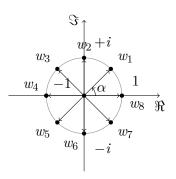
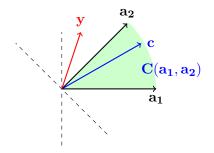
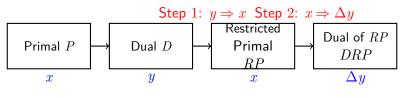
Root of unity



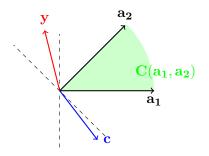
Farkas lemma



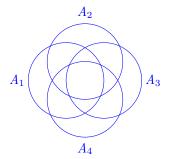


Step 3:
$$y = y + \theta \times \Delta y$$

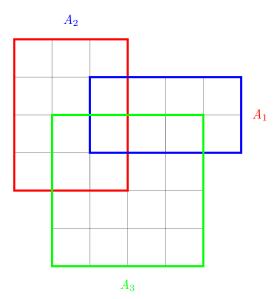
Farkas lemma



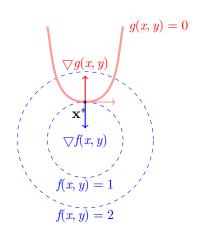
Max Coverage Problem



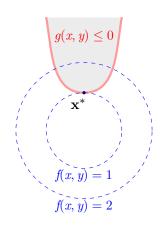
Max Coverage Problem2



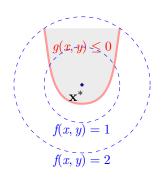
Lagrangian

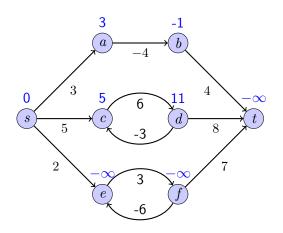


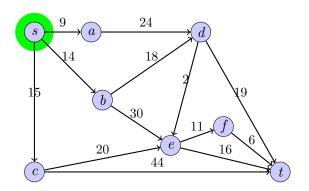
Lagrangian

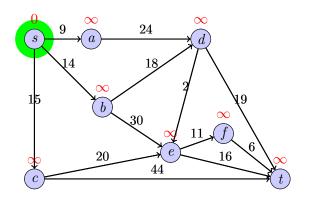


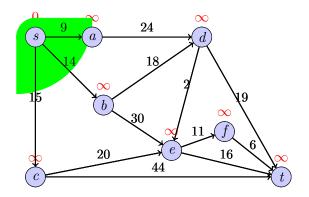
Lagrangian

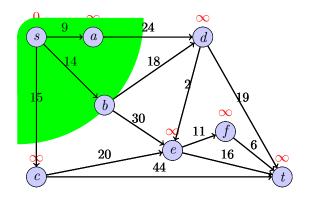


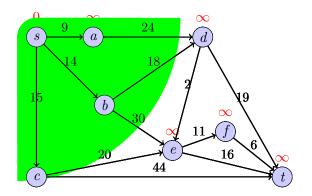


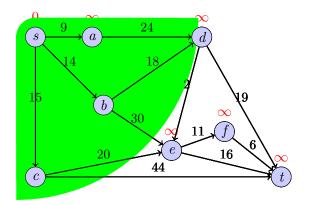


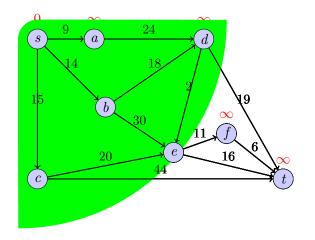


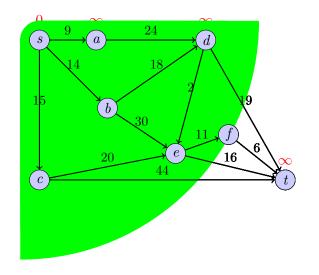


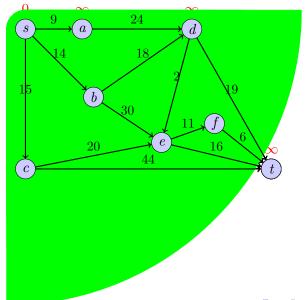


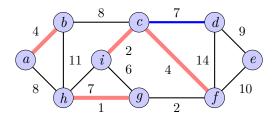




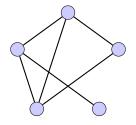




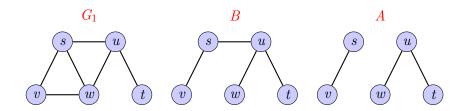




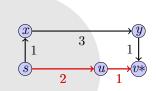
Pentagon



CCCCCCC

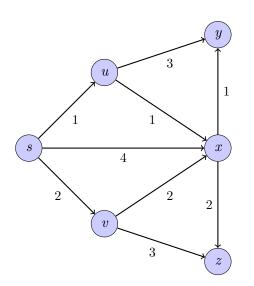


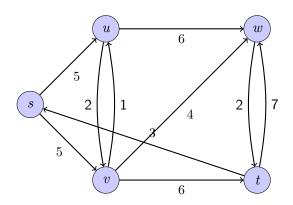
CCCCCCC



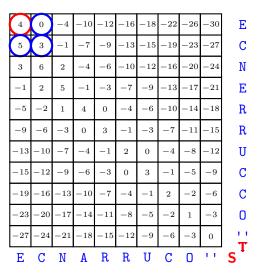
S: explored area

CCCCCCC





Lec6 Alignment matrix Suffix FULL



Lec6 Alignment matrix Prefix FULL

S:	1.1	0	C	U	R	R	A	N	C	E
T:'	0	-3	-6	-9	-12	-15	-18	-21	-24	-27
0	-3	1	-2	-5	-8	-11	-14	-17	-20	-23
C	-6	-2	2	-1	-4	-7	-10	-13	-16	-19
C	-9	-5	-1	1	-2	-5	-8	-11	-12	-15
U	-12	-8	-4	0	0	-3	-6	-9	-12	13
R	-15	-11	-7	-3	1	1	-2	-5	-8	-11
R	-18	-14	-10	-6	-2	2	ı	-3	-6	-9
E	-21	-17	-13	-9	-5	-1	1	-1	-4	-5
N	-24	-20	-16	-12	-8	-4	-2	2	-1	-4
C	-27	-23	-19	-15	-11	-7	-5	-1	3	0
E	-30	-26	-22	-18	-14	-10	-8	-4	0	4

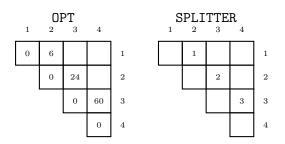
Lec7 Shortest Path example FULL

	k=0	1	2	3	4	5
S	0	0	0	0	0	0
U	-	1	1	1	1	1
٧		2	2	2	2	2
X	-	4	2	2	2	2
Y	1	1	4	3	3	3
Z	_	_	5	4	4	4

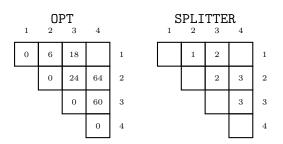
Lec6 Alignment matrix Prefix

S:	1.1	0	C	U	R	R	A	N	С	E
T:'	0	-3	-6	- 9	-12	-15	-18	-21	-24	-27
0	-3									
C	-6									
C	-9									
U	-12									
R	-15									
R	-18									
E	-21									
N	-24									
C	-27									
E	-30									

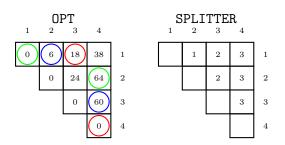
Lec6 Step1



Lec6 Step2



Lec6 Step3



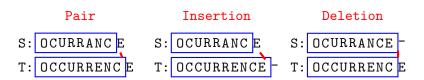
Lec6 444

 $\frac{n}{2}$

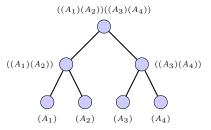
S: OCUR RANCE

 $\begin{array}{c|c} \texttt{T:} & \texttt{OCCUR} & \texttt{RENCE} \\ \hline & 1 \leq q \leq n \end{array}$

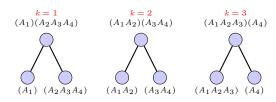
Lec6 333



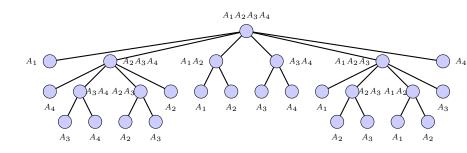
Lec6 DP 1



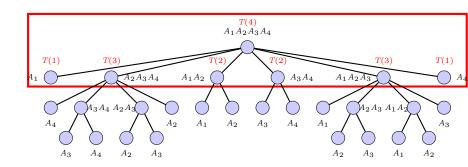
Lec6 DP 2

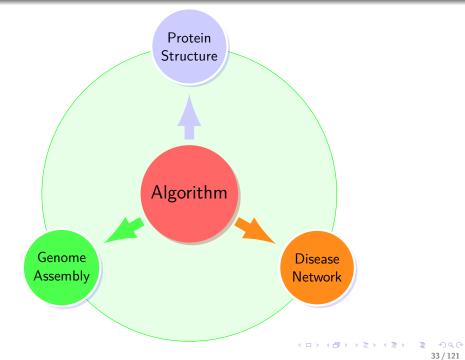


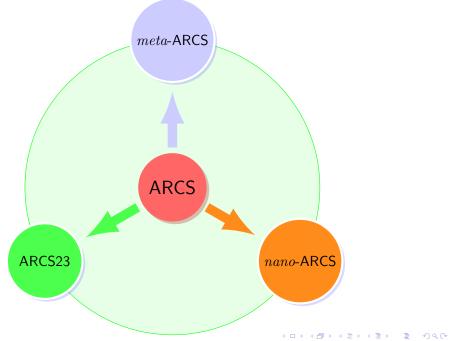
Lec6 DP 3

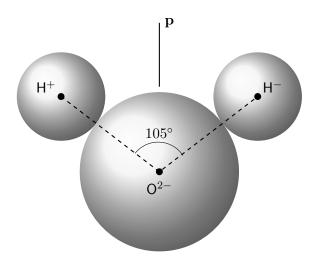


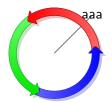
Lec6 DP4











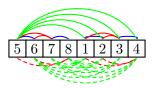
Lec5. Where did we save? Merge sort

$\overline{}$		\sim					
8	7	6	5	4	3	2	1

 ${\it MergeSort}$ step 1: 4 ops



 $\operatorname{MERGESORT}$ step 2: 4 ops, save: 4 ops



MERGESORT step 3: 4 ops, save: 12 ops

Lec5. Where did we save?

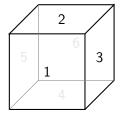
		$\overline{}$						
ı	8	7	6	5	4	3	2	1

:

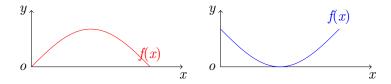


 ${\tt INSERTSORT:~28~ops}$

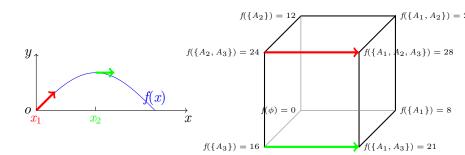
cube



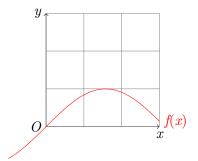
f(x) convex



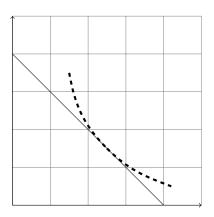
f(x) convex



f(x)

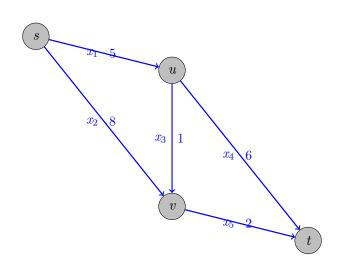




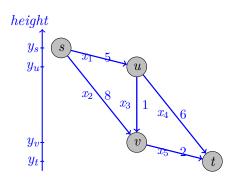


Lec5 Closest Pair n points

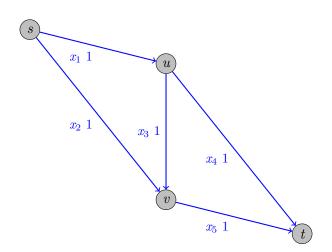




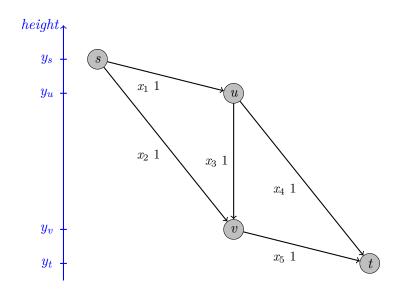
Shortest path

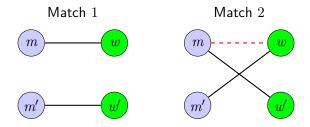


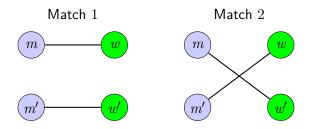
Dual

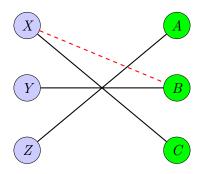


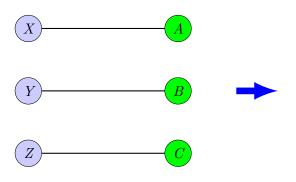
dual of shortest path

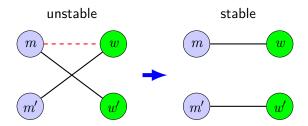


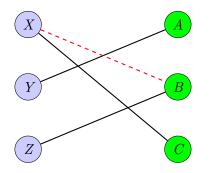


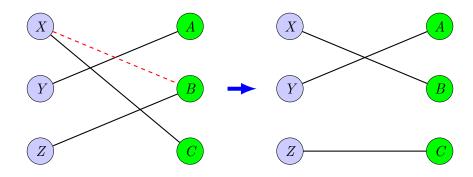


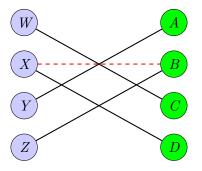


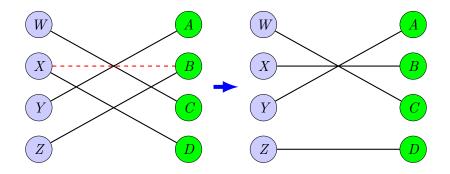


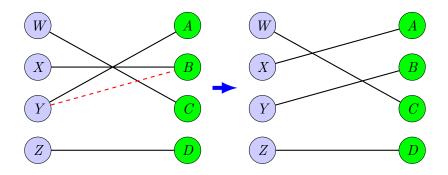


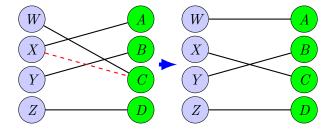


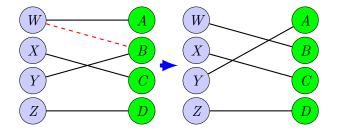


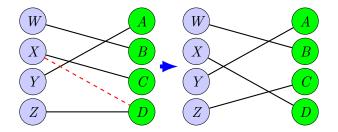


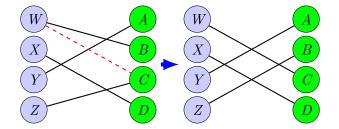




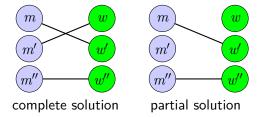


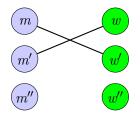


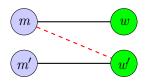


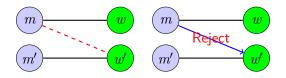


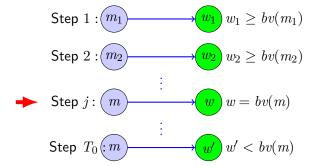
Stable Proof 1

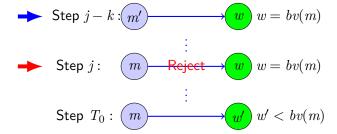


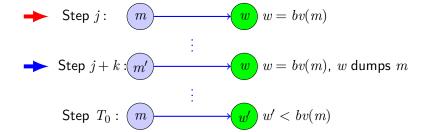




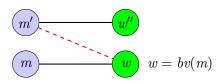




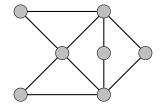




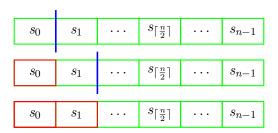
Stable match S'



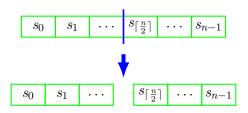
network example



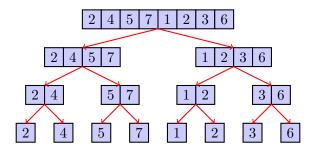
Lec5 1



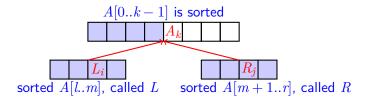
Lec5 2



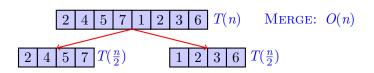
Lec5 how to divide?



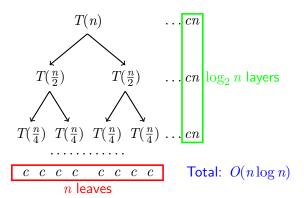
Lec5 how to combine?



Lec5 time complexity?



Lec5 tree



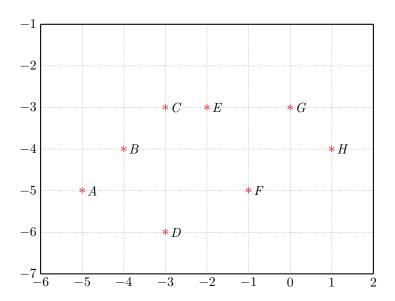
Lec5 Splitter

best splitter

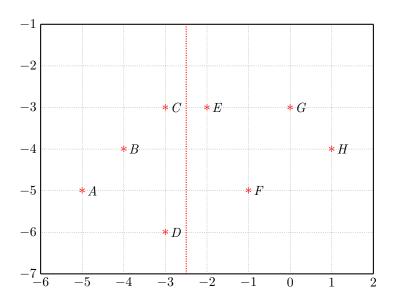


good splitters

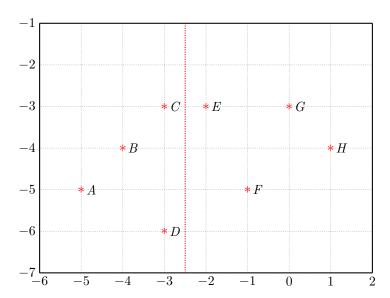
Lec5 Closest Pairs



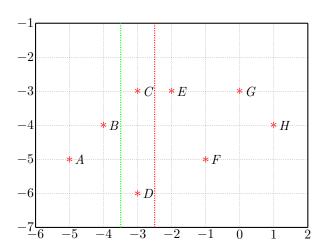
Lec5 Closest Pairs

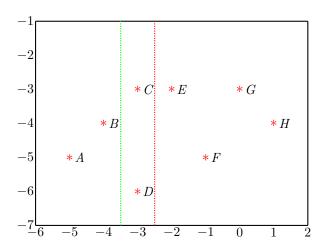


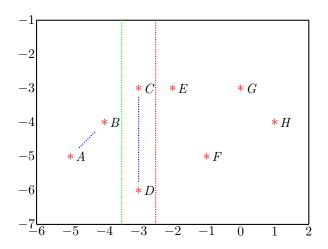
Lec5 Closest Pairs Middle Red Line

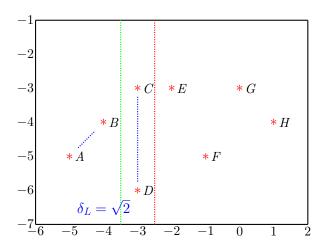


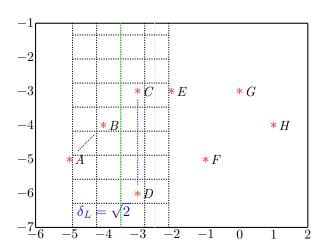
Leech Closest Pairs Left

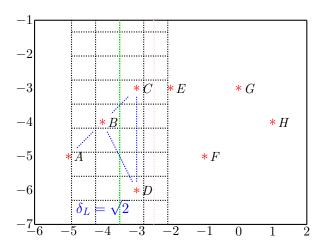




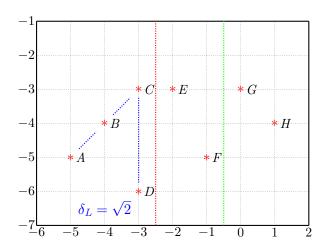


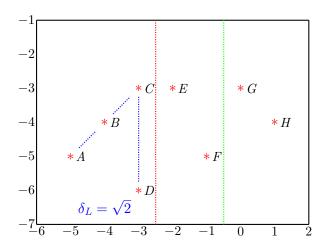


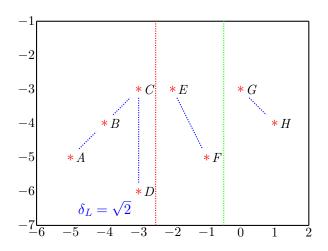


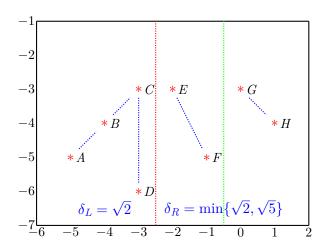


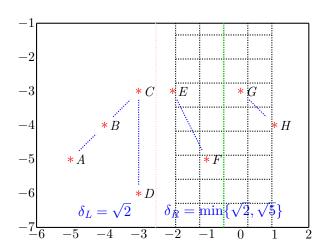
Lec5 Closest Pair Right

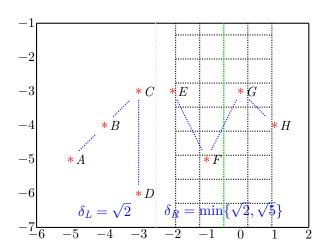


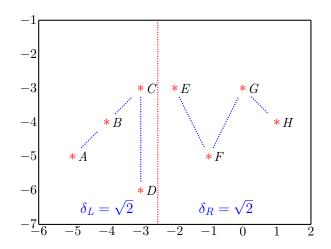


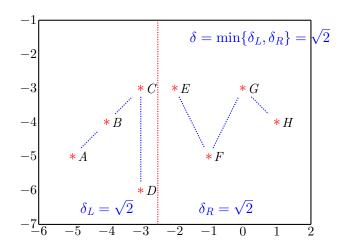


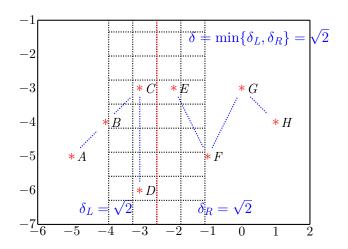


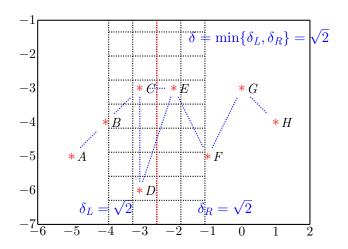


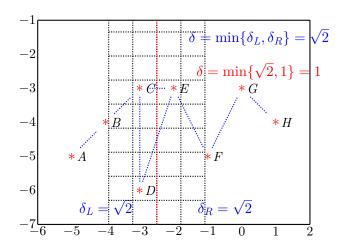




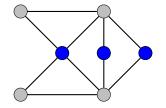


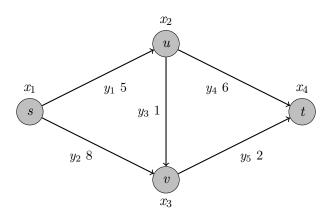






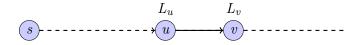
Examples





Edmonds Karp

Step k:

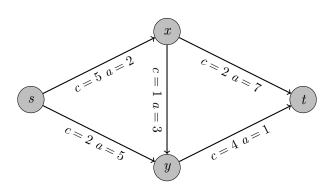


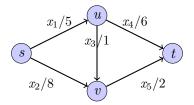
Step k+1: s-----vvv-------v

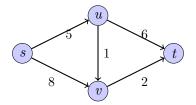
Primal and dual

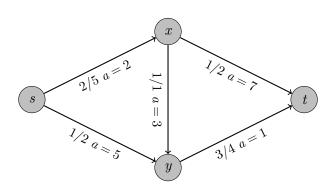


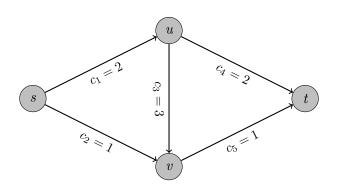
Step k'':

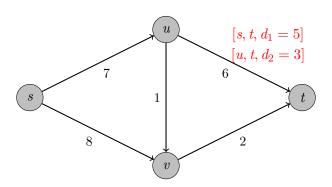


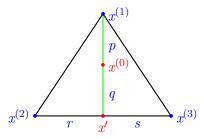


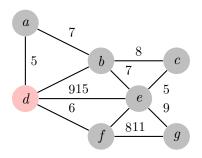


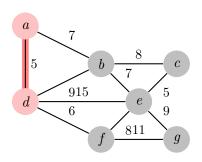


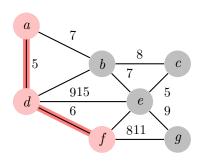


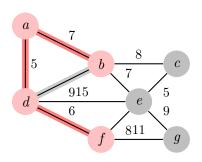


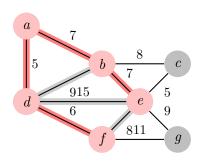


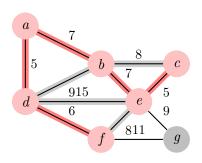


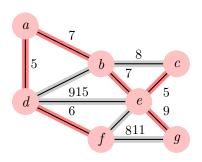




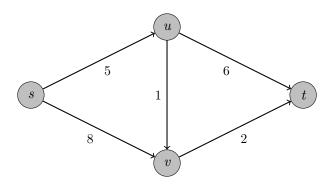




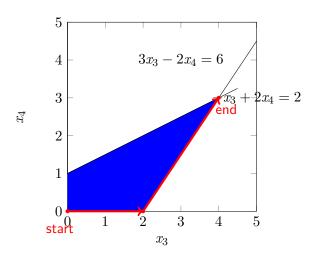


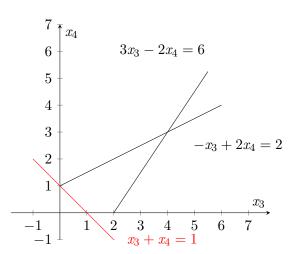


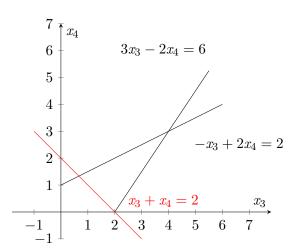
Max Flow

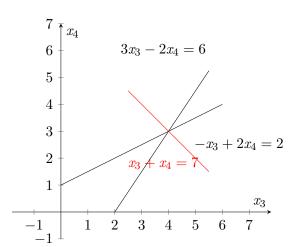


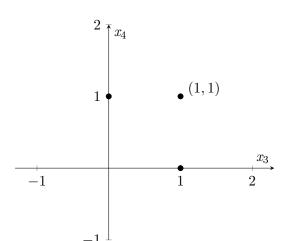
LP example

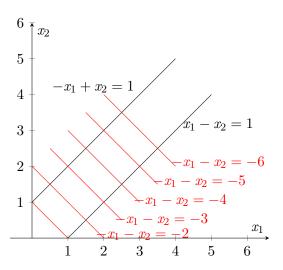


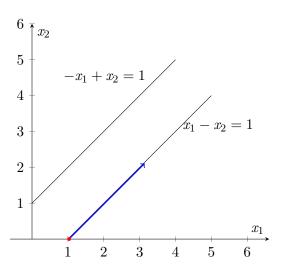


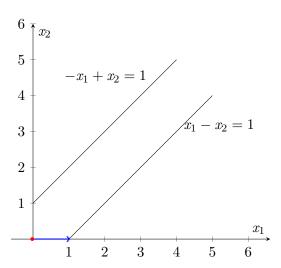


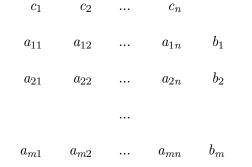


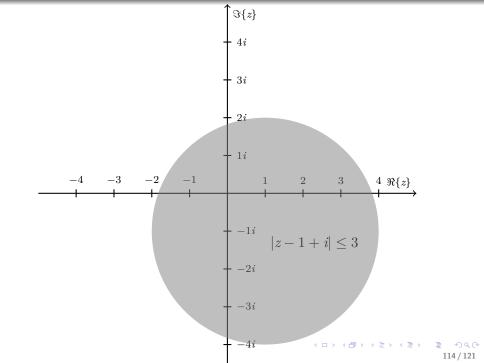












$$\begin{pmatrix} 0 & c_1 & c_2 & \cdots & c_m & \cdots & c_n \\ b_1 & a_{11} & a_{12} & \cdots & a_{1m} & \cdots & a_{1n} \\ b_2 & a_{21} & a_{22} & \cdots & a_{2m} & \cdots & a_{2n} \\ \vdots & \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ b_m & a_{m1} & a_{m2} & \cdots & a_{mm} & \cdots & a_{mn} \end{pmatrix}$$

$$\Longrightarrow \times \mathbf{B^{-1}}$$

$$\begin{pmatrix} \mathbf{c}_{\mathbf{B}}^{\mathbf{T}}\mathbf{B}^{-1}\mathbf{b} & 0 & 0 & \cdots & 0 & \mathbf{c}_{\mathbf{N}}^{\mathbf{T}} - \mathbf{c}_{\mathbf{B}}^{\mathbf{T}}\mathbf{B}^{-1}\mathbf{N} \\ & 1 & 0 & \cdots & 0 \\ \mathbf{B}^{-1}\mathbf{b} & 0 & 1 & \cdots & 0 & \mathbf{B}^{-1}\mathbf{N} \\ & \vdots & \vdots & \ddots & \vdots \\ & 0 & 0 & \cdots & 1 & \end{pmatrix}$$

 \Rightarrow

$$\begin{pmatrix} -\frac{a_{me}}{a_{le}}b_{l} & \dots & -\frac{c_{e}}{a_{le}} & \dots & 0 & \dots \\ b_{1} - \frac{a_{1e}}{a_{le}}b_{l} & \dots & -\frac{a_{1e}}{a_{le}} & \dots & 0 & \dots \\ b_{2} - \frac{a_{2e}}{a_{le}}b_{l} & \dots & -\frac{a_{2e}}{a_{le}} & \dots & 0 & \dots \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ \frac{1}{a_{le}}b_{l} & \dots & \frac{1}{a_{le}} & \dots & 1 & \dots \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ b_{m} - \frac{a_{me}}{a_{le}}b_{l} & \dots & -\frac{a_{me}}{a_{le}} & \dots & 0 & \dots \end{pmatrix}$$

LP x1x2-1

