

Question 4.

It ~~is~~ true.

Proof: According to the general division theorem, any integer can be presented as $bn+r$, while r

$$0 \leq r < |b|.$$

if $b=4$, so all integer can be expressed as $4n+r$.

because $0 \leq r < 4$, so ^{only} ~~are~~ these situations are available:

$$4n+0, \quad 4n+1, \quad 4n+2, \quad 4n+3$$

clearly $4n+0$ and $4n+2$ are even

So odd number can only be $4n+1$ and $4n+3$

This ~~proofs~~ proves the statement.