

entropart: An R Package to Measure and Partition Diversity

Eric Marcon
AgroParisTech
UMR EcoFoG

Bruno Hérault
Cirad
UMR EcoFoG

Abstract

entropart is a package for R designed to estimate diversity based on HCDT entropy or similarity-based entropy.

It allows calculating species-neutral, phylogenetic and functional entropy and diversity, partitioning them and correcting them for estimation bias.

Keywords: biodiversity, entropy, partitioning.

1. Introduction

Diversity measurement can be done through a quite rigorous framework based on entropy, *i.e.* the amount of uncertainty calculated from the frequency distribution of a community (Patil and Taillie 1982; Jost 2006; Marcon, Scotti, Hérault, Rossi, and Lang 2014a). Tsallis entropy, also known as HCDT entropy (Havrdá and Charvát 1967; Daróczy 1970; Tsallis 1988), is of particular interest (Jost 2006; Marcon *et al.* 2014a) namely because it gathers the number of species, Shannon (1948) and Simpson (1949) indices of diversity into a single framework. Interpretation of entropy is not straightforward but one can easily transform it into Hill numbers (Hill 1973) which have many desirable properties (Jost 2007): mainly, they are the number of equally-frequent species that would give the same level of diversity as the data.

Marcon and Hérault (2015) generalized the duality of entropy and diversity, deriving the relation between phylogenetic or functional diversity (Chao, Chiu, and Jost 2010) and phylogenetic or functional entropy (we will write *phylodiversity* and *phyloentropy* for short), as introduced by Pavoine, Love, and Bonsall (2009). Special cases are the well-known PD (Faith 1992) and FD (Petchey and Gaston 2002) indices and Rao's (1982) quadratic entropy. The same relation holds between Ricotta and Szeidl's entropy of a community (Ricotta and Szeidl 2006) and similarity-based diversity (Leinster and Cobbold 2012).

The **entropart** package for R (R Core Team 2015) enables calculation of all these measures of diversity and entropy and their partitioning.

Diversity partitioning means that, in a given area, the γ diversity D_γ of all individuals found may be split into within (α diversity, D_α) and between (β diversity, D_β) local assemblages. α diversity reflects the diversity of individuals *in* local assemblages whereas β diversity reflects the diversity *of* the local assemblages. Marcon *et al.* (2014a) derived the decomposition of

Tsallis γ entropy into its α and β components, generalized to phylodiversity (Marcon and Hérault 2015) and similarity-based diversity (Marcon, Zhang, and Hérault 2014b).

Estimators of diversity are biased because of unseen species and also because they are not linear functions of probabilities (Marcon *et al.* 2014a). α and γ diversities are underestimated by naive estimators (Chao and Shen 2003; Dauby and Hardy 2012). β diversity is severely biased too when sampling is not sufficient (Beck, Holloway, and Schwanghart 2013). Bias-corrected estimators of phylodiversity have been developed by Marcon and Hérault (2015). Estimators of similarity-based diversity were derived by Marcon *et al.* (2014b). The package includes them all (Marcon and Hérault 2015).

In summary, the framework supported by the package is as follows. First, an information function is chosen to describe the amount of surprise brought by the observation of each individual. In the simplest case of species-neutral diversity, it is just a decreasing function of probability: observing an individual of a rarer species brings more surprise. Various information functions allow evaluating species-neutral, phylogenetic or functional entropy. Surprise is averaged among all individuals of a community to obtain its entropy. Entropy is systematically transformed into diversity for interpretation. Diversity is an effective number of species, *i.e.* the number of equally-different and equally-frequent species that would give the same entropy as the data. The average entropy of communities of an assemblage is α entropy, while the entropy of the assemblage is γ entropy. Their difference is β entropy. After transformation, β diversity is the ratio of γ to α diversity. It is an effective number of communities, *i.e.* the number of equally-weighted communities with no species in common (and where species are maximally distinct between communities) necessary to obtain the same diversity as the data. Estimation-bias correction is more easily applied to entropy before transforming it into diversity.

This framework is somehow different from that of Chao, Chiu, and Jost (2014) who define α diversity in another way (see Marcon and Hérault 2015, for a detailed comparison), such that α entropy is not the average surprise of an assemblage. They also propose a definition of functional diversity (Chiu and Chao 2014) based in the information brought by pairs of individuals that is not supported in the package.

The successive sections of this paper presents the package features, illustrated by worked examples based on the data included in the package.

2. Package organization

2.1. Data

Most functions of the package calculate entropy or diversity of a community or of an assemblage of communities called a “meta-community”. Community functions accept a vector of probabilities or of abundances for species data. Each element of the vector contains the probability or the number of occurrences of a species in a given community. Meta-community functions require a particular data organization in a `MetaCommunity` object described here.

A `MetaCommunity` is basically a list. Its main components are `$Nsi`, a matrix containing the species abundances whose lines are species, columns are communities and `$Wi`, a vector containing community weights. Creating a `MetaCommunity` object is the purpose of the `MetaCommunity` function. Arguments are a dataframe containing the number of individuals

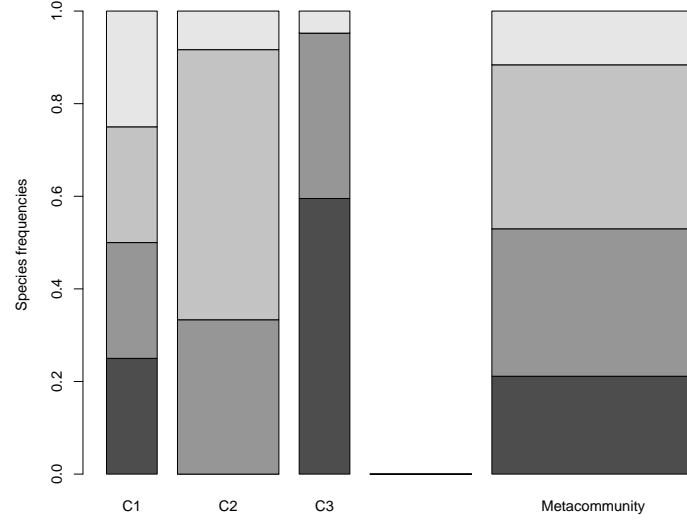


Figure 1. Plot of a **MetaCommunity**. Communities (named C1, C2 ad C3) are represented in the left part of the figure, the metacommunity to the right. Bar widths are proportional to community weights. Species abundances are represented vertically (4 species are present in the meta-community, only 3 of them in communities C2 and C3).

per species (lines) in each community (columns), and a vector containing the community weights. The following example creates a **MetaCommunity** made of three communities of unequal weights with 4 species. The weighted average probabilities of occurrence of species and the total number of individuals define the meta-community as the assemblage of communities.

```
library("entropart")
df <- data.frame(C1 = c(10, 10, 10, 10), C2 = c(0, 20, 35, 5),
                 C3 = c(25, 15, 0, 2))
row.names(df) <- c("sp1", "sp2", "sp3", "sp4")
df

##      C1 C2 C3
## sp1 10  0 25
## sp2 10 20 15
## sp3 10 35  0
## sp4 10  5  2

w <- c(1, 2, 1)
MC <- MetaCommunity(Abundances = df, Weights = w)
```

A meta-community is partitioned into several local communities (indexed by $i = 1, 2, \dots, I$). n_i individuals are sampled in community i . Let $s = 1, 2, \dots, S$ denote the species that compose the meta-community, $n_{s,i}$ the number of individuals of species s sampled in the local community i , $n_s = \sum_i n_{s,i}$ the total number of individuals of species s , $n = \sum_s \sum_i n_{s,i}$ the total number of sampled individuals. Within each community i , the probability $p_{s,i}$ for an individual to belong to species s is estimated by $\hat{p}_{s,i} = n_{s,i}/n_i$. The same probability for the meta-community is p_s . Communities have a weight w_i , satisfying $p_s = \sum_i w_i p_{s,i}$. The commonly-used $w_i = n_i/n$ is a possible weight, but the weighting may be arbitrary (e.g. the sampled areas). The component **\$Ps** of a **MetaCommunity** object contains the probability of occurrence of each species in the meta-community, calculated this way:

```
MC$Ps

##      sp1      sp2      sp3      sp4
## 0.2113095 0.3184524 0.3541667 0.1160714
```

The number of individuals $\$Ns$ of a `MetaCommunity` is theoretically unknown, since communities are just samples of it. The total number of individuals is $\$N$. For simplicity, it is set to the total number of individuals of all communities. If community weights are their number of individuals, $\$Ns$ is just the sum of the numbers of individuals per species of communities. Else, $\$Ns$ may contain non-integer values, respecting the probabilities $\$Ps$ and summing to $\$N$.

A `MetaCommunity` can be summarized and plotted (Figure 1).

The package contains an example dataset containing the inventory of two 1-ha tropical forest plots in Paracou, French Guiana ([Marcon, Hérault, Baraloto, and Lang 2012](#)):

```
data("Paracou618")
summary(Paracou618.MC)

## Meta-community (class 'MetaCommunity') made of 1124
## individuals in 2 communities and 425 species.
##
## Its sample coverage is 0.92266748426447
##
## Community weights are:
## [1] 0.5720641 0.4279359
## Community sample numbers of individuals are:
## P006 P018
## 643 481
## Community sample coverages are:
##      P006      P018
## 0.8943859 0.8463782
```

`Paracou618.MC` is a meta-community made of two communities named “P006” and “P018”, containing 425 species (their name is *Family_Genus_Species*, abbreviated to 4 characters). The values of the abundance matrix are the number of individuals of each species in each community. Sample coverage will be explained later.

The dataset also contains a taxonomy and a functional tree. `Paracou618.Taxonomy` is an object of class `phylog`, defined in `ade4` ([Dray and Dufour 2007](#)), namely a phylogenetic tree. This example data is only a taxonomy, containing family, genus and species levels for the sake of simplicity. `Paracou618.Functional` is an object of class `hclust` containing a functional tree based on leaf, height, stem and seed functional traits ([Hérault and Honnay 2007](#); [Marcon and Hérault 2015](#)). The package accepts any ultrametric tree of class `phylog` or `hclust`. `Paracou618.dist` is the distance matrix (actually a `dist` object) used to build the functional tree.

Numeric vectors containing species abundances (such as the $\$Ns$ component of `MetaCommunity`) or probabilities (such as $\$Ps$) may be converted to abundance vectors (`AbdVector`) or probability vectors (`ProbaVector`) to clarify their content. By default, the `as.AbdVector` function transforms abundance values into integer if they are not (the $\$Ns$ components of a `MetaCommunity` is typically not an integer vector if community weights are not proportional to their numbers of individuals):

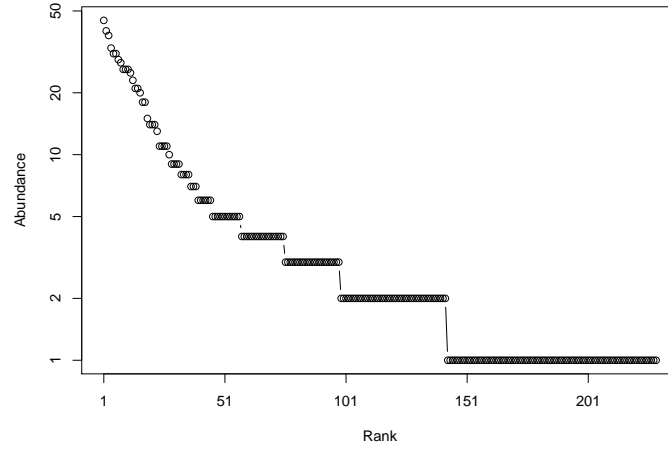


Figure 2. Plot of a `ProbaVector`. Rank-Abundance curve (Whittaker plot) of the Paracou species distribution.

```
data("Paracou618")
PAbd <- as.AbdVector(Paracou618.MC$Ns)
```

The `as.ProbaVector` function transforms abundances to probabilities if necessary:

```
PProba <- as.ProbaVector(Paracou618.MC$Ps)
```

`AbdVector` and `ProbaVector` objects both are `SpeciesDistribution` objects which can be plotted (Figure 2).

2.2. Utilities

The deformed logarithm formalism (Tsallis 1994) is very convenient to manipulate entropies. The deformed logarithm of order q is defined as:

$$\ln_q x = \frac{x^{1-q} - 1}{1 - q} \quad (1)$$

It converges to \ln when $q \rightarrow 1$, see figure 3.

The inverse function of $\ln_q x$ is the deformed exponential:

$$e_q^x = [1 + (1 - q)x]^{\frac{1}{1-q}} \quad (2)$$

Functions of the packages are `lnq(x, q)` and `expq(x, q)`.

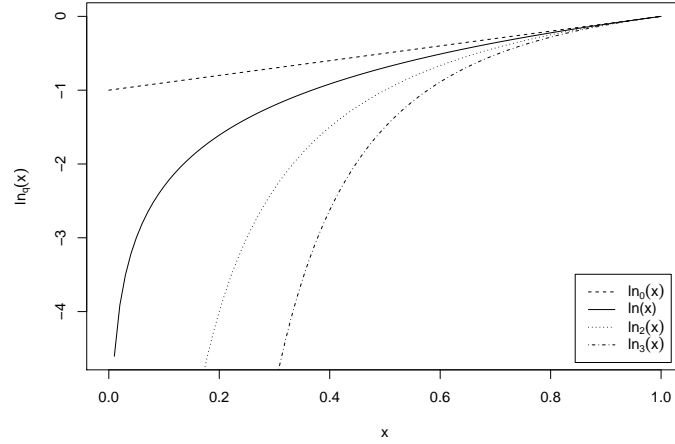


Figure 3. Curves of $\ln_q x$ for different values of q between 0 and 4 ($\ln_1 x = \ln x$).

3. Species-neutral diversity

3.1. Community functions

HCDT entropy

Species-neutral HCDT entropy of order q of a community is defined as:

$${}^qH = \frac{1 - \sum_s p_s^q}{q - 1} = - \sum_s p_s^q \ln_q p_s = \sum_s p_s \ln_q \frac{1}{p_s} \quad (3)$$

q is the order of diversity (*e.g.*: 1 for Shannon). Entropy can be calculated by the **Tsallis** function. Paracou meta-community entropy of order 1 is:

```
Tsallis(PProba, q = 1)
```

```
##      None
## 4.736023
```

For convenience, special cases of entropy of order q have a clear-name function: **Richness** for $q = 0$, **Shannon** for $q = 1$, **Simpson** for $q = 2$.

```
Shannon(PProba)
```

```
##      None
## 4.736023
```

Entropy values have no intuitive interpretation in general, except for the number of species 0H and Simpson entropy 2H which is the probability for two randomly chosen individuals to belong to different species.

Sample coverage

A useful indicator of sampling quality is the sample coverage (Good 1953; Chao, Lee, and Chen 1988; Zhang and Huang 2007), that is to say the probability for a species of the community to be observed in the actual sample. It equals the sum of the probability of occurrences of all observed species. Its historical estimator is (Good 1953):

$$\hat{C} = 1 - \frac{S^1}{n} \quad (4)$$

S^1 is the number of singletons (species observed once) of the sample, and n is its size. The estimator has been improved by taking into account the whole distribution of species (Zhang and Huang 2007). The `Coverage` function calculates it, allowing to choose the estimator (Zhang and Huang's by default):

```
Coverage(PAbd)
```

```
## ZhangHuang
## 0.9226675
```

The sample coverage cannot be estimated from probability data: abundances are required.

Its interpretation is straightforward: some species have not been sampled. Their number is unknown but their total probability of occurrence can be estimated accurately. Here, it is a bit less than 8%. From another point of view, the probability for an individual of the community to belong to a sampled species is C : 8% of them belong to missed species. The number of missed species may be estimated by `Richness` but this is not the point here. The sample coverage is the foundation of many estimators of entropy.

Bias corrected estimators

Correction of estimation bias is used to improve the estimation of entropy despite unobserved species and also mathematical issues (Bonachela, Hinrichsen, and Muñoz 2008). Bias-corrected estimators (often relying on sample coverage) are returned by functions whose names are prefixed by `bc`, such as `bcTsallis`. They are similar to the non-corrected ones but they use abundance data and propose several bias-correction techniques to select in the `Correction` argument. A “Best” correction is calculated by default, detailed in the help file of each function.

```
bcTsallis(PAbd, q = 1)
```

```
## ChaoWangJost
## 4.892159
```

The best correction for Tsallis entropy follows Chao and Jost (2015). It combines an unbiased estimator previously derived by Zhang and Grabchak (2016) and an estimate of the remaining bias.

All community functions such as `Tsallis` are actually generic methods that can handle several types of data the appropriate way: if the first argument of the function is a `ProbaVector` (or a numeric vector summing to 1), no bias correction is applied. If it is an `AbdVector` (or an integer vector), the bias-corrected estimator is used (*e.g.* `bcTsallis`). Numeric vectors

summing to more than 2 are considered as abundances but some bias corrections do not allow non-integer values, so they will round them with a warning.

The different ways to use the functions are a matter of personal preference. `bcTsallis` is equivalent to `Tsallis` with an abundance vector:

```
Tsallis(PAbd, q = 1)

## ChaoWangJost
## 4.892159
```

whilst `Tsallis` with a probability vector does not allow bias correction:

```
Tsallis(PProba, q = 1)

## None
## 4.736023
```

Bias-corrected entropy is ready to be transformed into explicit diversity.

Effective numbers of species

Entropy should be converted into “true diversity” (Jost 2007), *i.e.* effective number of species equal to Hill (1973) numbers:

$${}^qD = \left(\sum_s p_s^q \right)^{\frac{1}{1-q}} \quad (5)$$

This can be done by the deformed exponential function, or using directly the `Diversity` or `bcDiversity` functions (equal to the deformed exponential of order q of `Tsallis` or `bcTsallis`)

```
expq(Tsallis(PAbd, q = 2), q = 2)

## ChaoWangJost
## 73.13163

Diversity(PAbd, q = 2)

## ChaoWangJost
## 73.13163
```

The effective number of species of the Paracou dataset is estimated to be 73 after bias correction (rather than 69 without it). It means that a community made of 73 equally-frequent species has the same Simpson entropy as the actual one. This is much less than the actual 425 sampled species. Simpson’s entropy focuses on dominant species.

Hurlbert’s diversity

Hurlbert’s index of diversity (Hurlbert 1971) of order k is the expected number of species observed in a sample of size k .

$${}_kS = \sum_s \left[1 - (1 - p_s)^k \right] \quad (6)$$

Greater values of k give more importance to rare species.

An unbiased estimator of ${}_kS$ has been provided by Hurlbert, for values of k up to the sample size n :

$${}_k\hat{S} = \sum_s \left[1 - \binom{n - n_s}{k} / \binom{n}{k} \right] \quad (7)$$

The effective number of species ${}_kD$ can be found by solving the following equation (Dauby and Hardy 2012):

$${}_kS = {}_kD \left[1 - \left(1 - \frac{1}{{}_kD} \right)^k \right] \quad (8)$$

Hurlbert's index is calculated by the `Hurlbert` function. Its unbiased estimator is obtained by `bcHurlbert` (implicitly if an abundance vector is used). Its effective number of species is calculated by `HurlbertD` or `bcHurlbertD`.

```
Hurlbert(PProba, k = 2)

## Biased
## 1.985449

Hurlbert(PAbd, k = 2)

## Unbiased
## 1.986326

HurlbertD(PAbd, k = 2)

## Unbiased
## 73.13163
```

Hurlbert's diversity of order 2 is identical to Simpson's diversity.

3.2. Meta-community functions

Meta-community functions allow partitioning diversity according to Patil and Taillie's concept of diversity of a mixture (Patil and Taillie 1982), *i.e.* α entropy of a meta-community is defined as the weighted average of community entropy, following Routledge (1979):

$${}^qH_\alpha = \sum_i w_i {}^q_iH_\alpha \quad (9)$$

${}^q_iH_\alpha$ is the entropy of community i :

$${}^q_iH_\alpha = \frac{1 - \sum_s p_{s,i}^q}{q - 1} = - \sum_s p_{s,i}^q \ln_q p_{s,i} = \sum_s p_{s,i} \ln_q \frac{1}{p_{s,i}} \quad (10)$$

Jost's (2007) definition of α entropy is not supported explicitly in the package since it only allows partitioning of equally weighted communities. In this particular case, both definitions are identical.

γ entropy of the meta-community is defined as α entropy of a community. β entropy, the difference between γ and α , is the generalized Jensen-Shannon divergence between the species distribution of the meta-community and those of communities (Marcon *et al.* 2014a):

$${}^qH_\beta = {}^qH_\gamma - {}^qH_\alpha = \sum_s p_{s,i}^q \ln_q \frac{p_{s,i}}{p_s} = \sum_s p_{s,i} \ln_q \frac{p_s}{p_{s,i}} \quad (11)$$

β entropy should be transformed into diversity, *i.e.* an effective number of communities:

$${}^qD_\beta = e_q^{\frac{{}^qH_\beta}{1-(q-1){}^qH_\alpha}} \quad (12)$$

Basic meta-community functions

These values can be estimated by the meta-community functions named **AlphaEntropy**, **AlphaDiversity**, **BetaEntropy**, **BetaDiversity**. They accept a **Metacommunity** and an order of diversity q as arguments, and return an **MCEntropy** or **MCdiversity** object which can be summarized and plotted. **GammaEntropy** and **GammaDiversity** return a number. Estimation-bias corrections are applied by default:

```
e <- AlphaEntropy(Paracou618.MC, q = 1)
summary(e)

## Neutral alpha entropy of order 1 of metaCommunity
## Paracou618.MC with correction: Best
##
## Entropy of communities:
##   P006   P018
## 4.384539 4.706510
## Average entropy of the communities:
## [1] 4.522322
```

The Shannon α entropy of the meta-community is 4.52. It is the weighted average entropy of communities.

Diversity Partition of a metacommunity

The **DivPart** function calculates everything at once. Its arguments are the same but bias correction is not applied by default. It can be, using the argument **Biased = FALSE**, and the correction chosen by the argument **Correction**. It returns a **DivPart** object which can be summarized (entropy is not printed by **summary**) and plotted:

```
p <- DivPart(q = 1, MC = Paracou618.MC, Biased = FALSE)
summary(p)

## HCDT diversity partitioning of order 1 of metaCommunity
## Paracou618.MC
## with correction: Best
## Alpha diversity of communities:
##   P006   P018
## 80.20125 110.66525
## Total alpha diversity of the communities:
## [1] 92.04908
## Beta diversity of the communities:
## ChaoWangJost
##   1.447498
## Gamma diversity of the metacommunity:
## ChaoWangJost
##   133.2409
```

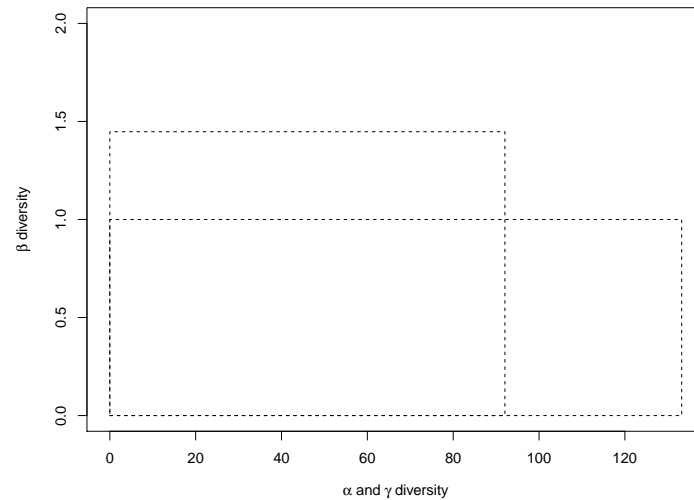


Figure 4. Plot of the diversity partition of the meta-community `Paracou618.MC`. The long rectangle of height 1 represents γ diversity, equal to 133 effective species. The narrower and higher rectangle has the same area: its horizontal size is α diversity (92 effective species) and its height is β diversity (1.45 effective communities).

```
p$CommunityAlphaEntropies
```

```
##      P006      P018
## 4.384539 4.706510
```

The α diversity of communities is 92 effective species (it is the exponential of the entropy calculated previously). This is more than Simpson diversity (73 species, calculated above) because less frequent species are taken into account. γ diversity of the meta-community is 133 effective species. β diversity is 1.45 effective communities, *i.e.* the two actual communities are as different from each other as 1.45 ones with equal weights and no species in common.

Diversity Estimation of a metacommunity

The `DivEst` function decomposes diversity and estimates confidence interval of α , β and γ diversity following [Marcon *et al.* \(2012\)](#). If the observed species frequencies of a community are assumed to be a realization of a multinomial distribution, they can be drawn again to obtain a distribution of entropy.

```
de <- DivEst(q = 1, Paracou618.MC, Biased = FALSE, Correction = "Best",
             Simulations = 100)
```

```
## =====
```

```
summary(de)
```

```
## Diversity partitioning of order 1 of MetaCommunity
## Paracou618.MC
## with correction: Best
## Alpha diversity of communities:
```

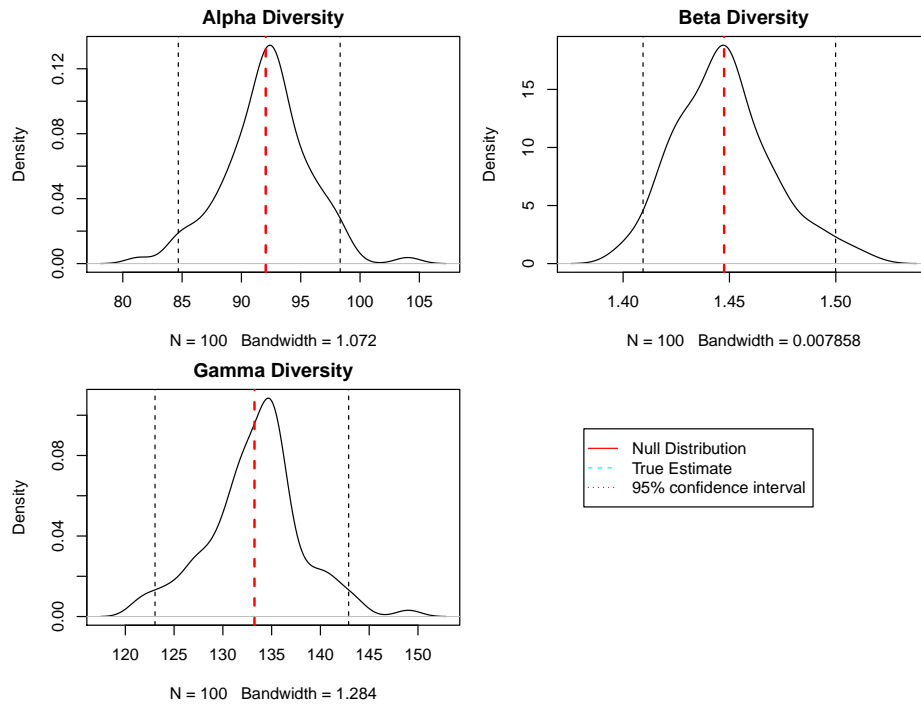


Figure 5. Plot of the diversity estimation of the meta-community Paracou618.MC. α , β and γ diversity probability densities are plotted, with a 95% confidence interval.

```
##      P006      P018
## 80.20125 110.66525
## Total alpha diversity of the communities:
## [1] 92.04908
## Beta diversity of the communities:
## ChaoWangJost
## 1.447498
## Gamma diversity of the metacommunity:
## ChaoWangJost
## 133.2409
## Quantiles of simulations (alpha, beta and gamma diversity):
##      0%      1%      2.5%      5%      10%      25%
## 81.34990 84.04835 84.68131 85.85257 87.51551 90.00749
##      50%      75%      90%      95%      97.5%      99%
## 92.25163 94.01741 96.66509 97.60709 98.32372 99.10372
##      100%
## 104.02515
##      0%      1%      2.5%      5%      10%      25%
## 1.399179 1.402550 1.409378 1.414313 1.421308 1.431690
##      50%      75%      90%      95%      97.5%      99%
## 1.446809 1.461077 1.476038 1.490686 1.499904 1.504217
##      100%
## 1.514379
##      0%      1%      2.5%      5%      10%      25%
## 121.3212 121.6020 123.0445 124.6838 127.0422 130.7377
##      50%      75%      90%      95%      97.5%      99%
## 133.7500 135.5387 138.8464 141.1592 142.8943 143.9463
##      100%
## 149.0191
```

The result is a **Divest** object which can be summarized and plotted (Figure 5).

The uncertainty of estimation is due to sampling: the distribution of the estimators corresponds to the simulated repetitions of sampling in the original multinomial distribution of species. It ignores the remaining bias of the estimator, which is unknown. Yet, except for $q = 2$, the corrected estimators *are* biased (even though much less than the non-corrected ones), especially when q is small. New estimators to reduce the bias are included in the package regularly.

Diversity Profile of a metacommunity

DivProfile calculates diversity profiles, *i.e.* the value of diversity against its order (Figure 6). The result is a **DivProfile** object which can be summarized and plotted.

```
dp <- DivProfile(seq(0, 2, 0.2), Paracou618.MC, Biased = FALSE,
  NumberOfSimulations = 10)

## =====

summary(dp)

## Diversity profile of MetaCommunity Paracou618.MC
## with correction: Best
## Diversity against its order:
##      Order Alpha Diversity Beta Diversity
## ChaoWangJost 0.0      238.36351      1.321238
## ChaoWangJost 0.2      204.17972      1.323271
## ChaoWangJost 0.4      170.72117      1.335708
## ChaoWangJost 0.6      139.89024      1.361171
## ChaoWangJost 0.8      113.37058      1.399674
## ChaoWangJost 1.0       92.04908      1.447498
## ChaoWangJost 1.2       75.81819      1.498587
## ChaoWangJost 1.4       63.87372      1.546905
## ChaoWangJost 1.6       55.18979      1.588960
## ChaoWangJost 1.8       48.84485      1.623736
## ChaoWangJost 2.0       44.13559      1.651781
##      Gamma Diversity
## ChaoWangJost      314.93484
## ChaoWangJost      270.18504
## ChaoWangJost      228.03372
## ChaoWangJost      190.41457
## ChaoWangJost      158.68180
## ChaoWangJost      133.24089
## ChaoWangJost      113.62013
## ChaoWangJost       98.80658
## ChaoWangJost       87.69438
## ChaoWangJost       79.31112
## ChaoWangJost       72.90234
```

Small orders of diversity give more weight to rare species. P018 can be considered more diverse than P006 because their profiles (Figure 6, top right) do not cross (Tothmeresz 1995): its diversity is systematically higher. The shape of the β diversity profile shows that the communities are more diverse when their dominant species are considered.

The bootstrap confidence intervals of the values of diversity (Marcon *et al.* 2012, 2014a) are calculated if **NumberOfSimulations** is not 0.

Alternative functions

Beta entropy can also be calculated by a set of functions named after the community functions, such as **TsallisBeta**, **bcTsallisBeta**, **SimpsonBeta**, etc. which require two vectors of

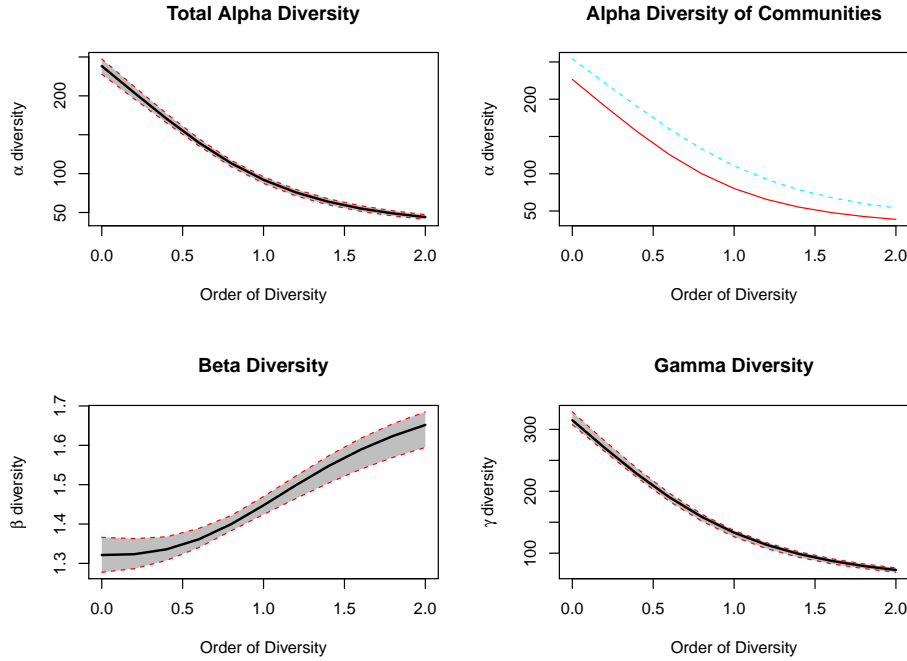


Figure 6. Diversity profile of the meta-community `Paracou618.MC`. Values are the number of effective species (α and γ diversity) and the effective number of communities (β diversity). Community P006 is represented by the solid line and community P018 by the dotted line. α and γ diversity decrease from $q = 0$ (number of species) to $q = 2$ (Simpson diversity) by construction.

abundances or probabilities instead of a `MetaCommunity` object: that of the community and the expected one (usually that of the meta-community). Bias correction is currently limited to Chao and Shen’s correction. The example below calculates the Shannon β entropy of the first community of `Paracou618` and the meta-community.

```
ShannonBeta(Paracou618.MC$Psi[, 1], PProba)
```

```
##      None
## 0.3499358
```

These functions are available for particular uses, when a `MetaCommunity` is not available or not convenient to use (*e.g.* simulations). Meta-community functions are preferred in general.

4. Phylogenetic diversity

Phylogenetic or functional diversity generalizes HCDT diversity, considering the distance between species (Marcon and Hérault 2015). Here, all species take place in an ultrametric phylogenetic or functional tree (Figure 7). The tree is cut into slices, delimited by two nodes. The first slice starts at the bottom of the tree and ends at the first node. In slice k , L_k leaves are found. The probabilities of occurrence of the species belonging to branches that were below leaf l in the original tree are summed to give the grouped probability $u_{k,l}$. HCDT

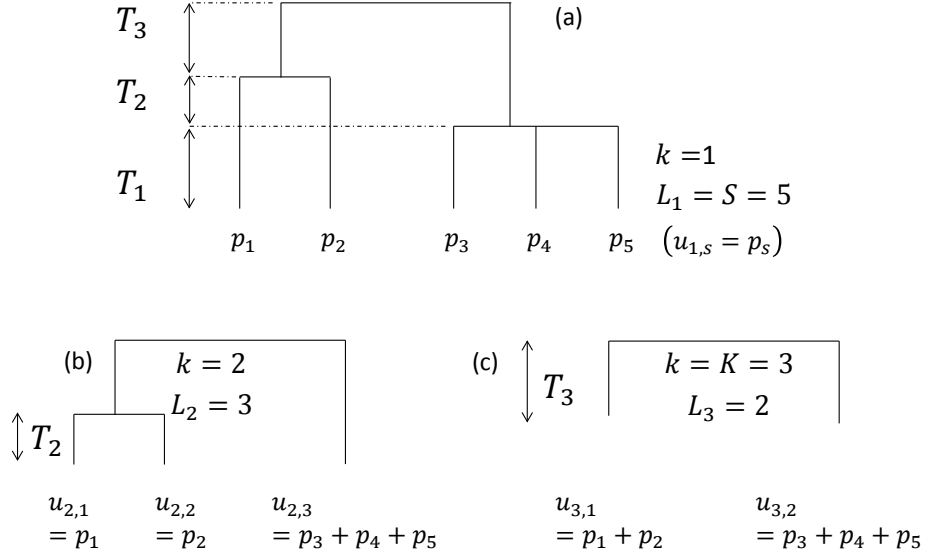


Figure 7. Hypothetical ultrametric tree. (a) The whole tree contains three slices, delimited by two nodes. The length of slices is T_k . (b) Focus on slice 2. The tree without slice 1 is reduced to 3 leaves. Frequencies of collapsed species are $u_{k,l}$. (c) Slice 3 only.

entropy can be calculated in slice k :

$${}_k^q H = - \sum_l u_{k,l}^q \ln_q u_{k,l} \quad (13)$$

Then, it is summed over the tree slices. Phyloentropy can be normalized or not. We normalize it so that it does not depend on the tree height:

$${}^q \overline{H}(T) = \sum_{k=1}^K \frac{T_k}{T} {}_k^q H \quad (14)$$

Unnormalized values are multiplied by the height of the tree, such as ${}^q PD(T)$ (Chao *et al.* 2010).

Phyloentropy is calculated as HCDT entropy along the slices of the trees applying possible estimation-bias corrections, summed, possibly normalized, and finally transformed into diversity:

$${}^q \overline{D}(T) = e_q^{{}^q \overline{H}(T)} \quad (15)$$

4.1. Community functions

PhyloEntropy and the estimation-bias-corrected **bcPhyloEntropy** are the phylogenetic analogs of **Tsallis** and **bcTsallis**. They accept the same arguments plus an ultrametric tree of class **phylo**, **hclust** or **phylog**, and **Normalize**, a boolean to normalize the tree height to 1 (by default).

Phylogenetic diversity is calculated by `PhyloDiversity` or `bcPhyloDiversity`, analogous to the species-neutral diversity functions `Diversity` and `bcDiversity`.

Results are either a `PhyloDiversity` or a `PhyloEntropy` object, which can be plotted (Figure 8) and summarized.

```
phd <- bcPhyloDiversity(PAbd, q = 1, Tree = Paracou618.Taxonomy,
  Normalize = TRUE)
summary(phd)

## alpha or gamma
## phylogenetic or functional diversity of order 1
## of distribution PAbd
## with correction: Best
## Phylogenetic or functional diversity was calculated according to the tree
## Paracou618.Taxonomy
##
## Diversity is normalized
##
## Diversity equals: 54.78324
```

The phylogenetic diversity of order 1 of the Paracou dataset is 55 effective species: 55 totally different species (only connected by the root of the tree) with equal probabilities would have the same entropy. It can be compared to its species-neutral diversity: 133 species. The latter is the diversity of the first slice of the tree. When going up the tree, diversity decreases because species collapse. On Figure 8, the diversity of the second slice, between $T = 1$ and $T = 2$, is that of genera (63 effective genera) and the last slice contains 20 effective families. The phylogenetic entropy of the community is the average of the entropy along slices, weighted by the slice lengths. Diversity can not be averaged the same way.

A less trivial phylogeny would contain many slices, resulting in as many diversity levels with respect to T .

The `AllenH` function is close to `PhyloEntropy`: it also calculates phyloentropy but the algorithm is that of [Allen, Kon, and Bar-Yam \(2009\)](#) for $q = 1$ and that of [Leinster and Cobbold \(2012\)](#) for $q \neq 1$. It is much faster since it does not require calculating entropy for each slice of the tree but it does not allow estimation-bias correction. `ChaoPD` calculates phylo-diversity according to [Chao *et al.* \(2010\)](#), with the same advantages and limits compared to `PhyloDiversity`.

For convenience, `PDFD` and `Rao` functions are provided to calculate unnormalized phyloentropy of order 0 and 2.

4.2. Meta-community functions

`DivPart`, `DivEst` and `DivProfile` functions return phylogenetic entropy and diversity values instead of species-neutral ones if a tree is provided in the arguments.

```
dp <- DivPart(q = 1, Paracou618.MC, Biased = FALSE, Correction = "Best",
  Tree = Paracou618.Taxonomy)
summary(dp)

## HCDT diversity partitioning of order 1 of metaCommunity
## Paracou618.MC
## with correction: Best
## Phylogenetic or functional diversity was calculated
```

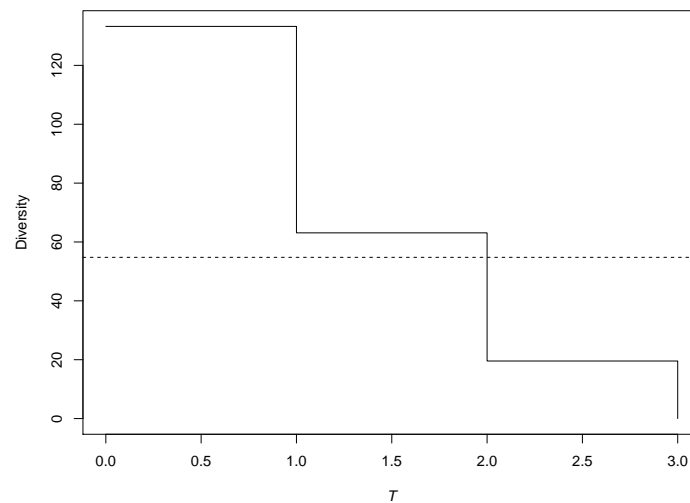



Figure 8. Plot of the γ phylodiversity estimation of the meta-community `Paracou618.MC`. The effective number of taxa of Shannon diversity is plotted against the distance from the leaves of the phylogenetic tree. Here, the tree is based on a rough taxonomy, so diversity of species, genera and families are the three levels of the curve. The dotted line represents the value of phylodiversity.

```
## according to the tree
## Paracou618.Taxonomy
##
## Diversity is normalized
##
## Alpha diversity of communities:
##      P006      P018
## 36.66108 51.98951
## Total alpha diversity of the communities:
## [1] 42.57235
## Beta diversity of the communities:
## [1] 1.286827
## Gamma diversity of the metacommunity:
## [1] 54.78324
```

The decomposition is interpreted as the species-neutral one: γ diversity is 55 effective species, made of 1.3 effective communities of 43 effective species.

Other meta-community functions, such as `AlphaEntropy` behave the same way:

```
summary(BetaEntropy(Paracou618.MC, q = 2, Tree = Paracou618.Taxonomy,
  Correction = "None", Normalize = FALSE))

## HCDT beta entropy of order 2 of metaCommunity Paracou618.MC
## with correction: None
##
## Phylogenetic or functional entropy was calculated according to the tree
## Paracou618.Taxonomy
##
## Entropy is not normalized
## Entropy of communities:
##      P006      P018
## 0.04117053 0.02325883
```

```
## Average entropy of the communities:
## [1] 0.03350547
```

Compare with Rao's `divc` computed by `ade4`:

```
library("ade4")
divc(as.data.frame(Paracou618.MC$Wi), disc(as.data.frame(Paracou618.MC$Nsi),
  Paracou618.Taxonomy$Wdist))

##              diversity
## Paracou618.MC$Wi 0.03350547
```

5. Similarity-based diversity

Leinster and Cobbold (2012) introduced similarity-based diversity of a community ${}^qD^Z$. A matrix \mathbf{Z} describes the similarity between pairs of species, defined between 0 and 1. A species ordinariness is its average similarity with all species (weighted by species frequencies), including similarity with itself (equal to 1). Similarity-based diversity is the reciprocal of the generalized average of order q (Hardy, Littlewood, and Pólya 1952) of the community species ordinariness.

The `Dqz` function calculates similarity-based diversity. Its arguments are the vector of probabilities of occurrences of the species, the order of diversity and the similarity matrix \mathbf{Z} . The `bcDqz` function allows estimation-bias correction (Marcon *et al.* 2014b).

This example calculates the γ diversity of the meta-community Paracou. First, the similarity matrix is calculated from the distance matrix between all pairs of species as 1 minus normalized dissimilarity.

```
DistanceMatrix <- as.matrix(Paracou618.dist)
Z <- 1 - DistanceMatrix/max(DistanceMatrix)
bcDqz(PAbd, q = 2, Z)

##      Best
## 1.48295
```

If \mathbf{Z} is the identity matrix, similarity-based diversity equals HCDT diversity:

```
Dqz(PProba, q = 2, Z = diag(length(PProba)))

##      None
## 68.7215

Diversity(PProba, q = 2)

##      None
## 68.7215
```

Functional diversity of order 2 is only 1.48 effective species, which is very small compared to 69 effective species for Simpson diversity. 1.48 equally-frequent species with similarity equal to 0 would have the same functional diversity as the actual community (made of 425 species). This means that species are very similar from a functional point of view. The very low values

returned by ${}^qD^Z$ are questioned by [Chao *et al.* \(2014\)](#) and discussed in depth by [Marcon *et al.* \(2014b\)](#): the choice of the similarity matrix is not trivial.

The similarity-based entropy of a community ${}^qH^Z$ ([Leinster and Cobbold 2012](#); [Ricotta and Szeidl 2006](#)) has the same relations with diversity as HCDT entropy and Hill numbers. The `Hqz` function calculates it:

```
Hqz(PProba, q = 2, Z)

##      None
## 0.3208152

lnq(Dqz(PProba, q = 2, Z), q = 2)

##      None
## 0.3208152
```

As species-neutral entropy, ${}^qH^Z$ has no straightforward interpretation beyond the average surprise of a community.

All meta-community functions can be used to estimate similarity-based diversity: argument `Z` must be provided:

```
e <- AlphaEntropy(Paracou618.MC, q = 1, Z = Z)
summary(e)

## Similarity-based alpha entropy of order 1 of metaCommunity
## Paracou618.MC with correction: Best
##
## Phylogenetic or functional entropy was calculated according to the similarity matrix
## Z
##
## Entropy of communities:
##      P006      P018
## 0.3945541 0.3934725
## Average entropy of the communities:
## [1] 0.3940912
```

The α functional entropy of the meta-community is the average entropy of communities.

6. Advanced tools

The package comes with a set of tools to realize frequents tasks: run Monte-Carlo simulations on a community, quickly calculate its diversity profile, apply a function to a species distribution along a tree, and manipulate meta-communities.

6.1. Random communities

The `rCommunity` function allows creating random communities. Their species probability distribution can be drawn in a well-known distribution (such as a log-normal one) or obtained from the data, just by dividing abundances by the total number of individuals ([Marcon *et al.* 2012](#)), or derived from a more sophisticated model by [Chao and Jost \(2015\)](#). Finally, the specified number of communities are drawn in a multinomial distribution.

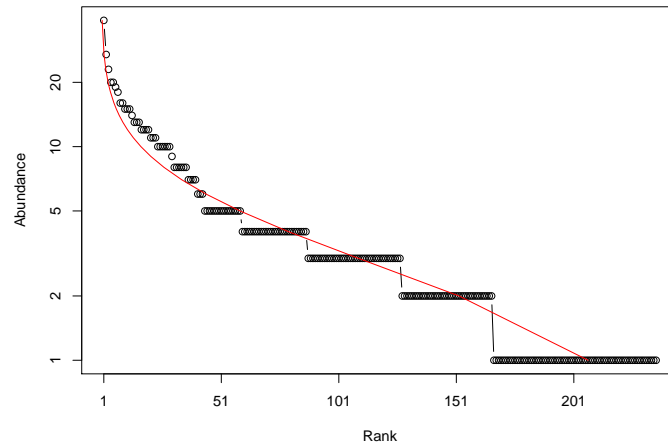


Figure 9. Whittaker plot of a simulated community from a log-normal distribution. The red line is the fit of a log-normal distribution estimated from the data.

The log-normal (Preston 1948), the log-series (Fisher, Corbet, and Williams 1943), the geometric (Motomura 1932), and the broken-stick (MacArthur 1957) distributions can be simulated.

This example code draws a single community of 1000 individuals according to a log-normal distribution with 300 species. Many species are not observed in the 1000-individual sample: the observed number of species is shown, with an estimation of the actual number (which should be 300). The simulated community is plotted, with its log-normal distribution fitted from the data (Figure 9). Estimated parameters can be compared to the original ones.

```
NsRef <- rCommunity(n = 1, size = 1000, S = 300, Distribution = "lnorm",
  sd = 1)
Richness(as.ProbaVector(NsRef))

## None
## 236

Richness(NsRef)

## Chao1
## 298.7577

plot(NsRef, Distribution = "lnorm")

## $mu
## [1] 1.018011
##
## $sigma
## [1] 0.875599
```

6.2. Entropy of Monte-Carlo simulated communities

The EntropyCI function is a versatile tool to simplify simulations. Simulated communities

are obtained by random draws in a multinomial distribution of species and their entropy is calculated. The arguments of `EntropyCI` are an entropy function (any entropy function of the package accepting a vector of species abundances, such as `bcTsallis`), the number of simulations to run, the observed species frequencies and the method to obtain probabilities for the multinomial distribution (the same as that of `rCommunity`).

The result is a numeric vector containing the entropy value of each simulated community. Entropy can be finally transformed into diversity (but it is not correct to use a diversity function in simulations because the average simulated value must be calculated and only entropy can be averaged).

This example shows how to use the function. First, the distribution of the γ HCDT entropy of order 1 (Shannon entropy) of the Paracou meta-community is calculated and transformed into diversity. Then, the actual diversity is calculated and completed by the 95% confidence interval of the simulated values.

```
SimulatedDiversity <- expq(EntropyCI(FUN = Tsallis, Simulations = 100,
  Ns = PAbd, q = 1), q = 1)

## =====

Diversity(PAbd, q = 1)

## ChaoWangJost
##      133.2409

quantile(SimulatedDiversity, probs = c(0.025, 0.975))

##      2.5%      97.5%
## 122.1042 143.5507
```

These results are identical to those of the `DivEst` function but a single community can be addressed (`DivEst` requires a `MetaCommunity`).

6.3. Diversity or Entropy Profile of a community

This function is used to calculate diversity or entropy profiles based on community functions such as `Tsallis` or `ChaoPD`. It is similar to `DivProfile` but does not require a `MetaCommunity` for argument. It can compute a bootstrap confidence envelope of the estimation of the profile, like `EntropyCI`. It returns a `CommunityProfile` object which can be plotted. Profiles can be added to an existing plot by the `CEnvelope` function.

This example evaluates bias correction on the diversity profile of the Paracou dataset. First, diversity profiles are calculated with and without bias correction. The corrected profile is calculated with its confidence envelope:

```
bcProfile <- CommunityProfile(Diversity, PAbd, NumberOfSimulations = 10)

## =====

Profile <- CommunityProfile(Diversity, PProba)
```

Then, they can be plotted altogether (Figure 10):

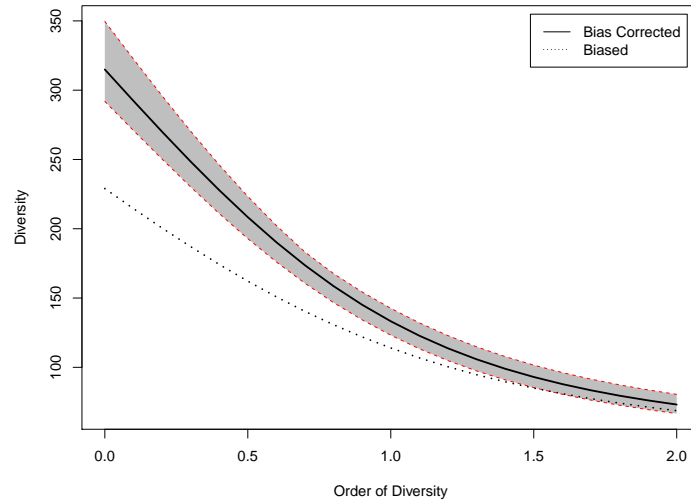


Figure 10. γ diversity profile of the the meta-community Paracou618.MC, without bias correction (dotted line) and with correction (solid line). .

```
plot(bcProfile)
CEnvelope(Profile, lty = 3)
legend("topright", c("Bias Corrected", "Biased"), lty = c(1,
  3), inset = 0.02)
```

6.4. Applying a Function over a Phylogenetic Tree

The `PhyloApply` function is used to apply an entropy community function (generally `bcTsallis`) along a tree, the same way `lapply` works with a list.

This example shows how to calculate Shannon entropy along the tree containing the taxonomy to obtain species, genus and family entropy shown on figure 8:

```
pa <- PhyloApply(Tree = Paracou618.Taxonomy, FUN = bcTsallis,
  NorP = PAbd)
summary(pa)

## bcTsallis applied to PAbd along the tree:
## Paracou618.Taxonomy
##
## Results are normalized
##
## The average value is: 4.003384
##
## Values along the tree are:
##      1      2      3
## 4.892159 4.144688 2.973306

exp(pa$Cuts)

##      1      2      3
## 133.24089 63.09794 19.55647

exp(pa$Total)

## [1] 54.78324
```

6.5. Manipulation of meta-communities

Several meta-communities, combined in a list, can be merged two different ways: the `MergeMC` function simplifies hierarchical partitioning of diversity: it considers the aggregated data of each meta-community as a community and builds an upper-level meta-community with them. The α entropy of the new meta-community is the weighted average γ entropy of the original meta-communities.

`MergeC` combines the communities of several meta-communities to create a single meta-community containing them all. Last, `ShuffleMC` randomly shuffles communities accross meta-communities to allow simulations to test differences between meta-communities.

This example shows how to do this. A first meta-community is created, weights of communities are proportional to their number of individuals:

```
(df <- data.frame(C1 = c(10, 10, 10, 10), C2 = c(0, 20, 35, 5),
  C3 = c(25, 15, 0, 2), row.names = c("sp1", "sp2", "sp3",
    "sp4")))

##      C1 C2 C3
## sp1 10  0 25
## sp2 10 20 15
## sp3 10 35  0
## sp4 10  5  2

w <- colSums(df)
MC1 <- MetaCommunity(Abundances = df, Weights = w)
```

Then a second one:

```
(df <- data.frame(C1 = c(10, 4), C2 = c(3, 4), row.names = c("sp1",
  "sp5")))

##      C1 C2
## sp1 10  3
## sp5  4  4

w <- colSums(df)
MC2 <- MetaCommunity(Abundances = df, Weights = w)
```

They can be merged to obtain a single meta-community containing all original communities:

```
mergedMC1 <- MergeC(list(MC1, MC2))
mergedMC1$Nsi

##      MC1.C1 MC1.C2 MC1.C3 MC2.C1 MC2.C2
## sp1      10      0     25      10      3
## sp2      10     20     15       0      0
## sp3      10     35      0       0      0
## sp4      10      5      2       0      0
## sp5       0      0      0       4      4
```

They can also be merged considering each of them as a community of a higher-level meta-community:

```
mergedMC2 <- MergeMC(list(MC1, MC2), Weights = sapply(list(MC1,
  MC2), function(x) (x$N)))
mergedMC2$Nsi
```

```
##      MC1 MC2
## sp1  35  13
## sp2  45   0
## sp3  45   0
## sp4  17   0
## sp5   0   8
```

Hierarchical diversity partitioning can then be achieved:

```
dpAll <- DivPart(q = 1, MC = mergedMC2)
summary(dpAll)

## HCDT diversity partitioning of order 1 of metaCommunity
## mergedMC2
##
## Alpha diversity of communities:
##      MC1      MC2
## 3.772161 1.943574
## Total alpha diversity of the communities:
## [1] 3.463277
## Beta diversity of the communities:
##      None
## 1.236351
## Gamma diversity of the metacommunity:
##      None
## 4.281826
```

The γ diversity of the top assemblage (MC1 and MC2) is 4.28 effective species, made of 1.24 effective meta-communities of 3.46 effective species. The α diversity of each meta-community of the top assemblage is their γ diversity when it is partitioned in turn:

```
dpMC1 <- DivPart(q = 1, MC = MC1)
summary(dpMC1)

## HCDT diversity partitioning of order 1 of metaCommunity MC1
##
## Alpha diversity of communities:
##      C1      C2      C3
## 4.000000 2.429521 2.273918
## Total alpha diversity of the communities:
## [1] 2.741671
## Beta diversity of the communities:
##      None
## 1.375862
## Gamma diversity of the metacommunity:
##      None
## 3.772161
```

The γ diversity of MC1 is 3.77 effective species, made of 1.38 effective meta-communities of 2.74 effective species. The same decomposition can be done for MC2.

7. Conclusion

The entropart package allows estimating biodiversity according to the framework based on HCDT entropy, the correction of its estimation-bias (Grassberger 1988; Chao and Shen 2003; Chao and Jost 2015) and its transformation into equivalent numbers of species (Hill 1973; Jost 2006; Marcon *et al.* 2014a). Phylogenetic or functional diversity (Marcon and Hérault 2015) can be estimated, considering phyloentropy as the average species-neutral diversity over slices

of a phylogenetic or functional tree (Pavoine *et al.* 2009). Similarity-based diversity Leinster and Cobbold (2012) can be used to estimate (Marcon *et al.* 2014b) functional diversity from a similarity or dissimilarity matrix between species without requiring building a dendrogram and thus preserving the topology of species (Pavoine, Ollier, and Dufour 2005; Podani and Schmera 2007).

The classical diversity estimators (Shannon and Simpson entropy) can be found in many R packages. **vegetarian** (Charney and Record 2009) allows calculating Hill numbers and partitioning them according to Jost’s framework. Bias correction is never available except in the **EntropyEstimation** (Cao and Grabchak 2014) package which provides the Zhang and Grabchak’s estimators of entropy and diversity and their asymptotic variance (not included in **entropart**). Phylodiversity and similarity-based diversity are not available in any package as far as we know. So we believe **entropart** is a useful toolbox for ecologists who need to estimate the diversity of actual, undersampled communities and to partition it.

References

- Allen B, Kon M, Bar-Yam Y (2009). “A New Phylogenetic Diversity Measure Generalizing the Shannon Index and Its Application to Phyllostomid Bats.” *American Naturalist*, **174**(2), 236–243.
- Beck J, Holloway JD, Schwanghart W (2013). “Undersampling and the Measurement of Beta Diversity.” *Methods in Ecology and Evolution*, **4**(4), 370–382.
- Bonachela JA, Hinrichsen H, Muñoz MA (2008). “Entropy Estimates of Small Data Sets.” *Journal of Physics A: Mathematical and Theoretical*, **41**(202001), 1–9.
- Cao L, Grabchak M (2014). “EntropyEstimation.” URL <http://cran.r-project.org/package=EntropyEstimation>.
- Chao A, Chiu CH, Jost L (2010). “Phylogenetic Diversity Measures Based on Hill Numbers.” *Philosophical Transactions of the Royal Society B*, **365**(1558), 3599–609.
- Chao A, Chiu CH, Jost L (2014). “Unifying Species Diversity, Phylogenetic Diversity, Functional Diversity and Related Similarity/Differentiation Measures Through Hill Numbers.” *Annual Review of Ecology, Evolution, and Systematics*, **45**, 297–324.
- Chao A, Jost L (2015). “Estimating diversity and entropy profiles via discovery rates of new species.” *Methods in Ecology and Evolution*, **6**(8), 873–882.
- Chao A, Lee SM, Chen TC (1988). “A generalized Good’s Nonparametric Coverage Estimator.” *Chinese Journal of Mathematics*, **16**, 189–199.
- Chao A, Shen TJ (2003). “Nonparametric Estimation of Shannon’s Index of Diversity When There Are Unseen Species in Sample.” *Environmental and Ecological Statistics*, **10**(4), 429–443.
- Charney N, Record S (2009). “vegetarian: Jost Diversity Measures for Community Data.” URL <http://cran.r-project.org/package=vegetarian>.

- Chiu CH, Chao A (2014). “Distance-Based Functional Diversity Measures and Their Decomposition: a framework based on hill numbers.” *PloS one*, **9**(7), e100014.
- Daróczy Z (1970). “Generalized Information Functions.” *Information and Control*, **16**(1), 36–51.
- Dauby G, Hardy OJ (2012). “Sampled-Based Estimation of Diversity Sensus Stricto by Transforming Hurlbert Diversities into Effective Number of Species.” *Ecography*, **35**(7), 661–672.
- Dray S, Dufour AB (2007). “The ade4 Package: Implementing the Duality Diagram for Ecologists.” *Journal of Statistical Software*, **22**(4), 1–20.
- Faith DP (1992). “Conservation Evaluation and Phylogenetic Diversity.” *Biological Conservation*, **61**(1), 1–10.
- Fisher RA, Corbet AS, Williams CB (1943). “The Relation Between the Number of Species and the Number of Individuals in a Random Sample of an Animal Population.” *Journal of Animal Ecology*, **12**, 42–58.
- Good IJ (1953). “On the Population Frequency of Species and the Estimation of Population Parameters.” *Biometrika*, **40**(3/4), 237–264.
- Grassberger P (1988). “Finite Sample Corrections to Entropy and Dimension Estimates.” *Physics Letters A*, **128**(6–7), 369–373.
- Hardy G, Littlewood J, Pólya G (1952). *Inequalities*. Cambridge University Press.
- Havrda J, Charvát F (1967). “Quantification Method of Classification Processes. Concept of Structural alpha-Entropy.” *Kybernetika*, **3**(1), 30–35.
- Hill MO (1973). “Diversity and Evenness: A Unifying Notation and Its Consequences.” *Ecology*, **54**(2), 427–432.
- Hérault B, Honnay O (2007). “Using Life-History Traits to Achieve a Functional Classification of habitats.” *Applied Vegetation Science*, **10**(1), 73–80.
- Hurlbert SH (1971). “The Nonconcept of Species Diversity: A Critique and Alternative Parameters.” *Ecology*, **52**(4), 577–586.
- Jost L (2006). “Entropy and Diversity.” *Oikos*, **113**(2), 363–375.
- Jost L (2007). “Partitioning Diversity into Independent Alpha and Beta Components.” *Ecology*, **88**(10), 2427–2439.
- Leinster T, Cobbold C (2012). “Measuring Diversity: the Importance of Species Similarity.” *Ecology*, **93**(3), 477–489.
- MacArthur RH (1957). “On the Relative Abundance of Bird Species.” *Proceedings of the National Academy of Sciences of the United States of America*, **43**(3), 293–295.
- Marcon E, Hérault B (2015). “entropart, an R Package to Partition Diversity.” *Journal of Statistical Software*, **67**(8), 1–26.

- Marcon E, Hérault B (2015). “Decomposing Phylodiversity.” *Methods in Ecology and Evolution*, **6**(3), 333–339.
- Marcon E, Hérault B, Baraloto C, Lang G (2012). “The Decomposition of Shannon’s Entropy and a Confidence Interval for Beta Diversity.” *Oikos*, **121**(4), 516–522.
- Marcon E, Scotti I, Hérault B, Rossi V, Lang G (2014a). “Generalization of the Partitioning of Shannon Diversity.” *PLOS One*, **9**(3), e90289.
- Marcon E, Zhang Z, Hérault B (2014b). “The Decomposition of Similarity-Based Diversity and its Bias Correction.” *HAL*, **hal-00989454**(version 1), 1–12.
- Motomura I (1932). “On the statistical treatment of communities.” *Zoological Magazine*, **44**, 379–383.
- Patil GP, Taillie C (1982). “Diversity as a Concept and its Measurement.” *Journal of the American Statistical Association*, **77**(379), 548–561.
- Pavoine S, Love MS, Bonsall MB (2009). “Hierarchical Partitioning of Evolutionary and Ecological Patterns in the Organization of Phylogenetically-Structured Species Assemblages: Application to Rockfish (Genus: *Sebastes*) in the Southern California Bight.” *Ecology Letters*, **12**(9), 898–908.
- Pavoine S, Ollier S, Dufour AB (2005). “Is the Originality of a Species Measurable?” *Ecology Letters*, **8**, 579–586.
- Petchey OL, Gaston KJ (2002). “Functional Diversity (FD), Species Richness and Community Composition.” *Ecology Letters*, **5**, 402–411.
- Podani J, Schmera D (2007). “How Should a Dendrogram-Based Measure of Functional Diversity Function? A rejoinder to Petchey and Gaston.” *Oikos*, **116**(8), 1427–1430.
- Preston FW (1948). “The Commonness, And Rarity, of Species.” *Ecology*, **29**(3), 254–283.
- R Core Team (2015). *R: A Language and Environment for Statistical Computing*. R Foundation for Statistical Computing, Vienna, Austria. URL <http://www.R-project.org>.
- Rao C (1982). “Diversity and Dissimilarity Coefficients: a Unified Approach.” *Theoretical Population Biology*, **21**, 24–43.
- Ricotta C, Szeidl L (2006). “Towards a Unifying Approach to Diversity Measures: Bridging the Gap Between the Shannon Entropy and Rao’s Quadratic Index.” *Theoretical Population Biology*, **70**(3), 237–243.
- Routledge R (1979). “Diversity Indices: Which Ones are Admissible?” *Journal of Theoretical Biology*, **76**(4), 503–515.
- Shannon CE (1948). “A Mathematical Theory of Communication.” *The Bell System Technical Journal*, **27**, 379–423, 623–656.
- Simpson EH (1949). “Measurement of Diversity.” *Nature*, **163**(4148), 688.

- Tothmeresz B (1995). “Comparison of Different Methods for Diversity Ordering.” *Journal of Vegetation Science*, **6**(2), 283–290.
- Tsallis C (1988). “Possible Generalization of Boltzmann-Gibbs Statistics.” *Journal of Statistical Physics*, **52**(1), 479–487.
- Tsallis C (1994). “What are the Numbers that Experiments Provide?” *Química Nova*, **17**(6), 468–471.
- Zhang Z, Grabchak M (2016). “Entropic Representation and Estimation of Diversity Indices.” *Journal of Nonparametric Statistics*, **28**(3), 563–575.
- Zhang Z, Huang H (2007). “Turing’s Formula Revisited.” *Journal of Quantitative Linguistics*, **14**(2-3), 222–241.

Affiliation:

Eric Marcon
AgroParisTech
Campus agronomique, BP 316
97310 Kourou, French Guiana
E-mail: eric.marcon@ecofog.gf

Bruno Hérault
Cirad
Campus agronomique, BP 316
97310 Kourou, French Guiana
E-mail: bruno.herault@ecofog.gf