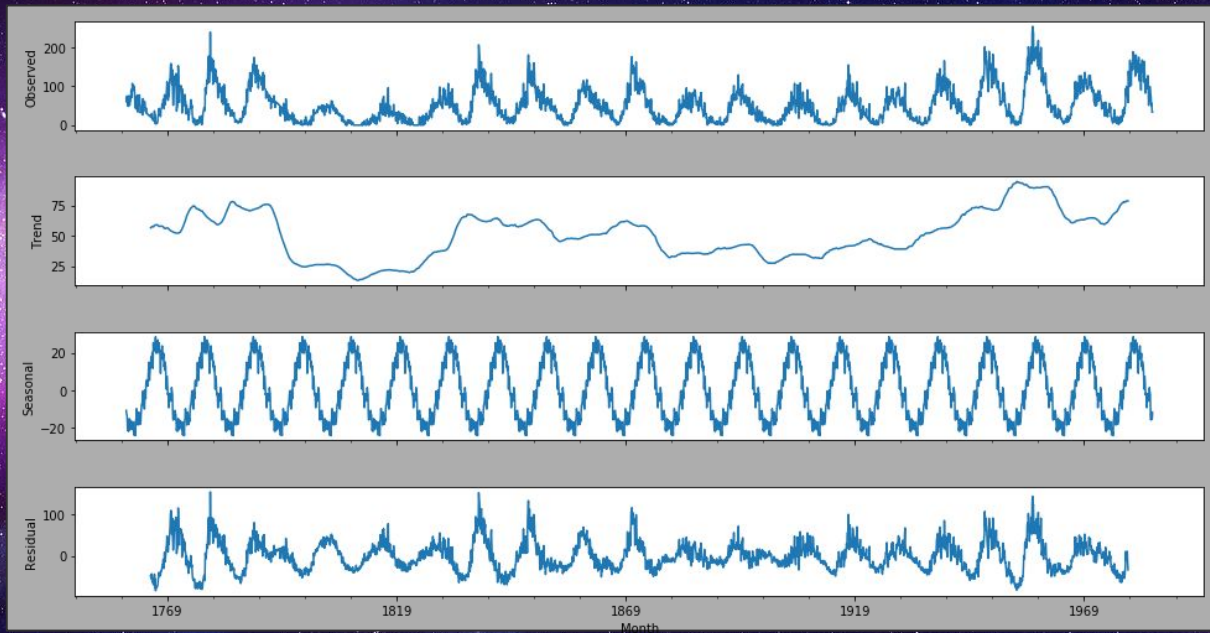
# Decompose

Original Data

Trend

Seasonal

Residual





# ARMA

Best parameters

$p = 1$

$d = 0$

$q = 2$

| ARMA Model Results |                  |                     |           |           |        |        |
|--------------------|------------------|---------------------|-----------|-----------|--------|--------|
| Dep. Variable:     | Sunspots         | No. Observations:   | 2256      |           |        |        |
| Model:             | ARMA(1, 0)       | Log Likelihood      | -9455.359 |           |        |        |
| Method:            | css-mle          | S.D. of innovations | 15.989    |           |        |        |
| Date:              | Mon, 15 Jul 2019 | AIC                 | 18916.718 |           |        |        |
| Time:              | 14:16:21         | BIC                 | 18933.882 |           |        |        |
| Sample:            | 01-01-1749       | HQIC                | 18922.982 |           |        |        |
|                    | - 12-01-1936     |                     |           |           |        |        |
|                    | coef             | std err             | z         | P> z      | [0.025 | 0.975] |
| const              | 45.0436          | 3.475               | 12.964    | 0.000     | 38.234 | 51.854 |
| ar.L1.Sunspots     | 0.9035           | 0.009               | 99.998    | 0.000     | 0.886  | 0.921  |
| Roots              |                  |                     |           |           |        |        |
|                    | Real             | Imaginary           | Modulus   | Frequency |        |        |
| AR.1               | 1.1068           | +0.0000j            | 1.1068    | 0.0000    |        |        |
| const              | 45.043609        |                     |           |           |        |        |
| ar.L1.Sunspots     | 0.903512         |                     |           |           |        |        |

# SARIMA

## Statespace Model Results

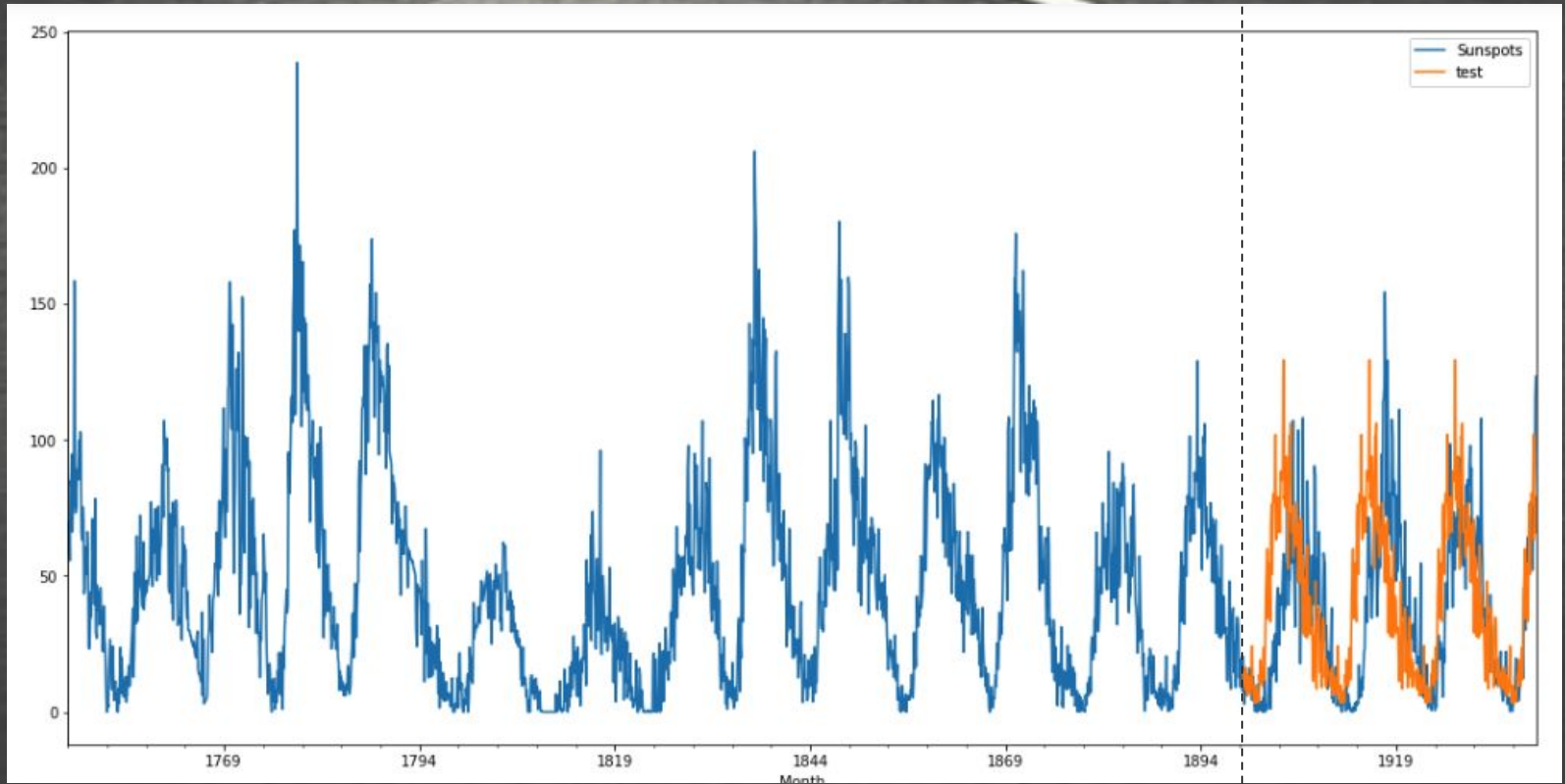
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=====
Dep. Variable:                Sunspots    No. Observations:           2256
Model:                SARIMAX(1, 0, 1)x(0, 1, 0, 132)    Log Likelihood            -9452.861
Date:                Mon, 15 Jul 2019    AIC                      18911.723
Time:                14:07:07    BIC                      18928.706
Sample:                01-01-1749    HQIC                     18917.940
                  - 12-01-1936
```

Covariance Type: opg

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=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
ar.L1          0.9520        0.006    158.981      0.000        0.940        0.964
ma.L1         -0.4635        0.018   -25.419      0.000       -0.499       -0.428
sigma2        429.4240        8.731    49.186      0.000       412.312       446.536
=====
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=====
Ljung-Box (Q):                132.73    Jarque-Bera (JB):                582.89
Prob(Q):                      0.00    Prob(JB):                      0.00
Heteroskedasticity (H):        0.66    Skew:                          -0.07
Prob(H) (two-sided):           0.00    Kurtosis:                      5.56
=====
```

# SARIMA Model Prediction





# Sunspots Forecast until Jan 2010

