

Part One

Given the following code segment:

```
int zoc(int m, int n){
    int x, y;
    if (m == 0 | n == 0)
        return (m+n);
    x = zoc(m-1, n);
    y = zoc(m, n-1);
    return (x+y)
}
```

Question One

What is the value returned if the fuction zoc is called with parameter m=3 and n=2?

15

Question Two

Give the mathematical recurrence function of zoc(m, n):

$$\text{zoc}[m, n] = \text{zoc}[m-1, n] + \text{zoc}[m, n-1]$$

Question Three

Describe the procedure (recursive calls) of deriving zoc(3, 2):

So the recursion base case stops at 1, because at that point n and m respectively will be zero. Then we recurse up the call stack, such that the following call stack returns:

x=1, y=1
x=2, y=2
x=1, y=1
x=2, y=2
x=4, y=4
x=1, y=1
x=2, y=2
x=4, y=3
x=8, y=7
15

Here I have elected to indicate the first term, as in the code above with x and the second term with y.

Part Two

Answer the questions based on the following program segment:

```
for(j=1; j<=n; ++j)
{
    i=j+1;
    do
    {
        if (theArray[i]<theArray[j])
            swap(theArray[i], theArray[j])
        ++i;
    }while(i <= n);
}
```

Question One

In the above program segment, how many times has comparison of `(theArray[i]<theArray[j])` been executed?

$$n^2$$

times.

Question Two

What is the asymptotic complexity of the above algorithm?

$$O(n^2)$$