

Question 3.

It is True

Proof: ~~If n is odd, n^2 is odd. n can be expressed as $2a+1$,
 n can be expressed as $2b+1$~~

~~thus~~

Let $n=1$. $n^2+n+1 = 1+1+1=3$, so when $n=1$, this statement is true.

For $n+1$, $(n+1)^2+(n+1)+1 = n^2+2n+1+n+1+1$

$$= (n^2+n+1) + 2n+2.$$

because (n^2+n+1) is odd, and $(2n+2)$ is even. thus $(n+1)^2+(n+1)+1$ is odd.

this is proven by redudant