

Question 10.

$$\text{Let } A_n = [1, \frac{1}{n} + 1]$$

1. For  $A_{n+1} \subset A_n$ .

$$A_{n+1} = [1, \frac{1}{n+1} + 1]$$

$$A_n = [1, \frac{1}{n} + 1]$$

because  $\frac{1}{n+1} + 1 < \frac{1}{n} + 1$ .

$$\text{thus, } [1, \frac{1}{n+1} + 1] \subset [1, \frac{1}{n} + 1]$$

2. the limit of  $\frac{1}{n} + 1$  is 1.

$$\bigcap_{n=1}^{\infty} A_n = [1, 1] = 1.$$

So, the example  $A_n = [1, \frac{1}{n} + 1]$  satisfies the stated property.