
EE564 First Project II: TESLA Model S Induction Motor

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ID

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Specifications

In this project, design of the induction motor that is used in **Tesla Model S**. Normally it has different variations, to keep things simple; **RWD 85 Model** will be used that has the following specs:

- **Maximum Power:** 270 kW
- **Maximum Torque:** 441 Nm
- **Top Speed:** 225 km/h

Except for these given specs, these are also found from internet:

- **Number of poles:** 4
- Maximum RPM value of our motor is 21848 RPM. This value is calculated by considering Tesla Model S has 21" tires and 9.73 to 1 gear ratio.

If we assume average speed is 85 km/h. Then rated RPM value of motor will be 7960 RPM.

In this case supply frequency will be 265 Hz.

- **Number of phases:** 3
- **Line supply voltage:** 400 V
- **Rated Power:** 185 kW

Main Dimensions of Stator Core

Boldea's The Induction Machine Handbook is going to be used to determine parameters and dimensions of motor. In Chapter 15, it is explained that $D_{is}^2 L$ output constant concept will be used. For internal stator diameter formula below will be used:

$$D_{is}^3 = \frac{2pp_1 S_{gap}}{\pi \lambda f C_0}$$

To be able to calculate D_{is} , airgap power is needed.

At this point targeted efficiency is taken as 95 %.

Power factor is taken as 0.89

Another required parameter to be able to calculate airgap power is K_E that is defined as E_1 to V_{in} ratio in equation 14.8.

$$K_E \approx 0.98 - 0.005p_1$$

Now everything is ready for airgap apparent power:

$$S_{gap} = \frac{K_E P_n}{\eta_1 \cos \phi}$$

Airgap power is calculated as 212.2 KVA.

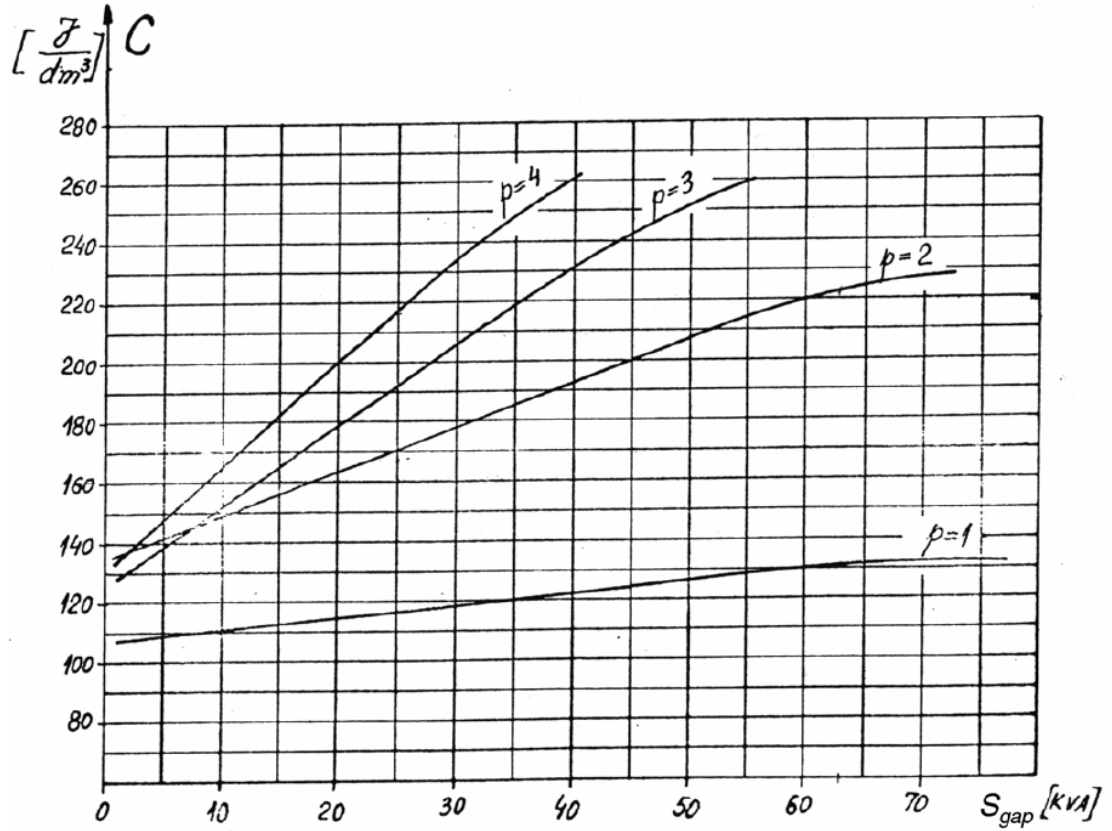
After this calculation, missing parameters are stack aspect ratio and Esson's constant C_0 . Stack aspect ratio is selected from table below:

Table 15.1. Stack aspect ratio λ

$2p_1$	2	4	6	8
λ	0.6 – 1.0	1.2 – 1.8	1.6 – 2.2	2 -3

It is selected as 1.5.

Esson's constant is selected using Figure 14.14.



Because our calculated airgap power is out of figure's range it isn't possible to read a certain value but for two pole-pairs after 60 kVA Esson's constant starts to saturate and for our airgap apparent power this value is taken as 240 J/dm³.

Now we are ready to calculate internal stator diameter:

Internal diameter of stator is calculated as 17.827 cm.

For realistic dimensions it is going to be taken as 17.9 cm.

Now we can calculate stack length, deriving its formula from equation 15.2:

$$L = \frac{\lambda \pi D_{1a}}{2p}$$

Stack length L is 21.09 cm.

For being realistic it is going to be taken as 21.1 cm.

By using equation 14.14 it is possible to calculate the pole pitch:

$$\tau = \frac{\pi D_{1a}}{2p}$$

Pole pitch is 14.06 cm.

Next step is deciding external stator diameter. For its calculation, table below will be used.

Table 15.2. Inner/outer stator diameter ratio

$2p_1$	2	4	6	8
$\frac{D_{is}}{D_{out}}$	0.54 – 0.58	0.61 – 0.63	0.68 – 0.71	0.72 – 0.74

It gives us information about ratio of internal and external stator diameters. For 4 poles this ratio will be taken as 0.61.

External diameter of stator is calculated as 29.344 cm.

For realistic dimensions it is going to be taken as 29.4 cm.

For suitable airgap calculation book's equation of 14.38 may be used as well as the equation defined during the EE564 lecture of 6th April. Here it is important to remind that the minimum airgap is 0.2 mm.

Formula discussed in the lecture is as follows:

$$airgap = 0.18 + 0.006P^{0.4}mm$$

Book equation of 14.38 is

$$airgap = 0.1 + 0.012P^{\frac{1}{3}}mm$$

As known, too small airgap would produce large space airgap field harmonics and additional losses while a too large one would reduce the power factor and efficiency. Therefore, average of these two calculated airgap values will be used as actual airgap value.

Airgap is calculated as 0.8656 mm.

For being realistic it is going to be taken as 0.87 mm.

The Stator Winding

Following James Hendershot's lecture notes, for 4 poles and 185 kW of rated power Stator slot number will be selected. Our rated power is nearly 250 HP and from table below, it is advised to choose 58 stator slots for our case.

HP	2 POLE			4 POLE		
	STD	EM	XE	STD	EM	XE
1	32/24	32/24	32/24	28/36	45/36	45/36
1.5	32/24	32/24	32/24	28/36	45/36	45/36
2	32/24	32/24	32/24	28/36	45/36	45/36
3	32/24	32/24	32/2	28/36	45/36	45/36
5	32/24	32/24	32/24	28/36	45/36	45/36
7.5	28/36	28/36	28/36	28/36	45/36	45/36
10	28/36	28/36	28/36	28/36	45/36	45/36
15	28/36	28/36	28/36	40/48	40/48	40/48
20	28/36	20/36	28/36	40/48	40/48	40/48
25	28/36	28/36	28/36	40/48	40/48	40/48
30	28/36	28/36	28/36	40/48	40/48	40/48
40	28/36	28/36	28/36	40/48	40/48	40/48
50	28/36	28/36	28/36	40/48	40/48	40/48
60	38 or 40/48	38 or 40/48	38 or 40/48	47/60	47/60	47/60
75	38 or 40/48	38 or 40/48	38 or 40/48	47/60	47/60	47/60
100	38 or 40/48	38 or 40/48	38 or 40/48	73/60	47/60	47/60
125	38 or 40/48	38 or 40/48	38 or 40/48	58/72	58/72	58/72
150	38 or 40/48	38 or 40/48	38 or 40/48	58/72	58/72	58/72
200	38 or 40/48	38 or 40/48	38 or 40/48	58/72	58/72	56or58/72
250	38 or 40/48	38 or 40/48	38 or 40/48	56or58/72	56or58/72	56or58/72

Here we should remember that the total number of slots per stator should be divisible by the number of phases. So it should be a number that is multiple of 3.

$$q = \frac{N_s}{2pm}$$

If we think about its formula above (taken from book; 4.7), it is possible to see that choosing N_s/m integer doesn't guarantee that q is an integer. In fact it doesn't have to be an integer and may be selected as a fraction. But in most induction machines, q is an integer to provide complete (pole to pole) symmetry for the winding. So in our case N_s must be multiple of $2pm=12$. Advised number is 58, so N_s would be taken as 60. It was tried and seen that number of conductors, flux density and other parameters don't meet the expectations. So it is going to be taken as 48.

Number of slots per pole per phase is 4 .

Now we should decide pitch factor. It can be selected as $5/6$ to reduce 5th harmonic and reduce 7th harmonics. So two layered winding with chorded coils will be used.

Selected pitch angle is 150 degree .

It is possible to calculate the electrical angle between emfs in neighboring slots α_{ec}

$$\alpha_{ec} = \frac{2\pi p}{N_s}$$

It is 0.262 radian means 15 degree.

Now we can calculate pitch factor. Due to chording coils of stator, induced voltage will drop but by means of harmonics we will have better results.

$$k_p = \sin\left(\frac{\lambda}{2}\right)$$

Pitch factor is calculated as 0.97 .

Using formula below it is possible to calculate distribution factor.

$$k_d = \frac{\sin(q \frac{\alpha}{2})}{q \sin \frac{\alpha}{2}}$$

Distribution factor is calculated as 0.96 .

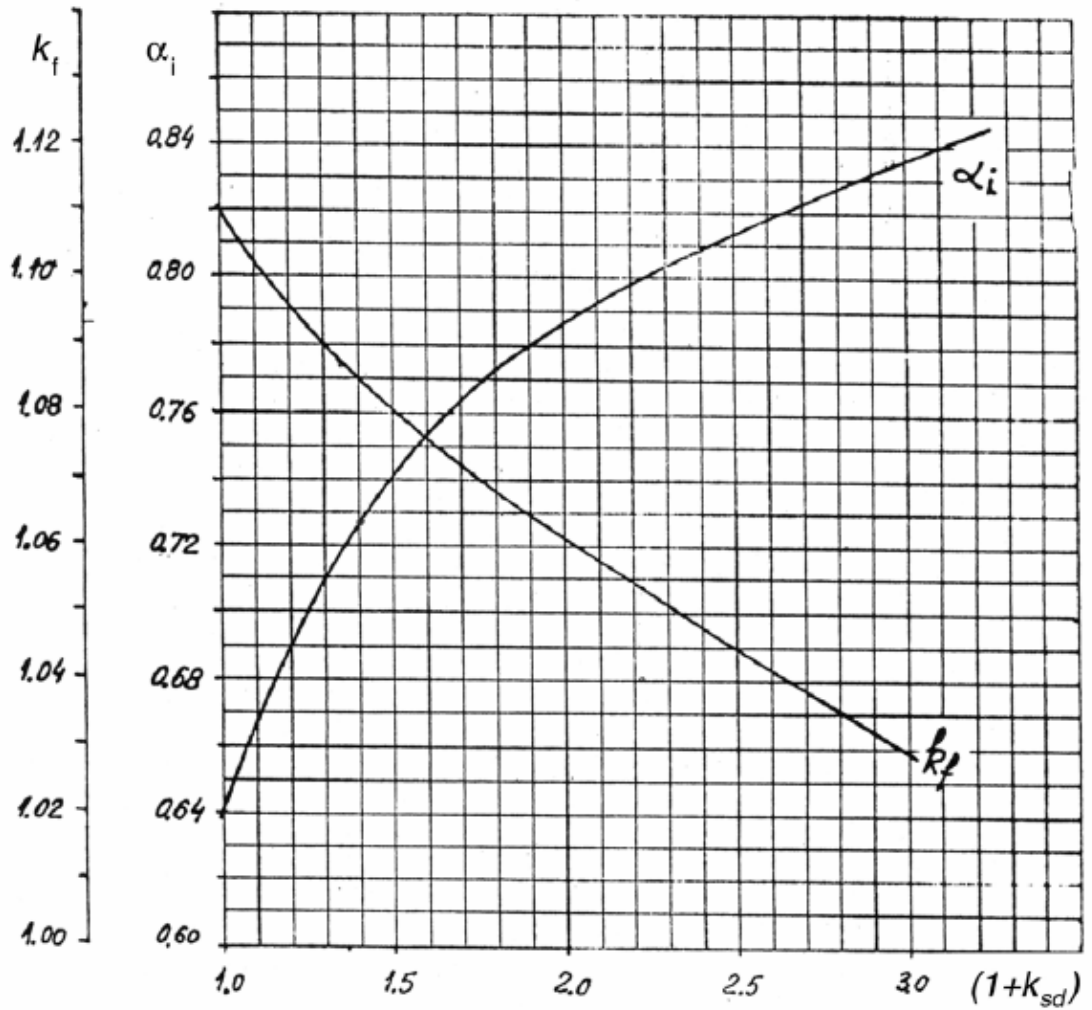
Multiplication of distribution and pitch factors are called as winding factor.

Winding factor is calculated as 0.93 .

Using recommended intervals given in 15.11, it is possible to select the airgap flux density. For 4 poles suggested interval is 0.65 to 0.78 Tesla. To decrease iron losses minimum of this interval will be taken as airgap flux density.

The pole coefficient K_f and form factor K_f depend on the tooth saturation factor $1+K_{st}$. If $1+K_{st}$ is taken as 1.4 then K_{st} is 0.4.

Using this value and graph below, it is possible to select form factor and flux density shape factor.



Form factor is selected as 1.085 .

Flux density shape factor is selected as 0.729 .

Using these coefficients it is possible to calculate pole flux.

$$\phi = \alpha_i \tau L B_g$$

Pole flux is calculated as 15.137 mWb.

The number of per phase can be calculated using formula below given with (15.12).

$$N_{ph} = \frac{K_E V_{ph}}{4 K_f K_w f \phi}$$

The number of turns per phase is calculated as 17.0 turns/phase.

The number of conductors per slot ns can be calculated using formula below:

$$n_s = \frac{a_1 N_{ph}}{p_1 q}$$

Here we use the number of current paths in parallel and will be taken as 1 for our case.

It is calculated as 2.13 .

It should be an even number as there are two distinct coils per slot in a double layer winding. So n_s is selected as 2.

If we turn back and recalculate the actual airgap flux density:

Recalculated airgap flux density is 0.745 T .

Now we can calculate rated current. 15.16 formula will be used:

$$I_{in} = \frac{P_n}{\eta \cos \phi_n \sqrt{3} V_1}$$

Rated phase current is calculated as 315.8 A .

To be able to calculate wire cross section, current density will be selected first. Here, recommendation 15.17 will be followed and for 4 poles current density will be taken as 6 A/mm².

$$A_{co} = \frac{I_{in}}{J_{cos}}$$

Magnetic cross section area is calculated as 52.64 mm².

Using cross-sectional wire area information it is possible to calculate the diameter wire gauge.

$$d_{co} = \sqrt{\frac{4A_{co}}{\pi}}$$

Wire gauge diameter is 8.19 mm.

Because this diameter is not small, 30 conductors will be paralleled to decrease the diameter of each conductor.

New wire gauge diameter is 1.49 mm.

By using table 15.3, it is possible to jump from wire diameter to insulated wire diameter.

Insulated wire gauge diameter is 1.53 mm.

Stator Slot Sizing

Since we know wire diameter, number of conductors in parallel and number of turns per slot, it is possible for us to calculate the slot area. Only missing parameter is fill factor selection. For round wire and at our rated power level it is advised to be taken between 0.4 and 0.44. So it is selected as 0.44. For useful area calculation formula (15.21) will be used:

$$A_{su} = \frac{\pi d_{co}^2 a_p n_s}{4K_{fill}}$$

Calculated useful slot area is 239.256 mm².

There are two recommended stator slot shapes in the book as follows:

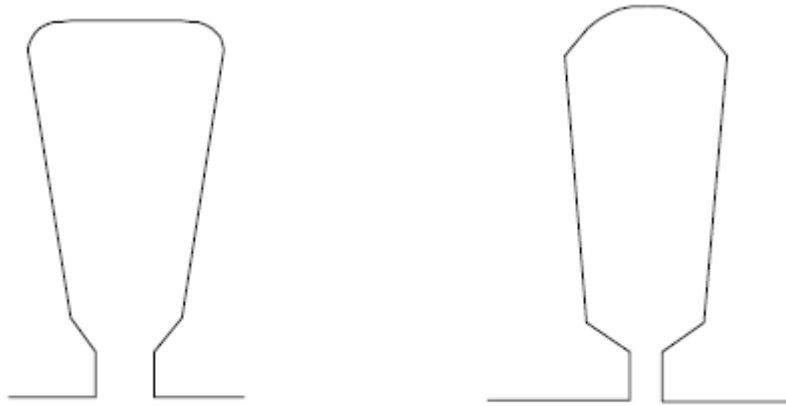


Figure 15.4 Recommended stator slot shapes

For ease of calculation and to be able to use explained slot geometry, left-hand side of stator slot shape is selected.

For this shape, explained lengths and are as in the figure below:

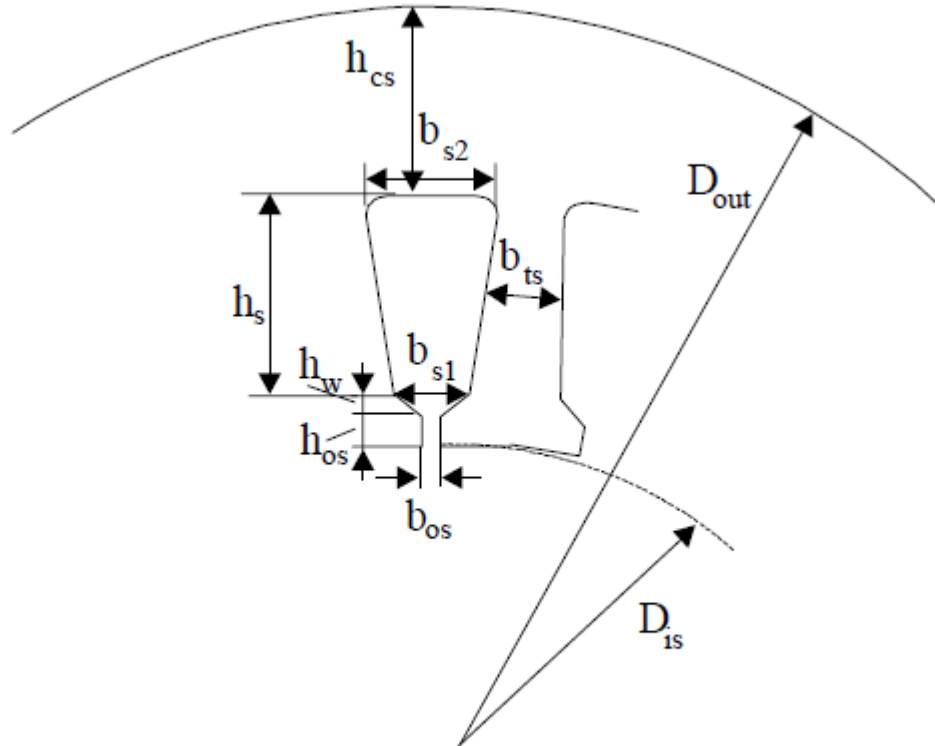


Figure 15.5 Stator slot geometry

Here, some parameters will be selected via following books' suggestions and some of them will be calculated.

Suggested variables are b_{os} , h_{os} and h_w . b_{os} can be defined as slot opening length and it is selected as 2 mm. h_{os} is the height of slot opening and it is taken as 1 mm. h_w is wedge height and it is selected as 3 mm.

Assuming that all the airgap flux passes through stator teeth:

$$B_g \tau_s L \approx B_{ts} b_{ts} L K_{Fe}$$

Here, K_{fe} is a constant to include lamination insulation's effect and suggested to be defined as 0.96. It is suggested to have a tooth flux density between 1.5 and 1.65 T. Let us take it as 1.6 T and determine b_{ts} :

Slot pitch isn't calculated yet, it is possible to use equation (15.3) for it.

$$\tau_s = \frac{\tau}{3q}$$

Slot pitch is 11.716 mm.

Tooth width is 5.685 mm.

It is better to take it as 5.6 mm.

For this value let us recalculate flux density of tooth:

Recalculated tooth-flux density is 1.62 Tesla.

This value is still inside the suggested range.

With the variables we know, using equation (15.23) it is possible to calculate the slot lower width:

$$b_{s1} = \frac{\pi(D_{is} + 2h_{os} + 2h_w)}{N_s} - b_{ts}$$

Lower slot width is 6.6 mm.

At this point missing variables are slot height and upper slot width. If slot area's round corners are ignored and area is taken as a trapezoid, its are would be;

$$A_{su} = h_s \frac{b_{s1} + b_{s2}}{2}$$

Also, we have(15.25) formula as follows:

$$b_{s2} \approx b_{s1} + 2h_s \tan \frac{\pi}{N_s}$$

From these 2 equations;

$$b_{s2} = \sqrt{4A_{su} \tan \frac{\pi}{N_s} + b_{s1}^2}$$

Upper slot width is 10.3 mm.

$$h_s = \frac{2A_{su}}{b_{s1} + b_{s2}}$$

Slot height is 28.3 mm.

Now we can proceed in calculating mmf of airgap and teeth. The airgap mmf is:

$$F_{mg} \approx K_c * g * \frac{B_g}{\mu_0}$$

Here, K_c is the Carter's coefficient and it helps us to consider airgap surface as smooth and make our calculations directly. It is expected that it is greater but close to 1; its formula is:

$$K_c = \frac{\tau_s}{\tau_s - b_e}$$

$$b_e = K b_{os}$$

$$K = \frac{\frac{b_{os}}{g}}{5 + \frac{b_{os}}{g}}$$

Carter coefficient is calculated as 1.06 .

Now airgap mmf may be calculated:

The airgap mmf is 545.336 Aturns.

Using tooth flux density and tooth's related heights we may calculate also mmf of stator tooth. Its formula is given with (15.30) and as follows:

$$F_{mts} = H_{ts}(h_s + h_{os} + h_w)$$

Only missing parameter is H of stator tooth and its value will be taken from table 15.4 of lamination magnetization curve.

H of stator tooth is selected as 2960 A/m for 1.62 Tesla.

So the stator tooth mmf is 95.608 Aturns.

Using formula given in (15.29) it is possible to calculate rotor tooth mmf since we take $1 + K_{st}$ value as 1.4 at the earlier part of design.

$$1 + K_{st} = 1 + \frac{F_{mts} + F_{mtr}}{F_{mg}}$$

Rotor tooth mmf is found as 122.526 Aturns.

As this value is only slightly larger than that of stator tooth, we may go on with the design process.

Only missing dimension for stator side is its back core and this value may be calculated with the formula below (15.32):

$$h_{cs} = \frac{D_{out} - (D_{is} + 2(h_s + h_{os} + h_w))}{2}$$

Back core is calculated as 2.5 cm.

Here, we should take a look at to the flux density to avoid a saturation.

$$B_{cs} = \frac{\phi}{2Lh_{cs}}$$

Back core flux density is 1.42 Tesla.

This is an acceptable value, therefore outer diameter won't be changed.

Rotor Slots

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